

Short-term River Streamflow Modeling Using Ensemble-based Additive Learner Approach

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Abstract

Accurate streamflow (Q_t) prediction can provide critical information for urban hydrological management strategies such as flood mitigation, long-term water resources management, land use planning and agricultural and irrigation operations. Since the mid-20th century, Artificial Intelligence (AI) models have been used in a wide range of engineering and scientific fields, and their application has increased in the last few years. In this study, the predictive capabilities of the reduced error pruning tree (REPT) model, used both as a standalone model and within five ensemble-approaches, were evaluated to predict streamflow in the Kurkursar basin in Iran. The ensemble-approaches combined the REPT model with the bootstrap aggregation (BA), random committee (RC), random subspace (RS), additive regression (AR) and disjoint aggregating (DA) (i.e. BA-REPT, RC-REPT, RS-REPT, AR-REPT and DA-REPT). The models were developed using 15 years of daily rainfall and streamflow data for the period 23 September 1997 to 22 September 2012. A set of eight different input scenarios was constructed using different combinations of the input variables to find the most effective scenario based on the linear correlation coefficient. A comprehensive suite of graphical (time-variation graph, scatter-plot, violin plot and Taylor diagram) and quantitative metrics (root mean square error (RMSE), mean

30 absolute error (MAE), Nash-Sutcliffe efficiency (NSE), Percent of BIAS (PBIAS) and the ratio of
31 RMSE to the standard deviation of observation (RSR)) was applied to evaluate the prediction
32 accuracy of the six models developed. The outcomes indicated that all models performed well
33 but the AR-REPT outperformed all the other models by rendering lower errors and higher
34 precision across a number of statistical measures. The use of the BA, RC, RS, AR and DA
35 models enhanced the performance of the standalone REPT model by about 26.82%, 18.91%,
36 7.69%, 28.99% and 28.05% respectively.

37

38 Keywords: Streamflow prediction, ensemble-based model, AR-REPT algorithm, Iran.

39

40 **1. Introduction**

41 Accurate prediction of streamflow and its patterns is vital for water resources planning and
42 management projects. The major benefit of streamflow prediction is to reduce the impact of
43 floods on infrastructure, property, and public health by issuing warnings for impending flood
44 events. Moreover, streamflow prediction can provide hydrologists significant information to
45 develop the sustainable design of water infrastructure, examine the behavior of rivers for
46 operational purposes, water quality assessment, the estimation of water prices, and the adoption
47 of sustainable agricultural practices (Güven, 2009; Yaseen et al., 2015). However, this is not an
48 easy task due to its complexity, dynamic character, randomness, and non-linearity which results
49 from the effect of the numerous physical mechanisms and characteristics involved in its
50 generation, namely interception and stemflow, soil characteristics, catchment characteristics
51 (topography and shape), land-use and land-cover, evapotranspiration and climate change.

52 Methods for streamflow prediction can be classified into short-term and long-term forecasting
53 categories. Short-term (real-time) flood forecasting (e.g., hourly and daily) is important for the
54 development of early warning systems (Chiang et al., 2004; Guven, 2009; Yaseen et al., 2015),
55 while long-term forecasting (e.g., weekly, monthly, and annually) is of vital importance for the
56 appropriate planning of reservoir management, erosion control, efficient hydro-power
57 generation, irrigation management decisions, scheduling water releases, and many other
58 applications.

59 Generally, there are four main methodologies used for streamflow forecasting, namely empirical
60 formulas, statistical models, conceptual/physically-based modeling and data-driven techniques.
61 Empirical formulas (i.e. Creager, Fuller, and Dicken) are simple methods developed based on
62 specific datasets and for given catchment conditions, thus, they are not accurate for use in other
63 catchments and therefore not very popular among hydrologists. The coefficients in these
64 equations are determined for a specific catchment and hence, they are not reliable for other
65 catchments, particularly those located in different climates. Since the publication of the
66 pioneering study by Box and Jenkins in 1970, the classical statistical black-box time-series
67 models, such as Auto Regressive Moving Average (ARMA), Auto Regressive Integrated
68 Moving Average (ARIMA), Auto Regressive Integrated Moving Average with exogenous input
69 (ARIMAX), (simple) Linear Regression (LR), and Multiple Linear Regression (MLR) have been
70 frequently employed for streamflow forecasting (Box and Jenkins, 1970; Salas, 1980; Wu et al.,
71 2009; Valipour et al., 2012a,b; Valipour, 2012, 2015; Valipour et al., 2013;). However, these
72 models fail to capture the non-stationary and non-linear character of streamflow processes.
73 Conceptual or physically-based hydrological models can be used for understanding the complex
74 generation of runoff in a catchment. Physically-based distributed approaches, like MIKE SHE,

75 are developed based on pixel-scale catchment characteristics, and therefore require great effort,
76 the inclusion of numerous hydrological variables, and therefore a large amount of input data
77 (Costabile et al. 2012). These models are difficult to implement due to the great volume of data
78 required for calibration, which is especially challenging to obtain in developing countries like
79 Iran (Yaseen et al, 2017).

80 In recent decades, data-driven or soft computing (SC) approaches have received increasing
81 attention among hydrologists and have been used on a wide range of hydrological applications,
82 including streamflow forecasting, to formulate the non-linear relationships between the predictor
83 and predicted variables. They require less input data and fewer parameters to develop the model
84 (Carlson et al. 1970; Hipel and Mcleod 1994; Ahmed and Sarma 2007; Afan et al. 2014; Singh
85 and Cui 2015). SC models are very successful and common tools used for prediction and
86 forecasting due to its ability to extract patterns from historical data, which is used for the
87 prediction of future events. They also have a non-linear and more flexible structure and the
88 ability to predict complex phenomena with high accuracy. They generally lead to excellent
89 results with good level of agreement between predicted and observed data when used for
90 streamflow forecasting (Chen et al., 2015; Deo and Sahin, 2016; Huang et al., 2014;
91 Kasiviswanathan et al., 2016; Meshgi et al., 2015; Zhang et al., 2015). Examples of such
92 methods, that have been used in streamflow prediction, are Artificial Neural Network (ANN),
93 Support Vector Machine (SVM), Adaptive Neuro Fuzzy Inference System (ANFIS), Genetic
94 Algorithm (GA), Gene Expression Programming (GEP), Extreme Learning Machine (ELM), and
95 Neuro-Wavelet Techniques (Nourani et al. 2014; Yaseen et al. 2015; Malik et al. 2020).
96 Moreover, these are widely adopted to solve hydrological problems including rainfall and

97 precipitation forecasting (Nourani et al., 2009), sediment transport (Kisi et al., 2012), and
98 groundwater modeling (Taormina et al., 2012; Tapoglou et al., 2014; French et al., 1992).

99 ANNs, which are the approach most widely used model in hydrological applications, can be
100 classified into two types: (1) supervised (e.g., Feed Forward Back Propagation (FFBP), Radial
101 Basis Function (RBF), Multi-Layer Perceptron (MLP), and Generalized Regression Neural
102 Network (GRNN)), and (2) unsupervised (e.g., Self-Organizing Map (SOM)), which has been
103 employed in numerous studies for streamflow modeling and forecasting (Abrahart and See,
104 2000; Allawi and El-Shafie, 2016; Bray and Han, 2004; Cigizoglu, 2005; Danandeh Mehr et al.,
105 2014; Deo and Sahin, 2016; Ghorbani et al., 2016; Hsu et al., 2002; Singh et al. 2018; Liu and
106 Shi. 2019). Recently, the popularity of ANNs has decreased due to their low convergence speed
107 and low generalization ability, especially when the data record is short for training purposes,
108 and/or the range of the testing data is out of that used for training (Hooshyaripor et al. 2014),
109 which leads to local minimum and the random initial determination of weights in each
110 simulation. Adaptive neuro-fuzzy inference systems (ANFIS) were developed to overcome most
111 of the limitations of ANNs, through the use of an ensemble approach (i.e. coupling ANNs with
112 fuzzy logic). Anusree and Varghese (2016) compared the modeling performance of ANN and
113 ANFIS for daily streamflow prediction in the Karuvannur catchment and they reported an
114 improvement in accuracy of ANFIS over ANN, but this approach also has weaknesses.
115 Limitations in ANFIS arise from inefficiencies when defining the weights of membership
116 functions, which significantly affect the model's predictive potential (Bui et al. 2016). Support
117 vector machine (SVM) is a type of neuron based approach which has been reported to be more
118 powerful than ANFIS and ANNs. Quej et al. (2017) applied ANFIS, ANN and SVM models for
119 the prediction of solar radiation in the Yucatán Peninsula, México, and found that the SVM

120 model outperforms the other two models. The superiority of SVM over ANFIS and ANN
121 algorithms has also been reported for streamflow prediction (Kakaei Lafdani et al., 2013; He et
122 al., 2014). In addition, the lack of transparency in the results is another unfavourable
123 characteristic of some methods like the SVM, which can be tackled by adopting non-parametric
124 techniques (Auria and Moro, 2009). SVM is also susceptible to hyper-parameter selection
125 (Burgess, 1998; Waseem Ahmad et al., 2018).

