

Leak Detection and Localization in Water Distribution Networks Using Conditional Deep Convolutional Generative Adversarial Networks

Mohammad Mahdi Rajabi^{1*}, Pooya Komeilian², Xi Wan³, Raziye Farmani³

¹ *Civil and Environmental Engineering Faculty, Tarbiat Modares University, PO Box 14115-397, Tehran, Iran.*

² *Department of Civil Engineering, Sharif University of Technology, Tehran, Iran.*

³ *Centre for Water Systems, Department of Engineering, University of Exeter, Exeter, Devon EX4 4QF, UK.*

* Corresponding author E-mail: mmrajabi@modares.ac.ir

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1 **Abstract**

2 This paper explores the use of ‘*conditional convolutional generative adversarial networks*’
3 (CDCGAN) for image-based leak detection and localization (LD&L) in water distribution
4 networks (WDNs). The method employs pressure measurements and is based on four pillars: (1)
5 hydraulic model-based generation of leak-free training data by taking into account the demand
6 uncertainty, (2) conversion of hydraulic model input demand-output pressure pairs into images
7 using kriging interpolation, (3) training of a CDCGAN model for image-to-image translation, and
8 (4) using the structural similarity (SSIM) index for LD&L. SSIM, computed over the entire
9 pressure distribution image is used for leak detection, and a local estimate of SSIM is employed
10 for leak localization. The CDCGAN model employed in this paper is based on the pix2pix
11 architecture. The effectiveness of the proposed methodology is demonstrated on leakage datasets
12 under various scenarios. Results show that the method has an accuracy of approximately 70% for
13 real-time leak detection. The proposed method is well-suited for real-time applications due to the
14 low computational cost of CDCGAN predictions compared to WDN hydraulic models, is robust
15 in presence of uncertainty due to the nature of generative adversarial networks, and scales well to
16 large and variable-sized monitoring data due to the use of an image-based approach.

17 **Keywords:** Leak; anomaly detection; generative adversarial networks; image-to-image translation;
18 structural similarity index.

19 **1. Introduction**

20 With the rapid development of supervisory control and data acquisition (SCADA) technologies,
21 real-time monitoring of hydraulic parameters is becoming increasingly commonplace in many
22 water distribution networks (WDNs) (Zhou et al., 2019). Monitoring is often performed by
23 installing pressure and flow sensors in the transmission mains, allowing for an improved
24 understanding of system behavior, and diagnosis of anomalous events, the most notable of which
25 is pipe leaks. In this context, diagnosis of leakage often includes at least two aspects: (a) ‘leakage
26 detection’, which is to detect if leakage has occurred, and usually ends with binary results (i.e. leak
27 alarm on or off), or fuzzy values and probabilities between 0 to 1 to represent the likelihood of a
28 leakage event in the system (Mounce et al., 2010). (b) ‘Leak localization’ (or isolation) is the
29 process of narrowing down the potential location of a leak to a specific area or district. The latter

30 is a precursor to finding the leaky pipe(s) and then pinpointing the exact leakage location (Al
31 [Qahtani et al. 2020](#)).

32 **1.1. Literature Review**

33 Several past studies (e.g. [Kang et al., 2017](#); [Guo et al., 2021](#)) rely on auxiliary data such as acoustic
34 and vibration signals, for more accurate LD&L in presence of nuisance factors. Despite the
35 effectiveness, obtaining such data is labor intensive, and the quality of these data can be affected
36 by background noise and other events in the system or its environment ([Wu and Liu, 2017](#)).

37 Leakages in pipeline systems can also be detected using transient analysis by relying on the
38 principle of pressure transient wave reflection. A comprehensive overview of these methods was
39 provided by [Abdulshaheed et al. \(2017\)](#). However, the effectiveness of transient analysis-based
40 detection techniques is heavily influenced by pipe characteristics and external factors ([Kammoun
41 et al., 2022](#)). Furthermore, this approach is unsuitable for detecting leaks over long pipe distances
42 since pressure waves only propagate short distances. Additionally, implementing this technique
43 often requires intricate mathematical algorithms and substantial computational resources ([Wan et
44 al., 2022](#)).

45 Pressure and flow sensors have the advantage of being easy to install, enabling real-time
46 monitoring, and being sensitive to leakage events. Therefore, leakage detection and localization
47 (LD&L) using pressure/flow data has received increasing attention in the past decades. LD&L
48 using pressure/flow data can be done through one of the following two groups of methods. The
49 distinguishing factor between the two is whether a hydraulic model is used or not ([Wan et al.,
50 2022](#)).

51 A. ‘Data-driven’ methods rely on historical monitoring data and involve spatial analysis of
52 changes across a WDN, or temporal pattern analysis of time series data. Methods in this
53 group may involve: (1) defining control limits by calculating some statistical characteristic
54 (e.g. exponentially weighted moving average) of historical measurements and defining data
55 that is outside these limits as potential leaks (e.g. [Jung et al., 2015](#); [Loureiro et al., 2016](#)).
56 These methods often rely on assumptions such as the Gaussianity of data distribution and
57 the uncorrelation of errors. (2) Using historical data to train a predictor model that learns
58 the expected behavior of the system in leak-free circumstances, and comparing the
59 residuals between the observed and predicted value with a threshold to identify leaks. A
60 variety of machine learning tools, such as support vector machines and classic neural

61 networks have been employed in this context (e.g. [Mounce et al., 2011](#); [Romano et al.,](#)
62 [2012](#); [Tijani et al., 2022](#); [Tariq et al., 2022](#)). (3) Reframing the spatial/temporal pattern
63 recognition as a classification problem (using e.g. Bayesian classifiers) (e.g. [Wu et al.,](#)
64 [2016](#)). This method requires labeled data, i.e. an indication of whether a chosen data
65 instance pertains to a leak or not. (4) Formulating LD&L as a clustering problem by
66 grouping similar data into different clusters, and identifying leaks as those that are
67 dissimilar to normal cluster(s) (e.g. [Wu and Liu, 2020](#)).

68 B. ‘Model-based’ methods, also known as physically-based or process-based methods, rely
69 on the comparison of measured data with those of a calibrated WDN hydraulic model.
70 Model-based methods include: (1) formulating LD&L as an inverse modeling problem
71 using an optimization algorithm, and one or multiple objective function(s) (e.g. [Sanz et al.,](#)
72 [2016](#)). (2) Relying on sensitivity-to-leak analysis (e.g. [Perez et al., 2014](#)), where model-
73 generated pressure disturbances caused by all possible leak locations and magnitudes are
74 stored in a leak-sensitivity matrix and matched against the difference between measured
75 and simulated data ([Soldevila et al., 2017](#)). (3) Generating pressure or pressure residual
76 maps of each leakage scenario using the hydraulic model, employing the resulting data to
77 train a classifier, and finally utilizing the trained classifier for LD&L. The latter is
78 sometimes referred to as a mixed model-based/data-driven approach ([Soldevila et al.,](#)
79 [2016](#)).

80 Both data-driven and model-based methods have their advantages and limitations, and it is
81 unfeasible to draw a conclusion about which method is universally superior ([Wan et al., 2022](#)).
82 Data-driven approaches directly incorporate experimental data, and hence don’t require a deep
83 knowledge of the system operation and physical equations. Data-driven methods are best suited
84 for WDNs with a long-term monitoring dataset and were found to be effective in leak detection.
85 However, their performance in leak localization is debated ([Wu and Liu, 2017](#)). It is generally
86 difficult to obtain enough correct labeled data to train a high-accuracy model in a supervised
87 manner ([Zhang et al., 2020](#)); therefore data-driven LD&L methods often rely on unsupervised or
88 semi-supervised training. Many commonly used tools within the context of the data-driven
89 approach have limitations in learning complex features and using them requires the manual design
90 of suitable feature extractors ([Zhou et al., 2019](#)). Data-driven methods are particularly vulnerable
91 to missing or faulty data ([Hu et al., 2021](#)).

