

EVALUATION OF A PATIENT-SPECIFIC FINITE ELEMENT MODEL TO SIMULATE CONSERVATIVE TREATMENT IN ADOLESCENT IDIOPATHIC SCOLIOSIS

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Abstract

Study design: Retrospective validation study

Objectives: To propose a method to evaluate, from a clinical standpoint, the ability of a finite element model (FEM) of the trunk to simulate orthotic correction of spinal deformity, and to apply it to validate a previously described FEM

Summary of background data: Several FEMs of the scoliotic spine have been described in the literature. These models can prove useful in understanding the mechanisms of scoliosis progression and in optimizing its treatment, but their validation has often been lacking or incomplete.

Methods: Three-dimensional geometries of ten patients before and during conservative treatment were reconstructed from bi-planar radiographs. The effect of bracing was simulated by modeling displacements induced by the brace pads. Simulated clinical indices (Cobb angle, T1-T12 and T4-T12 kyphosis, L1-L5 lordosis, apical vertebral rotation, torsion, rib hump) and vertebral orientations and positions were compared to those measured in the patients' three-dimensional geometries.

Results: Errors in clinical indices were of the same order of magnitude as the uncertainties due to 3D reconstruction; for instance, Cobb angle was simulated with a root mean square error of 5.7° and rib hump error was 6.4°. Vertebral orientation was simulated with a root mean square error of 4.8° and vertebral position with an error of 2.5 mm.

Conclusions: The methodology proposed here allowed in-depth evaluation of subject-specific simulations, confirming that FEMs of the trunk have the potential to accurately simulate brace action. These promising results provide a basis for ongoing 3D model development, toward the design of more efficient orthoses.

Keywords: brace; adolescent idiopathic scoliosis; simulation; 3d reconstruction; biplanar radiography

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Introduction

Adolescent Idiopathic Scoliosis (AIS) is a three-dimensional deviation of the spinal axis [1], which develops in most cases during adolescence and can lead to functional impairment. The scoliotic deformity is usually quantified radiographically using the Cobb angle [2], a 2D parameter measured in the frontal plane that only suffices for a superficial description of the scoliosis. Surgery is often required at skeletal maturity in the case of severe scoliosis (Cobb angle higher than 45°), while conservative treatment (bracing or casting) is preferred when progressive scoliosis is diagnosed earlier (Cobb angle 20°-35°). The challenge of orthotic treatment is to stop or slow down the progression of the spinal curvature prior to skeletal maturity, in order to avoid surgery. Orthotic treatments are widely used for progressive curves; their effectiveness have often been questioned [3, 4], but a recent by Weinstein et al. [5] showed that bracing could significantly reduce scoliosis progression, especially in those patients with high level of compliance to brace wear.

Low-dose bi-planar radiographs can be used in routine clinical practice to assess patient specific spinal geometry during conservative treatment, allowing better description of the correction in three dimensions [6]. Testing different brace designs in order to optimize correction, however, requires multiple radiographic images; radiation doses can then accumulate over the several years that are often needed for this treatment.

Subject specific biomechanical models can help to better understand the mechanisms of bracing [7] and ultimately to plan the optimal conservative treatment for a specific subject, thus reducing the number of x-rays needed. Model validation, however, remains a challenge [8] because of the difficulties of obtaining *in-vivo* data to compare to the simulation output. Several studies have used finite

element models (FEM) for bracing simulation without thoroughly evaluating model consistency [9-11], although attempts to compare simulation and experimental measurements have been performed, generally in a very small number of patients, using 2D or 3D geometrical parameters [12-15]. Cobb angle was the main parameter evaluated, while lordosis and kyphosis were only evaluated in one study with six patients [15]. Rib hump, frontal shift and sagittal shift were only assessed in one patient [13]. Vertebral position [12, 14] and plane of maximum deformation were evaluated in less than four patients [12-14]. Transverse plane parameters (vertebral orientation, apical rotation, torsion) and rib hump are of clinical importance [16], but they have often been neglected in previous studies.

The goal of this study was to propose a method for detailed evaluation of a FEM simulating bracing effects in AIS patients. For that purpose, simulated key geometrical indices (including transverse plane deformity parameters) were compared with those measured *in-vivo*.

