Incorporating subject-specific geometry to compare metatarsal stress during running with different foot strike patterns

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Abstract

Stress fracture of the second metatarsal is a common and problematic injury for runners. The choice of foot strike pattern is known to affect external kinetics and kinematics but its effect on internal loading of the metatarsals is not well understood. Subject-specific models of the second metatarsal can be used to investigate internal loading in a non-invasive manner. This study aimed to compare second metatarsal stress between habitual rearfoot and non-rearfoot strikers during barefoot running, using a novel subject-specific mathematical model, including accurate metatarsal geometry. Synchronised force and kinematic data were collected during barefoot overground running from 20 participants (12 rearfoot strikers). Stresses were calculated at the plantar and dorsal periphery of the midshaft of the metatarsal using a subject-specific beam theory model. Non-rearfoot strikers demonstrated greater external loading, bending moments and compressive forces than rearfoot strikers, but there were no difference in peak stresses between groups. Statistical parametric analysis revealed that non-rearfoot strikers had greater second metatarsal stresses during early stance but that there was no difference in peak stresses. This emphasises the importance of bone geometry when estimating bone stress and supports the suggestion that external forces should not be assumed to be representative of internal loading.
Introduction

Running is increasingly popular (van der Worp et al., 2015) and is associated with longevity (Chakravarty et al., 2008, Lee et al., 2014, Schnohr et al., 2013, Wang et al., 2013). However distance running is associated with a high incidence of lower limb injuries (van Gent et al., 2007). One particularly burdensome injury is stress fracture of the metatarsals, which account for 4% of all sporting injuries (Chuckpaiwong et al., 2007). The second metatarsal is one of the most common sites of stress fracture (Bennell et al., 1996, Bennell et al., 1998, Gross and Bunch, 1989, Iwamoto and Takeda, 2003, Milgrom et al., 1985) with 10% of all fractures occurring in the metatarsals and 80% - 90% of these located in the second and third metatarsals (Chuckpaiwong et al., 2007).

Bones are repeatedly loaded during running and this can lead to the accumulation of microdamage. Microdamage accumulation and its repair is a normal and healthy response to loading, and given enough time will result in the bone becoming more resistant to the loading applied. However, microdamage accumulation alters the properties of bone (Burr et al., 1998) and can increase its susceptibility to stress fracture (Burr, 2011). Metatarsal stress fractures are thought to develop due to cyclic overloading with an intermediate remodelling process, which initially weakens the bone prior to increasing strength (Martin et al., 2015). Without sufficient recovery, further loading can lead to excessive microdamage accumulation (Milgrom et al., 2002, Schaffler and Jepsen, 2000) and increased risk of stress fracture.

Runners can be categorised by their foot strike pattern (Nunns et al., 2013). Most commonly runners land on their heel (rearfoot strike) (de Almeida et al., 2015). This is
associated with an early impact peak in the vertical ground reaction force time history and high vertical force loading rates (Lieberman et al., 2010). Conversely, those who do not rearfoot strike display a less distinct impact peak and the vertical force loading rates are typically lower than for a rearfoot striker (Ahn et al., 2014, Lieberman et al., 2010). There has been much discussion about the merits and shortcomings of each foot strike pattern, which is confounded when the influence of footwear is considered. Running in a minimalist shoe tends to result in a more anterior initial foot contact, resulting in increased loading at the metatarsal phalangeal joint (Firminger and Edwards, 2016) - a potential mechanism for increased stress fracture risk. Metatarsal stress fractures have also been reported when converting from standard running shoes to minimalist shoes (Cauthon et al., 2013, Salzler et al., 2012). However, it is not clear if this was influenced by the effect of the footwear per se or an accompanying change in foot strike. Estimates of metatarsal loading when running with different foot strikes is required to further understand the potential mechanisms for stress fracture.

Efforts to estimate internal bone loading have included direct measurement techniques and mathematical modelling. Direct measurement of bone strain using bone staple strain gauges (Arndt et al., 2002, Milgrom et al., 2002) is invasive, making this impractical for applied research questions due to the limited participant numbers. Mathematical models ranging from simple beam theory (Gross and Bunch, 1989, Nunns et al., 2017, Stokes et al., 1979) to more computationally expensive finite element simulations (Firminger et al., 2017, Li et al., 2017) are a viable alternative and have been used to estimate internal forces acting on the metatarsals during both running and walking. Previously beam theory has provided valuable insight into potential mechanisms for second metatarsal stress fracture (Gross and Bunch, 1989).
This previous research modelled the metatarsal as a hollow elliptical beam and concluded that more accurate, subject-specific bone geometry is required to improve understanding of stress fracture risk.