92 Model-based methods are preferred when limited historical data is available, but come at the cost
93 of building and calibrating a hydraulic model. Moreover, the high computation demand of
94 hydraulic models often hinders achieving real-time LD&L. A common challenge for both model-
95 based and data-driven methods is that pressure and flow rate can be affected by other factors apart
96 from leakages, such as variability and stochasticity in demand and random errors in sensor
97 measurements. These are often difficult to distinguish from leaks. For model-based methods, the
98 effect of input parameter uncertainty on the model output flow and pressure, adds to this
99 complexity (Menapace et al., 2018; Sun et al., 2019). Hence model-based methods do not perform
100 well in larger WDNs where the models' output uncertainty is often higher compared to smaller
101 WDNs (Zhou et al., 2019). The performance of the model-based sensitivity-to-leak analysis
102 method is particularly well-known to decrease due to the nodal demand uncertainty and noise in
103 the measurements (Cugueró-Escofet et al., 2015).

104 The above-described challenges have forced previous LD&L studies to focus mainly on
105 hypothetical burst events in simple WDNs (Wan et al., 2022). As highlighted by recent review
106 papers (e.g. Gupta and Kulat, 2018; Chan et al., 2018; Wan et al., 2022), more effort is needed to
107 solve these challenges by developing novel methods that are: (a) robust in presence of various
108 forms of uncertainty, (b) can scale to very large monitoring datasets, (c) can learn complex features
109 from raw data, (d) rely less on manual design, and (e) are well-adapted to a limitation in labeled
110 training data.

111 A promising approach to achieve this objective is to exploit deep neural networks (DNNs). DNNs
112 rely on hierarchical projections of the input space into increasingly low-dimensional latent
113 representations (Goodfellow et al., 2016), enabling them to learn complex features from large
114 amounts of data without the need for developing manual features by domain experts (Chalapathy
115 and Chawla, 2019). In recent years, several DNN-based anomaly detection methods have been
116 introduced for a variety of applications, demonstrating significantly better performance than
117 conventional anomaly detection with an increase in the scale of data and complexity of the problem
118 (Pang et al., 2021). Example applications of DNNs in LD&L include the use of convolutional
119 neural networks (CNNs) for burst localization based on data from short-duration pressure
120 observations (Zhou et al., 2019); supervised training of a CNN using hydraulic model-generated
121 samples of all possible leaks for leak localization (Javadiha et al., 2019). These approaches, like
122 many older methods, require a well-calibrated hydraulic model to generate synthetic data that

123 accurately represent real-life situations for training a deep learning model. However, acquiring and
124 maintaining a well-calibrated hydraulic model can be challenging for water companies.
125 Regression analysis has been used as an alternative method to learn the data patterns representing
126 the healthy state of a WDN from historical monitoring data instead of a hydraulic model. As an
127 example, [Ye and Fenner \(2011\)](#) utilized the Kalman filter to fit historical flow measurements and
128 identify burst events by comparing predicted and observed values, while also employing the
129 weighted least squares regression to model the data. However, these approaches treat each data
130 point of a day independently, and thus, they do not fully consider the autocorrelation of the time
131 series data.
132 [Mounce et al. \(2010\)](#) employed a neural network to learn the normal flow behavior from
133 monitoring data and detect leaks based on prediction errors. A key limitation of their approach is
134 the inability to share features across different steps of a time series, whereas temporal pattern
135 recognition requires the ability to process evolving patterns. To address this problem, recurrent
136 neural networks such as long short-term memory (LSTM) networks have been explored for
137 leakage detection ([Wang et al., 2020](#); [Xu et al., 2020](#)). While the results of these LSTM-based
138 methods have shown high detection accuracy, there are still some limitations that need to be
139 addressed. Specifically, these methods are often restricted to univariate time series analysis, which
140 only allows for the analysis of data from a single sensor at a time. However, it's known that data
141 from sensors in the same network are spatially correlated, and considering topology information
142 and the spatial relation of the sensors is essential for accurate leak detection.

143 **1.2. Study Objectives**

144 Recent research progress has demonstrated the effectiveness of DNNs in solving LD&L problems,
145 and it is becoming increasingly clear that DNNs present an opportunity for improving current
146 practice. In this work, we will be leveraging some of the most recent advances in DNNs, to develop
147 a robust methodology for achieving accurate real-time LD&L in complex settings. Our
148 methodology is based on the use of ‘*conditional convolutional generative adversarial networks*’
149 (CDCGAN) for image-based anomaly detection. Partially similar methods have been used in other
150 applications for anomaly detection (e.g. [Ezeme et al., 2020](#); [Luo et al., 2021](#); [Qiu et al., 2022](#)), but
151 to the best of our knowledge, this method has not been applied to leak detection in WDNs.
152 Relying on flow measurements for LD&L is often easier than pressure measurements, because
153 flow data allows for the use of simple mass balance relations, and pressure data is less sensitive to

154 leak events, especially when the pressure sensor is located far from the leak location (Ye and
155 Fenner, 2011). However, pressure meters are easier to install and less costly than flow meters
156 (Zhou et al., 2019; Sun et al., 2019), provide instantaneous data, and are better for LD&L in WDNs
157 where there is a dense mesh of pipes with only flow measurements at the entrance of each DMA
158 (Soldevila et al., 2017). Hence, this work focuses on the use of pressure data for LD&L.

159 The rest of the paper is organized as follows. Section 2 presents the background of semi-supervised
160 anomaly detection (SSAD) and CDCGANs. Section 3 presents the proposed methodology for
161 LD&L. Section 4 details the application of the method to a WDN, followed by a discussion of the
162 main findings. Finally, Section 5 draws the main conclusions of the work and introduces some
163 potential extensions.

164 **2. Theoretical Background**

165 **2.1. Semi-Supervised Deep Anomaly Detection**

166 Leaks result in anomalous pressure observations, and most notably, a contextual anomaly.
167 Therefore, LD&L in WDNs can be described as a particular case of the general problem of
168 anomaly detection and isolation in dynamic systems (Soldevila et al., 2016). Most problems in this
169 context suffer from the limited availability of labeled anomalous data (Schlegl et al., 2019). For
170 LD&L, this is mostly because (a) historical monitoring data on leak events is often scarce and may
171 be unreliable, (b) full-scale physical experiments (using e.g. fire hydrants) are very costly, and (c)
172 model-generated leak data are limited to the specifications of the model, and comprehensive
173 evaluation of all possible leak locations and magnitudes is often computationally unfeasible.
174 Supervised anomaly detection is limited to already known anomalies, hence lack of labeled
175 anomalous data severely limits its value (Wan et al., 2022). SSAD is a way to employ a large set
176 of unlabeled data alongside limited labeled data to construct a classifier with good generalization
177 ability (Tu et al., 2018). In SSAD, easier-to-obtain samples of normal (i.e. leak-free) data are
178 given, and the model learns a discriminative boundary around the normal instances. New data
179 instances that don't belong to the normal class are identified as anomalous. SSAD methods rely
180 on the assumption that points which are close to each other in the learned feature space are more
181 likely to share the same label (Chalapathy and Chawla, 2019).

182 **2.2. Generative Adversarial Networks**

183 GANs trained in a semi-supervised manner have shown great promise, even with few labeled data
 184 (Mu et al., 2021). The GAN architecture, in its basic form, is composed of a generator (G) and a
 185 discriminator (D) neural network (Goodfellow et al., 2014). A random input latent space $z \sim p_z$
 186 (often sampled from a normal or uniform probability distribution, e.g. $z \sim \mathcal{N}(0,1)$) is mapped to
 187 the data space ϕ by the generator, which tries to generate new examples that are ideally identical
 188 to the training dataset p_{data} . The discriminator is responsible for classifying a given generator
 189 output ϕ as either real (i.e. indistinguishable from the training dataset p_{data}) or fake (non-identical
 190 to the training dataset) (Wang et al., 2017). These models are trained together in a zero-sum
 191 manner, also called min-max and adversarial, such that improvements in the discriminator come
 192 at the cost of reduced capability of the generator, and vice versa (Arjovsky and Bottou, 2017; Gui
 193 et al., 2021). This can be represented by the following objective function (Zheng et al., 2020):

$$\min_G \max_D \mathbb{E}_{\phi \sim p_{data}} [\log D(\phi)] + \mathbb{E}_{z \sim p_z} [\log(1 - D(G(z)))] \quad (1)$$

194 GANs have several key advantages: (a) GANs are well-adapted to SSAD, eliminating the need for
 195 the often time-consuming, cumbersome, and sometimes unfeasible task of providing labeling for
 196 anomalous data (Singh and Raza, 2021), (b) Markov chains and inference are not needed during
 197 learning, and only backpropagation is used to obtain gradients (Goodfellow et al., 2014; Mirza and
 198 Osindero, 2014), and (c) GANs are capable of learning many noise types and mimicking complex
 199 (including very sharp) data distributions (Wunderlich and Sklar, 2022).