126 Though significant progress has been accomplished in the development and application of SC
127 models to hydrology, researchers are still exploring novel, robust, and more reliable approaches
128 to overcome the shortcomings of the traditional approaches. New developments in data mining
129 as well as the recent advances in modeling capabilities of AI techniques promise to offer more
130 reliable approaches for solving regression problems in a diverse range of scientific realms
131 (Sharafati et al, 2019; Khosravi et al. 2019). For example, in the field of hydrology, Random
132 forest (RF) methods have been recently applied to predict apparent shear stress in channels
133 (Khozani et al., 2019), random tree (RT) algorithms were used to predict nitrate and strontium in
134 groundwater (Bui et al., 2020a) and solar radiation (Sharafati et al., 2019), Reduced Error
135 Pruning Tree (REPTree), random committee (RC), M5P and Instance-Based K-nearest (IBK)
136 neighbours were applied for the prediction of fluoride concentration in groundwater (Khosravi et
137 al., 2020a), Cross-Validation Parameter Selection (CVPS) and Randomizable Filtered
138 Classification (RFC) were used to predict water quality (Bui et al., 2020b), the Bagging
139 Algorithm (BA) was used to predict bedload transport rates (Khosravi et al., 2020b), and the
140 Kstar model applied to predict suspended sediment load prediction (Salih et al., 2019). In
141 addition to the studies mentioned above, additional research have focussed in the comparison of
142 these new the algorithms over traditional SC ones, demonstrating their superiority in several

143 studies across a wide range of hydrology applications. For example, Sihag et al. (2020) reported
144 a superior performance of the RF model over the SVM and ANN for modeling infiltration
145 processes. They showed that the RF model has a better prediction potential than the SVM and
146 MLP models. Granata et al. (2018) found that the performance of the RF and M5P models was
147 superior to that of the SVM model for the prediction of spring discharges in Italy.

148 A more recent development to achieve higher prediction performance is based on the use of
149 ensemble-based approaches, which have attracted the attention of researchers all over the world
150 due to their flexibility and benefit of combining multiple models with well-known advantages.
151 For example, Khosravi et al. (2020b) demonstrated an enhanced performance of an ensemble-
152 based approach by combining the RF, M5P, RT and REPT with the BA model. Bui et al. (2020b)
153 used an ensemble-based approach by combining the BA and CVPS models with RF, M5P, RT
154 and REPT, and found out that hybridization can improve the models' prediction potential.

155 In this study we explore the use of a new set of ensemble-based algorithms to investigate
156 possible improvements in their prediction potential with respect to standard stand-alone models
157 frequently used for streamflow prediction in the past studies. This will allow us to overcome not
158 only the limitations of the more traditional approaches (low convergence speed, low
159 generalization potential for short input data time series), but also enhance the performance of
160 more advanced stand-alone models and avoid the problem of overfitting and complex tree
161 selection. The REPT algorithm has been successfully applied in many different areas of
162 hydrology, and has therefore been selected in the current study as the base-model for streamflow
163 prediction in the Kurkursar catchment (Iran). The REPT algorithm integrates Reduced Error
164 Pruning (REP) with a Decision Tree algorithm. The REP has the advantage of reducing the
165 complexity of the tree structure without reducing the model performance, and preventing over-

166 fitting problems. We pursue the main goal of improving prediction potential of the standalone
167 REPT model by developing and investigating the performance of five ensemble-based
168 algorithms, generated by combining the REPT model with the BA, random committee (RC),
169 random subspace (RS), additive regression (AR) and disjoint aggregating (DA) algorithms.
170 Although the BA-REPT, RC-REPT and RS-REPT have been already employed in hydrological
171 applications, AR-REPT and DA-REPT models are new ensemble-based models which have not
172 yet been previously used hydrology or any other geosciences, application.

173

174 **2- Study area**

175 The Kurkursar catchment is located in northern Iran between longitudes 51°29' and 51°42' E and
176 latitudes 36°29' and 36°40' N, has an area of 75.495 km² (Fig 1). The catchment's mean altitude
177 is about 860 m, and the overall mean slope is around 21.80%. The catchment has a skewed shape
178 and is bounded on the north by the Caspian Sea, on the south by the Mashlak River and a portion
179 of the Chalus catchment, and on the west by the Chalus catchment. Various geomorphological
180 forms such as flood plains, alluvial fans, and sedimentary dams have been identified in the
181 catchment. The region has a Mediterranean climate with average annual rainfall and streamflow
182 of 900 mm and 1.2 m³/s, respectively. The maximum and minimum discharges are 78 and 0.002
183 m³/s, respectively. Seventy-nine percent of the heavy precipitation events take place during
184 November to April. The annual maximum daily rainfall occurs with a frequency of 33% in
185 autumn, 42% in winter, and 25% in spring seasons (Rashidi et al. 2016). Temperatures during
186 the year range from below 0°C during winter to 45°C during summer. The Kurkursar catchment
187 is located upstream of Noshahr city, so accurate prediction of its discharge is imperative for the

188 establishment of meaningful flood mitigation plans for this city. Some recent disastrous flood
189 events have caused irreparable damages to infrastructure in the study area, including bridges,
190 rural buildings, main roads, water and gas pipelines, and the agricultural sector.

191
192 Fig 1. Location of the Kurkursar River and the Hydrometry station in the catchment (after
193 Rashidi et al. 2016)

194

195 **3-Methodology**

196 **3.1-Data collection and preparation**

197 Data for a 15-year period (23 September 1997 to 22 September 2012), including precipitation
198 and discharge for the Kurkursar river, were collected and compiled from the Mazandaran
199 Meteorological Organization and regional water authority. The daily rainfall (R_t) time series data
200 were obtained from four meteorological weather stations equipped with rainfall gauges, and
201 streamflow (Q_t) data was sourced from the Kurkursar hydrometric station situated at outlet of the
202 Kurkursar catchment. Spatially averaged values of rainfall data for the catchment were obtained
203 using the Thiessen polygon approach (Melesse et al. 2011) and used as an input to the model.

204 The entire dataset was divided into two periods, the first portion comprising 70% of the data
205 (from 23 September 1997 to 22 September 2008) was used as training dataset for model
206 development, and the second portion including the remaining 30% of the data (from 23
207 September 2008 to 22 September 2012) was used as validation dataset (Ayele et al. 2017;
208 Khsoarvi et al. 2018c; Termeh et al. 2019; Nohani et al. 2019) for model evaluation purposes.
209 Some basic statistical information on the training and validation datasets is presented in Table 1.

210

211 Table 1. Basic statistics for the training and testing datasets

212

213 **3.2. Different input variables combination scenarios**

214 Auto-correlation and linear correlation coefficients (r) were applied to define effective input
215 variables for streamflow prediction. Rainfall (R_t) and streamflow (Q_t) values, and their values at
216 lag-times of 1, 2, 3 days (i.e. R_{t-1} , R_{t-2} , R_{t-3} and Q_{t-1} , Q_{t-2} , Q_{t-3}) were used to identify the best input
217 variable combination. Based on the r -values, eight different input scenarios were constructed and
218 examined (Table 2). Each scenario was constructed according to coefficient value between input
219 and target variables. The first scenario was based on the assumption that the variable with the
220 highest r -value is able to predict streamflow with high accuracy. Next, the variable with the
221 second highest r -value was added to the first scenario to build the second scenario. This approach
222 was continued until the variable with the lowest r -value was added to construct the last input
223 scenario (Table 2). During this stage, each model was implemented using default operator
224 values, just to determine the impact of each input scenario on the results. The r criterion was
225 applied to determine the most effective scenario, with higher r leading to the most effective the
226 input scenario.

227

228 Table 2. Different input scenarios

229

230 **3.3-Determination of optimal operator values**

231 Optimal values for the various operators were obtained through a trial and error method (Kisi et
232 al. 2012, 2016; Khosravi et al, 2018a, Sharafati et al, 2019) using the Waikato Environment for
233 Knowledge Analysis (WEKA 3.9) software developed by University of Waikato, New Zealand.
234 At first each model was implemented using default values of the operators, and then a wide
235 range of higher and lower values was examined until the optimum values for each operator was
236 determined. The Root Mean Square Error (RMSE) metric was applied to obtain optimum
237 operators, with lowest RMSE leading to optimum values.