Methods

General principle

The evaluation method aimed to compare the simulated correction of the trunk induced by the orthosis with the actual correction as measured on in-brace radiographs. Patient-specific FEMs of the trunk were built from the standing radiograph of the patient's trunk before and during treatment. Orthosis action was simulated in the model by applying local displacements at each pad position, as described below. "Simulated clinical indices" were then calculated from the deformed FEM shape after simulation. "Radiological indices" were measured from the 3D reconstruction of the patient's actual geometry of spine and ribcage within the orthosis. These two sets of

clinical indices were then compared to determine the simulation error.

Subjects

Ten AIS patients were retrospectively included (Table 1), nine girls and one boy, with a mean Cobb angle of $25 \pm 13^\circ$ (range $13^\circ - 54^\circ$). Low-dose bi-planar radiographs (EOS system, EOS imaging, Paris, France) were performed in the standing position both before and during casting (n = 5, P1 - P5) or bracing (n = 5, P6 - P10); these radiographs were performed as part of clinical routine and were included retrospectively after approval of the local ethical committees. Both braces and casts were adjusted according to the clinician's indications. The delay between the two acquisitions (without and with brace) was three months or less (Table 1).

3D Geometry

For each patient, the three-dimensional geometry of the pelvis, spine and ribcage was reconstructed using previously described techniques [17-22] by experienced users. Briefly, these methods allow the personalization of parametric models of bony structures (vertebrae, ribs, pelvis), based on transversal and longitudinal inferences, to fit the radiographic images of the patient (postero-anterior and lateral). A first reconstruction can be obtained by digitizing specific anatomical landmarks in order to quickly calculate clinical parameters; for the present study, however, each model was manually adjusted to fit the original radiographs for maximum accuracy.

It was hypothesized that vertebrae were not deformed by the orthosis action, implying that the spinal curve correction was due to vertebral displacement and soft tissue deformation alone. Therefore, in order to minimize the reconstruction errors in vertebral shape, the average shape of each vertebra and the pelvis was calculated between the two reconstructions

(with/without brace) and used for simulations. This actually improves the model's degree of personalization, assuming that growth did not significantly affect vertebral anatomy in the maximum 3 month delay between examinations, since it reduces the reconstruction errors. Ribs, on the other hand, were not averaged since they could be deformed by the brace action.

Finite element model

The personalized FEM (5188 elements, 1997 nodes), implemented in ANSYS V11 (Ansys Inc., Canonsburg, PA, USA), has been previously described [23-27]. The main components of the model were the pelvis, sacrum, thoracic and lumbar vertebrae, intervertebral discs, ligaments and ribcage; material properties are summarized in Table 2. A custom made algorithm allowed transformation of vertebral volume models to beam models.

The ribcage was composed of ribs, costal cartilage, intercostal membrane, intercostal ligaments, sternum and costovertebral and costo-transverse joints. Ribs and costal cartilage were modeled by elastic beams, and in the present study they were improved from previous works by adapting their Young's modulus according to the patient's Risser grade [28], while their second moments of area were adapted according to vertebral level from an existing database of scoliotic adolescent rib morphology [29]. Intercostal ligaments were represented by cable elements and the intercostal membrane by linear elastic shells. The sternum was modeled with linear elastic shell elements. The ribcage was connected to vertebrae by the costovertebral and costotransverse joints, as previously characterized [10, 25].

Table 1. Characteristics of patients before orthotic treatment. Clinical indices were calculated from the 3D reconstruction without the orthosis.

	Gender	Orthosis type	Time between the two acquisitions	Risser grade	Cobb angle(°)	Lordosis L1/L5 (°)	Kyphosis T1/T12(°)	Kyphosis T4/T12(°)	Max Rib Hump (°) (level)	Apical rotation (°)	Torsion Index (°)
P1	F	Cast	Same day	0	13.3	64.4	42.7	33.4	12.4 (T10)	4.6	3.6
P2	F	Cast	Same day	5	24.5	42.3	36.3	40.5	8.2 (T4)	15.2	3.8
P3	F	Cast	2 days	2	53.7	54.3	30.0	9.1	16.1 (T10)	14.8	17.9
P4	F	Cast	1 day	0	39.8	57.3	26.2	2.8	13.4 (T10)	10.1	5.9
P5	M	Cast	1 day	2	12.8	62.0	62.3	44.0	10.0 (T6)	7.3	2.4
P6	F	Brace	2 months	0	17.7	51.8	41.7	39.5	4.8 (T7)	7.7	1.7
P7	F	Brace	Same day	0	15.3	20.6	23.4	34.0	7.6 (T9)	13.8	4.9
P8	F	Brace	3 months	0	27.3	38.1	9.8	6.2	-1.1 (T9)	7.4	9.8
P9	F	Brace	2 months	0	27.6	65.0	36.1	29.0	10.8 (T6)	5.1	4.5
P10	F	Brace	2 months	0	21.3	43.5	24.2	20.8	8.3 (T8)	17.9	2.3