200 GANs allow for the synthesis of novel images, videos, numeric and audio data, or text from a
 201 random input (Al Qahtani et al., 2021). Hence, GANs are commonly used for data synthesis to
 202 facilitate the training of other ML models when data is insufficient or to correct the overtraining
 203 of a DNN (Zamora et al., 2021). For image data, the generator and discriminator frequently take
 204 the form of deep CNNs (see Radford et al., 2015 as a pioneering work). The resulting architecture
 205 is often referred to as deep convolutional GAN (DCGAN).

206 2.3. Conditional Training

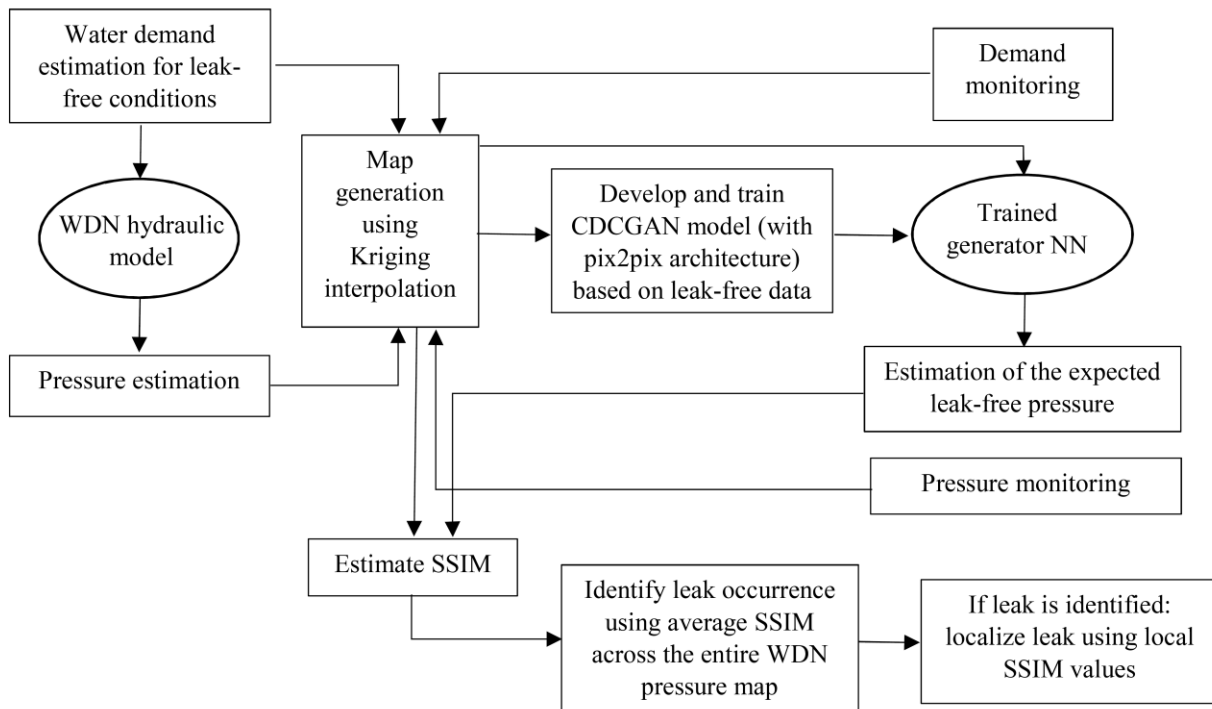
207 GAN models generate new plausible examples of a given dataset, but their outputs are practically
 208 random and uncontrollable. There is no way to control the outputs other than discovering the
 209 complex relationship between the input latent space and the GAN-generated outputs, which is
 210 generally difficult and often unfeasible (Wang et al., 2018). However, GANs can be conditioned
 211 on auxiliary inputs, allowing for the targeted generation of outputs. This can be done by hot-

212 encoding the conditioning data and concatenating it to the input of the generator (noise input) as
 213 well as the discriminator (generated data) (Denton et al., 2015; Qasim et al., 2020). Conditional
 214 GANs are considered semi-supervised models (Zhang et al., 2019). In a conditional GAN, both
 215 the generator and the discriminator models are conditioned, and hence the trained generator model
 216 can be used as a standalone model to generate data in the domain of interest. The most common
 217 strategy is to condition GANs on class labels (i.e. class-conditional GANs), but GANs can also be
 218 conditioned on the auxiliary image(s) in the context of *image-to-image translation* tasks
 219 (Brownlee, 2019). The conditional training of a DCGAN-based model is referred to as CDCGAN.

220 3. Methodology

221 The proposed methodology employs a CDCGAN in the context of SSAD to identify and locate
 222 leaks in a WDN. The methodology is based on four pillars: (1) hydraulic model-based generation
 223 of training data, (2) conversion of hydraulic model input-output pairs into images, (3) semi-
 224 supervised training of a CDCGAN model for image-to-image translation, and (4) using the
 225 structural similarity (SSIM) index for LD&L. These pillars are described in the following
 226 subsections. A flowchart of the proposed methodology is provided in Fig. 1.

227



228

229

Fig. 1. Flowchart of the proposed methodology.

230

231 **3.1. Hydraulic Model-Based Generation of Training Data**

232 In a hypothetical leak-free condition, it is subjectively assumed that the uncertain demand in node
233 i and time step t (denoted by $d_{i,t}$) is represented by a normal distribution with a mean ($\mu(d_{i,t})$)
234 equal to the field data (or estimates) of demand, and a standard deviation of $\sigma(d_{i,t}) = 0.1\mu(d_{i,t})$
235 (Soldevila et al., 2017). We employ Latin hypercube sampling (LHS) to produce a variety of
236 random, plausible values for pipe parameters and demand time series and feed them to the
237 EPANET model to obtain the resulting pressure time series in the observation nodes. We refer to
238 data obtained from hydraulic simulations as ‘model-generated data’.

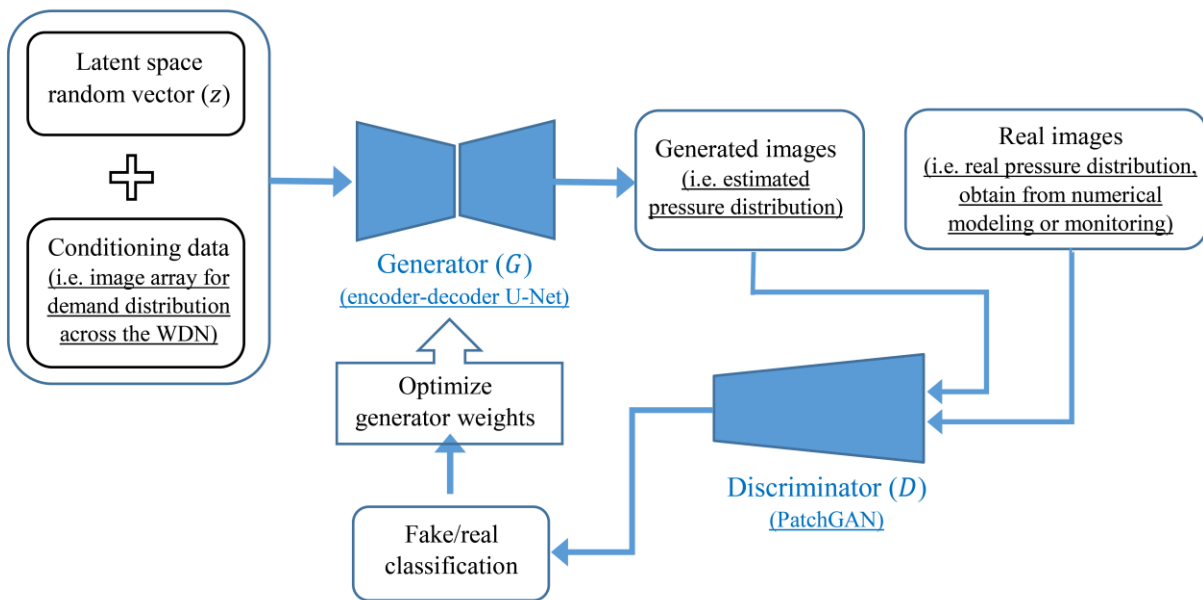
239 **3.2. Transforming Demand and Pressure Data to Images**