238 **3.4- Description of models**

239 As mentioned in the introduction, a standalone and five ensemble-based data-mining algorithms,
240 namely REPT, BA-REPT, RC-REPT, RS-REPT, AR-REPT and DA-REPT, were employed to
241 model and predict streamflow at the Kurkursar River outlet using the WEKA software 3.9.

242 ***3.4.1-Reduced error pruning tree (REPT)***

243 The REPT model is well known as the fastest tree learner, and it is developed as a combination
244 of the Reduced Error Pruning (REP) and the Decision Tree (DT) learning algorithm methods. It
245 is constructed as a decision or regression tree based on information gains or reductions in the
246 variance (Mohamed et al., 2012). First, the DT algorithm is utilized to simplify the modeling
247 process using the training dataset for the production of a large number of trees with various sizes.
248 The best tree, based on the accuracy of data classification and avoids misclassification, is chosen.
249 Then, the REP is employed to reduce the complexity of the structure of the chosen decision tree
250 and to prevent overfitting problems (Mohamed et al., 2012). The REP algorithm is one of the
251 simplest and most popular pruning techniques, and aims at eliminating some branches to obtain

252 the most accurate sub-tree through the post-pruning method (Chen et al., 2009; Esposito et al.,
253 1999; Mohamed et al. 2013)

254 **3.4.2-Bootstrap aggregating (BA)**

255 The BA is known as one of the most effective ensemble methods in which repeated sampling
256 builds different data subsets, raising the extent and diversity of component learners by training
257 the data subsets (Opitz:1999). This model is capable of solving classification and regression
258 problems by reducing the defects of component learners and recognizing unstable classifiers. In
259 the algorithm, based on the core idea of BA, the training process is done through in the following
260 main steps: (i) generating bootstrap samples randomly and independently from the original
261 training dataset by replacing; (ii) repeating bootstrap samples several times to create a certain
262 amount of independent datasets; (iii) determining a weak learning algorithm to train various sub-
263 datasets and obtaining the sequence of predictive functions; and (iv) voting for outcomes to
264 select the outcome with the highest number of votes as the final result (Bauer and Kohavi,
265 1999). BA has extensively been combined with various weak classifiers to improve many base
266 learners, such as decision trees (Mert et al., 2014), SVMs (Pham et al., 2018), and naïve Bayes
267 trees (Pham and Prakash, 2017). In this study, the BA has been used to train the REPT base
268 learner for rainfall-runoff modeling.

269 **3.4.3-Random committee (RC)**

270 Random committee is a meta-algorithm, which has proven very efficient for the enhancement of
271 the learning ability of most classifiers. This algorithm is able to construct a hybrid of base
272 classifiers. In the present study, the final estimation of a random tree was produced through
273 straight averaging probability prediction (Khosravi, 2018a). Although RCs use different numbers
274 of seeds, the classifiers are created based on similar data. The algorithm in this study was applied

275 in 10 iterations with a number of seeds of 1 using the same parameters as those in the
276 development of the RT model.

277 **3.4.4-Random subspace (RS)**

278 RS is a combination of a data mining and a parallel learning algorithm introduced by Ho (1998).
279 This model is similar to the BA, which is known as a classic integrated algorithm, as it builds a
280 decision tree using the classifier that has the highest level of precision and accuracy based on the
281 training data (Mielniczuk and Teisseyre 2014). The only difference between RS and BA is that in
282 the former, the training subset is created based on the original randomly selected training set
283 (Mielniczuk and Teisseyre, 2014; Xia et al., 2015). The features of the series for each training
284 sub-classifier in the final prediction results are obtained through a combination of voting
285 methods (Zhang and Jia, 2007). The operation of the sub-classifiers relies on integrated learning
286 diversity. The subcategories of RS are employed to specify the differences in the training
287 performances of sub-classifiers and the adopted ensemble learning method is used to pool
288 samples with various spatial specifications (Nanni and Lumini, 2008).

289 **3.4.5. Additive regression (AR)**

290 Structured additive regression (Fahrmeir et al., 2004) is a nonparametric regression method
291 which was proposed first by Breiman and Friedman in 1985. The AR is considered as an
292 indispensable section of the alternating conditional-expectations algorithm. This algorithm is
293 able to provide a generalization of the generalized linear and additive models by building a
294 restricted class of non-parametric regressions. During each iteration of the AR algorithm, the
295 standalone model (i.e. REPT) is fit to the residuals from the former iteration. Finally during the
296 last iteration, the final prediction is generated from adding all previous predictions together. It is

297 also a more flexible and interpretable predictor than the general regression. In generic notation, a
298 brief description of the AR predictor is given by:

$$299 \quad F(\mathbf{X}) = \sum_{m=0}^M \beta_m h(\mathbf{X}; \mathbf{a}_m) \quad (1)$$

300 where $h(\mathbf{X}; \mathbf{a}_m)$ are unknown as the basic function and independent model output made by
301 inputs \mathbf{X} and model parameters \mathbf{a}_m at iteration m ($m = 1, \dots, M$ and M is the number of
302 iterations), β_m are a set of basis coefficients at iteration m , and $F(\mathbf{X})$ is the AR algorithm output.

303 The best results are achieved when the standalone and AR algorithms' parameters (\mathbf{a}_m and β_m)
304 are used in a stepwise method (i.e., each set of parameters is estimated at a particular iteration).

305 Fig 2 shows the conceptual model of developing the hybrid model by coupling AR with the
306 standalone algorithms (here as an example, REPT).

307

308 Fig 2. Conceptual model for the development of the AR hybrid algorithms (Mitchell, 1997)

309 **3.4.6. Disjoint aggregating (Dagging)**

310 The Disjoint Aggregating (Dagging) is a resampling integration and group-sampling technique
311 that was proposed by Ting and Witten (1997). Dagging and Bagging work in a similar way but in
312 the Dagging method, the training dataset is used for classification of several disjoint subsets by
313 using separate samples rather than bootstrap samples (Chen et al., 2019b). In the Dagging model,
314 the majority voting combines several classifiers to build the final prediction and improve the
315 accuracies of the basic classifiers (Kotsianti and Kanellopoulos 2007). In order to build a robust
316 model, the weak learners are trained on various subsets of the training set (Onan et al., 2016).

317

318 **3. 5. Model evaluation and comparison**

319 In order to evaluate the performance of each of the models developed, and to compare their
320 efficiency, six statistical metrics, namely the coefficient of determination (R^2), RMSE, Mean
321 Absolute Error (MAE), Nash-Sutcliffe Efficiency (NSE), Percentage of bias (PBIAS), and the
322 ratio of RMSE to the standard deviation of the observations (RSR) were utilized for validation
323 period (Table 3).

324

325 **Table 3.** Different indicators used for streamflow (Q_t) prediction performance (Q_t^{obs} and Q_t^{pred}
326 are the measured and predicted values of Q_t , respectively, $\overline{Q_t^{pred}}$ is the mean predicted value of
327 Q_t , and N is the sample size number of data)

328

329 In addition to the statistical metrics, three commonly used graphical approaches, namely scatter
330 plots, Taylor diagrams (Taylor 2001) and Violin plots were used to visually compare the
331 performances of the models. In the scatter plot, a lower scatter of cloud points around the 1:1 line
332 indicates higher model accuracy. The Violin plot shows the mean, median, maximum, and
333 minimum predicted values, and similar shapes of the violin plots for the predicted and observed
334 values indicate high model performance. This approach allows for a better evaluation of the
335 models in terms of their accuracy for predicting extreme values. The Taylor diagram
336 incorporates the linear correlation coefficient (r), standard deviation, and RMSE simultaneously.
337 The advantages of this comprehensive assessment have made it a popular criterion for
338 visualizing overall model performance (Choubin et al. 2018).

339 **4- Results and analysis**

340 4.1- Best Input Combination

341 Selecting the optimal input variables is the first step in developing a predictive artificial
342 intelligence model. Also as the effectiveness of each input variable is not equal, and some of
343 them might have a null or negative effect on the results, it is necessary to determine the
344 effectiveness of each of the input variables. In the present study the r approach between inputs
345 and outputs has been applied to determine the effectiveness of each input variable (Fig 3). The
346 results reveal that rainfall values (R_t) are the most effective variables for Q_t prediction ($r = 0.56$),
347 followed by Q_{t-1} ($r = 0.46$), Q_{t-2} ($r = 0.29$), R_{t-1} ($r = 0.28$), Q_{t-3} ($r = 0.25$), R_{t-2} ($r = 0.12$) and R_{t-3}
348 ($r = 0.07$). Accordingly, and as expected, it was found that the greater the lag-time, the lower the
349 r value and the predictive effectiveness of the variable.

