

1 Modulation of pulsatile GnRH dynamics 2 across the ovarian cycle via changes in 3 the network excitability and basal activity 4 of the arcuate kisspeptin network.

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16 **Abstract**

17 Pulsatile GnRH release is essential for normal reproductive function. Kisspeptin secreting
18 neurons found in the arcuate nucleus, known as KNDy neurons for co-expressing neurokinin
19 B, and dynorphin, drive pulsatile GnRH release. Furthermore, gonadal steroids regulate
20 GnRH pulsatile dynamics across the ovarian cycle by altering KNDy neurons' signalling
21 properties. However, the precise mechanism of regulation remains mostly unknown. To
22 better understand these mechanisms we start by perturbing the KNDy system at different
23 stages of the estrous cycle using optogenetics. We find that optogenetic stimulation of KNDy
24 neurons stimulates pulsatile GnRH/LH secretion in estrous mice but inhibits it in diestrous
25 mice. These in-vivo results in combination with mathematical modelling suggest that the
26 transition between estrus and diestrus is underpinned by well-orchestrated changes in
27 neuropeptide signalling and in the excitability of the KNDy population controlled via
28 glutamate signalling. Guided by model predictions, we show that blocking glutamate
29 signalling in diestrous animals inhibits LH pulses, and that optic stimulation of the KNDy
30 population mitigates this inhibition. In estrous mice, disruption of glutamate signalling
31 inhibits pulses generated via sustained low-frequency optic stimulation of the KNDy
32 population, supporting the idea that the level of network excitability is critical for pulse

33 generation. Our results reconcile previous puzzling findings regarding the estradiol-
34 dependent effect that several neuromodulators have on the GnRH pulse generator dynamics.
35 Therefore, we anticipate our model to be a cornerstone for a more quantitative understanding
36 of the pathways via which gonadal steroids regulate GnRH pulse generator dynamics.
37 Finally, our results could inform useful repurposing of drugs targeting the glutamate system
38 in reproductive therapy.

39 **Introduction**

40 The dynamics of gonadotropin-releasing hormone (GnRH) secretion is critical for
41 reproductive health. In female animals, GnRH secretion is tightly regulated across the
42 ovarian cycle. Pulsatile secretion dominates most of the cycle, with frequency and amplitude
43 modulated by the ovarian steroid feedback. Positive feedback from increasing estradiol levels
44 triggers a preovulatory surge of GnRH/LH secretion (Christian and Moenter, 2010).
45 Furthermore, there is ample evidence that ARC kisspeptin neurons are prime mediators of the
46 ovarian steroid feedback on the pulsatile dynamics of GnRH/LH secretion (McQuillan et al.,
47 2019), although the mechanisms remain unclear.

48 *In-vitro* studies have shown that gonadal steroids have a dramatic effect on the
49 electrophysiology of ARC kisspeptin neurons. For instance, spontaneous firing activity of
50 ARC kisspeptin neurons from castrated mice appears elevated compared to intact animals
51 (Ruka et al., 2016) and estradiol replacement attenuates ARC kisspeptin neuron activity in
52 gonadectomised animals (Ruka et al., 2016; Wang et al., 2018). More recently, fiber
53 photometry data from female mice show that the ARC kisspeptin neuronal population
54 (KNDy network) pulses at a relatively constant frequency throughout the ovarian cycle apart
55 from the estrous phase where the frequency is dramatically reduced (McQuillan et al., 2019).
56 This slowdown of LH frequency is thought to be a direct consequence of the increasing
57 progesterone levels associated with ovulation (McQuillan et al., 2019), although studies using
58 the rhesus monkey show that raising pre-ovulatory estrogen levels are also important
59 (O'Byrne et al., 1991). Studies in sheep indicate the inhibitory effects of progesterone are
60 mediated through increased dynorphin signalling (Goodman et al., 2011; Moore et al., 2018),
61 however this is less clear in mice where ovarian steroids have a negative effect on Dyn
62 mRNA levels (Navarro et al., 2009).

63 Perplexing is also the differential effect of various neuromodulators on LH secretion
64 depending on the gonadal steroid background. For instance, N-methyl-D-aspartate (NMDA)

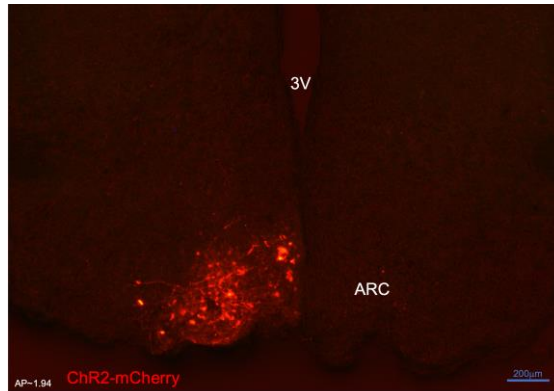
65 robustly inhibits LH pulses in the ovariectomized monkey whereas in the presence of
66 estradiol this effect is reversed, and NMDA stimulates LH secretion (Reyes et al., 1990;
67 Reyes et al., 1991). Similar reversal of action on LH dynamics depending on the underlying
68 ovarian steroid milieu has been also documented for other neurotransmitter and
69 neuropeptides in other species (Kalra and Kalra, 1983; Brann and Mahesh, 1992; Arias et al.,
70 1993; Bonavera et al., 1994; Scorticati et al., 2004) and highlights the complex mechanisms
71 underlying the modulation the GnRH pulse generator by gonadal steroids.

72 Here, using mathematical modelling along with optogenetic stimulation of ARC kisspeptin
73 neurons we embark to understand how the dynamics of the pulse generator are modulated
74 across the ovarian cycle. Our mathematical model suggests that the level of excitability
75 within the ARC kisspeptin network—the propensity of kisspeptin neurons to signal and
76 activate each other—is one of the key parameters modulated in different stages of the cycle
77 by gonadal steroids. Previous studies have shown that ARC kisspeptin neurons synapse on
78 each other (Yip et al., 2015; Qiu et al., 2016) and are glutamatergic (Cravo et al., 2011; Qiu
79 et al., 2011; Kelly et al., 2013; Nestor et al., 2016; Qiu et al., 2016; Wang et al., 2018). Based
80 on these findings we hypothesise that population excitability should be enabled primarily via
81 glutamate signalling. We test our predictions *in-vivo* and show that glutamatergic
82 transmission is an important factor for the pulsatile behaviour of the KNDy network.

83 **Results**

84 **The dynamic response of the KNDy network to sustained, low-frequency optic** 85 **stimulation is estrous cycle dependent.**

86 Using optogenetics we perturbed the KNDy network to test whether and how sex steroids
87 modulate the system's dynamical response. ARC kisspeptin-expressing neurons were
88 transduced with a Cre-dependent adeno-associated virus (AAV9-EF1-dflox-hChR2-
89 (H134R)-mCherryWPRE-hGH) to express ChR2 (Fig. 1; see Materials and Methods) and
90 were optogenetically stimulated at the estrous and the diestrous phase of the cycle, measuring
91 LH pulse frequency as a readout. Sustained, low-frequency optic stimulation was used to
92 emulate elevated basal activity in ARC kisspeptin neurons or persistent stimulatory signals to
93 the KNDy population from other neuronal populations.