Table 2. Main elements used in the model for the main structural components and their material properties (adapted from Describes *et al.* [23])

Item	Element	E (MPa)	ν (-)	Reference
Vertebral bodies	Beam	1000	0.3	[23]
Intervertebral discs	Beam	1 to 35	0.45	[30]
Pedicles	Beam	5000	0.3	[23]
Spinous processes	Beam	3500	0.3	[23]
Posterior arches	Beam	5000	0.3	[23]
Transverse processes	Beam	3500	0.3	[23]
Articular facets	Shell	5000	0.3	[23]
Apophysis	Beam	5000	0.3	[23]
Sternum	Beam	10000	0.2	[23]
Ribs	Beam	2790-7440	0.1	[28, 29]
Costovertebral joints	Beam	5 to 50	0.2	[25]
Costal cartilage	Beam	480	0.1	[23]
Intercostal ligaments	Cable	multilinear	0.2	[31]

Simulation

A preliminary step of each simulation was the displacement of the T1 vertebra and of the pelvis to the target position (i.e., its position in the in-brace configuration), in order to simulate the tendency of the subject to maintain balance. The pelvis was then fixed while T1 vertebra was allowed to translate in the vertical axis during the application of brace action. This action was simulated by applying local displacements induced by the orthotic pads, as described below.

Radio-opaque markers were embedded in the casts in order to detect pad regions

on the radiographs (Fig. 1a). For the other four patients wearing a brace, pressure regions were directly identified on the radiographs by observing external envelope deformations (Fig. 1b). Sets of nodes corresponding to these pressure regions were then manually identified on the model, as shown in Figure 1c.

Figure 2 shows an example of displacements applied to the model to simulate the orthosis action on a rib. Displacements were calculated as the difference between pad region position before treatment and in-brace; the average displacements of each pad region were then applied to the in-brace model in order to simulate brace action. After the simulation, the final geometry was retransformed in the volume models in order to calculate clinical indices.

Calculation of clinical

indices

Clinical indices were calculated in both the simulated and actual 3D geometry. Clinical indices were calculated in the patient frame of reference defined by the pelvis.

Rib hump was defined as the angle between the antero-posterior axis of the local coordinate system of the vertebra and the segment joining the most posterior sections of the ribs. It was calculated at each vertebral level in the reconstruction without the orthosis, and the vertebral level corresponding to maximum rib hump was noted. The rib hump at this same level was then calculated on the reconstruction with the orthosis and on the simulated