350

351 Fig 3. r value between input variables and streamflow

352

353 Eight different input combinations scenarios were constructed and compared (Table 4), the
354 effectiveness of each input combination was evaluated in the training and validation phases using
355 the estimated r . The results of the r value during the validation phase showed that the best input
356 combination scenario is different for every model developed. Combination No. 7 (i.e.
357 combination of all input variables) had the highest r values and proved to be the most effective
358 for the standalone REPT model. For all the ensemble based models, with the exception of RC-
359 REPT, the input scenario No. 8 (i.e. combination of R_t , R_{t-1} , and Q_{t-1} variables) was identified as
360 the most effective scenario. For the RC-REPT model, combination No. 3, which is the
361 combination of R_t , Q_{t-1} , and Q_{t-2} variables, is the optimum input scenario. These results are in

362 agreement with the findings of variable importance using r , which showed that variables with
363 low r are not effective for the prediction of complex phenomena like streamflow, which has also
364 been reported in previous studies (Yaseen et al. 2017). It can be concluded that specifying the
365 optimal value for each operator and choosing the best input variable play a decisive role in the
366 predictive potential of each model. The results shown in Table 4 indicate that best input scenario
367 (i.e. gray shadow) has about 18.18%, 31.86%, 29.54%, 26.19%, 32.6% and 31.18% higher
368 predictive potential (for REPT, BA-REPT, RC-REPT, RS-REPT, AR-REPT and DA-REPT,
369 respectively) than the worst input scenario, and this obviously highlights the importance of the
370 selection of the best input scenario on the results.

371 Discrepancy between the models' performance at this stage, results from the different
372 computational structure of each algorithm. It shows that for the standalone REPT model to
373 achieve high prediction potential, the input needs to involve all different variables, and that even
374 in this case, it still has a lower performance than the ensemble-based models. From a modeling
375 perspective, the best model should have two characteristics; (1) high performance and (2) require
376 a lower number of input variables, as sometimes, measuring some input variables is difficult and
377 time consuming. Thus, our result show that the standalone model (i.e. REPT) is not the best
378 option as it involves a high number of input variables.

379 Table 4. Efficiency of different input scenarios for the training and validation phases based on
380 the r metric

381

382 **4.2- Evaluation of the developed models**

383 After identifying the best input combination scenario and the optimal value for each operator, the
384 performance of each of the models developed using the training dataset, was assessed using the
385 validation dataset in the evaluation stage. The results of this evaluation were used to estimate and
386 compare model performance (Khosravi et al 2016; 2018a.b; 2019; 2020a; Chen et al, 2019a).
387 Time-variation graphs and scatter plots for the measured and predicted streamflow values are
388 presented in Figure 4. These results indicate that the AR-REPT model is remarkably more
389 accurate in capturing peak-flow values than the other models, as indicated by less scatter in the
390 cloud points. Therefore, it has the best predictive potential for the estimation of streamflow,
391 while the standalone REPT model, with the highest scatter in cloud points, has the worst
392 prediction ability. Performance of the other models has an acceptable level of accuracy.

393 Fig 4. Time-variation graph and scatter plot for the measured vs. predicted values over the
394 validation period

395

396 Figure 5 presents the results for the violin plots obtained for all models, and shows the
397 maximum, minimum, median (Q_{50}), first quartile (Q_{25}), and third quartile (Q_{75}) of the predicted
398 Q_t and the measured Q_t values. It can be seen that the BA-REPT, DA-REPT and AR-REPT
399 ensemble based models are able to predict the maximum streamflow values accurately.
400 Maximum streamflow is the source of flooding and its prediction with high accuracy is very
401 important for the design of flood mitigation plans. The outcomes indicate that the AR-REPT
402 model has the higher prediction accuracy for lower streamflow values. Overall, the violin plots
403 show that the plot corresponding to the AR-REPT ensemble based model has a closer shape to
404 that of the plot for the measured values.

405

406

Fig 5. Violin plots for the measured and predicted streamflow values

407

408 For further analysis of the efficiency of the developed models, a Taylor diagram is presented in
409 Figure 6. This diagram confirms the superiority of the AR-REPT model compared with the other
410 data-driven models, and that the REPT model has the lowest prediction potential. It shows that
411 the r values obtained using measured data and the prediction results obtained using the AR-, DA-
412 and BA- ensemble-based models vary between 0.90 and 0.95, while the r values for the
413 remaining models vary between 0.80 and 0.90.

414

415

Fig 6. Taylor diagram to visualize the performance of the models

416

417 Six quantitatively statistical performance criteria to assess the performance of the developed
418 models over the evaluation period are presented in Table 5. Based on the R^2 criteria, all
419 developed algorithms have a very good performance (Ayele et al., 2017). Since R^2 is
420 standardized for detecting the differences between the mean and variance of the measured and
421 predicted values, and it is highly sensitive to outliers, it is not capable of evaluating the
422 performance of the models by itself (Legates and McCabe, 1999; Shiri and Kisi, 2012), so other
423 metrics (NSE and RSR) are used to further assess model performance.

424

425 Based on the NSE and RSR metrics, REPT, RC-REPT and RS-REPT have a good performance,
while the remaining algorithms have a very good prediction capability. Over all, the AR-REPT

426 model ($R^2 = 0.857$, $RMSE = 0.682 \text{ m}^3/\text{s}$, $MAE = 0.258 \text{ m}^3/\text{s}$, $NSE = 0.845$, $PBIAS = -3.150$ and
427 $RSR = 0.392$) outperforms all the other models, followed by DA-REPT ($R^2 = 0.848$, $RMSE =$
428 $0.706 \text{ m}^3/\text{s}$, $MAE = 0.274 \text{ m}^3/\text{s}$, $NSE = 0.834$, $PBIAS = -3.602$ and $RSR = 0.406$), BA-REPT (R^2
429 $= 0.834$, $RMSE = 0.730 \text{ m}^3/\text{s}$, $MAE = 0.300 \text{ m}^3/\text{s}$, $NSE = 0.820$, $PBIAS = -2.100$ and $RSR =$
430 0.420), RS-REPT ($R^2 = 0.790$, $RMSE = 0.880 \text{ m}^3/\text{s}$, $MAE = 0.350 \text{ m}^3/\text{s}$, $NSE = 0.740$, $PBIAS = -$
431 2.800 and $RSR = 0.500$), RC-REPT ($R^2 = 0.706$, $RMSE = 1.000 \text{ m}^3/\text{s}$, $MAE = 0.450 \text{ m}^3/\text{s}$,
432 $NSE = 0.650$, $PBIAS = -4.900$ and $RSR = 0.590$) and REPT ($R^2 = 0.704$, $RMSE = 1.200 \text{ m}^3/\text{s}$, MAE
433 $= 0.420 \text{ m}^3/\text{s}$, $NSE = 0.600$, $PBIAS = -3.300$ and $RSR = 0.630$) (Table 5 and 6) (In Table 6, the
434 best model gets a lower rank for each criteria).

435

436 Table 5. Quantitative model evaluation for the validation phase

437

438 Table 6. Model performance ranking

439

440 5. Discussion

441 Streamflow in the Kurkursar catchment is predicted in the present study through several
442 standalone and ensemble-based machine learning algorithms. Our results show that the
443 ensemble-based models developed have a higher performance than the standalone model. Based
444 on the NSE metric, the BA-, RC-, RS-, AR- and DA- models enhance the performance of the
445 standalone REPT model by about 26.82%, 18.91%, 7.69%, 28.99% and 28.05% respectively. In
446 addition, our results show that all the models developed in this study have a reasonably good
447 capability to predict the streamflow. The main reason is that Kurkursar catchment is located in

448 North of Iran, and has a Mediterranean climate and thus rainfall patterns are fairly regular, while
449 the rainfall patterns in arid and semi-arid regions display larger temporal variable leading to
450 more complex rainfall-runoff processes and lower predictability of streamflow patterns based on
451 rainfall.

452 The fact that the AR model outperforms the other models, is likely to be due to the use of the 1D
453 smoother approach to construct a restricted class of non-parametric regression. This results in the
454 model to be less affected by the Curse of dimensionality. The DA algorithm utilizes the majority
455 voting approach to build the final prediction (Tama and Comuzzi, 2019), and through this, a
456 robust and reliable prediction can be achieved by the weak learners being trained on a different
457 subset of the training set (Onan et al., 2016). Using multiple weak learners in combination, the
458 BA has a better performance than the RC and RS ensemble-based models by reducing (1)
459 variance and (2) over-fitting through the bootstrap procedure. In most cases, hybrid models are
460 more flexible and can provide better prediction than individual models. Therefore, ensemble-
461 based models are more reliable and accurate, especially for predictions of complex hydrological
462 processes like the one in the present study (Ghorbani et al., 2017; Yaseen et al., 2017, De'ath and
463 Fabricius, 2000).