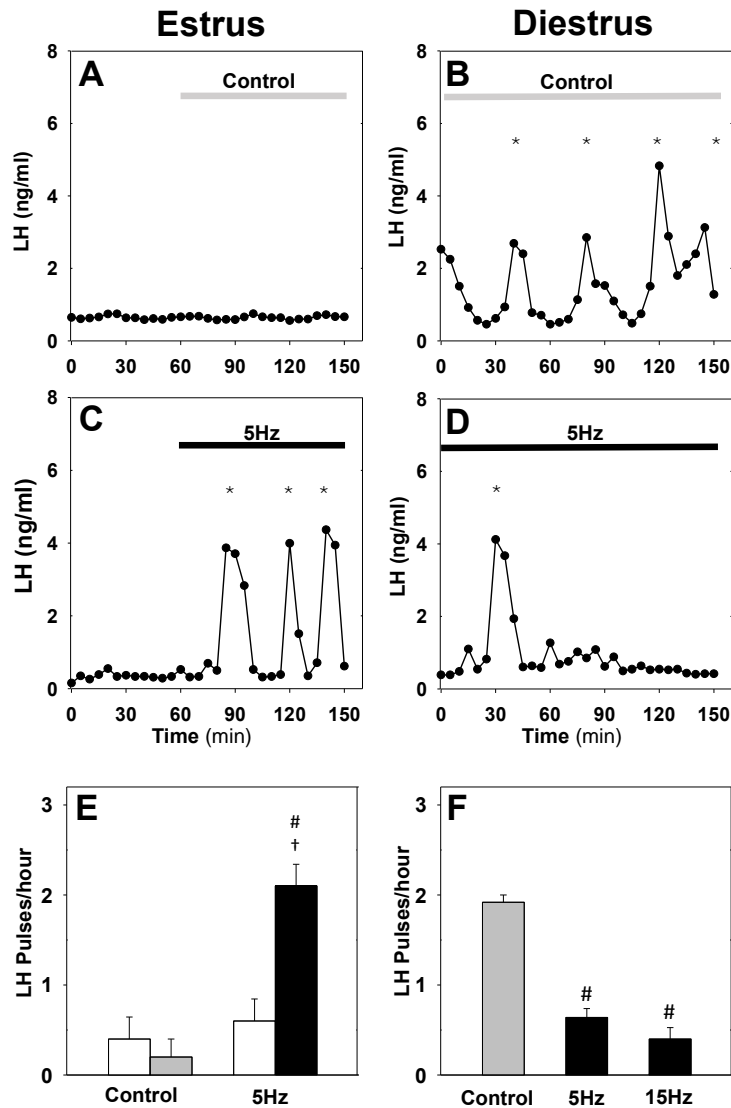
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95 **Figure 1. Expression of arcuate nucleus (ARC) kisspeptin neurones with ChR2-mCherry in Kiss-Cre**
96 **mouse.** Coronal section showing red mCherry fluorescence positive neurons in the ARC which indicates ChR2
97 receptor expressing kisspeptin neurones, following unilateral injection of AAV9.EF1.dfloxed.hChR2(H134R)-
98 mCherry.WPRE.hGH into the ARC of Kiss-Cre mouse. Note the absence of mCherry fluorescence in the other
99 side of ARC. 3V, Third ventricle.

100

101 In estrous mice, we find that sustained optogenetic stimulation of ARC kisspeptin neurons at
102 5Hz immediately triggers robust LH pulses at a frequency of 2.10 ± 0.24 pulses/hour (Fig. 2
103 A,C&E), which is in agreement with our previous findings (Voliotis et al., 2019) and
104 highlights how pulsatile dynamics can emerge as a population phenomenon without the need
105 of a pulsatile activation signal (Strogatz, 2018). In diestrous mice, on the other hand,
106 optogenetic stimulation of ARC kisspeptin neurons at 5Hz has a subtle slowdown effect on
107 LH pulse frequency over the 1.5 h stimulation period (Fig. 2-figure supplement 1). To
108 investigate this response in greater detail we revised our experimental protocol, removing the
109 control period and extending the stimulation period to 2.5 h. With the extended protocol we
110 measure 0.64 ± 0.09 and 0.40 ± 0.13 LH pulses/hour under sustained optic stimulation at 5
111 and 15Hz, respectively; these frequencies are significantly lower than the LH pulse frequency
112 we observe in control animals, which receive no optic stimulation (Fig. 2 B,D&F). We note
113 that we observe normal LH pulse frequencies in WT animals receiving sustained optic
114 stimulation for 2.5h (Fig. 2-figure supplement 2).

115 Our data illustrate how natural variation of ovarian steroids across the ovarian cycle leads to
116 qualitative changes in the dynamical response of ARC kisspeptin neurons to optical
117 stimulation. These changes are most probably driven by the effect that gonadal steroids have
118 on the intrinsic electrophysiological properties of ARC kisspeptin neurons (Ruka et al., 2016)
119 and the neuromodulator signalling capacity within the KNDy network (Vanacker et al.,
120 2017).



121

122 **Figure 2. Differential effect of optic stimulation of ARC kisspeptin neurons in estrous and diestrous Kiss-**
 123 **Cre mice. (A-B) Representative examples showing LH secretion in response to no stimulation (grey bar) or**
 124 **sustained blue light (473 nm, 5-ms pulse width, black bar) activation of kisspeptin neurons at 5 Hz in estrous**
 125 **(C) and diestrous (D) mice. (E) Summary showing mean \pm SEM LH pulse frequency over the 60min control**
 126 **period (white bars) and over the subsequent stimulation period (black bar) in estrous mice. (F) Summary**
 127 **showing mean \pm SEM LH pulse frequency in the control (grey bar) and stimulated (black bars) diestrous mice.**
 128 *Denote LH pulses. #P < 0.05 vs control; †P < 0.05 vs pre-stimulation; n = 5-6 per group.

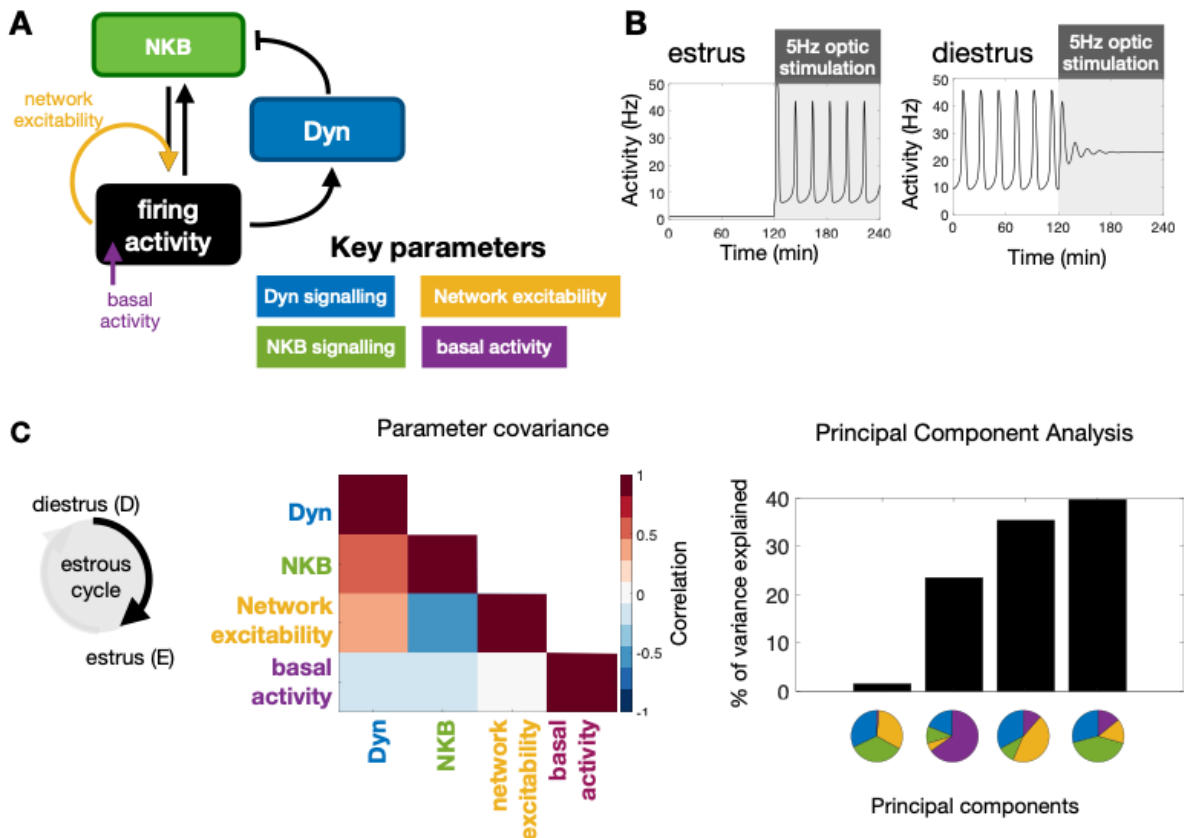
129 **A mathematical model predicts key mechanisms modulating the behaviour of the KNDy**
 130 **pulse generator across the estrous cycle.**

131 Interrogating the KNDy network at different stages of the estous cycle via optic stimulation
 132 and measuring the effect on LH pulse frequency allows use of our mathematical model
 133 (Voliotis et al., 2019) to understand how key system parameters change under gonadal steroid
 134 control. The model describes the dynamical behaviour of ARC kisspeptin neurons using three

135 dynamical variables: representing the levels of Dyn, NKB and neuronal activity (Fig. 3 A).
136 Furthermore, rather than focusing on the biophysical details of regulation, the model
137 postulates that gonadal steroids could potentially modulate the behaviour of the KNDy
138 system across the cycle via acting on four system-level parameters: (i) level of Dyn
139 signalling, (ii) level of NKB signalling, (iii) network excitability (i.e., propensity of neurons
140 in the population to transmit signals to one another), and (iv) basal neuronal activity.
141 Employing Bayesian inference techniques (see material and methods), we sample values for
142 these four parameters, which allow the model to replicate the mean LH frequency we observe
143 experimentally in estrus and diestrus mice with and without 5Hz optic stimulation (Fig. 2
144 E&F). Inspection of the dynamical behaviour of the model, using the identified diestrus
145 parameter values, reveals that in response to optic stimulation in diestrus pulsatile dynamics
146 could die out gradually (i.e, there is a transient period before activity shuts down; see Fig. 3 B
147 for an illustrative example), which is confirmed by the delayed inhibition of LH pulses we
148 observed experimentally in diestrus mice.

