# OPTIMISATION OF A CONCEPTUAL AIRCRAFT MODEL USING A GENETIC ALGORITHM AND 3D COMPUTATIONAL FLUID DYNAMICS

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## Summary

Aircraft design is fundamentally a multidisciplinary design activity which involves different models and tools for various aspects of the design. This paper uses a Multidisciplinary Design Optimisation (MDO) for design of a simplified commercial aircraft, aiming to optimise the objectives of cost, weight and drag. NSGA-II is used to optimise the weight and cost by changing the geometry to introduce lightweight airframe materials and composites with lower density. Reducing weight of the structure is one of the major ways to improve the performance of aircraft. Lighter, stronger material will allow a higher speed and greater range which may contribute to reducing operational costs. Drag reduction is also a major factor in aircraft design. Reduction of drag in an aircraft means that it can have a lower fuel consumption or travel at higher speed, both of which are beneficial to plane performance. A smart structural optimisation algorithm helps to optimise the cost, weight and drag, while drag is analysed based on CFD modelling results. The results are validated against some wind tunnel tests.

Key Words: Optimisation, aircraft, NSGA-II, CFD

#### Introduction

The first commercial aircraft started back on 1st January 1914. It operated between St. Petersburg and Tampa, yet only lasted for four months. Since then, engineers and scientists start to design and investigate different methods to improve the performance of aircraft. The original aims are to increase the distance of travel and the capacity of the aircraft. Nowadays, commercial aircrafts are fairly developed and improved compared to the first commercial aircraft. Even though the aircrafts have massively improved compared to the earlier designs. but there are still areas to improve. Designers always try to come up with better designs and the aims have changed from achieving basic performance to improving the performance of flight such as reducing the fuel consumption. To achieve these aims, designers have applied various techniques and technologies to assist with their design works. For example, the use of computational simulation, wind tunnel experiment and mathematical models has helped to refine, improve and optimise the aircrafts in terms of their structure, material choice and geometry in order to achieve a "better" design. Aircraft design always contains more than one objective; e.g., reduction of fuel consumption, reduction of weight and increase in the payload; and involves various disciplines such as structure dynamics, fluid dynamics and materials engineering. In this paper, MDO is used to optimise a simplified model of a commercial aircraft in order to reduce weight, drag and cost, simultaneously.

### **Materials and Methods**

During the conceptual design, ideas were formulated, rephrased, rejected or modified. Traditionally, aircraft design is separated into different areas of focus, such as structure, materials, dynamics and cost and there are aims and constraints in each area.

For example, the design of airframe focuses on structure and shape while the design of the wing will focus on lift and drag. All parts of an aircraft are closely related and interlinked with each other. Therefore, achieving one objective might have an adverse effect on the other design objective. For instance, replacing aluminium alloy by light-weight materials such as carbon fibre and other composites to achieve a weight reduction will have a trade-off of increased production cost. A complex design, such as aircraft, need to achieve different design objectives while there are different trade-offs. An MDO is a methodology to achieve the "best" solution by changing the design variables and maintaining different design constraints [1].

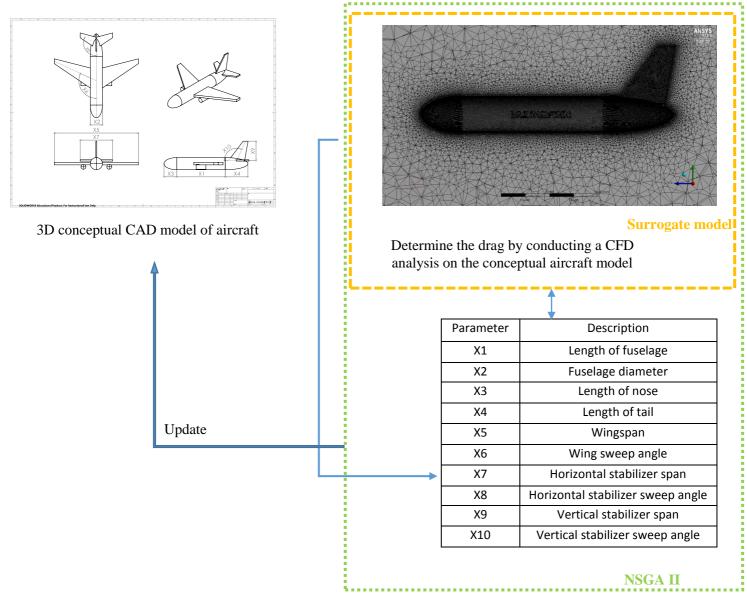


Figure 1: Application of the NSGA-II algorithm and the assigned parameters in the model