240 Demand and pressure values at various observation points (OPs) in a single time step are employed
241 to create images of demand and pressure. This results in the creation of two ‘*image time series*’
242 for the entire duration of interest. These images are created by interpolating pointwise values using
243 the kriging method with a Gaussian variogram model. Kriging is a popular choice for interpolating
244 data points to a continuous spatial field (Kleijnen, 2017), and has been previously used in several
245 studies including Javadiha et al. (2019) for pressure and/or demand interpolation in WDNs. The
246 kriging method is implemented here using the PyKriging python library (Murphy, 2014). The
247 resulting interpolated values are then scaled into the interval 0 and 255 to generate rectangular
248 greyscale images with 256×256 pixels.

249 **3.3. CDCGAN for Image-to-image Translation**

250 The demand-pressure image pairs are subsequently employed for training a CDCGAN, to learn
251 how certain demand distribution maps to the associated leak-free pressure distribution. The
252 CDCGAN model employed in this work is based on the pix2pix architecture (Isola et al., 2017).
253 Pix2pix is composed of a generator and a discriminator network, as portrayed in Fig. 2. The
254 generator is an encoder-decoder CNN (ED-CNN) based on a modified U-Net architecture
255 (Ronneberger et al. 2015). The ED-CNN consists of (a) an encoder subnetwork that receives the
256 input image, passes it through a contracting process in which features of increasing semantic depth
257 and decreasing spatial resolution are learned from the input image, and outputs feature maps, and
258 (b) a decoder which receives the feature maps and employs deconvolution and up-sampling to

259 constructed an output image with the same spatial resolution as the original input (Rajabi et al.,
 260 2022). The encoder is made of several blocks, where each block consists of a convolutional layer
 261 proceeded by batch normalization and leaky Rectified linear unit (ReLU) activation function.
 262 Blocks of the decoder consist of a transposed convolutional layer, followed by batch
 263 normalization, dropout (applied only to the first 3 blocks), and ReLU activation function. Skip
 264 connections are employed between the encoder and decoder. The discriminator in pix2pix is a
 265 convolutional PatchGAN classifier that maps each generator output to a 70×70 square patch of
 266 the input image. The patches overlap to cover the 256×256 -pixel image. The discriminator is
 267 made of several blocks with each block consisting of a convolution layer, batch normalization, and
 268 Leaky ReLU activation function. The objective function in pix2pix training is the sum of the GAN
 269 loss, a binary cross-entropy, and an L_1 norm between the generated image and the ground truth
 270 (Isola et al., 2017). In this work, the pix2pix-based CDCGAN is developed using the open-source
 271 python library TensorFlow and is trained on Google Colab.



272

273

Fig. 2. The architecture of CDCGAN and how it is trained with demand-pressure image pairs

274

275 3.4. Leak Detection and Localization

276 After the model is trained, the CDCGAN generator is fed with new demand images (for which
 277 some are associated with leaks in the WDN) and outputs the pressure distribution image which

278 represents what is expected in leak-free conditions. The SSIM index is then used for measuring
 279 the similarity between the ground truth (either field or model-generated data), and the CDCGAN-
 280 predicted pressure images. SSIM is a perceptual metric that quantifies the difference between two
 281 images from the same image capture and has been used in many image quality assessment
 282 applications (Chen and Bovik, 2011). SSIM is calculated on various windows of an image. The
 283 measure between two windows x and y of common size $N \times N$ is a weighted combination of
 284 three comparative measures, namely luminance ($l(x, y)$), contrast ($c(x, y)$), and structure ($s(x, y)$)
 285 which are defined as follows (Wang et al., 2004):

$$l(x, y) = \frac{2\mu_x\mu_y + c_1}{\mu_x^2 + \mu_y^2 + c_1} \quad (2)$$

$$c(x, y) = \frac{2\sigma_x\sigma_y + c_2}{\sigma_x^2 + \sigma_y^2 + c_2} \quad (3)$$

$$s(x, y) = \frac{\sigma_{xy} + c_3}{\sigma_x\sigma_y + c_3} \quad (4)$$

286 Where μ_x and μ_y are the average of x and y respectively, σ_x and σ_y are their standard deviations,
 287 and σ_{xy} is their covariance. c_1 , c_2 and c_3 are variables included to avoid instability when the
 288 denominator is close to zero. SSIM ranges between 0 to 1, where 1 denotes a perfect match
 289 between the reconstructed and original images. Here, SSIM is multiplied by 100 to give a
 290 percentage score. SSIM can be estimated locally (which we denote by $SSIM_l$) or computed over
 291 the entire image (represented by $SSIM_o$).

292 Due to factors such as demand uncertainty, the target, and CDCGAN predicted pressure images
 293 are not expected to perfectly match even in leak-free conditions. Therefore the mean and standard
 294 deviation of $SSIM_o$ in absence of a leak, is first estimated by employing an independent set of
 295 leak-free demand-pressure image pairs. The resulting values are then employed to derive a
 296 threshold that differentiates between leak-free and leak conditions. We choose this threshold
 297 (T_{SSIM_o}) to be mean minus three times the standard deviation of $SSIM_o$. This choice is based on
 298 the three-sigma rule, which is widely used in statistics and quality control to identify outliers or
 299 abnormal values in a dataset. This rule assumes that the data follows a normal distribution and that
 300 approximately 99.7% of the data will fall within three standard deviations of the mean (Panda and
 301 Khilar, 2015). However, the appropriateness of this rule depends on the characteristics of the data
 302 and the specific needs of the analysis. A more conservative threshold value, such as mean minus

303 four or five times the standard deviation, may reduce the risk of false alarms but increase the risk
304 of missed detections.

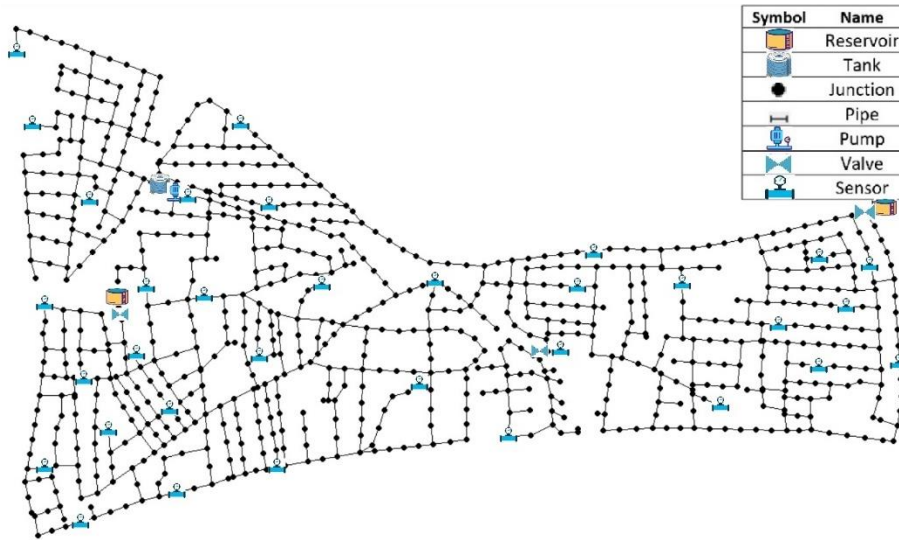
305 Furthermore, it is well-known that one abnormal data point cannot signify a leakage event, while
306 continuous disruptive data is more suitable to indicate the occurrence of a leak (Wan et al., 2022).
307 In this study, if the $SSIM_o$ obtained from comparing the ground truth and the CDCGAN predicted
308 pressure is less than T_{SSIM_o} for 5 consecutive time steps (i.e. snapshots of pressure observation),
309 we conclude that there is a leak somewhere in the WDN. The selection of the number of
310 consecutive time steps is dependent on the sensitivity of the detection method and the noise level
311 in the system. A smaller number of time steps may produce false alarms due to measurement noise,
312 while a larger number of time steps may delay the detection of leaks. A balance between the risk
313 of false alarms and missed detections is often sought in practice, and five consecutive time steps
314 may be a suitable choice. If a leak is identified, leak localization is then carried out by using the
315 local SSIM ($SSIM_l$). For leak localization, the area with the lowest value of $SSIM_l$ across the
316 pressure map at each time step is identified as the most probable leak location.