The aim of this study was to quantify the forces and stresses acting on the second metatarsal during barefoot running, using a subject-specific mathematical model, including accurate metatarsal geometry. Further, this model was used to compare metatarsal loading in rearfoot (RF) and non-rearfoot (NRF) strikers during running. It was hypothesised that NRF strikers would experience greater peak internal second metatarsal loading than RF strikers.

**Methods**

**Participants**

20 injury-free participants who described themselves as experienced at running and who were currently participating in running activity >3 times per week and >150 mins per week were recruited. Participants reported no current injuries affecting their running and no lower limb injuries that prevented their normal training within the last year. Eligible participants provided written informed consent. The study was approved by the Sport and Health Sciences Ethics Committee, University of Exeter. Sample size was estimated using G*Power (Faul et al., 2007). Peak pressures under the central forefoot in RF and NRF strikers during running in minimalist shoes were used to determine effect size (Kernozek et al., 2014) as this is an important input variable into the stress model. 12 participants was sufficient based on an alpha of 0.05 and power of 95%. A more conservative sample size of 20 was recruited to account for the subject-specific approach that was expected to increase between-participant variability. Prior to the full running protocol, foot strike was assessed in participants’
own running shoes during running over a pressure plate. Participants were not informed of their foot strike pattern. This was later compared to their barefoot trials: two participants displayed a foot strike that was consistently more anterior when barefoot than shod, and these participants were included in the NRF group; two further participants displayed a combination of foot strikes during barefoot running, in which case additional trials were collected such that a complete set matching the shod trial were obtained. RF strikers were classified according to the methods of Cavanagh and Lafontaine (1980) (N = 12; 7 Female; age 28 ± 11 years; mass 62.6 ± 10.4 kg; height 1.65 ± 0.07 m); whilst NRF strikers were those with a more anterior foot strike (N = 8; 3 Female; age 20 ± 3 years; mass 72.3 ± 12.3 kg; height 1.73 ± 0.09 m).

MR Imaging

To determine metatarsal geometry, magnetic resonance (MR) images were collected from each participant whilst lying supine within a 1.5 T superconducting whole body scanner (Gyroscan Intera, Philips, The Netherlands). The second metatarsal was identified via palpation and marked with a fish oil capsule. The unloaded foot was placed against a flat vertical barrier within a quadrature head coil to minimize movement and ensure a consistent foot position. Stacks of triaxial MR images covering the whole of the foot and centred around the second metatarsal were acquired. A T1 weighted (repetition time 20 ms, echo time 4.0 ms, flip angle 50°) 3D gradient echo sequence was utilised with an in-plane resolution of 0.3 x 0.3 mm and slice thickness of 0.7 mm. Depending on the imaging orientation, 60 - 160 slices within a stack were required for full coverage.

Running Protocol
Height and mass were measured whilst participants wore their own running kit. Synchronised kinematic, kinetic and plantar pressure data were collected during barefoot running at 3.6 ms\(^{-1}\) using four CX1 units (Codamotion, Charnwood Dynamics Ltd., U.K.) with an integrated force plate (1000 Hz) (AMTI, MA, USA). 19 markers (200 Hz) represented bony landmarks of the foot and shank, similar to the Oxford Foot Model (Carson et al., 2001).

A separate plantar pressure plate (RSscan 0.5 m Hi-End Footscan, Belgium) was placed over the force plate such that the pressure plate was entirely within the boundaries of the force plate. This was positioned flush with a runway comprised of EVA foam - a contact surface intended to represent a shoe midsole. Pressure data were collected at 200 Hz using Footscan software (RSscan Gait v7). An opportunity to warm up was provided and familiarisation trials were completed until the participant was comfortable running at the desired speed. Speed was monitored using light gates (WITTY system, Microgate, Bolzano, Italy). The experimental protocol involved running at a constant speed with a right foot contact within the pressure plate boundaries. A trial was successful when the right foot contacted the pressure plate, speed was 3.6 ms\(^{-1}\) (±5%), markers remained visible during foot contact and the investigator observed no unusual movement. Ten successful trials were recorded per participant.

Data Analysis

The procedure for pressure analysis was taken from Rice et al. (2013) and analysis was performed using RSscan Footscan Gait v7.