Traditionally, design is a process focusing on one area at a time and the areas down the stream are heavily dependent on the previous results. As modern design has developed and become more complex, it has become very difficult to optimise multiple design objectives. MDO is a design process which evaluates all design variables simultaneously and considers the trade-off and interaction between different objectives and disciplines. MDO is a methodology for the design of complex engineering systems that are governed by mutually interacting physical phenomena and made up of distinct interacting subsystems in their design.

The rapid development in the computational analysis in recent years has been largely influencing MDO. Many simulation results can now be linked and considered in the calculation process, which could be a significant aid, especially in aircraft design. Areas like wing lift and drag can be more easily considered during the design process. Apart from CFD or FEA, MDO can also involve diverse tools such as cost modelling and even experimental results. Nondominated Sorting Genetic Algorithm (NSGA-II) is a modified version of NSGA which is a multiobjective optimisation model and was one of the first evolutionary algorithms [2, 3]. It generates a set of solutions, also known as Pareto-optimised solutions, which are superior to the rest of the solutions. There is no absolute better solution within this Pareto-optimised solutions and hence the choice of an optimal solution over the others requires problem knowledge and other problem factors. In this study, the ten initial parameters (Figure 1) were defined in order to optimise the three main objectives. These ten parameters will update in each iteration based on the geometrical parameters' ranges of the aircraft models to generate the optimal solution. Also, a surrogate model was constructed based on the initial results from the CFD model and the remaining simulations were analysed based on this model predictions to observe and choose the most promising ones until a "good design" can be achieved. By generating a surrogate model using CFD simulation which has been validated by the wind tunnel results (Figure 2) and adapted in the NSGA-II model, the range of optimal solutions are generated.

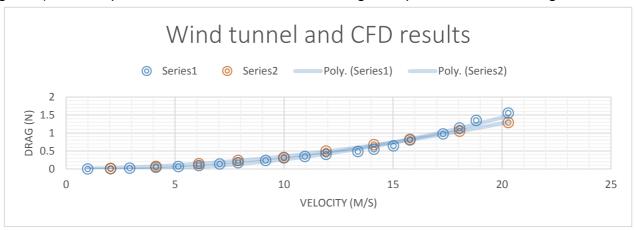
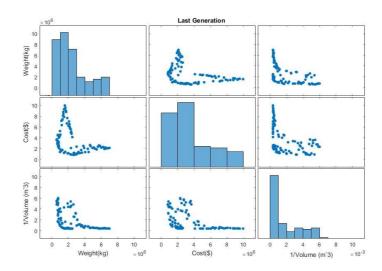


Figure 2: Validating the CFD model against the wind tunnel results based on the Drag force (N) and the Velocity (m/s)

### Results and conclusion

By combining the surrogate optimisation model generated by multiple CFD simulations and NSGA II, multiobjective genetic algorithm, a Pareto front is generated which clearly shows a trade-off between different objectives. There is a significant trade-off between weight and cost, as weight decreases, the costs increases (Figure 3) [4, 5]. This trend clearly exists between the weight and Fuselage volume and also cost and the volume. The results help to find a range of solutions in order to optimise the the topology of the structure [6].



**Figure 3:** Optimisation results from the NSGA-II algorithm for the three main objectives of Cost, Weight and Fuselage volume

Based on the developed algorithm, the optimised ranges for the main 10 parameters are illustarted (Table 1) in order to minimise the aforementioned objectives.

Parameters	Initial range	Optimised range
X1	15 – 50	36.86 – 50
X2	3.76 - 8.5	6.648 - 8.5
X3	3.96 – 5	4.173 – 5
X4	7 – 15	8.115 – 13.473
X5	26 – 80	26 – 31.62
X6	90 – 125	105.03 – 123.23
X7	10 – 30	10 – 15.834
X8	115 – 140	119.694 – 127.67
Х9	6 – 15	6 – 10.559
X10	115 – 140	115 – 139.07