149 Next, we focus on how the four key parameters change between diestrus and estrus. We
150 measure the change in each parameter using the log-ratio of its estrous to diestrus value and
151 calculate the covariance matrix of these log-ratios from our set of inferred parameter values.
152 We find a positive (linear) correlation between changes in Dyn and NKB signalling strength,
153 and negative (linear) correlation between changes in NKB signalling strength and network
154 excitability (Fig. 3 C). That is, the model predicts that NKB signalling strength and network
155 excitability are characterised by opposite (in direction) correlations during the transition from
156 diestrus to estrus (one decreasing the other increasing; we note the model predicts that both
157 combinations are possible), whereas NKB and Dyn signalling remain correlated in the same
158 direction (either increasing or decreasing; we note the model predicts that both combinations
159 are possible). Finally, we apply Principal Component Analysis to study the sensitivity of the
160 system with respect to changes in the four parameters (see Materials and Methods). We
161 calculate the principal components in dataset with the inferred parameter changes. Principal
162 components explaining small portions of the variance in the dataset (i.e., principal component
163 with the smallest eigenvalue) correspond to parameter combinations to which the system
164 dynamics are most sensitive (stiff parameter combinations). These combinations are the most
165 critical in terms of regulation as small deviations in how these parameters co-vary result in
166 significant shifts in the system's dynamics. Interestingly, the principal component capturing
167 the smallest share of the variance is comprised of the parameters controlling NKB signalling,
168 Dyn signalling and network excitability in approximately equal portions, and therefore the

169 model predicts that co-ordinated changes in these three parameters should be critical for the
 170 observed changes in system dynamics between diestrus and estrus. Interestingly, the second
 171 smallest principal component is largely determined by change in the basal activity parameter,
 172 suggesting that basal activity is another independent handle for modulating the system's
 173 dynamics. Taken together our theoretical findings suggest that co-ordinated changes in
 174 KNDy signalling as well as changes in KNDy basal activity may be crucial pathways of
 175 regulation across the reproductive cycle.



176
 177 **Figure 3. Model predictions on the key mechanisms modulating the behaviour of the KNDy pulse**
 178 **generator across the ovarian cycle.** (A) Schematic illustration of the coarse-grained model of the ARC KNDy
 179 population. The model comprises three dynamical variables representing the average levels of Dyn and NKB
 180 secreted by the population, and its average firing activity. We hypothesise that four key parameters modulate the
 181 behaviour of the system across the ovarian cycle: (i) Dyn signalling strength; (ii) NKB signalling strength; (iii)
 182 network excitability and (iv) basal neuronal activity. Estimates for the four parameters in estrus and diestrus are
 183 inferred from LH pulse frequency data in estrus and diestrus animals; with or without 5Hz optic stimulation
 184 (Fig. 2 E&F) (B) System response to low frequency stimulation during estrus and diestrus, using the maximum
 185 a-posteriori estimate of the parameter values inferred from the frequency data. (C) Analysis of parameter
 186 changes across the cycle. For each of the four parameter ($\theta^i; i = 1,2,3,4$) the diestrus-to-estrus change is defined
 187 as the log-ratio between the corresponding parameter values, i.e., $\log_{10} \frac{\theta^i_{\text{estrus}}}{\theta^i_{\text{diestrus}}}$. Normalised covariance
 188 (correlation) matrix of parameter changes reveals negative correlation between changes in NKB signalling

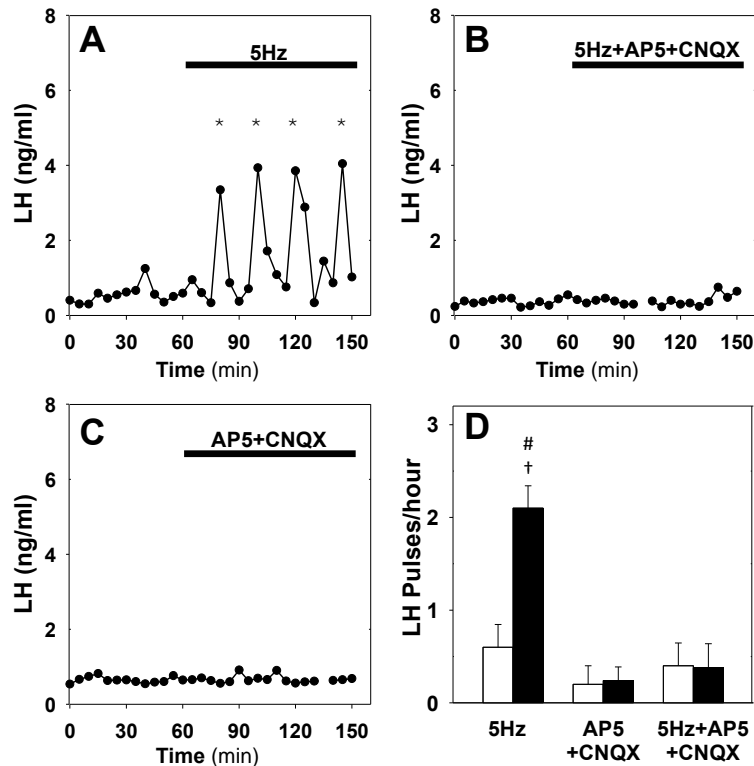
189 strength and network excitability, and positive correlation between Dyn signalling strength and both NKB
190 signalling. Eigen-parameters are visualised as pie charts. The eigen-parameter explaining the least of the
191 variance in the posterior distribution corresponds to the stiffest parameter combination to which the system is
192 most sensitive.

193 **Disrupting glutamatergic transmission in the KNDy population blocks LH pulses**

194 Since KNDy neurons are primarily glutamatergic (Cravo et al., 2011; Nestor et al., 2016; Qiu
195 et al., 2016; Qiu et al., 2018) and synapse to one another (Yip et al., 2015; Qiu et al., 2016)
196 we hypothesise that glutamate transmission should directly affect the levels of excitability
197 within the KNDy network. Hence, we disrupt signalling via glutamate receptors to explore
198 in-vivo how network excitability affects the ability of the system to generate and sustain LH
199 pulses across the estrous cycle.

200 First, using Kiss-Cre estrous mice we test whether glutamatergic transmission is necessary
201 for the optogenetic induction of LH pulses. We drive the ARC kisspeptin population using
202 sustained, low-frequency optic stimulation (5 Hz) in the presence of the combined NMDA
203 and AMPA receptor antagonists (AP5 and CNQX, respectively). We find that blocking
204 signalling via glutamate receptors inhibits the capacity of optic stimulation to generate and
205 sustain pulsatile LH secretion (Fig. 4 A,B&D). This is in agreement with the model
206 prediction that network excitability (ability of KNDy neurons to communicate and
207 synchronise) is critical for sustained pulse generation. The combined AP5 and CNQX in the
208 absence of optic stimulation had no effect (Fig. 4 C&D).