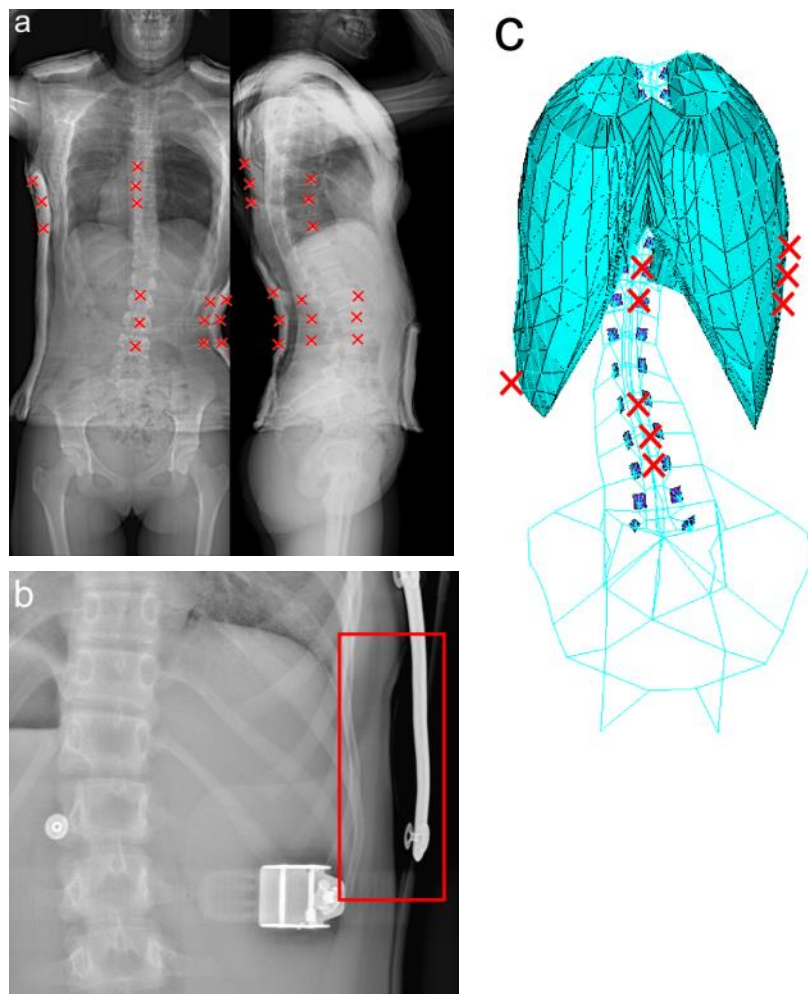


Fig. 1 a) × symbols show radio-opaque markers embedded in cast pad regions. b) Rectangle showing an example of brace pressure region identified by soft tissue compression. c) sets of nodes on the finite element model describing pressures regions.

Table 3. Uncertainty of clinical indices, vertebral positions and orientations in 3D reconstruction. Tolerances in the present work were determined by considering the propagation of uncertainty.

	Reconstruction uncertainty [19-21]	Error tolerance
Kyphosis T1-T12 (°)	5.5	7.8
Kyphosis T4-T12 (°)	3.8	5.4
Lordosis L1-L5 (°)	4.6	6.5
Cobb angle (°)	3.1	4.4
Apical rotation (°)	3.4	4.8
Torsion index (°)	4.0	5.7
Rib hump (°)	5.0	7.1
Vertebral Position X,Y,Z (mm)	1.2, 1.1, 0.8	1.7, 1.6, 1.1
Vertebral Orientation Lateral,sagittal,axial (°)	2.4, 2.3, 3.9	3.4, 3.3, 5.5

geometry in order to assess rib hump correction by the orthosis.

Torsion index was calculated as the mean of the absolute value of the sum of axial intervertebral rotations in inferior and superior semi-curvatures [32].

Statistics

The precision ($2RMS_{SD}$) for measurement of vertebral position and orientation, and for calculation of clinical indices based on 3D reconstruction from biplanar radiographs have been previously determined [19, 20] (Table 3). When comparing two 3D reconstructions, the minimal error that can be expected is $\varepsilon = \sqrt{2 \cdot (2RMS_{SD})^2}$ because both reconstructions are affected by the same uncertainty [33]. Therefore, the differences between simulated and actual clinical indices were compared to tolerance values thus calculated (Table 3).

The root mean square errors (RMSE) of vertebral orientation and position were also calculated by pooling all vertebral levels to evaluate overall geometry. Pearson's correlation coefficients were calculated between actual and simulated vertebral displacements; significance was set at $p < 0.05$. Calculations were

performed with Matlab 2011 (Mathworks, Natick, MA, USA).

Results

Differences between radiological and simulated clinical indices for each patient are presented in Table 4, as well as the measured valued with the orthosis; 77 % of the simulated values were in the tolerance error interval, while all values are of the same order of magnitude as the tolerance. For instance, RMSE of Cobb angle was 5.7° (against an error tolerance of 4.4°), RMSE of rib hump was 5.6° (tolerance: 7.1°). Only axial rotation was 2° higher than the tolerance (7° RMSE against 4.8° tolerance).

Schematic representations of vertebral positions and spinal midlines are given in Figure 3 and 4. Differences in vertebral orientation and positions between the simulation and the reconstruction within the brace are presented in Table 5; they are of the same order of magnitude as the reconstruction tolerances.

Correlation coefficients between simulated and actual vertebral positions were higher than 0.8 ($p < 0.01$) for all patients.

Discussion

This study proposes a method to evaluate the relevance of a patient specific finite element model for the simulation of orthotic treatment of spinal deformities. Orthotic treatment was simulated and evaluated, but the method described could equally well be applied to evaluate simulations of other spine and/or ribcage treatments. Key three-dimensional clinical indices were measured after simulation and compared to the *in-vivo* values obtained with bi-planar radiographs. These indices are necessary for a complete clinical and geometrical description of the scoliotic trunk, and are therefore essential when evaluating simulation performance.

Table 4.

Differences between measured and simulated clinical indices (measured in-brace values between parentheses) and root mean square error (RMSE).