#### References

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```
function [y, cons] = TP CONSTR objfun(x)
 [Ane, Ate] = elliptical (x);
Abo=pi*x(1)*x(2); An=integral(Ane,-x(3),0); Ata=integral(Ate,-x(4),0);
Awis= ((x(5)/4)+1.5)*(x(5)/2);
Awint= (2*(((x(5)/2))/sind(x(6)))+1.5)*0.75;
Awi=Awis+2*Awint; Astas= ((x(7)/2.5)+1.5)*(x(7)/2);
Astat=(2*(((x(7)/2))/sind(x(8)))+1.5)*0.4;
Asta=Astas+2*Astat; Arus=(((x(9)/1.2)+1.5)*x(9))/2;
Arut=(2*(((x(9)/2))/sind(x(10)))+1.5)*0.3;
Aru=Arus+Arut; En= (1.5/2)^2*pi*3;
tbl = readtable('test2.xlsx','range','A1:K101','ReadVariableNames',false);
tbl.Properties.VariableNames =
{'X1','X2','X3','X4','X5','X6','X7','X8','X9','X10','drag'};
   gprMd =
fitrgp(tbl,'drag','KernelFunction','squaredexponential','FitMethod','fic','Predict
Method', 'exact', 'Standardize', 1);
  C = \{x(1), x(2), x(3), x(4), x(5), x(6), x(7), x(8), x(9), x(10), []\};
T = cell2table(C);
T.Properties.VariableNames =
{'X1','X2','X3','X4','X5','X6','X7','X8','X9','X10','drag'};
y = [0,0,0];
cons = [0,0];
   y(1) = predict(gprMd,T);
y(2) =
 ((x(11)/(x(11)+x(12)+x(13)))*1750+(x(12)/(x(11)+x(12)+x(13)))*2800+(x(13)/(x(11)+x(12)+x(13)))*2800+(x(13)/(x(11)+x(12)+x(13)))*2800+(x(13)/(x(11)+x(12)+x(13)))*2800+(x(13)/(x(11)+x(12)+x(13)))*2800+(x(11)+x(12)+x(13)))*2800+(x(11)+x(12)+x(13)))*2800+(x(11)+x(12)+x(13)))*2800+(x(11)+x(12)+x(13)))*2800+(x(11)+x(12)+x(13)))*2800+(x(11)+x(12)+x(13)))*2800+(x(11)+x(12)+x(13)))*2800+(x(11)+x(12)+x(13)))*2800+(x(11)+x(12)+x(13)))*2800+(x(11)+x(12)+x(13)))*2800+(x(11)+x(12)+x(13)))*2800+(x(11)+x(12)+x(13)))*2800+(x(11)+x(12)+x(12)+x(13)))*2800+(x(11)+x(12)+x(13)+x(13)))*2800+(x(11)+x(12)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13)+x(13
 (12) + x (13)) \times 7850 \times 0.5 \times (((Abo) + (abs (An)) + (abs (Ata)) + (2*Awi) + (2*Asta) + (2*Aru) + (2*En) \times (12) \times (13) 
)));
y(3) =
 ((x(11)/(x(11)+x(12)+x(13)))*1750*6.38+(x(12)/(x(11)+x(12)+x(13)))*2800*1.38+(x(13)))*1750*6.38+(x(13)/(x(11)+x(12)+x(13)))*1750*6.38+(x(12)/(x(11)+x(12)+x(13)))*1750*6.38+(x(12)/(x(11)+x(12)+x(13)))*1750*6.38+(x(12)/(x(11)+x(12)+x(13)))*1750*6.38+(x(12)/(x(11)+x(12)+x(13)))*1750*6.38+(x(12)/(x(11)+x(12)+x(13)))*1750*6.38+(x(12)/(x(11)+x(12)+x(13)))*1750*6.38+(x(12)/(x(11)+x(12)+x(13))))*1750*6.38+(x(12)/(x(11)+x(12)+x(13))))*1750*6.38+(x(12)/(x(11)+x(12)+x(13))))*1750*6.38+(x(12)/(x(11)+x(12)+x(13))))*1750*6.38+(x(12)/(x(11)+x(12)+x(13))))*1750*6.38+(x(12)/(x(11)+x(12)+x(13))))*1750*6.38+(x(12)/(x(11)+x(12)+x(13))))*1750*6.38+(x(12)/(x(11)+x(12)+x(13))))*1750*6.38+(x(12)/(x(11)+x(12)+x(13)))
/(x(11)+x(12)+x(13)) *7850*0.3) * (0.5*((Abo)+(abs(An))+(abs(Ata))+(2*Awi)+(2*Asta)
+(2*Aru)+(2*En));
c(1) = x(1) * (x(2)/2)^2*pi;
c(2) = x(1) * (x(2)/2)^2*pi;
%c(3) = y(3);
    if (c(1)<150)% new deisgn has a lower payload than the original Boeing 737 100
              cons(1) = abs(c(1)-150)*100000;
    if (c(2) >= 150)
                            cons(2) = 150/((abs(c2) - 150) * 100000);
    %if (c(3) <= 0)
                                cons(3) = 0.001/((abs(c2)-150)*100000);
%end
end
clear All
  boundary
  options = nsgaopt();
                                                                                                                                                % create default options structure
options.popsize = 100;
                                                                                                                                          % populaion size
options.maxGen = 100;
                                                                                                                                           % max generation
                                                                                                                                               % number of objectives
  options.numObj = 2;
options.numVar = 13;
                                                                                                                                           % number of design variables
options.numCons = 2;
                                                                                                                                             % number of constraints
                                                                                                                                             % lower bound of x
options.lb = lb;
options.ub = ub;
                                                                                                                                             % upper bound of x
options.objfun = @TP_CONSTR_objfun; % objective function handle
options.plotInterval = 5;
                                                                                                                                             % interval between two calls of
"plotnsga".
   result = nsga2(options);
                                                                                                                                               % begin the optimization!
    %plotting
%optimisation history
function varargout = plotnsga(varargin)
gui Singleton = 1;
gui_State = struct('gui_Name',
                                                                                                                                  mfilename, ...
                                                                    'gui_Singleton', gui_Singleton, ...
'gui_OpeningFcn', @plotnsga_OpeningFcn, ...
                                                                     'gui_OutputFcn', @plotnsga_OutputFcn, ...
                                                                     'gui LayoutFcn', [], ...
```