209 Next, we test whether glutamatergic transmission is critical for the endogenous LH pulses
210 observed in diestrus. Treatment of diestrous mice with the combined NMDA and AMPA
211 receptor antagonists resulted in a significant reduction of LH pulse frequency from $2.50 \pm$
212 0.29 to 0.45 ± 0.15 pulses/hour (Fig. 5 B&D), confirming that the glutamatergic transmission
213 is indeed critical for sustained pulsatility. Moreover, combining NMDA and AMPA receptor
214 antagonist treatment with low frequency optic stimulation (5 Hz) partially restored LH
215 pulsatility to 1.58 ± 0.17 pulses/hour (Fig. 5 C&D), suggesting low glutamatergic
216 transmission within the KNDy population or from upstream neuronal populations could be
217 offset by other exogenous inputs or elevated basal activity. This finding is in agreement with
218 the model prediction that basal activity and signalling between KNDy neurons are
219 independent pathways of modulating the system's dynamical behaviour.



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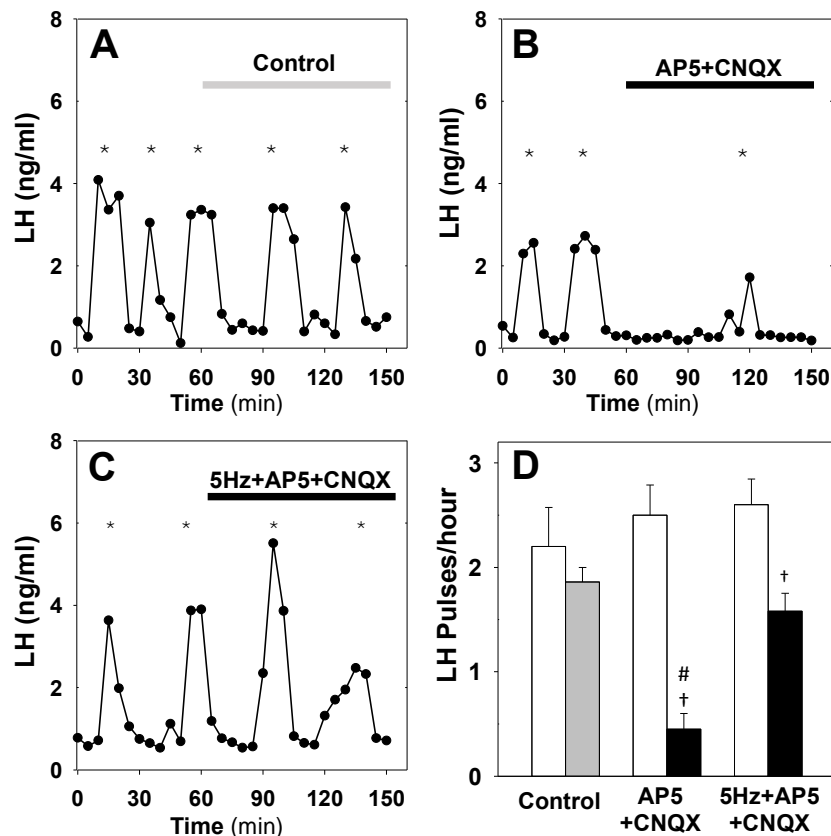
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Figure 4. Effect of NMDA+AMPA receptor antagonists on pulsatile LH secretion in estrus. Representative examples showing LH secretion in estrous mice in response to optic stimulation (5Hz blue light, 473 nm, 5-ms pulse width) (A) and optic stimulation combined with the NMDA+AMPA receptor antagonist (bolus ICV injection [12 nmol AP5 + 5 nmol CNQX] over 5 min, followed by a continuous infusion [20 nmol AP5 and 10 nmol CNQX] for the remaining 90 min) treatment (B). NMDA+AMPA receptor antagonist alone had no effect (C). (D) Summary showing mean \pm SEM LH pulse frequency over the 60min non-stimulatory period (white bars) and over the subsequent 90 min stimulation period or appropriate non-stimulatory period in presence of NMDA+AMPA receptor antagonist alone (black bar) in diestrous mice. *Denote LH pulses. $\dagger P < 0.05$ vs pre-stimulation. $\# P < 0.05$ compared to antagonist treatment groups; $n = 5-6$ per group.



230

231 **Figure 5. Effect of NMDA+AMPA receptor antagonists on pulsatile LH secretion in diestrus.**

232 Representative examples showing pulsatile LH secretion in response to ICV administration of aCSF as control

233 (A), treatment with NMDA+AMPA receptor antagonists (AP5+CNQX: bolus ICV injection [12 nmol AP5 + 5

234 nmol CNQX] over 5 min, followed by a continuous infusion [20 nmol AP5 and 10 nmol CNQX] for the

235 remaining 90 min) (B) and combined NMDA/AMPA receptor antagonist treatment and sustained optic

236 stimulation (blue light 473 nm, 5-ms pulse width) at 5Hz (C). (D) Summary showing mean \pm SEM LH pulse

237 frequency over the 60min non-stimulatory period (white bars) and over the subsequent 90 min stimulation

238 period in control mice (grey bar) and mice receiving treatment (black bar). *Denote LH pulses. $\dagger P < 0.05$ vs pre-

239 stimulation. #P < 0.05 compared to 5 Hz stimulation plus antagonist treatment and aCSF control groups; n = 5-6

240 per group.

241 Discussion

242 Using optogenetics we perturbed the GnRH pulse generator at different stages of the ovarian

243 cycle aiming to understand how gonadal steroids modulate key properties of the system.

244 Previous studies have shown how the pulsatile activity generated by the kisspeptin neuronal

245 network is modulated across the estrous cycle (Han et al., 2015; McQuillan et al., 2019). Our

246 data show that the stage of the cycle also has a profound effect on the dynamical response of

247 the kisspeptin population to sustained, low frequency optic stimulation. Such stimulation

248 triggers acceleration of LH pulses during estrus and deceleration during diestrus. Previously,
249 our mathematical model of the KNDy network has predicted an upper and a lower bifurcation
250 point that determine the system's range of pulsatile behaviour as the system is driven
251 externally (Voliotis et al., 2019). Our data suggest that the gonadal state plays a critical role
252 in shifting these bifurcation points by modulating key parameters of the system. In particular,
253 during estrous the system is positioned below the lower bifurcation point and optogenetic
254 stimulation of ARC kisspeptin neurons at 5Hz moves the system across the lower bifurcation
255 point leading to the sudden emergence of pulsatile behaviour. In contrast, during diestrus the
256 system is within the pulsatile regime and optogenetic stimulation of ARC kisspeptin neurons
257 at frequencies greater than 5Hz moves the system across the upper bifurcation point and its
258 dynamics relax progressively from pulsatile to quiescent. Our data therefore highlight the
259 critical role of gonadal steroids in modulating the dynamical response of the KNDy network
260 to small changes in basal activity of ARC kisspeptin neurons or in how the population
261 processes external perturbations and afferent inputs.

262 Using our mathematical model of the system we gained insight into possible mechanisms via
263 which gonadal steroids modulate the dynamic behaviour of the GnRH pulse generator. Based
264 on the differential effect that optic stimulation had on LH pulse frequency in estrous versus
265 diestrous animals, the model predicted that network excitability is an important parameter,
266 which is actively regulated throughout the ovarian cycle. Importantly, KNDy network
267 excitability is most probably co-regulated with parameters controlling the strength of Dyn
268 and NKB signalling as the system transitions between the different phases of the ovarian
269 cycle. In particular, our analysis predicts (i) a strong negative correlation between changes in
270 NKB signalling strength and changes in network excitability, and (ii) a strong positive
271 correlation in changes between NKB and Dyn signalling. We propose that these regulatory
272 relationships ensure robust control of LH frequency over the estrous cycle (Fig. 6 & Fig. 6-
273 figure supplement 1). For example, the positive correlation in the regulation of NKB and Dyn
274 signalling enables robust transition between pulsatile and quiescent dynamics, in contrast to
275 negative correlation that would make the system far more sensitive to the magnitude of the
276 change, i.e, changes that are too small or too large could fail to trigger LH pulses (see Fig 6-
277 figure supplement 1).