464 Results from previous studies using SC approaches have also reported excellent model
465 performance for streamflow prediction. For example, Kisi et al. (2012) used ANN, Gene
466 Expression Programming (GEP), and ANFIS algorithms for streamflow modeling in Turkey and
467 observed that GPE performed better than the other two models. The R^2 values for obtained for
468 ANN, GEP, ANFIS, and MLR were 0.97, 0.93, 0.80, and 0.70, respectively. Rajurkar et al.
469 (2000) modelled daily flows in India using ANN hydrological models. They obtained an R^2 of
470 0.92 and NSE of 0.702 for the best ANN model. Rezaie-Balf et al. (2017) simulated rainfall-

471 runoff processes in the Tajan catchment in northern Iran using a tree algorithm of model tree
472 (MT), ANN and multivariate adaptive regression splines (MARS). They concentrated on the
473 effects of data input size, involving the number of effective input variables for rainfall-runoff
474 processes and the number of data values in the time series, on the quality of the runoff
475 simulation. They found that the data mining model (i.e. MT) ($R^2 = 0.80$ and $RMSE = 6.70 \text{ m}^3 \text{ s}^{-1}$)
476 was superior to ANN ($R^2 = 0.78$ and $RMSE = 7.40 \text{ m}^3/\text{s}$) and MARS ($R^2 = 0.79$ and $RMSE =$
477 $7.47 \text{ m}^3/\text{s}$). It is important to note that the direct comparison of different models and their
478 prediction potential applied to datasets from different catchments is very difficult. Each
479 catchment has different characteristics and the main processes driving streamflow generation can
480 be very different across various catchments, so direct comparison is problematic. For example,
481 predictions from the effective ensemble-based model used in this study resulted in an R^2 of 0.85,
482 while Kisi et al. (2012) obtained an R^2 of 0.97 for streamflow prediction using an ANN model.
483 However, as mentioned in the introduction, several studies using ANN models have reported
484 much lower predictive performance. An important factor that affects the results in our study is
485 that the model is used to predict short-term or real-time flows, while many of the previous
486 studies have focused on long-term predictions. In addition, differences in algorithm structure
487 lead to very different model behavior, which are also affected by parameter selection, nature of
488 the amount data, data quality and length of the dataset (Asim et al. 2018).

489 There are several sources of uncertainty in the present study such as those stemming from the
490 analysis of a single study area; the randomized splitting of data into training and testing sets; the
491 uncertainty in the quality of input data and also from input variable selection. Also the lack of
492 availability of additional input variables such as evaporation, temperature, soil moisture data, etc.
493 are the main limitation of the current study, as additional input variables are highly desirable for

494 streamflow prediction. As a final note, each model has its own advantages and disadvantages and
495 they are different in terms of structure and complexity (Khosravi et al., 2018c). Different
496 artificial intelligence models, empirical equations, and physically based models have been
497 utilized in various studies for the simulation of hydrological processes. It is important to employ
498 a variety of physically based models to predict the streamflow (*e.g.*, SWAT, Wetspa, HEC-HMS,
499 SimHyd), validate their outputs using data mining algorithms, and, ultimately, based on the
500 characteristics of the models including complexity, data requirements, and accuracy, identify the
501 best model for future research. Further work is needed to investigate the generalization power of
502 these algorithms for streamflow prediction, which will include the application of the algorithms
503 developed in this study for other catchments with similar physical and climatic conditions. Also,
504 results can be used to generate management strategies for flooding at this particular catchment.

505

506 **6. Conclusions**

507 Streamflow prediction is essential for flood impact assessment, and the implementation of useful
508 flood management plans, however, due to the non-linear and chaotic nature of streamflow
509 generation processes, it remains a challenging task. To date, no universal guidelines have been
510 reported for streamflow prediction. In the present study, a standalone REPT model and five
511 ensemble-based data mining models (BA-REPT, RC-REPT, RS-REPT, DA-REPT and AR-
512 REPT) were employed to predict streamflow in the Kurkursar catchment in Iran. The main
513 findings of the study can be summarized as follows:

- 514 • R_t is the most effective variable for streamflow prediction followed by Q_{t-1} , Q_{t-2} , R_{t-1} ,
515 Q_{t-3} , R_{t-2} and R_{t-3}

- 516 • The greater the lag-time of each input variable, the lower its correlation coefficient and
517 effectiveness for prediction purposes.
- 518 • Due to the different structures of the models, the best input combination was not the same
519 for all the models applied.
- 520 • The AR-REPT ensemble-based model outperformed all the other models, followed by
521 DA-REPT, BA-REPT, RC-REPT, RS-REPT and REPT.
- 522 • The BA, RC, RS, AR and DA models enhance the performance of the standalone REPT
523 model by about 26.82%, 18.91%, 7.69%, 28.99% and 28.05% respectively.
- 524 • The PBIAS values showed that all the models overestimated streamflow.
- 525 • The violin-plots showed that the AR-REPT and DA-REPT ensemble-based models were
526 the best for predicting extreme streamflow values.

527

528 **Authorship contribution statement**

529 **KK:** conceptualization, model implementation and software, formal analysis, manuscript writing
530 and editing. **SM:** manuscript writing and interpretation of results. **PMS:** provided critical insights
531 on the analysis and contributed to writing and editing the manuscript and **RF:** Review and
532 editing.

533

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823 **Figure caption**

824 **Fig 1.** Location of the Kurkursar River and the Hydrometry station in the catchment (after
825 Rashidi et al. 2016)

826 **Fig 2.** Conceptual model of working AR hybrid algorithms (Mitchell, 1997)

827 **Fig 3.** r value between input variables and streamflow

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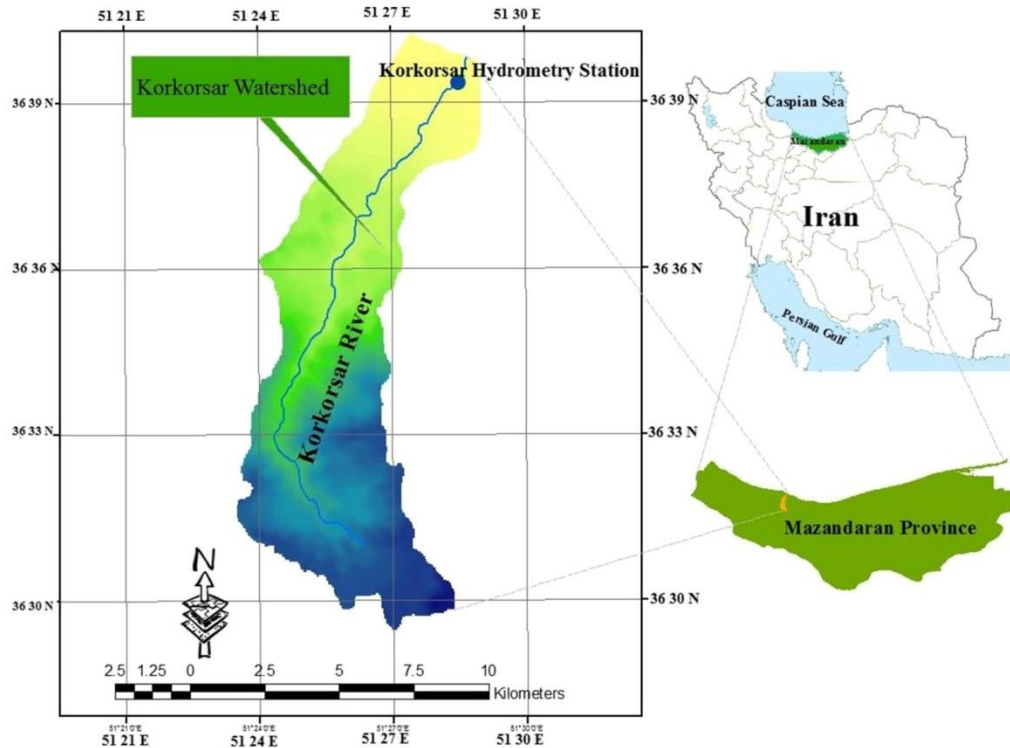
829 **Fig 4.** Time-variation graph and scatter plot for the measured vs. predicted values over the
830 validation period