Stress Model
The forces acting on the second metatarsal were estimated using a model similar to Stokes et al. (1979) and Gross and Bunch (1989), with stress calculated at the upper and lower surfaces of the bone at the midpoint of the shaft, using a similar approach to that of Meardon and Derrick (2014).

Figure 1 shows the forces considered in the model. Assumptions in the model are similar to Stokes et al. (1979) with the following alterations and additions:

1. Flexor muscle forces are represented by a long and short plantar tendon with equal load distribution between them
2. Forces and kinematics in the mediolateral direction are negligible
3. The external forces act at points underneath the distal metatarsal head and toe
4. The masses of the segments are negligible
5. The toe segment is parallel to the ground during ground contact

In an adaptation of an earlier approach (Stokes et al., 1979), the combined force due to the long and short plantar tendons was represented by a single force acting in the direction of the midpoint between the two tendons. The angle between tendons (β) was taken to be 10° (Jacob, 2001) thus the angle of plantar tendon action (θ) can be calculated using Equation 1, with definitions outlined in Figure 1.

\[
θ = α - \frac{β}{2}
\]

Equation 1

First the toe is considered in isolation (Figure 2). The moments acting about the MTP joint are equal to \(F_{x1}l\). Assuming these moments are attributed to the muscular forces acting at a distance \(r_1 + \varepsilon\) from the joint centre gives Equation 2 where the length \(\varepsilon\)
was the distance from the inferior metatarsal head to the beginning of the fatty tissue under the head.

\[ F_{\text{zk}} = P(\varepsilon + r_1) \]
Equation 2

In equilibrium the sum of linear forces equate to zero, giving equations Equation 3 and Equation 4. From these, joint reaction forces and plantar tendons forces (P) can be calculated.

\[ F_{\text{tz}} + F_{\text{tzc}} + P\sin\theta = 0 \]
Equation 3
\[ F_{\text{ty}} + F_{\text{tyc}} - P\cos\theta = 0 \]
Equation 4

Now the metatarsal can be considered (Figure 3). Resolving forces axially and perpendicularly gives equations Equation 5 and Equation 6. The bending moment at midshaft can be calculated using Equation 7.

\[ F_{\text{ax}} = F_{\text{mz}}\sin\alpha - F_{\text{my}}\cos\alpha + F_{\text{y}}\cos\alpha - F_{\text{y}}\sin\alpha \]
Equation 5
\[ F_{\text{sh}} = F_{\text{mz}}\cos\alpha + F_{\text{my}}\sin\alpha - F_{\text{z}}\cos\alpha - F_{\text{y}}\sin\alpha \]
Equation 6
\[ M_{\text{be}} = \left(\frac{l_m - r_2}{2}\right)(F_{\text{mz}}\cos\alpha + F_{\text{my}}\sin\alpha - F_{\text{z}}\cos\alpha - F_{\text{y}}\sin\alpha) \]
Equation 7

Lastly, stress can be calculated using these derived forces and bending moments, and the cross-sectional geometry of the metatarsal at midshaft.
Axially, the stress is given by Equation 8, and bending stress is calculated using Equation 9.

\[ \sigma_{ax} = \frac{F_{ax}}{CSA} \]

Equation 8: Axial stress calculation where CSA represents the cross-sectional area.

\[ \sigma_{be} = \frac{M_{be}r}{I} \]

Equation 9: Bending stress calculation where \( r \) represents the radial distance from the centre of the bone to the surface, \( I \) represents the area moment of inertia about the horizontal axis of the bone cross-section.

Finally, the midshaft stresses at the dorsal and plantar bony surfaces can be calculated using Equation 10.

\[ \sigma_d = \sigma_{ax} + \sigma_{be} \]
\[ \sigma_p = \sigma_{ax} - \sigma_{be} \]

Equation 10: Normal stress acting on the upper and lower surface of the midshaft, \( d \) and \( p \) represent dorsal and plantar surfaces, \( \sigma_{ax} \) represents axial stress and \( \sigma_{be} \) represents bending stress.

To obtain estimated ground reaction forces under the second metatarsal head and toe, the plantar pressure in each cell under the metatarsal head and second toe was summed and calculated as a percentage of the pressure across all cells in that frame of stance. Vertical and anterior-posterior ground reaction forces measured using the force plate were scaled by this percentage. This was repeated for each frame of stance. Length \( l_t \) was measured from the head of the metatarsal to the point of toe contact with the ground using a flat metal rule during standing. Angle \( \alpha \) was the sagittal plane vector angle between the proximal and distal second metatarsal markers and the ground during stance.