317 **4. Application**

318 **4.1. Description of the Case Study**

319 We analyze the effectiveness and accuracy of the proposed methodology using the L-Town
320 benchmark problem (Vrachimis et al., 2020). The L-Town problem for LD&L is founded on a
321 transient hydraulic model that mimics the characteristics of a real-world water distribution system.
322 This model is designed to simulate changes in flow and pressure in the pipes over time, which are
323 influenced by a variety of factors, including variations in demand and pump operations.
324 Additionally, the L-Town problem accounts for different types of leaks, ranging from small to
325 large leaks, and introduces them at different times during the simulation to create transient
326 conditions.

327 This case study encompasses a surface area of $3 \times 2.6 \text{ km}^2$ and a total pipe length of 42 km. There
328 are 782 junctions, 2 reservoirs, 1 tank, 905 pipes, 1 pump, and 3 pressure-reducing valves in the
329 WDN (see Fig. 3). The network is monitored using 33 pressure sensors. Sensor measurements are
330 assumed to be accurate, with no time delay, and are reduced to two decimal points. The
331 measurement dataset is one year in length and has 5-minute time steps.



332
333 **Fig. 3.** Map of the WDN used as our case study.
334

335 An EPANET-based model of the L-Town benchmark problem (Vrachimis et al., 2022) is
336 employed for data generation. This hydraulic model utilizes a pressure-driven analysis method to
337 simulate the network. The model was calibrated based on field measurements obtained from the
338 original water distribution system in L-Town (Steffelbauer et al., 2020). To facilitate iterative
339 model simulations, we couple this model with an EPANET-compatible Python library, named
340 Water Network Tool for Resilience (WNTR) (Klise et al., 2018) (available on GitHub:
341 <https://github.com/USEPA/WNTR>). WNTR has an application programming interface (API) that
342 allows for changes to the network operations and simulation of disruptive incidents such as leaks
343 and bursts (Klise et al., 2020).

344 **4.2. Generating the Training Data**

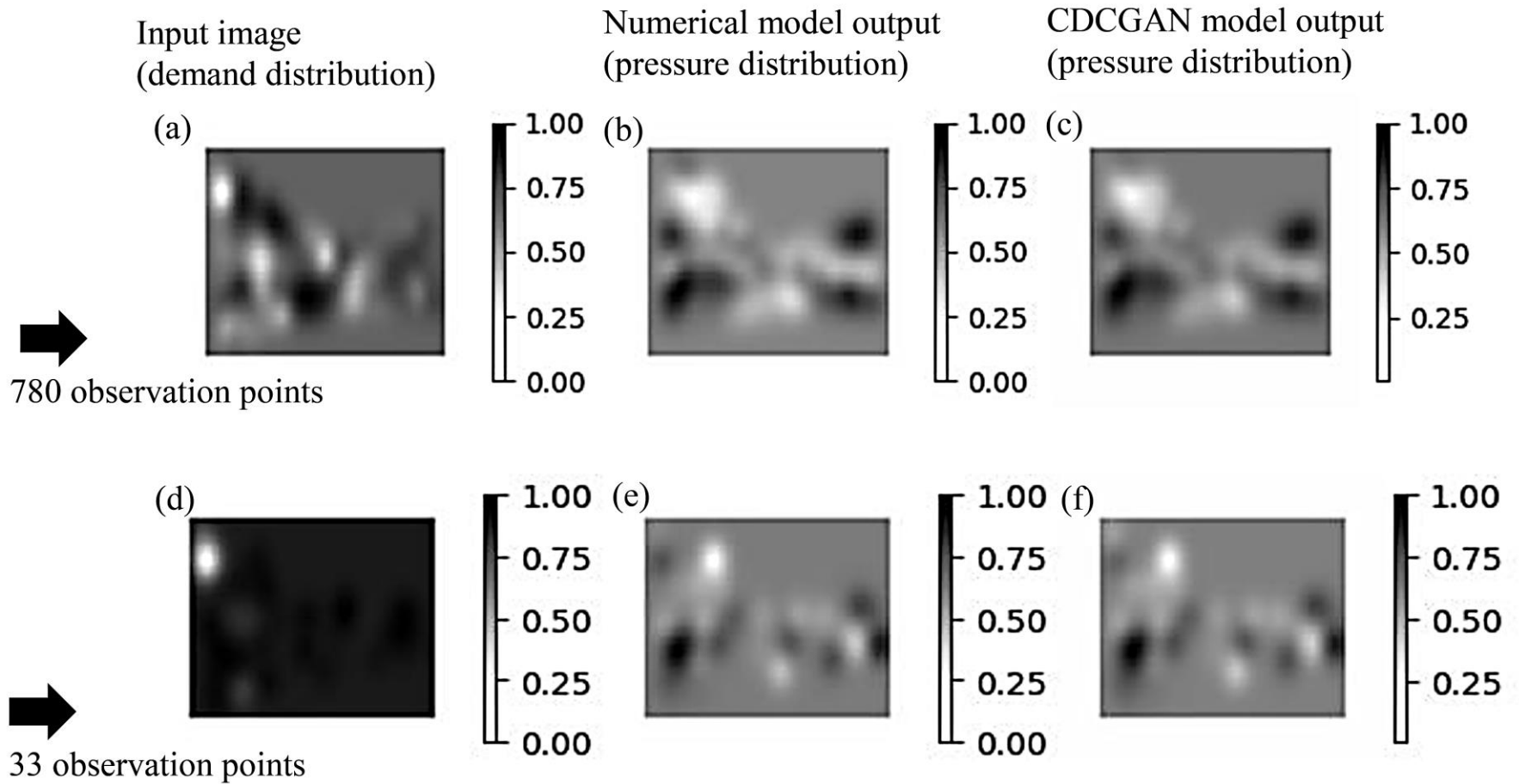
345 Data for CDCGAN training is generated using the leak-free EPANET model (Vrachimis et al.,
346 2020), following the scheme described in sub-sections 3.1 and 3.2. In this context, 365 daily
347 demand patterns with a time step of 5 minutes have been generated, taking into account demand
348 uncertainty. This results in 105,120 pairs of demand-pressure images, which are divided into
349 training and testing data by an 80%-20% split. This procedure is first done using pressure
350 observations in 780 nodes in the WDN (two nodes close to the reservoirs, which have exceptionally
351 high pressures, have been omitted from the original 782 nodes of the case study), and then repeated
352 by only incorporating the 33 locations for which pressure sensors are available (see **Fig. 3**).

353 In the process of generating pressure distribution images, since the temporal variations are small
354 compared to the spatial variations, we divided the WDN into four zones based on the range of
355 observed pressures (i.e. $zone_1: P < 33$ m, $zone_2: 33 < P < 40$ m, $zone_3: 40 < P < 50$ m, and
356 $zone_4: P > 50$ m), and then separately scaled pressure values into the interval 0 and 255 for each
357 zone. As an example of the leak-free images obtained from Kriging interpolation, **Fig. 4** depicts
358 demand and pressure distributions in randomly chosen time steps, obtained from 780 (**Figs. 4a,**
359 **4b**) and 33 OPs (**Figs. 4d, 4e**). As the demand in various nodes may serve different purposes, such
360 as residential, commercial, or industrial, reducing the number of data nodes (from 780 to 33) has
361 a greater impact on the interpolated demand maps than on the pressure maps.