831 **Fig 5.** Violin plots for the measured and predicted streamflow values

832 **Fig 6.** Taylor diagram to visualize the performance of the models

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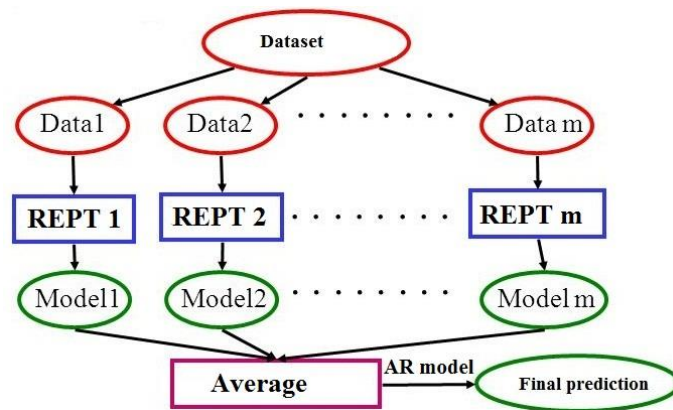
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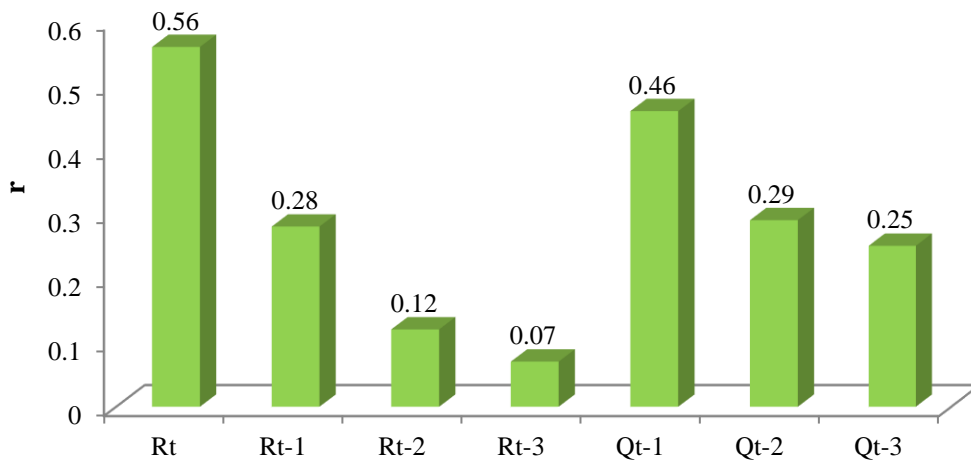
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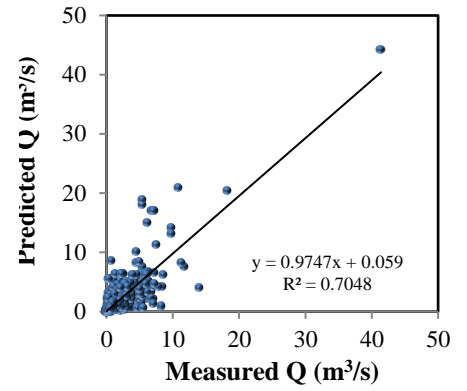
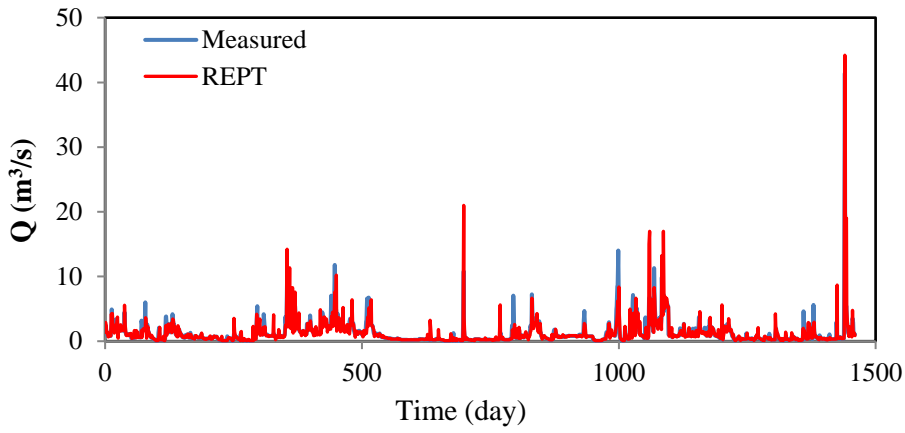
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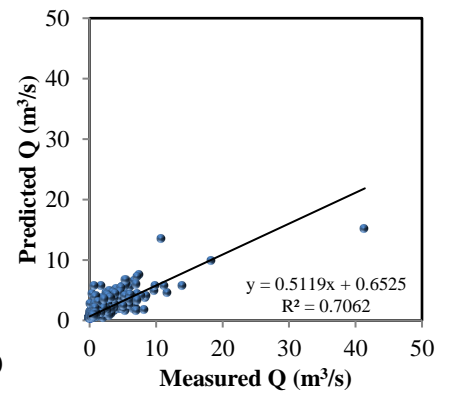
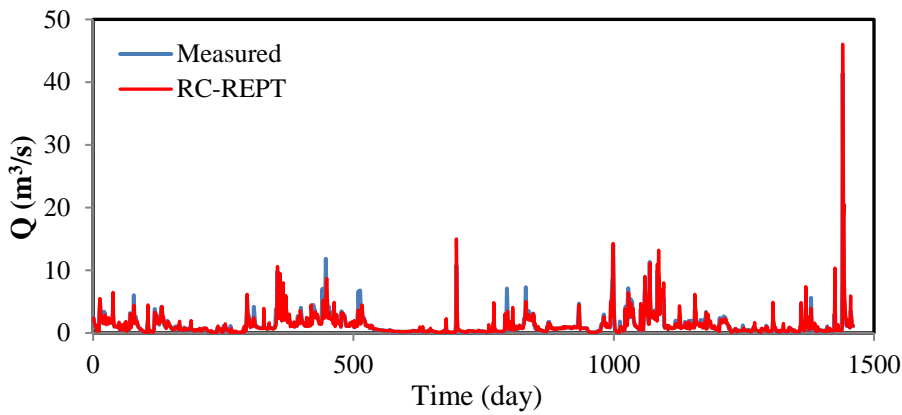
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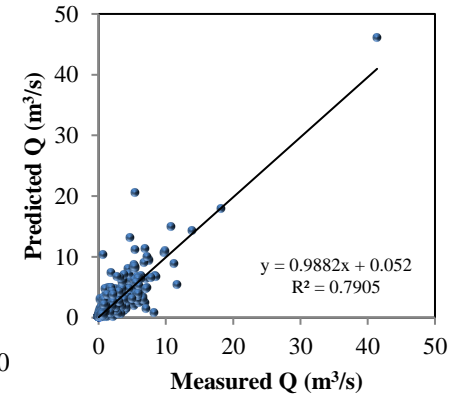
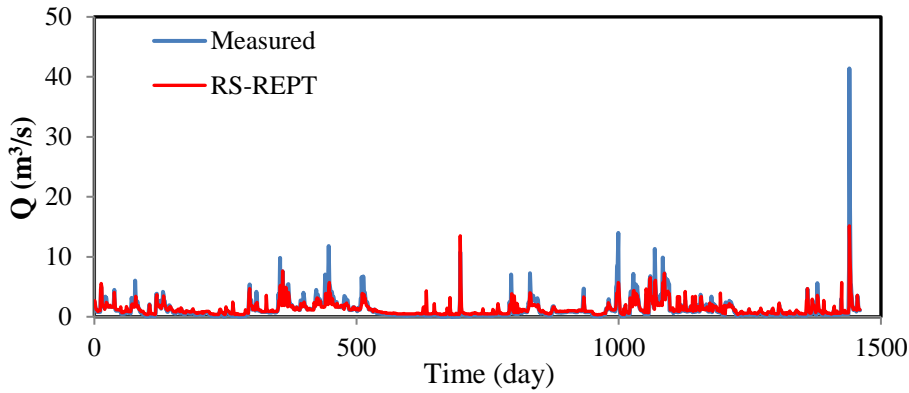
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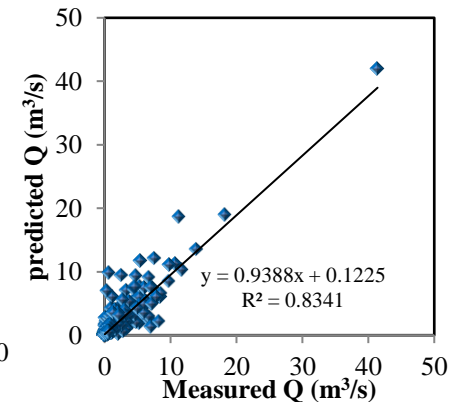
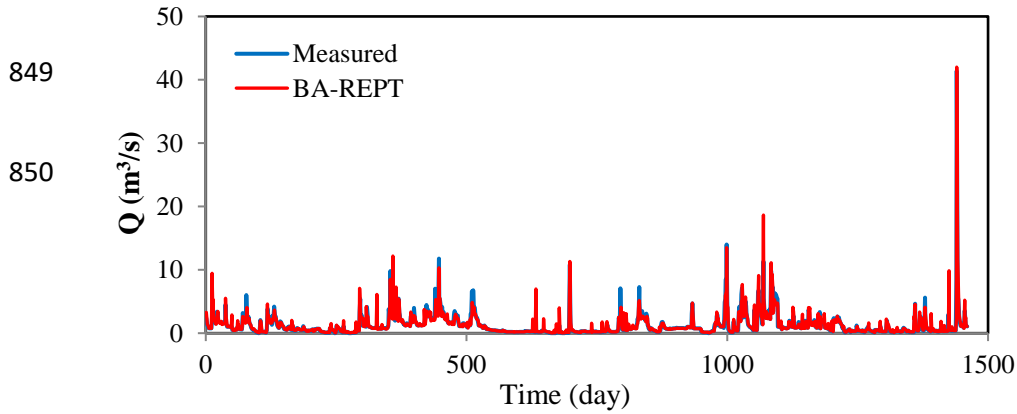
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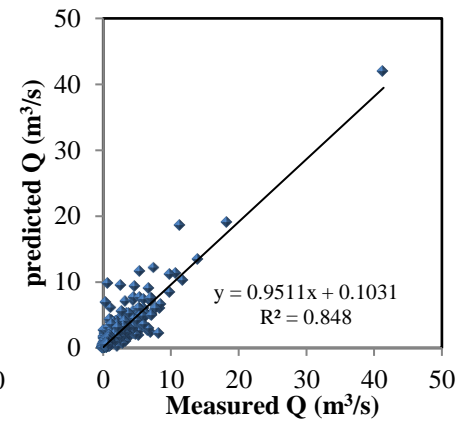
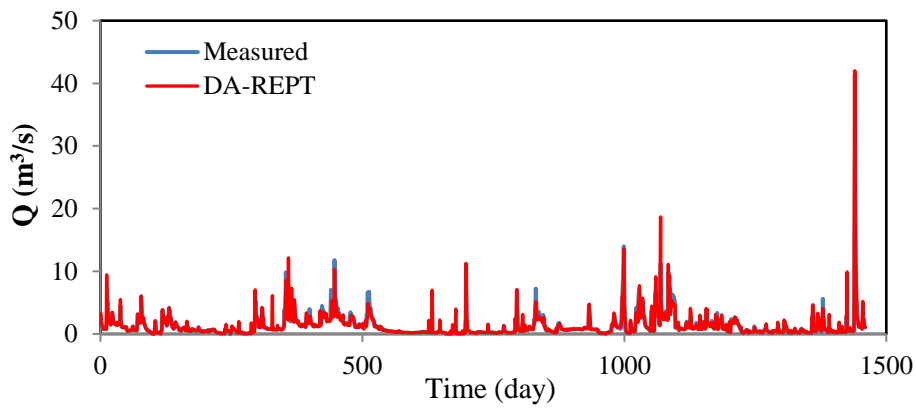
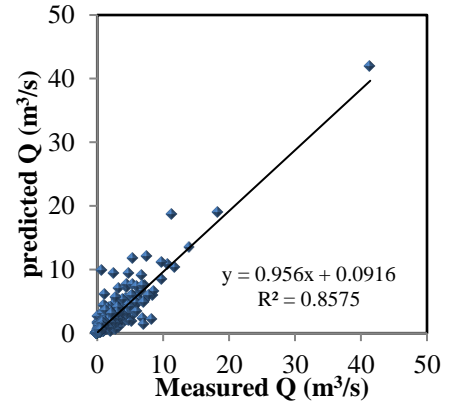
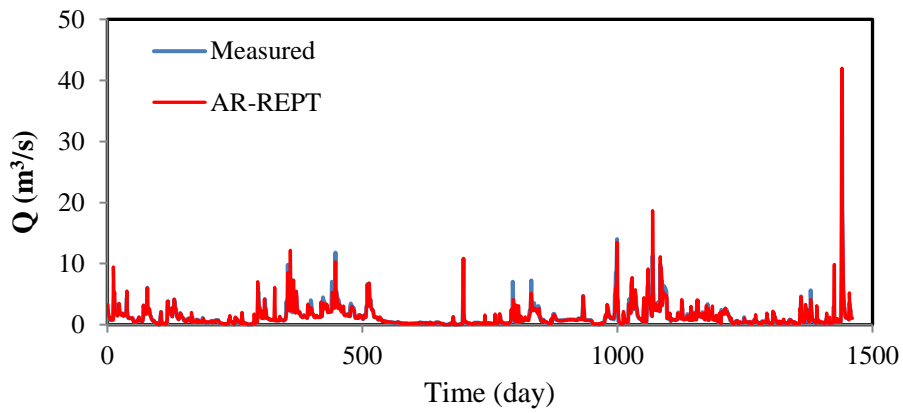