Indices	P1	P2	P3	P4	P5	P6	P7	P8	P9	P10	RMSE
Kyphosis T1-T12(°)	-3.5 (46.1)	-2.0 (35.8)	4.0 (6.7)	3.3 (17.9)	6.7 (48.8)	0.6 (39)	-3.1 (18.3)	2.1 (9.5)	0.8 (29.1)	4.3 (17)	3.7
Kyphosis T4-T12(°)	-2.7 (31.2)	-2.2 (30.5)	0.5 (-3.3)	3.5 (2.5)	5.0 (43.5)	3.0 (35.7)	-1.6 (25.6)	1.1 (4.9)	-5.1 (20.8)	4.6 (16.4)	3.5
Lordosis L1-L5 (°)	1.8 (-56.5)	-0.9 (-47.6)	-2.1 (-48)	-9.6 (-47.4)	3.0 (-55.4)	-2.0 (-42.9)	-1.1 (-19.8)	-0.4 (-32.6)	-4.6 (-38.9)	-9 (-32.8)	4.9
Cobb angle (°)	2.0 (-20.1)	-3.4 (-9.8)	-4.8 (-40.7)	8.4 (-32.8)	-0.5 (12.5)	5.9 (4.2)	3.4 (12.5)	-10.8 (-7.1)	-3.1 (-2.7)	-3.6 (-13.1)	5.7
Apical rot. (°)	-5.4 (-0.7)	-8.4 (-7)	-7.9 (-8.6)	-11.1 (-4.5)	-2.0 (4.9)	-0.1 (5.8)	1.6 (15.1)	-7.7 (-9.4)	-9.4 (0.6)	0.9 (-3.9)	7.0
Torsion index (°)	0.7 (3.2)	1.6 (1.8)	12.8 (4.6)	-9.4 (16)	-3.7 (5.9)	0.4 (1.7)	-2.3 (7.7)	6.0 (2.4)	5.1 (1.4)	-2.2 (3.7)	6.2
Rib hump (°)	-1.0 (12.5)	11.8 (-4.4)	3.2 (13.9)	-2.1 (6.4)	-6.9 (7.6)	2.5 (3.4)	6.3 (6.6)	5.8 (-2.7)	-1.1 (7.5)	-1.2 (-8.8)	5.6

Table 5.

Root mean square errors between rotation and position (all vertebral levels pooled) in the 3D reconstruction and the simulation for each patient, followed by global RMSE.

	P1	P2	P3	P4	P5	P6	P7	P8	P9	P10	RMSE
Frontal rotation (°)	2.8	3.5	2.9	4.0	2.5	2.0	2.4	3.9	1.8	3.1	2.4
Lateral rotation (°)	4.7	2.1	2.5	5.2	4.2	2.4	1.6	2.7	2.7	3.1	2.3
Axial rotation(°)	3.3	4.8	4.5	17.0	5.4	4.2	4.8	4.9	6.1	5.3	3.9
X (mm)	3.5	2.8	1.3	1.8	2.3	1.4	1.5	1.4	1.5	2.7	2.7
Y (mm)	2.9	2.1	1.7	4.6	1.5	1.3	4.6	3.3	1.4	2.3	2.3
Z (mm)	1.9	0.9	0.8	6.1	2.1	2.7	0.7	0.8	1.2	1.6	1.6

The FEM utilized in this study could reproduce the brace effect on the trunk to within acceptable error limits in nine patients, both in terms of clinical indices (Table 4) and spine geometry (Table 5), which were of the same order of magnitude as the uncertainties due to the reconstruction. The tolerance values that were adopted as a reference in this study (Table 3) can be considered the lowest theoretical errors attainable, since they represent the uncertainty that can be expected when comparing two 3D reconstructions; these tolerances imply that the simulation is as accurate as the 3D reconstruction on which it is based. Moreover, it can be assumed that those errors that are lower than these tolerances are not significant.

Two main limitations affect the FEM evaluated in the present study; first, gravitational forces [34] and muscle contributions [9, 35] were not explicitly implemented in the model. Therefore, the agreement between radiological indices

and simulation is only related to the passive mechanical response of the spine-ribcage complex. This limitation, however, only affects the realism of the interaction between the brace and the patient's voluntary response, which is beyond the scope of this paper. Viscoelastic behaviour of soft tissues was neglected as well, but this aspect probably does not play an important role in brace action, which is slow and the effects of which are measured after long delays.

Second, orthosis action was implemented by imposing known displacements to selected nodes, in order to simulate the pad pressure; this technique, however, does not allow prediction of the treatment action without (at least partial) *a priori* knowledge of the target results. Therefore the FEM was evaluated here in terms of its ability to capture the geometrical deformations of the spine and ribcage resulting from known brace pad displacements; in other words, this work aimed at validating the behavior of the trunk biomechanical model.