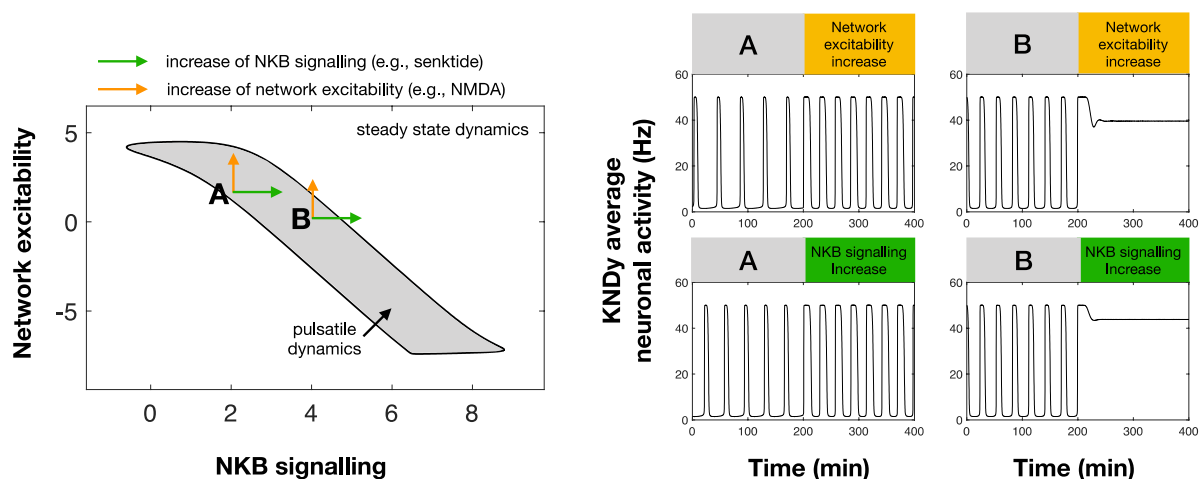
278 Recent transcriptomic data have revealed that treatment of ovariectomised mice with
279 estradiol reduces expression of NKB and Dyn in KNDy neurons, but increases expression of

280 glutamate transporters (vGlut2; leading to increased glutamate neurotransmission and
281 neuronal excitability in the population) (Qiu et al., 2018). These findings are in line with the
282 regulatory relationships predicted by the model and support the hypotheses that (i) correlated
283 changes in the NKB and Dyn signalling strength should be reflected mainly in the expression
284 levels of the two neuropeptides and consequently in their release availability, and (ii) a key
285 mechanism for regulating network excitability could be through the expression of glutamate
286 transporters. In normally cycling animals these changes should be driven by the combined
287 action of sex steroids. For example, although postovulatory increase in progesterone is linked
288 to deceleration of LH pulses in the luteal-phase, this inhibitory effect of progesterone is
289 conditional on prior exposure to high estradiol levels (Skinner et al., 1998) Moreover, data
290 from the rhesus monkey support that estradiol and progesterone could play distinct roles in
291 the deceleration of LH pulses from mid-cycle and throughout the luteal-phase (O'Byrne et al.,
292 1991). Our model provides a novel, systems-level understanding of how the genomic changes
293 in the KNDy population link to the dynamic behaviour of the pulse generator. Further
294 experiments will be needed to validate model prediction and link cyclic changes in the sex
295 steroid milieu to genomic pathways dynamically regulating the pulse generator.

296 The effect of cycle stage on the LH response to sustained optogenetic stimulation is
297 reminiscent of the well documented effect that gonadal steroids have on LH response to
298 various excitatory neurotransmitters and neuropeptides (e.g., NMDA). For instance,
299 investigations in the female monkey revealed an unexplained inhibition of LH in OVX
300 animals following treatment with NMDA, in contrast with the excitatory action of NMDA on
301 LH secretion in the presence of ovarian steroids (Reyes et al., 1990; Reyes et al., 1991).
302 Similar reversal of action on LH dynamics depending on the underlying ovarian steroid
303 milieu has been documented for various other neurotransmitters and NKB receptor agonists
304 (Kalra and Kalra, 1983; Scorticati et al., 2004). Our mathematical model supports that
305 ovarian steroids change key parameters of the KNDy network, which control the dynamic
306 behaviour of the system and its response to perturbations. As an illustration, Fig. 6 shows
307 how the dynamic behaviour of the model depends on network excitability and NKB
308 signalling. Since these parameters are governed by gonadal steroids (Qiu et al., 2018; Wang
309 et al., 2018), it is expected that the underlying steroid milieu will also modulate the effect of
310 perturbations on the dynamics of the system. For instance, the effect of stimulating NKB
311 signalling (e.g., via administration of NK3 receptor agonists) or network excitability (e.g., via
312 NMDA administration) could result in inhibition of the pulse generator if the system is

313 already located closer to the right boundary of the pulsatile dynamics region (e.g., point B in
 314 Fig. 6). Such points correspond to states with high pulse generator activity similar to pulse
 315 generator dynamics observed in many animal models after gonadectomy (Reyes et al., 1990;
 316 Kinsey-Jones et al., 2012). In contrast, similar perturbations but from a different point in the
 317 parameter space, lying closer to the left edge of the pulsatile region (e.g., point A in Fig. 6),
 318 could result in stimulation of the pulse generator (higher frequency). This illustrative example
 319 also highlights that the effect of gonadal steroids on the response of the pulse generator to
 320 perturbations is continuous rather than binary, that is, the behaviour of the pulse generator is
 321 modulated by the actual continuous levels of gonadal steroids rather than their mere presence
 322 of absence. Therefore, the underlying steroid levels could explain seemingly incompatible
 323 findings regarding the effect of NKB receptor agonism on LH secretion: ranging from
 324 stimulation (Navarro et al., 2011) or inhibition (Sandoval-Guzman and Rance, 2004; Kinsey-
 325 Jones et al., 2012) to no effects (Navarro et al., 2009) in rodents.

326



327
 328 **Figure 6. Differential effect of perturbations on the dynamics of the pulse generator.** Two-parameter (NKB
 329 signalling and network excitability) bifurcation diagram showing the region in the parameter space for which the
 330 system exhibits pulsatile dynamics (grey area). Two points (denoted by A and B) illustrate how an increase in NKB
 331 signalling or network excitability could have a differential effect on the dynamics of the system. For point A an
 332 increase in network excitability or NKB signalling could lead to an increase in the frequency and width of pulses.
 333 However, for point B a similar increase leads to pulse inhibition and steady state system dynamics. Furthermore, a
 334 negative correlation in how NKB signalling and network excitability co-vary (i.e., aligned with the direction of the
 335 pulsatile regime) make the system dynamics less sensitive to small perturbations and enable more robust control
 336 over the cycle.

337 Based on our model predictions regarding the importance of network excitability, we set out
 338 to uncover the role of this parameter on the dynamic response of the network in-vivo. We
 339 hypothesised that network excitability should depend, partly at least, on the levels of
 340 glutamate signalling as ARC kisspeptin neurons are known to be interconnected (Yip et al.,
 341 2015; Qiu et al., 2016) and communicate via glutamate (Cravo et al., 2011; Qiu et al., 2011;

342 Nestor et al., 2016; Qiu et al., 2016). Further evidence that estradiol regulates KNDy
343 neuronal excitability (Qiu et al., 2018) and that cycle stage regulates spontaneous
344 glutamatergic activity of KNDy neurons (Wang and Moenter, 2020) supports the model
345 prediction that network excitability is a critical network property regulated by gonadal
346 steroids. Therefore, to further test this prediction in-vivo we used glutamate receptor (NMDA
347 and AMPA) antagonists to inhibit excitability in the KNDy network. In diestrus animals
348 blocking glutamate receptors (NMDA and AMPA) inhibited LH pulses that were then
349 rescued via low frequency optogenetic stimulation of kisspeptin neurons. Furthermore, in
350 estrus animals, NMDA and AMPA receptor antagonism inhibited the induction of LH pulses
351 via optic stimulation. These experimental findings highlight the complex fine-balanced
352 mechanisms underlying pulse generation by the KNDy network. In particular, limited
353 network excitability within the KNDy population blocks LH pulsatility but this can be
354 mitigated by elevated basal neuronal activity. Similarly, increased basal neuronal activity can
355 induce pulse generation but this effect can be negated by decreased excitability within the
356 neuronal population. There is a caveat, however, as the glutamate receptor antagonists were
357 given by intracerebroventricular injection, and this raises the possibility of having interfered
358 with additional glutamatergic transmission from afferent populations. To the best of our
359 knowledge there is no evidence of such afferent populations in rodents, although supporting
360 evidence can be found the sheep literature (Merkley et al., 2015). Nevertheless, the
361 possibility of having blocked exogenous glutamatergic inputs does not invalidate our
362 findings, but further supports a key model prediction that basal activation of KNDy neurons
363 (either intrinsic or exogenous) is a critical pathway for modulating the dynamics of the pulse
364 generator. Overall, our model predicts that pulse generation is an emergent property of the
365 KNDy network depending both on single neuron properties such as basal activity and
366 exogeneous activation but also on how the neurons signal and communicate with each other.
367 Our results support this idea, highlighting the critical role of inter-neuronal communication in
368 enabling the population to pulse in synchrony.