```
'gui Callback',
if nargin && ischar(varargin{1})
   gui State.gui Callback = str2func(varargin{1});
end
 if nargout
    [varargout{1:nargout}] = gui mainfcn(gui State, varargin{:});
else
    gui mainfcn(gui State, varargin{:});
end
function plotnsga OpeningFcn(hObject, eventdata, handles, varargin)
handles.output = hObject;
guidata(hObject, handles);
 handles.bLoadFromFile = 0;
if( isempty(varargin) )
    error('PLOTNSGA:ParamError', 'Error: plotnsga should be called :
plotnsga(result, curGen) or plotnsga(''pops.txt'')');
 elseif(length(varargin) == 1)
    if( isstruct(varargin{1}) )
        handles.result = varargin{1};
        handles.currentGen = 1;
            elseif( ischar(varargin{1}) )
        global oldresult;
        oldresult = loadpopfile(varargin{1});
        evalin('base', 'global oldresult');
        handles.bLoadFromFile = 1;
                              = varargin{1};
        handles.strPopFile
        handles.result
                               = oldresult;
        handles.currentGen
                               = 1;
    end
    elseif(length(varargin) == 2)
    if( isstruct(varargin{1}) && isscalar(varargin{2}) )
        handles.result = varargin{1};
        handles.currentGen = varargin{2};
    else
        error('PLOTNSGA:ParamError', ...
            'Error: plotnsga should be called : plotnsga(result, curGen) or
plotnsga(''pops.txt'')');
    end
end
popsize = size(handles.result.pops, 1);
strList = repmat({''}, [1,popsize]);
for i = 1:popsize
    strList{i} = sprintf('%d', i);
                              set(handles.listPop, 'string', strList);
 curSel = handles.currentGen;
set(handles.listPop, 'value', curSel);
dispState(handles, curSel);
plotPopulation( handles, curSel );
guidata(hObject, handles);
 function varargout = plotnsga_OutputFcn(hObject, eventdata, handles)
varargout{1} = handles.output;
function btnStop_Callback(hObject, eventdata, handles)
global STOP NSGA;
STOP NSGA = 1;
function btnPause Callback(hObject, eventdata, handles)
if isempty(getappdata(0, 'gadsSolverState'))
    setappdata(0, 'gadsSolverState', 'pause');
    set(hObject,'String','Continue');
        waitfor(hObject,'String');
else
    setappdata(0, 'gadsSolverState', '');
    set(hObject, 'String', 'Pause');
end
```