Including an explicit description of the pads at this stage would have improved the realism of the brace simulation, but it would have also increased the sources of variability for the validation of the biomechanical model itself. Explicit brace modeling and analysis of contact forces could be implemented in further analysis, which should include muscular action and gravity as well; this is an essential step, especially when personalizing or designing braces in order to account for brace tolerability and comfort.

The ribcage is a particularly complicated

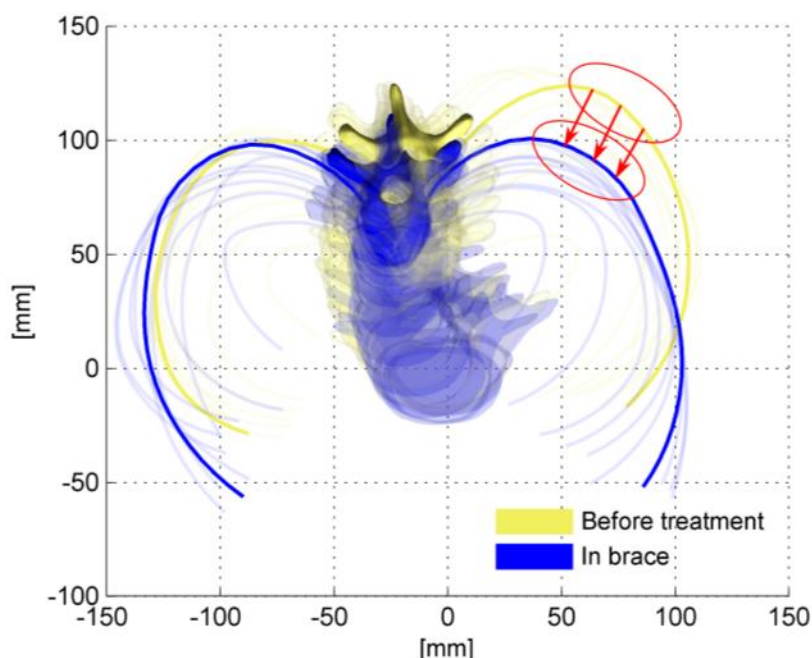


Fig. 2 Principle of application of boundary conditions: displacements were calculated as position differences of pad regions (oval outlines in the figure) between the before treatment and in-brace 3D reconstructions. These displacements were then applied to the FEM before treatment. Only the seventh left rib is highlighted in this example, although pad regions usually spanned at least three ribs.