The simplified bone geometry for the model was calculated using ImageJ (1.50i, National Institutes of Health, U.S.A.). The radii \( r_1 \) and \( r_2 \) were calculated using a circle.
fitting function from an image of the centre of the bone in the sagittal plane, ensuring the distal epiphysis was completely visible. Metatarsal length, $l_m$, was calculated in the sagittal plane on three consecutive slices in which the bone was completely in view - the mean was obtained.

Cross-sectional information was calculated using an automated custom Matlab script (Kenny et al., 2019). The cross-section image was imported and the brightness adjusted to make the cortical and trabecular bone areas more distinct from the background. A canny edge detection algorithm identified the edges of the bone and the cortical bone was divided into a series of triangles from which the area and area moment of inertia could be calculated (Figures 4 and 5). Peak values were calculated for $F_{mz}$, $F_{ax}$, $F_{sh}$, $M_{be}$, $\sigma_p$ and $\sigma_d$ and averaged over the ten trials for each participant.

**Statistical Analysis:**

Statistical analysis was conducted in SPSS (Version 24.0, SPSS Inc., Chicago, IL, USA) (discrete variables) and in Matlab using open source statistical parametric mapping (SPM) (http://www.spm1d.org (Pataky et al., 2016)), with a significance level of $P \leq 0.05$. Discrete variables (peak values and bone geometry) were examined using a Shapiro-Wilk test to confirm normality ($P \geq 0.05$). Means were compared using an independent T-Test. Effect sizes were calculated using Cohen’s d (Cohen, 1988). Time of peak stress was reported for descriptive purposes.

**Results**

There were no differences in weight or age between groups, however the NRF group was significantly taller than the RF group (1.73 ± 0.09 m vs 1.65 ± 0.07 m, $p=0.049$).

For all runners, the dorsal surface of the metatarsal was under compression
throughout stance whereas the plantar surface was under tension, with similar magnitudes of stress observed on each surface. Average peak compressive stress across the entire group of runners was 224 MPa.

Discrete Analysis

There was greater peak axial force (P = 0.001), peak bending moments (P = 0.019) and peak vGRF under the second metatarsal (P = 0.018) in NRF strikers compared to RF strikers (Table 1). However there was no difference in stresses or shear force between foot strikes. Peak dorsal stress values for each individual against body weight are presented in Figure 6. Peak bending stress contributed 96.3% (±4.39%) to the peak compressive stress on average.
SPM analysis

NRF strikers showed greater compressive stress on the dorsal surface (Figure 7A) and greater tensile stress on the plantar surface (Figure 7B) between 7.3% and 23.4% of stance (P < 0.001). There were no differences in dorsal or plantar stress at the time of peak stress.

Discussion

This study developed a novel approach to estimating metatarsal stress during running, adapted from previous beam theory models with the addition of accurate, subject-specific bone geometry and the inclusion of anterior-posterior ground and joint reaction forces. This model was used to compare stresses acting on the second metatarsal during running between runners with different habitual footstrike patterns. The dorsal compression observed throughout stance supports findings from strain gauge data (Arndt et al., 2002) with the exception that a short, initial period of dorsal tension was previously reported. These differences may be due to the location of the strain gauge and its alignment along the length of the bone. Peak pressure under the second metatarsal in the present study (RF: 412 kPa NRF: 572 kPa) was similar in magnitude to that reported by Nunns et al. (2013) (RF: 442 kPa NRF: 464 kPa). Gross and Bunch (1989) used a similar modelling approach during shod running to estimate second metatarsal strain, but modelled the cross-section as a hollow ellipse. Converting their reported strain value to stress using their reported Young’s Modulus (17 GPa) reveals stresses of 113 MPa, far lower than in the present study (224 MPa). Both models derived stress from midshaft bending moments which were similar between studies (9.35 N.m for RF strikers in the present study compared with 7.71 N.m reported by Gross and Bunch). This suggests the difference in stress magnitudes between studies is predominantly influenced by the difference in metatarsal geometry. There was a
large range of area moment of inertia values in the present study (8.15 × 10⁻¹¹ - 3.83 × 10⁻¹⁰ m⁴). When modelling the metatarsals in the present study as a hollow ellipse for comparison with Gross and Bunch the average area moment of inertia was 1.7 × 10⁻¹⁰ m⁴, 35 times smaller than the value reported by Gross and Bunch (5.8 e⁻⁹ m⁴), contributing to greater bending stress values despite similar bending moment values. Furthermore, the metatarsal stress reported by Gross and Bunch did not include the contribution due to axial compression.