369 **Materials and methods**

370 **Animals**

371 Adult Kiss-Cre heterozygous transgenic female mice aged between 8-14 weeks, 25-30 g,
372 were used for experiments (Yeo et al., 2016). Breeding pairs were obtained from the
373 Department of Physiology, Development and Neuroscience, University of Cambridge, UK

374 and mated in house at King's College London. Genotyping was performed using a multiplex
375 PCR protocol for detection of heterozygosity for the Kiss-Cre or wild-type allele as
376 previously described (Lass et al., 2020). Only mice with normal estrous cycles were used.
377 Daily vaginal smears were performed for the detection of the estrous and diestrous stages of
378 the ovarian cycle. Mice were singularly housed and provided with food (standard
379 maintenance diet; Special Dietary Services, Wittam, UK) and water ad libitum while being
380 kept under a 12:12 h light/dark cycle (lights on 0700 h) at $23 \pm 2^\circ\text{C}$. All animal procedures
381 performed were approved by the Animal Welfare and Ethical Review Body Committee at
382 King's College London and conducted in accordance with the UK Home Office Regulations.

383 **Surgical procedures**

384 Stereotaxic injection of AAV9-EF1-dflox-hChR2-(H134R)-mCherry-WPRE-hGH ($4.35 \times$
385 10^{13} GC/ml; Penn Vector Core; University of Pennsylvania, PA, USA) for targeted
386 expression of channelrhodopsin (ChR2) in ARC kisspeptin neurons was done under aseptic
387 conditions. The mice were anaesthetised using ketamine (Vetalar, 100 mg/kg, i.p.; Pfizer,
388 New York City, NY, USA) and xylazine (Rompun, 10 mg/kg, i.p.; Bayer, Leverkusen,
389 Germany). Kiss-Cre female mice ($n = 12$) or wild-type ($n = 3$) were secured in a Kopf
390 Instruments motorized stereotaxic frame (Kopf Instruments, Tujunga, CA, USA) and surgical
391 procedures on the brain were performed using a Robot Stereotaxy system (Neurostar,
392 Tübingen, Germany). Stereotaxic injection coordinates used to target the ARC were obtained
393 from the mouse brain atlas of Paxinos and Franklin (Paxinos and Franklin, 2004) (0.25 mm
394 lateral, 1.94 mm posterior to bregma and at a depth of 5.8 mm). A skin incision was made
395 and a small hole was drilled in the skull above the location of the ARC. A 2- μl Hamilton
396 micro-syringe (Esslab, Essex, UK) was attached to the robot stereotaxy and used to inject
397 0.3 μl of the AAV-construct into the ARC, unilaterally, at a rate of 100 nl/min. After the
398 injection, the needle was left in position for 5 min and then slowly lifted over 1 min. The
399 same coordinates as the injection site were then used to insert a fiber-optic cannula (200 μm ,
400 0.39 NA, 1.25 mm ceramic ferrule; Thorlabs, LTD, Ely, UK), however a depth of 5.78 mm
401 was reached to ensure the fiber-optic cannula was situated immediately above the injection
402 site. Additionally, an intracerebroventricular (ICV) fluid guide cannulae (26 gauge; Plastics
403 One) targeting the lateral ventricle (coordinates: 1.1 mm lateral, 1.0 mm posterior to bregma
404 and at a depth of 3.0 mm) was chronically implanted. Dental cement (Superbond C&B kit
405 Prestige Dental Products, Bradford UK) was used to fix the cannulae in place and the skin
406 incision was sutured. A one week recovery period was given post-surgery. After this period,

407 the mice were handled daily to acclimatize them to the tail-tip blood sampling procedure
408 (Steyn et al., 2013). Mice were left for 4 weeks to achieve effective opsin expression before
409 experimentation.

410 **Validation of AAV injection site and fibre optic and ICV cannula position**

411 Once experiments were completed, mice were given a lethal dose of ketamine and
412 transcardially perfused for 5 min with heparinized saline, followed by 10 min of ice-cold 4%
413 paraformaldehyde (PFA) in phosphate buffer, pH 7.4, for 15 min using a pump (Minipuls;
414 Gilson). Brains were collected immediately and post fixed at 4°C in 15% sucrose in 4% PFA
415 and left to sink. They were then transferred to 30% sucrose in PBS until they sank. The brains
416 were then snap-frozen on dry ice and stored at -80°C. Using a cryostat, every third coronal
417 brain section (30 µm) was collected between -1.34 mm to -2.70 mm from bregma and
418 sections were mounted on microscope slides, left to air-dry and cover slipped with ProLong
419 Antifade mounting medium (Molecular Probes, Inc, OR, USA). Verification and evaluation
420 of the injection site was performed using an Axioskop 2 Plus microscope equipped with
421 axiovision 4.7 (Zeiss). One of 12 Kiss-Cre mice failed to show mCherry fluorescence in the
422 ARC and was excluded from the analysis.

423 **Experimental design and blood sampling for LH measurement.**

424 For measurement of LH pulsatility during optogenetic stimulation, the tip of the mouse's tail
425 was removed with a sterile scalpel for tail-tip blood sampling (Czieselsky et al., 2016). The
426 chronically implanted fiber-optic cannula was attached to a multimode fiber-optic rotary joint
427 patch cables (Thorlabs) via a ceramic mating sleeve. This allows for freedom of movement
428 and blue light delivery (473 nm wavelength) using a Grass SD9B stimulator controlled DPSS
429 laser (Laserglow Technologies) during optogenetic stimulation.

430 The experimental protocol involved an hour long acclimatisation period, followed by 2.5 h of
431 blood sampling, where 5 µl of blood was collected every 5 min. For estrous and diestrous
432 mice, optic stimulation was initiated after 1 h of control blood sampling and was sustained
433 for 1.5 h h. Optic stimulation was delivered as 5ms pulses of light at 5 Hz with the laser
434 intensity measured at the tip of the fiber-optic patch cable set to 5mW (Voliotis et al., 2019).
435 Additionally, in separate experiments, diestrous mice were optically stimulated at 5 or 15 Hz
436 for 2.5 h, that is entire blood sampling period. Control mice (in estrus or diestrus) received no
437 optic stimulation. Wild-type mice (estrus and diestrus) received 5 Hz optic stimulation to
438 verify that our optic stimulation protocol had no undesirable effects on LH secretion.

439 Neuropharmacological manipulation of glutamatergic signalling was performed using a
440 combination of NMDA (AP5, Tocris, Abingdon, UK) and AMPA (CNQX, Alpha Aesar,
441 Heysham, UK) receptor antagonist treatment with or without simultaneous optogenetic
442 stimulation. The animals were prepared for optogenetic experimentation as described above
443 with additional preparation of the ICV injection cannula. Immediately after connection of the
444 fiber-optic cannula, the ICV injection cannula with extension tubing, preloaded with drug
445 solution (AP5 and CNQX dissolved in artificial CSF) or artificial CSF alone as control, was
446 inserted into the guide cannula. The extension tubing, reaching outside of the cage, was
447 connected to a 10 μ l Hamilton syringe mounted in an automated pump (Harvard Apparatus)
448 to allow for remote micro-infusion without disturbing the animals during experimentation.
449 After a 55 min control blood sampling period, as described above, and 5 min before the onset
450 of optic stimulation, a bolus ICV injection of drug solution (12 nmol AP5 and 5 nmol CNQX
451 in 2.3 μ l) was given over 5 min, followed by a continuous infusion (20 nmol AP5 and 10
452 nmol CNQX in 5.6 μ l) for the remaining 90 min of experimentation. Artificial CSF controls,
453 with or without optic stimulation, received the same ICV fluid regime. When no optic
454 stimulation was applied the same ICV administration and blood sampling regimen described
455 was applied. Stimulation and non-stimulation protocols were implemented in random order
456 for Kiss-Cre mice.