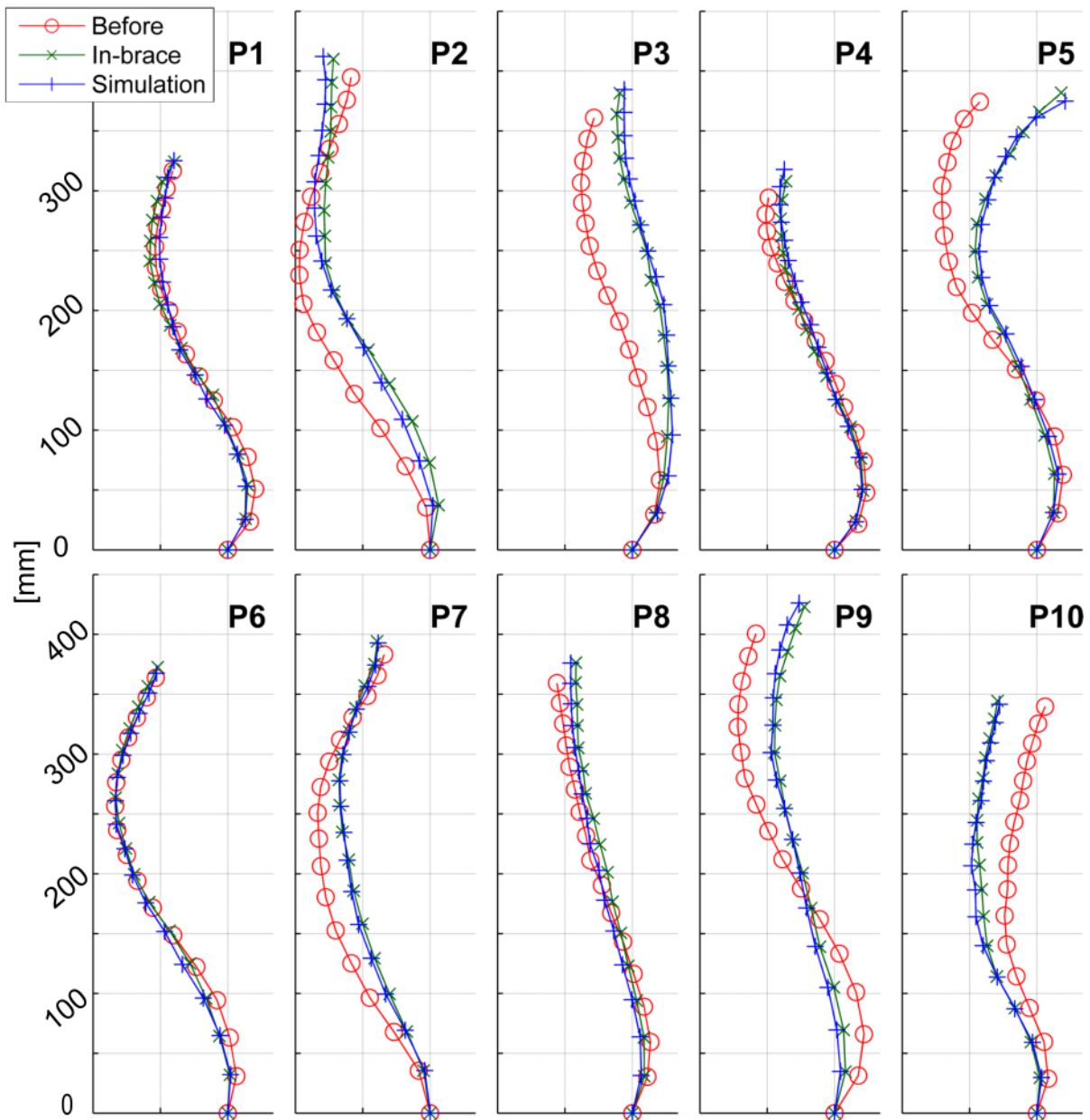


Fig. 3 Vertebral positions and spine midlines before treatment, in-brace and in simulated geometry: lateral views.

mechanical structure, the response of which depends on a large set of geometric and mechanical parameters. This study included a more accurate personalization of the spine and ribcage geometry than has been previously implemented, as well as an adaptation of the mechanical properties of the ribs according to the age of the subject. Personalization of mechanical properties of the intervertebral discs and costo-vertebral joints could be not introduced in the present study, since reliable techniques for *in-vivo* mechanical evaluation of these

structures are still lacking; a sensitivity study will help determine which mechanical properties are determinant for the simulation. Rib hump was simulated with an error of 6.4° [range $1^\circ - 12^\circ$], which is similar to the 7° error that was previously measured on one patient in the study performed by Périé *et al.* [13]. Rib hump differences between actual and simulated treatment could be related either to ribs and ribcage behavior (and therefore to the simulation of the pad action), or to the modeling of the costovertebral joints.

Errors in vertebral positions and clinical indices were relatively small. Kyphosis (T1-T12) and lordosis were simulated with average absolute errors of 4° and 5° , respectively, which is lower than the errors obtained by Desbiens *et al.* [15] (9.2° and 13° mean difference, respectively). While mean errors remained within the range of uncertainty, some patients had higher differences; these could be due to material properties, which were not subject specific in the current study due to the abovementioned limitations in

determining subject specific material properties.

Desbiens *et al.* [15] observed mean errors in Cobb angle of 4.4° , Périé *et al.* [12] obtained 3.9° in 6 patients while Chou *et al.* 3.5° [14]. A higher error of 8° was found by Périé *et al.* [13] but it was based on the evaluation of a single patient. In the present study, Cobb angle errors were lower than 6 degrees (average 6°) except for patients P4 and P8.