362 **4.3. CDCGAN Training and Validation**

363 Two separate CDCGANs are trained using images obtained from 780 and 33 OPs. We refer to
364 these two as CDCGAN₇₈₀ and CDCGAN₃₃ respectively. For both models, 30,000 epochs are
365 sufficient to reach a stable solution. Details of the hyper-parameter settings are presented in **Table**
366 **1**. The mean absolute percentage error (MAPE) is used to measure and quantify the prediction
367 errors. **Fig. 5** illustrates the MAPE histogram of the trained CDCGANs. The average MAPEs are
368 1.42%, and 0.67% for CDCGAN₇₈₀ and CDCGAN₃₃ respectively. **Fig. 5** and the average MAPEs
369 show that the prediction error of the CDCGAN₃₃ is lower than those of CDCGAN₇₈₀. This can be
370 attributed to the fact that more OPs result in more complex pressure maps that should be learned
371 by the model. For both CDCGANs, the error distribution is not uniform or normal and is skewed
372 to the right.

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Fig. 4. Comparison of the numerical model and CDCGAN metamodel outputs (i.e. pressure distribution) for the same input image (i.e. demand distribution), randomly chosen from the test dataset, for (a, b, c) 780, and (d, e, f) 33 observations points. In these images, the demand and pressure are unitless and normalized through division by the respective maximum values.

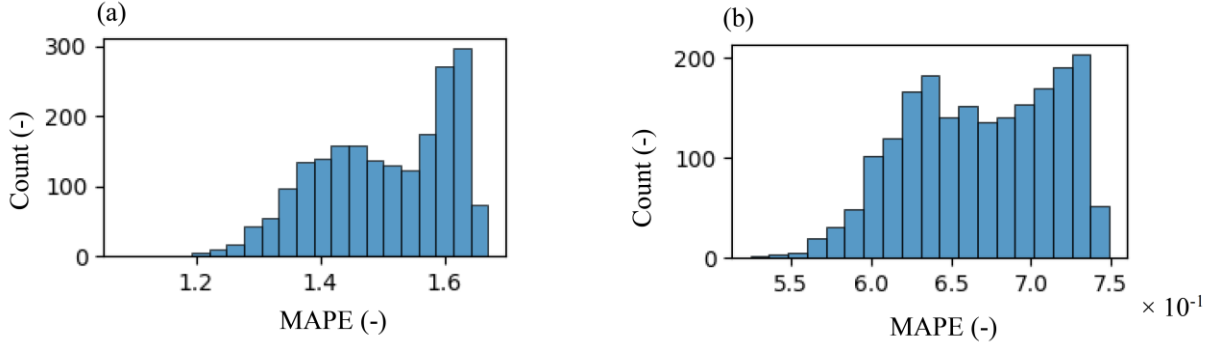


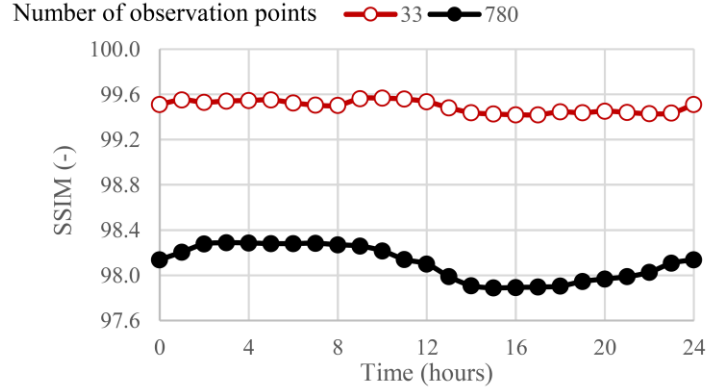
Fig. 5. Histogram of MAPE for the CDCGANs trained based on pressure images obtained from (a) 780, and (b) 33 observation points.

Table 1. Hyper-parameters values for the CDCGAN.

Name	Optimal choice
Optimizer	Adam
Learning rate	2×10^{-4}
The exponential decay rate for the 1st-moment estimates	0.5
Epochs	30,000
Normalization type	Batch
Weight of L_1 loss in the generator objective	100
Weight initialization method	Normal
Number of generator filters in the last conv layer	256
Number of discriminator filters in the first conv layer	256

Based on the trained CDCGANs, the SSIM is estimated for the test dataset using the method described in sub-section 3.4. To account for diurnal variations in demand and pressure, the leak detection threshold (T_{SSIM_0}) is then calculated on an hourly basis for 24 hours. The resulting thresholds are presented in **Fig. 6**. As demonstrated, hourly T_{SSIM_0} values are consistently larger for CDCGAN₃₃ compared to CDCGAN₇₈₀, because the prediction errors are also lower and the model-generated pressure maps more closely resemble the data.

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396 **Fig. 6.** Hourly thresholds of SSIM for leak detection.
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4.4. Leak Detection and Isolation

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Two sets of leakage scenarios, described in the following sub-sections, are employed to analyze the performance of the trained CDCGAN model in LD&L. In all scenarios, if leakage occurs and data points during the leak period are identified as anomalies by the CDCGAN model, the outcome is identified as a true positive (TP). On the other hand, if there is no leak in the WDN, and the model doesn't classify data points during the leak as anomalous, the outcome is a true negative (TN). The detection method can also fail. In this case, if the model fails to identify leaks, it results in a false negative (FN), and if it identifies leak-free conditions as anomalous, the outcome is a false positive (FP). Based on these concepts, several key metrics are calculated to evaluate the effectiveness of leak detection (Wan et al., 2022):

1. The true positive rate (TPR), is defined as:

$$TPR = \frac{TP}{TP + FN} \tag{5}$$

410

2. The true negative rate (TNR), is estimated as:

$$TNR = \frac{TN}{TN + FP} \tag{6}$$

411

3. Accuracy (ACC) is defined as:

$$ACC = \frac{TP + TN}{TP + TN + FP + FN} \tag{7}$$

412

413

For a TP, the detection time (DT) is employed to express the time interval between the actual start time of leakage and the time when a method successfully identifies an anomaly (i.e. CDCGAN

414 predicted pressure is less than T_{SSIM_o} for 5 consecutive time steps). In practice, it is highly
415 favorable to have the least DT to minimize water loss and its collateral damages. To quantify the
416 accuracy of leak localization, the graphical distance between the estimated leak location (i.e.
417 location with the minimum $SSIM_l$), and the actual leak location, is employed. We denote this by
418 GDRL.

419 **4.4.1. Hypothetical Single Leak Scenarios**

420 For the hypothetical single leaks, EPANET simulations are performed assuming that a single leak
421 has occurred in the WDN. Three different leak rates (with leak areas (LAs) equal to 0.0005, 0.005,
422 and 0.05 m²), and eight alternative leak locations are simulated, resulting in a total of 24
423 hypothetical single leak scenarios. Two leaks are selected to represent each of the four leak-free
424 pressure intervals defined in **Fig. 7**: one at the junction of 2 and the other at the junction of 3 pipes.
425 The leak area (A_L) is related to the leak flow rate (q_L) through the following equation ([Crowl and](#)
426 [Louvar, 2001](#)):

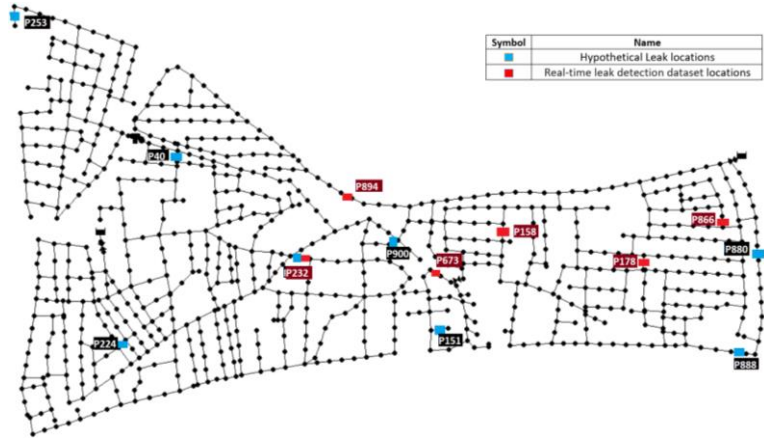
$$q_L = C_L A_L \sqrt{2gh_L} \quad (8)$$

427 Where C_L is the discharge coefficient with a default value of 0.75, h_L is the head, and g is the
428 acceleration of gravity. We assume that the leaks occur in a stepwise manner (with 10 equally
429 spaced steps) as demonstrated in **Fig. 8**, and are hence expected to cause a similarly stepwise
430 pressure drop in parts of the network. The simulation period pertains to the WDN conditions in
431 the first week of 2018, and the time steps are 5 minutes. For each scenario, this results in the
432 generation of 2,016 pairs of demand-pressure images. The generation of pressure images is once
433 done using 780 observations, and then again for 33 OPs, to assess how the performance of the
434 proposed approach is affected by the number of observation locations. For all hypothetical
435 scenarios, the leak starts at 0:00 of day five and ends at 24:00 of the same day.