457 The blood samples were snap-frozen on dry ice and stored at -80°C until processed. In-house
458 LH enzyme-linked immunosorbent assay (LH ELISA) similar to that described by Steyn *et*
459 *al.* was used for processing of the mouse blood samples (Steyn *et al.*, 2013). The mouse LH
460 standard (AFP- 5306A; NIDDK-NHPP) was purchased from Harbor-UCLA along with the
461 primary antibody (polyclonal antibody, rabbit LH antiserum, AFP240580Rb; NIDDK-
462 NHPP). The secondary antibody (donkey anti-rabbit IgG polyclonal antibody [horseradish
463 peroxidase]; NA934) was from VWR International. Validation of the LH ELISA was done in
464 accordance with the procedure described in Steyn *et al.* (Steyn *et al.*, 2013) derived from
465 protocols defined by the International Union of Pure and Applied Chemistry. Serially diluted
466 mLH standard replicates were used to determine the linear detection range. Nonlinear
467 regression analysis was performed using serially diluted mLH standards of known
468 concentration to create a standard curve for interpolating the LH concentration in whole
469 blood samples, as described previously (Voliotis *et al.*, 2019). The assay sensitivity was
470 0.031 ng/mL, with intra- and inter-assay coefficients of variation of 4.6% and 10.2%
471 respectively

472 **LH pulse detection and statistical analysis.**

473 Dynpeak algorithm was used for the detection of LH pulses (Vidal et al., 2012). The
474 differential effect of optogenetic stimulation on LH pulsatility in estrus and diestrus was
475 determined by looking at the frequency of LH pulses. For mice in estrus and for the
476 neuropharmacological experiments, the mean \pm SEM of LH pulses per hour were compared
477 between the 60 min pre-stimulation/drug delivery control period and subsequent 90 min
478 stimulation period. For mice in diestrus, the mean \pm SEM of LH pulses per hour were
479 compared between controls, 5 Hz and 15 Hz treatment groups, as optic stimulation was
480 applied from the beginning of blood sample period. No optic stimulation was applied to
481 control animals, however the same time points were compared. The frequency of LH pulses
482 in the 90-min optic stimulation/drug delivery period was also compared between treatment
483 groups. Mann-Whitney Rank Sum test was used to access LH frequency differences between
484 groups and determine statistical significance ($p < 0.05$). LH data publicly available
485 from <http://doi.org/doi:10.18742/RDM01-750>.

486 **Mathematical model of the KNDy network.**

487 We used a modified version of our previously published mathematical model of the KNDy
488 network (Voliotis et al., 2019). The model offers a high-level overview of the system,
489 wrapping many biophysical details into a coarse grain description for the sake of simplicity
490 and brevity. Importantly such a parsimonious model fits best to the high-level, holistic in-
491 vivo approach we use to study the system. Briefly, the model describes the ARC kisspeptin
492 population in terms of three variables: \bar{D} , the average concentration of Dyn secreted by the
493 population; \bar{N} , the average concentration of NKB secreted by the population; and \bar{v} , the
494 average firing activity of the population, measured in spikes/min. The variables obey the
495 following set of coupled ordinary differential equations (ODEs):

$$\frac{d\bar{D}}{dt} = f_D(\bar{v}) - d_D\bar{D}; \quad [1]$$

$$\frac{d\bar{N}}{dt} = f_N(\bar{v}, \bar{D}) - d_N\bar{N}; \quad [2]$$

$$\frac{d\bar{v}}{dt} = f_v(\bar{v}, \bar{N}) - d_v\bar{v}. \quad [3]$$

496

497 Parameters d_D , d_N and d_v control the characteristic timescale of each variable. The model
498 describes Dyn and NKB secretion as independent processes based on the observation that

499 Dyn and NKB are packaged in separate vesicles (Murakawa et al., 2016). The secretion rates
 500 of the two neuropeptides are given by:

$$f_D(\bar{v}) = k_D \frac{\bar{v}^2}{\bar{v}^2 + K_v^2};$$

$$f_N(\bar{v}, \bar{D}) = k_N \frac{\bar{v}^2}{\bar{v}^2 + K_v^2} \frac{K_D^2}{\bar{D}^2 + K_D^2}.$$

501 In the equations above neuronal activity (\bar{v}) stimulates secretion of both neuropeptides, and
 502 Dyn represses NKB secretion. The maximum secretion rate for the two neuropeptides is
 503 controlled by parameters k_D and k_N and we refer to these parameters as the strength of Dyn
 504 and NKB signalling respectively. Furthermore, we assume that distinct modes of Dyn and
 505 NKB regulation (e.g., in terms of their synthesis and depletion rate, intracellular transport,
 506 packaging dynamics) are reflected in their secretion rate and therefore model Dyn and NKB
 507 regulation throughout the estrous cycle as changes of parameters k_D and k_N . The effector
 508 levels at which saturation occurs are controlled via parameters K_v and K_D . Here, we are
 509 interested in investigating the effect of network excitability on the dynamics therefore we
 510 modify the equation for the neuronal activity, \bar{v} , by setting:

$$511 f_v(\bar{v}, \bar{N}) = v_0 \frac{1 - \exp(-I)}{1 + \exp(-I)}; I = -\log \frac{1-b}{1+b} + k_v \left(e + \frac{\bar{N}^{n_4}}{\bar{N}^{n_4} + K_N^{n_4}} \right) \bar{v}.$$

512 Here, we have introduced parameter k_v capturing the intrinsic network excitability, that
 513 relates to the strength of the synaptic connections between KNDy neurons that are essential
 514 for synchronising neural activity and enabling pulse generation. We note that this parameter
 515 will be directly affected by any neuromodulator (including Glutamate) that affects KNDy
 516 activity as well as by processes that affect KNDy neurons' synaptic density. Furthermore,
 517 parameter b controls the basal neuronal activation of the population, which could stem from
 518 synaptic noise or afferent inputs (extrinsic to the network). We assume that both k_v and b are
 519 regulated throughout the estrous cycle. Finally, v_0 is the maximum rate at which the firing
 520 rate increases in response to synaptic inputs I . Note the stimulatory effect of NKB (which is
 521 secreted at the presynaptic terminal) on neuronal activity (Qiu et al., 2016). The full list of
 522 model parameters is given in Table 1.

523

524 **Parameter inference**

525 We used Approximate Bayesian Computation (ABC) based on sequential Monte Carlo
 526 (SMC) (Toni et al., 2009) to infer four key model parameters (Dyn signaling strength, k_D ;
 527 NKB signalling strength, k_N ; network excitability k_v ; and basal activity, b) in the estrous and

528 diestrous phase of the ovarian cycle. For inference we used the average LH inter-pulse
529 interval observed in four different settings: estrous animals without optic stimulation (I_E) and
530 with 5Hz optic stimulation (I_{E+5Hz}); diestrus animals without optic stimulation (I_D) and with
531 5Hz optic stimulation (I_{D+5Hz}). Model simulations were generated in Matlab using function
532 ode45 under the four different settings for 6000min and by calculating the frequencies after
533 discarding the initial 1000min. The following discrepancy function was used to compare
534 simulated, $D^* = (I_E^*, I_{E+5Hz}^*, I_D^*, I_{D+5Hz}^*)$, and experimental, $D = (I_E, I_{E+5Hz}, I_D, I_{D+5Hz})$, data:

$$d(D, D^*) = \sum_{i=1}^4 |D_i - D_i^*|$$

535 Furthermore, for the ABC SMC algorithm the size of the particle population was set to 500
536 and the algorithm was run for $T = 4$ populations with corresponding tolerance levels
537 $\varepsilon_i = 54 - 2i, i = 0, \dots, 26$. Log-uniform prior distributions were used to explore the behavior
538 of the model under wide parameter ranges: $\log_{10}(k_D) \sim Uniform(-3, 3)$;
539 $\log_{10}(k_N) \sim Uniform(-3, 3)$; $\log_{10}(k_v) \sim Uniform(-3, 3)$; and
540 $\log_{10}(b) \sim Uniform(-3, 0)$. All remaining parameters were fixed to values found in the
541 literature (see Table 1). For each parameter an independent \log_{10} -normal perturbation kernel
542 with variance 0.05 was used. Matlab code can be found at
543 <https://git.exeter.ac.uk/mv286/kndy-parameter-inference.git>.