As for vertebral positions, correlation

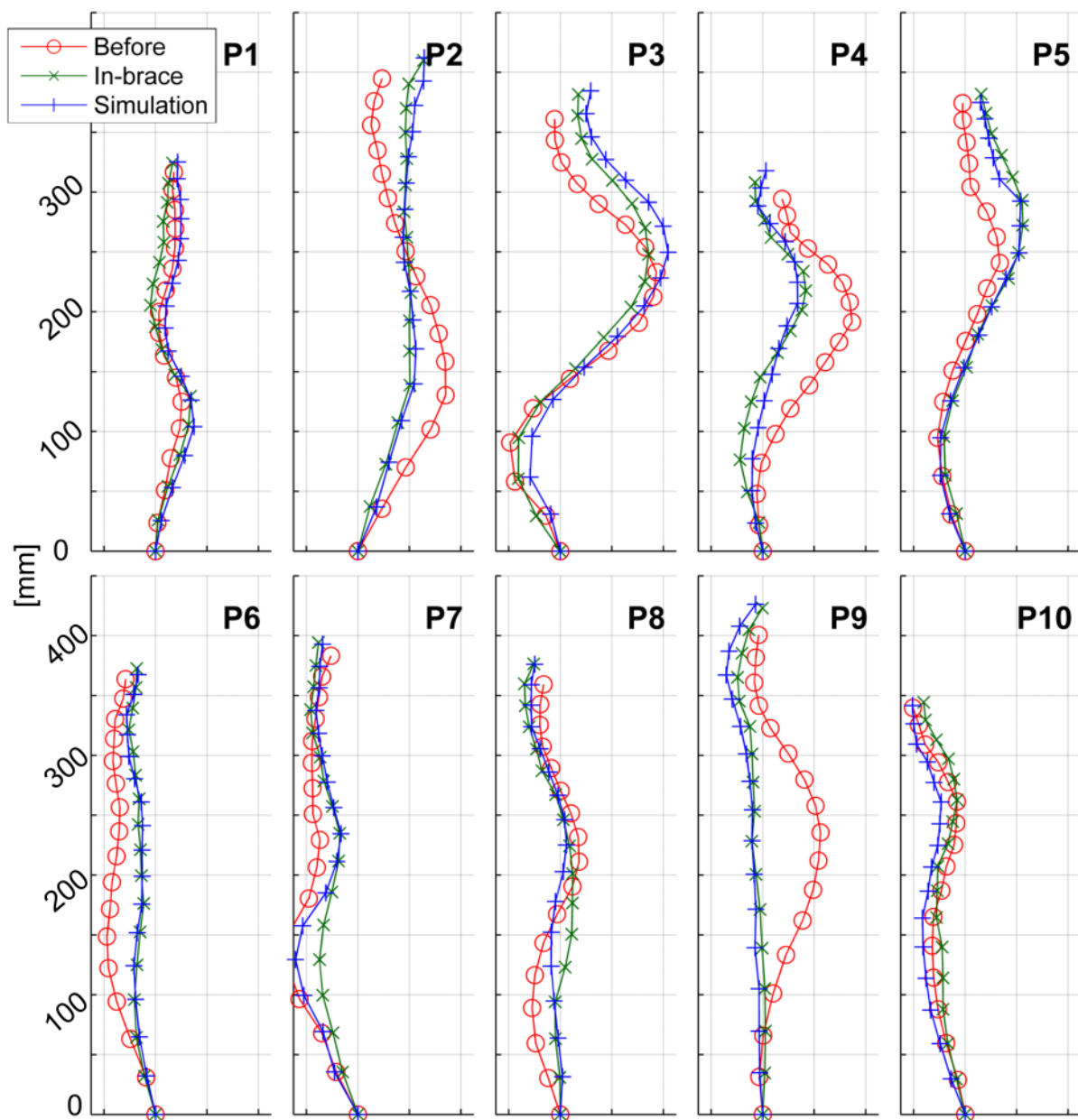


Fig. 4 Vertebral positions and spine midlines before treatment, in-brace and in simulated geometry: posterior views

coefficients indicated good agreement between simulation and *in vivo* measurements in nine patients. Similar agreements (coefficients of 0.9 and 0.99 respectively) were also measured in the studies by Périé *et al.* [12] and Chou *et al.*[14], but they were obtained in less than 4 patients. Vertebral orientations, apical rotation and torsion index were measured in the present study to complete the model validation in the transverse plane. Analysis of the literature shows that previous studies were often validated on a very small number of subjects (less or equal to 6). This study was conducted on slightly larger number of subjects, although they received two different treatments (5 were treated by cast, 5 by bracing). The results of this study now justify a larger multicentric data collection to further validate the model and better understand brace action.

The comparison of simulation results to *in vivo* radiographic measurements

suggests that the approach presented in this study could be used to assess the relevance of patient-specific bracing simulations. This method could also serve as benchmark for sensitivity studies in which the relationship between biomechanical model parameters and clinically measured indices is of interest.

The ability of the patient specific FEM approach for simulating a wide range of clinical indices appears to justify future research, in particular in the areas of spinal deformity brace simulation and planning.

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