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852 Fig 4. Time-variation graph and scatter plot for the measured vs. predicted values over the
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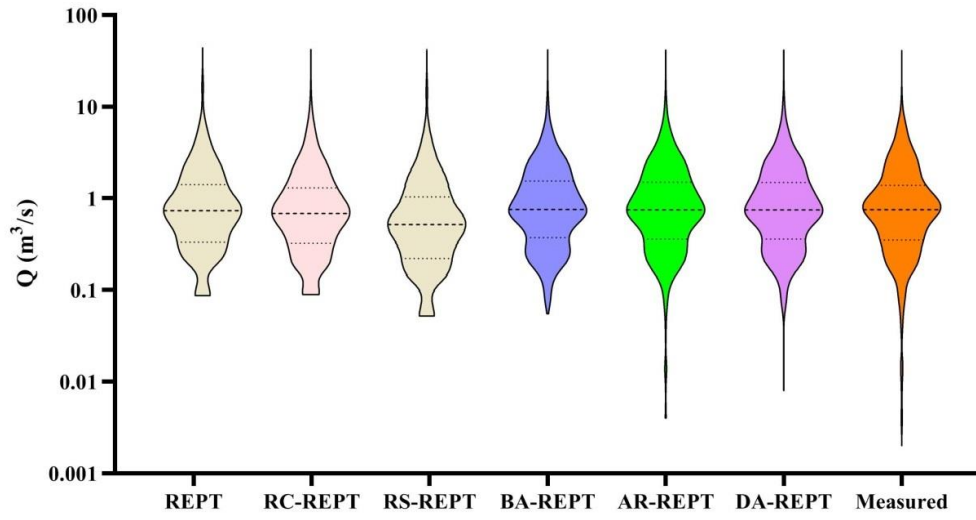
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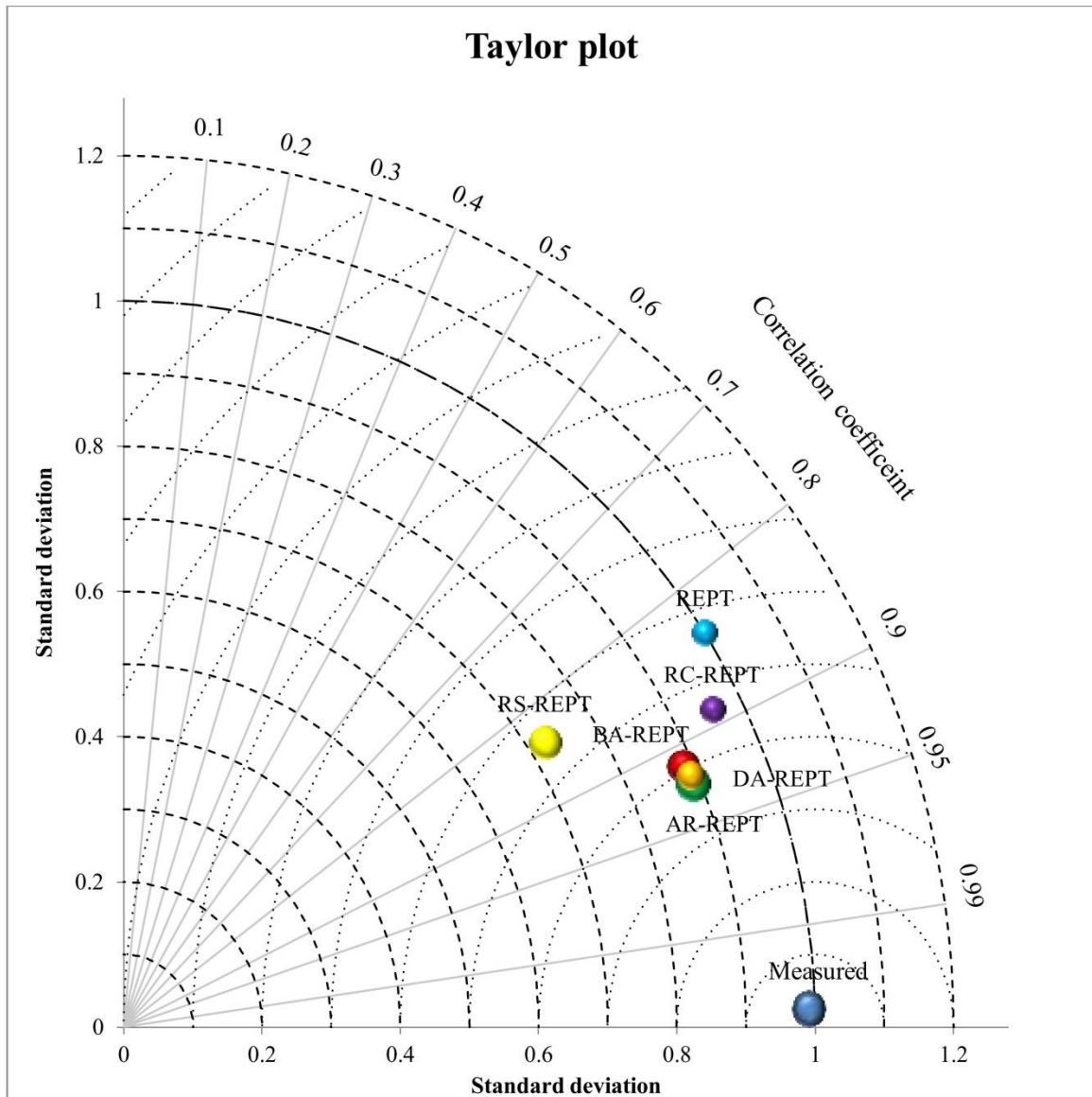
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Fig 5. Violin plots for the measured and predicted streamflow values