No	Parameter	Description	Value	Ref.
1	d_D	Dyn degradation rate	0.25 min^{-1}	(Voliotis et al., 2019)
2	d_N	NKB degradation rate	0.25 min^{-1}	(Voliotis et al., 2019)
3	d_v	Firing rate reset rate	10 min^{-1}	(Qiu et al., 2016)
4	k_D	Dyn signalling strength	inferred	
5	k_N	NKB signalling strength	inferred	(Ruka et al., 2016)
6	k_v	Network excitability	inferred	
7	v_0	Maximum rate of neuronal activity increase	$30000 \text{ spikes min}^{-2}$	(Qiu et al., 2016)
8	K_D	Dyn IC_{50}	0.3 nM	(Yasuda et al., 1993)
9	K_N	NKB EC_{50}	32 nM	(Seabrook et al., 1995)
10	$K_{v,1}$	Firing rate for half-maximal NKB and Dyn secretion	$1200 \text{ spikes min}^{-1}$	(Dutton and Dyball, 1979)
11	b	Basal activity	inferred	
12	e	NKB independent contribution to network excitability	inferred	

544 **Table 1. Model parameters values.**

545 Sensitivity & Principal Component Analysis

546 We used principal component analysis to study the sensitivity of the system with respect to
547 changes in the four inferred parameters (Toni et al., 2009). We calculate the principal

548 components in the dataset (sampled posterior distribution) of the inferred parameter changes.
549 Principal component analysis produces a set of linearly uncorrelated eigen-parameters
550 explaining the variance of the inferred changes (in the sampled posterior distribution.) These
551 eigen-parameters are linear weighted combinations of the initial parameters. The eigen-
552 parameter explaining the least of the variance in the posterior distribution corresponds to the
553 stiffest parameter combination. That is small deviations from the inferred way these
554 parameters co-vary would lead to changes in the model behaviour that make it incompatible
555 with the data.

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694

695 **Supplementary figures**

696 **Figure 2-figure supplement 1. Optogenetic stimulation of ARC kisspeptin neurons in diestrous Kiss-Cre**
697 **mice using the original protocol (A-C)** Representative examples showing LH secretion in diestrous Kiss-Cre
698 mice over a 60 min control period followed by a 90 min period of sustained blue light (473 nm, 5-ms pulse
699 width, black bar) activation of kisspeptin neurons at 5 Hz. There is a tendency for LH pulses to slow down
700 during the activation period: (A) 0.05 vs 0.222 pulses/h (slow down); (B), 0.03 vs 0.03 pulses/h (no change);
701 and (C) 0.03 vs 0.222 pulse/h (slow down). To investigate the possibility of an effect in more depth, we revised
702 the protocol by removing the control period and extending stimulating to 150min (see Fig. 1 in main text).
703 *Denote LH pulses.

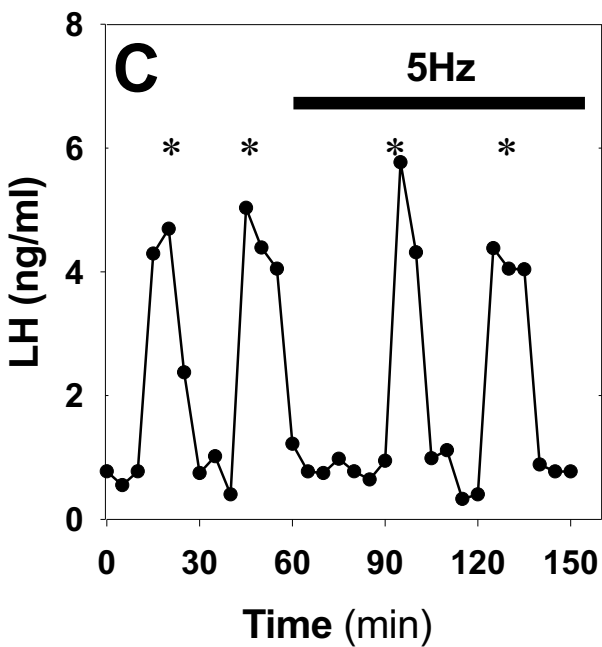
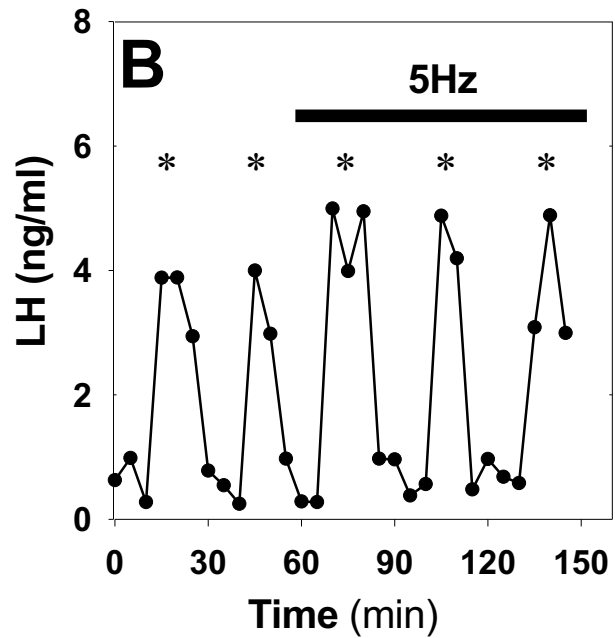
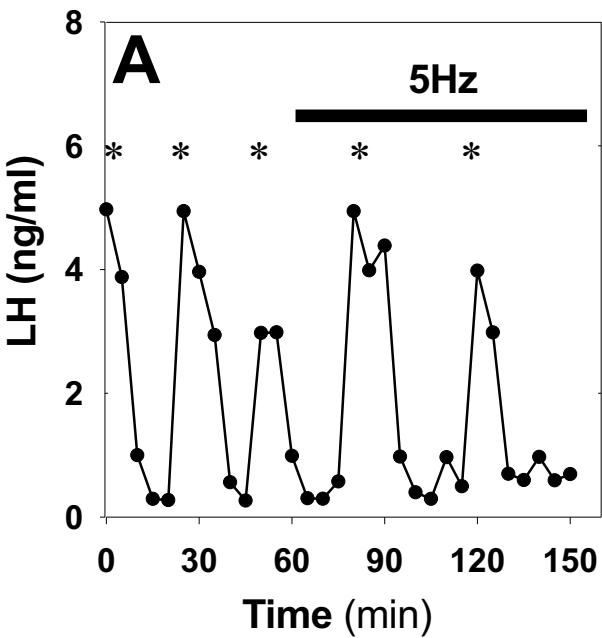
704
705 **Figure 2-figure supplement 2. Sustained optogenetic stimulation in control WT animals. (A-B)**
706 Representative examples showing normal LH secretion in diestrous WT animals under sustained blue light (473
707 nm, 5-ms pulse width, black bar) activation of kisspeptin neurons at 5 Hz. *Denote LH pulses.

708
709 **Figure 3-figure supplement 1.** Posterior distributions of diestrus-to-estrus parameter changes inferred from
710 data. The behaviour of the model depends upon four parameters: (i) Dyn signalling strength; (ii) NKB signalling
711 strength; (iii) network excitability and (iv) basal neuronal activity. For each of the four parameter ($\theta^i; i =$
712 $1,2,3,4$) we quantify the diestrus-to-estrus change as the log-ratio between the corresponding parameters, i.e.,
713 $\log_{10} \frac{\theta^i_{\text{estrus}}}{\theta^i_{\text{diestrus}}}$, and we infer them from frequency of LH pulses using Approximate Bayesian
714 Computation based on sequential Monte Carlo (see main text).

715
716 **Figure 6-figure supplement 1.** Dynamic behaviour of the KNDY system as a function of dynorphin and NKB
717 signalling. Positive correlation in the regulation of these two parameters (see positive co-regulation arrows)
718 allows robust control over the system's dynamics, i.e., large enough changes (regardless their actual magnitude)
719 will move the system from the quiescent into the pulsatile regime. Negative correlation in the regulation of the
720 two parameters (see negative co-regulation arrows) makes system dynamics more sensitive to the magnitude of
721 the change (arrow length), e.g., large changes can fail to trigger LH pulses.

722

Diestrus



WT Diestrus