In vivo strain estimates obtained during barefoot treadmill running (3.1 m.s⁻¹) from two participants were 1891 µε and 5315 µε (Milgrom et al., 2002). Using the same Young’s Modulus of 17 GPa, this equates to 32 MPa and 90 MPa respectively, also lower than in the present study. The average peak stress in the present study is higher than reported values for the failure point of cortical bone (e.g. 195 MPa, (Martin et al., 2015)) however, the reported value for the ultimate stress of cortical bone varies greatly depending on the sample site and testing method used (Wolfram and Schwiedrzik, 2016). The disparity between stress values in the present study and the literature, including data from strain gauges, suggests that the model presented here is more useful for understanding relative rather than absolute metatarsal loading values.

Compressive and tensile stresses were greater during early stance in NRF than RF strikers according to SPM analyses, but no statistically significant differences were observed at the time of peak stress. Whilst it should be noted that the group representing non-rearfoot strike runners included both midfoot, forefoot and toe strikers and these groups have different kinetic and kinematic characteristics (Nunns et al., 2013), the standard deviations of the peak stress values for this group were smaller than for the rearfoot strike group, providing confidence that this grouping is
robust when assessing peak second metatarsal stress. Observation of individual peak
stress values (Figure 6) supports this, demonstrating no marked differences in stress
magnitudes between groups, influenced in part by a wider range of values in the RF
runners. The differences in early stance could be expected based on the more anterior
foot contact in NRF than RF strikers, but it is important to note that the peak stresses
occurred at the same point during stance in the two foot strike categories. Therefore
the significant differences in stress between these groups only occurred in early stance
when the stress magnitudes were lower. The magnitude of bone stress is understood
to be important when considering risk of stress fracture, but it is not well-established
what magnitudes of peak stress may be detrimental. The results from the present
study suggest that whilst externally measured forces differ between runners with
different foot strike types, this does not equate to a difference in the magnitude of peak
metatarsal stress during running, and therefore may not influence the risk of stress
fracture via this mechanism. This does not mean that changing from a rearfoot strike
to a more anterior foot strike can be recommended as the results from the present
study were obtained from runners using their habitual foot strike. Changing foot strike
would introduce unaccustomed activity which was not considered in this analysis.

The external forces acting under the metatarsal head were significantly greater in the
NRF runners than RF runners and this was also the case for all calculated variables,
other than shear forces, that did not include subject-specific bone geometry. However
the stresses - which are influenced by subject-specific bone geometry - are similar
between groups. This supports research suggesting that external loading measures
such as plantar pressures and ground reaction forces may not be a valid method of
estimating internal loading (Matijevich et al., 2019) as well as research suggesting that
geometry is an important determinant of metatarsal stress magnitude (Nunns et al., 2017). The cross-sectional geometry in the present study was obtained using an automated approach and provided a less-simplified estimate of the geometry than used in previous beam theory approaches. The average cross-sectional area of 38 mm$^2$ in the present study falls between values of 18 mm$^2$ and 51 mm$^2$ that have previously been reported in the second metatarsal (Courtney et al., 1997, Marchi, 2005).

The model provides a useful tool for estimating internal metatarsal loading during barefoot running. However, models require assumptions and these introduce limitations. The model did not account for surrounding soft tissues in the foot. This soft tissue cushions and distributes forces, thus the model used may have overestimated stresses. Modelling the interaction of these soft tissues would be beneficial when investigating the forces in the metatarsals during running. Only non-deformable geometry was included and this does not reflect the complex three-dimensional shape of the metatarsal. The use of continuum mechanics such as a finite element model would reduce these limitations. This study assessed metatarsal stress during barefoot running, whereas the majority of runners wear shoes during running. Previous studies have shown that footwear can affect external forces differently depending on foot strike pattern (Rice et al., 2016). Assessment of metatarsal stress during barefoot running removed the confounding influence of footwear but does not truly represent the habitual running condition of the participants.

**Conclusion**
Habitual non-rearfoot strikers experience greater second metatarsal stresses during early stance than habitual rearfoot strikers during barefoot running, but similar peak stresses. This is despite non-rearfoot strikers experiencing greater peak external loading under the metatarsal head, resulting in greater peak bending moments about the midshaft than rearfoot strikers. These findings emphasise the importance of including subject-specific geometry when estimating bone stress and further supports the suggestion that external forces should not be assumed to be representative of internal loading.

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Conflict of Interest Statement
The authors declare that there is no conflict of interest regarding the content of this article.

References