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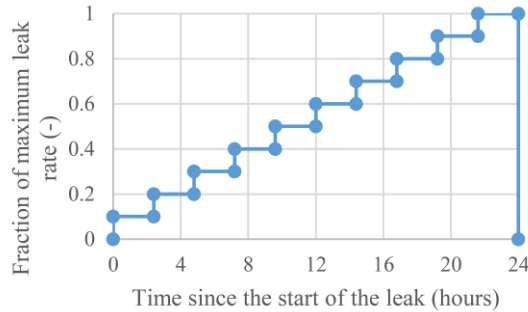
Leak location*	Pressure Range	Junction of	
		2 pipes	3 pipes
P-40	<30 m	■	
P-151			■
P-151	[30-40) m	■	
P-253			■
P-880	[40-50) m	■	
P 900			■
P-224	≥50 m	■	
P-888			■



438 * The numbers represent the node numbers in the L-Town WDN (Vrachimis et al., 2020)

439 **Fig. 7.** Location of hypothetical and real-time leaks in the WDN.

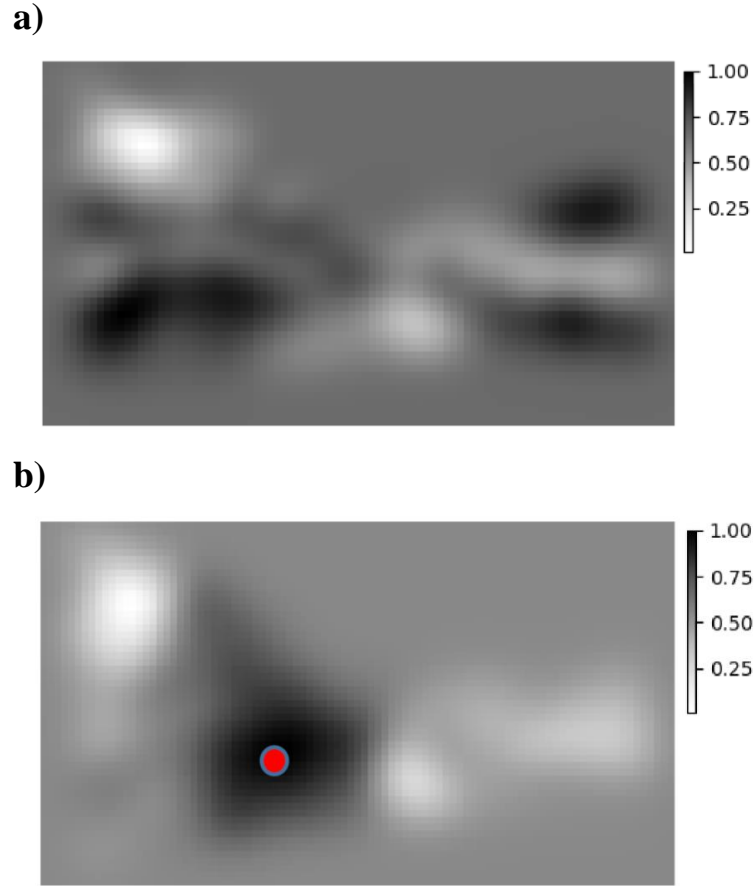
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444 **Fig. 8.** Stepwise increase in leak rate for the hypothetical single leak scenarios.

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447 As an example of the images acquired through Kriging interpolation, **Fig. 9** compares pressure
448 maps of a no-leak condition with one of the hypothetical single leakage scenarios ($LA = 0.05 \text{ m}^2$)
449 in the same time step. Both images are obtained using the EPANET numerical model using 780
450 Ops. This exemplary figure demonstrates that the pressure maps significantly differ between the
451 two cases, especially in the vicinity of the leak location. In our proposed leak identification
452 methodology, this difference is quantified using the SSIM index.



453

454 **Fig. 9.** Examples of how leaks appear in pressure image: (a) no-leak, and (b) leaky conditions. The red
 455 circle has been overlaid on the right image to show the location of the leak.

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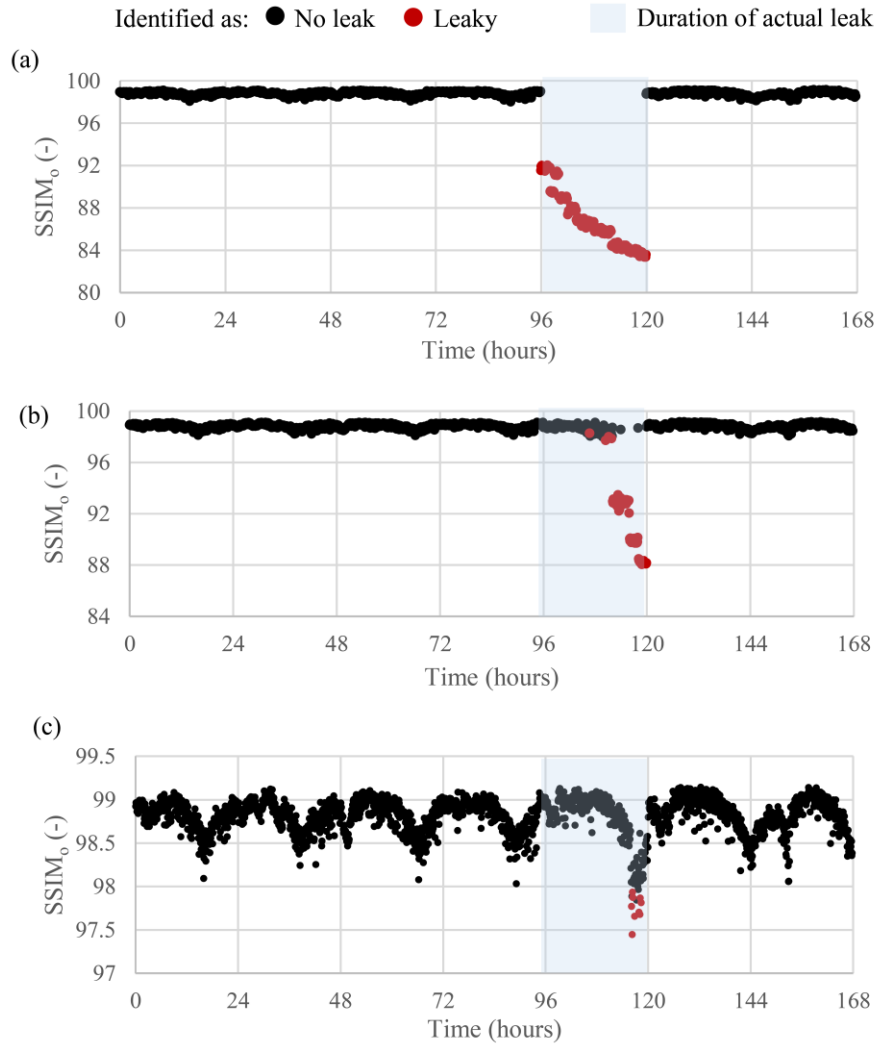
457 **Fig. 10** illustrates the $SSIM_o$ times series obtained from CDCGAN₇₈₀ for the hypothetical leak at
 458 P-40, based on three different leak rates. For the highest leak rate ($LA = 0.05 \text{ m}^2$), $SSIM_o$ drops
 459 below the hourly leak detection threshold (T_{SSIM_o}) as soon as the leak starts, and increases back to
 460 its normal range as the leak ends (**Fig. 10a**). Hence, the model is perfectly capable of identifying
 461 this burst with minimal DT.