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Fig 6. Taylor diagram to visualize the performance of the models

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868 **Table caption**

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870 **Table 1.** Basic statistics for the training and testing datasets

871 **Table 2.** Different input scenarios

872

873 **Table 3.** Different indicators used for streamflow prediction (Q_t) (Q_t^{obs} and Q_t^{pred} are the
874 measured and predicted values of Q_t , respectively, $\overline{Q_t^{pred}}$ is the mean predicted value of Q_t , and N
875 is the sample size number of data)

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877 **Table 4.** Efficiency of different input scenarios for the training and validation phases based on the
878 correlation coefficient metric

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880 **Table 5.** Model evaluation quantitatively during validation phase

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882 **Table 6.** Model performance ranking

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886

887 Table 1. Basic statistics for the training and testing datasets

Variables	Training dataset				Validation dataset			
	Min	Max	Mean	Std. deviation	Min	Max	Mean	Std. deviation
Rainfall	5.00	149.00	3.47	11.43	0.00	147.00	3.42	10.69
Streamflow	0.73	73.10	1.28	2.25	0.002	41.40	1.21	1.74

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Table 2. Different input scenarios

No.	input combination	Output
1	R_t	Q_t
2	R_t, Q_{t-1}	Q_t
3	R_t, Q_{t-1}, Q_{t-2}	Q_t
4	$R_t, Q_{t-1}, Q_{t-2}, R_{t-1}$	Q_t
5	$R_t, Q_{t-1}, Q_{t-2}, R_{t-1}, Q_{t-3}$	Q_t
6	$R_t, Q_{t-1}, Q_{t-2}, R_{t-1}, Q_{t-3}, R_{t-2}$	Q_t
7	$R_t, Q_{t-1}, Q_{t-2}, R_{t-1}, Q_{t-3}, R_{t-2}, R_{t-3}$	Q_t
8	R_t, R_{t-1}, Q_{t-1}	Q_t

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Table 3. Different indicators used for streamflow prediction (Q_t) (Q_t^{obs} and Q_t^{pred} are the measured and predicted values of Q_t , respectively, $\overline{Q_t^{pred}}$ is the mean predicted value of Q_t , and N is the sample size number of data)

Equation	Ref.	Range	Performance
$R^2 = 1 - \left(\frac{\sum_{i=1}^N (Q_t^{obs} - Q_t^{pred})^2}{\sum_{i=1}^N (Q_t^{obs})^2} \right)$	Najafi and Ardabili (2018)	$0.7 \leq R^2 \leq 0.1$ $0.6 \leq R^2 \leq 0.7$ $0.5 \leq R^2 \leq 0.6$ $0 \leq R^2 \leq 0.5$	Very good Good Satisfactory Unsatisfactory
$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^N (Q_t^{pred} - Q_t^{obs})^2}$	(Najafi and Ardabili 2018)		The lower the better
$MSE = \frac{1}{N} \sum_{i=1}^N (Q_{t_i}^{pred} - Q_{t_i}^{obs})^2$	(Najafi and Ardabili 2018)		The lower the better
$NSE = 1 - \frac{\sum_{i=1}^N (Q_t^{pred} - Q_t^{obs})^2}{\sum_{i=1}^N (Q_t^{pred} - \overline{Q_t^{pred}})^2}$	Moriasi et al, 2007	$0.75 < NSE \leq 1.00$ $0.65 < NSE \leq 0.75$ $0.50 < NSE \leq 0.65$ $0.4 < NSE \leq 0.50$ $NSE \leq 0.4$	Very good Good Satisfactory Acceptable Unsatisfactory
$PBIAS = \frac{\sum_{i=1}^N (Q_t^{pred} - Q_t^{obs})}{\sum_{i=1}^N Q_t^{pred}}$	Legates et al, 1999	$PBIAS < \pm 10\%$ $\pm 10\% \leq PBIAS < \pm 15\%$ $\pm 15\% \leq PBIAS < \pm 25\%$ $PBIAS \geq \pm 25\%$	Very good Good Satisfactory Unsatisfactory

$RSR = \sqrt{\frac{\sum_{i=1}^{i=N} (Q_t^{pred} - Q_t^{obs})^2}{\sum_{i=1}^{i=N} (Q_t^{pred} - \overline{Q_t^{pred}})^2}}$	Gupta et al. 1999	$0 \leq RSR \leq 0.50$ $0.50 < RSR \leq 0.60$ $0.60 < RSR \leq 0.70$ $RSR > 0.70$	Very good Good Satisfactory Unsatisfactory
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897 Table 4. Efficiency of different input scenarios for the training and validation phases based on the
898 correlation coefficient metric

Input	REPT		BA-REPT		RC-REPT		RS-REPT		AR-REPT		DA-REPT	
No.	Training	Testing	Training	Testing	Training	Testing	Training	Testing	Training	Testing	Training	Testing
1	0.79	0.63	0.65	0.62	0.79	0.63	0.79	0.63	0.66	0.63	0.67	0.64
2	0.99	0.75	0.96	0.81	0.99	0.75	0.9	0.66	0.96	0.82	0.97	0.83
3	0.99	0.73	0.95	0.84	0.99	0.88	0.99	0.75	0.95	0.85	0.96	0.85
4	0.99	0.71	0.81	0.85	0.99	0.82	0.98	0.74	0.83	0.85	0.85	0.86
5	0.99	0.77	0.95	0.83	0.99	0.79	0.99	0.81	0.96	0.84	0.97	0.85
6	0.99	0.69	0.96	0.86	0.99	0.82	0.98	0.69	0.97	0.87	0.97	0.88
7	0.99	0.74	0.96	0.86	0.99	0.8	0.87	0.82	0.97	0.87	0.98	0.88
8	0.99	0.73	0.93	0.91	0.99	0.81	0.87	0.84	0.97	0.92	0.97	0.93

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Table 5. Model evaluation quantitatively during validation phase

Models	R ²	RMSE (m ³ /s)	MAE (m ³ /s)	NSE	PBIAS (%)	RSR
REPT	0.704	1.25	0.420	0.600	-3.300	0.630
BA-REPT	0.834	0.73	0.300	0.820	-2.100	0.420
RC-REPT	0.706	1.000	0.450	0.650	-4.900	0.590
RS-REPT	0.790	0.88	0.350	0.740	-2.800	0.500
AR-REPT	0.857	0.682	0.258	0.845	-3.150	0.392
DA-REPT	0.848	0.706	0.274	0.834	-3.602	0.406

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Table 6. Model performance ranking

Models	R ²	RMSE (m ³ /s)	MAE (m ³ /s)	NSE	PBIAS (%)	RSR	Sum	Rank
REPT	6	6	5	6	4	6	33	6
BA-REPT	3	3	3	3	1	3	16	3

RC-REPT	5	5	6	5	6	5	32	5
RS-REPT	4	4	4	4	2	4	22	4
AR-REPT	1	1	1	1	3	1	8	1
DA-REPT	2	2	2	2	5	2	15	2

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