462 To demonstrate how the proposed method identifies the leak location, **Fig. 11** shows the $SSIM_l$
 463 map for three different time steps during the leak. The location of the minimum $SSIM_l$ and the
 464 actual leak location is also shown in the figure. During the leak, $SSIM_l$ significantly drops in the
 465 vicinity of the leak location, forming a zone of low $SSIM_l$ values around the leak location. The
 466 extent of this zone increases with increasing leakage rates. The estimated location of the leak

467 (pertaining to the minimum value of $SSIM_l$) gradually converges to the actual leak location with
468 an increased leakage rate. **Fig. 12a** shows how GDRL varies after the identification of the leak. GDRL
469 starts from about 12m and decreases with increasing leakage rate until it converges to 4 m. This is a
470 relatively highly accurate estimation compared to previous studies (see the review paper, by [Wan
471 et al., 2022](#)).

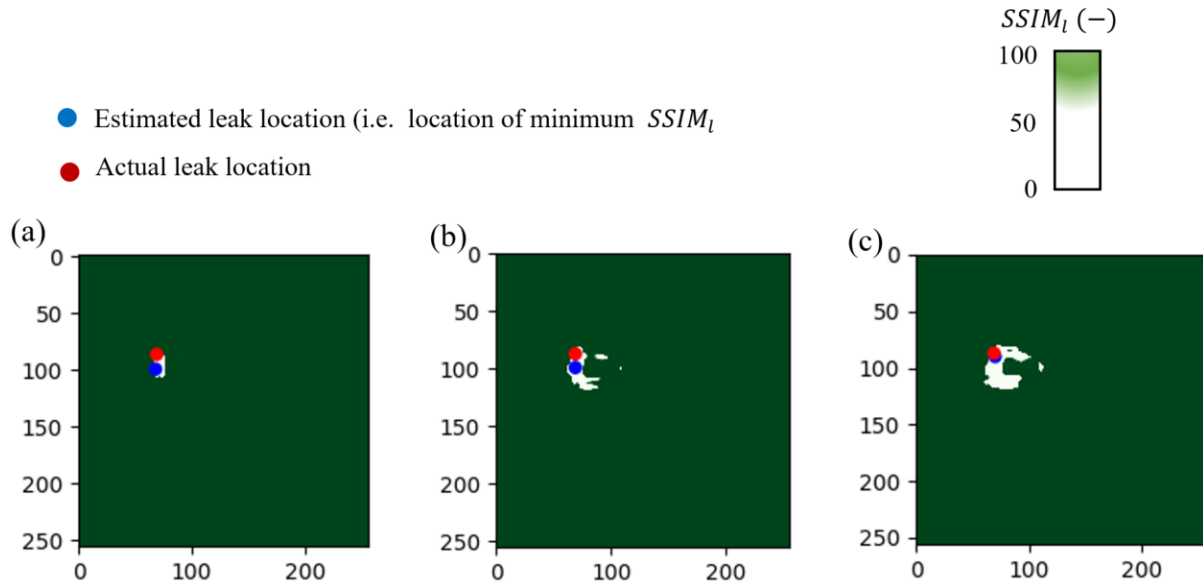
472 For the middle value of leak rate ($LA = 0.005 \text{ m}^2$), $SSIM_o$ becomes smaller than T_{SSIM_o} with
473 delay ($DT \cong 16$ hours), and after the leak rate has increased beyond 0.002 m^2 (**Fig. 10b**). **Fig. 12b**
474 demonstrates how GDRL varies after the leak is identified. GDRL starts from around 140 m, and
475 then sharply drops to about 12 m after a few hours. For the smallest value of leak rate ($LA =$
476 0.0005 m^2), DT equals about 21 hours, and the leak is identified only when the leak rate nears its
477 maximum value (**Fig. 10c**). GDRL is approximately 96 m in this scenario.

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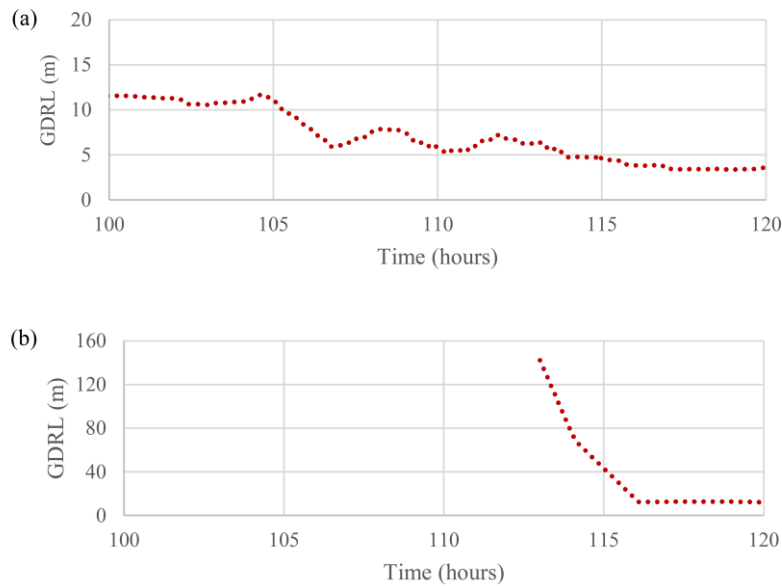


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Fig. 10. SSIM₀ time series the for the hypothetical leak at P-40, based on: (a) $LA = 0.05 \text{ m}^2$, (b) $LA = 0.005 \text{ m}^2$ and (c) $LA = 0.0005 \text{ m}^2$.



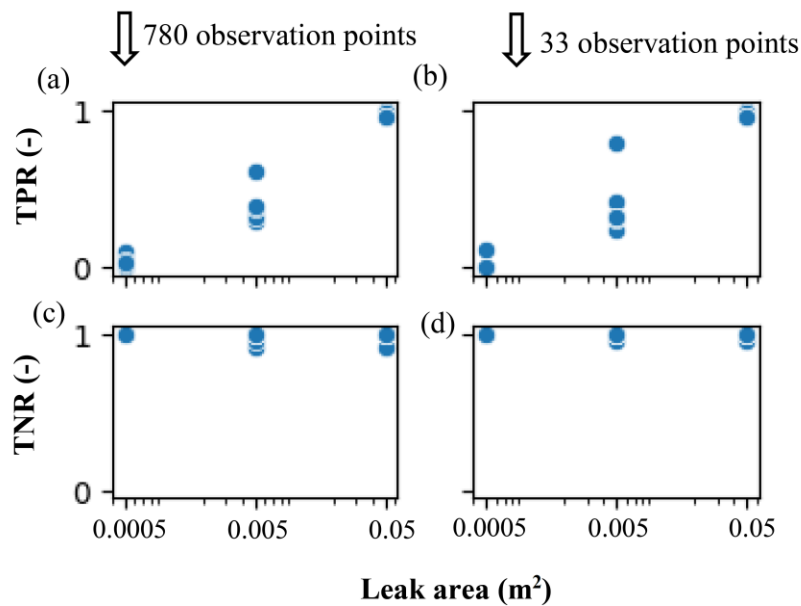
505
 506 **Fig. 11.** The $SSIM_l$ map for the hypothetical single leak at times: (a) $t = 100$, (b) $t = 110$, and (c) $t =$
 507 120 hours since the start of the synthetic leak simulations.
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 510 **Fig. 12.** GDRL time series for the hypothetical leak at P-40 based on: (a) $LA = 0.05 \text{ m}^2$, and (b) $LA =$
 511 0.005 m^2
 512

513 **Fig. 13** provides the TPRs and TNRs obtained from applying the proposed methodology to all
 514 hypothetical single leak scenarios. As demonstrated in **Fig. 13a, b** the TPR is close to the ideal
 515 value of one for $LA = 0.05 \text{ m}^2$, highly decreases with decreasing leak rates, and approaches zero

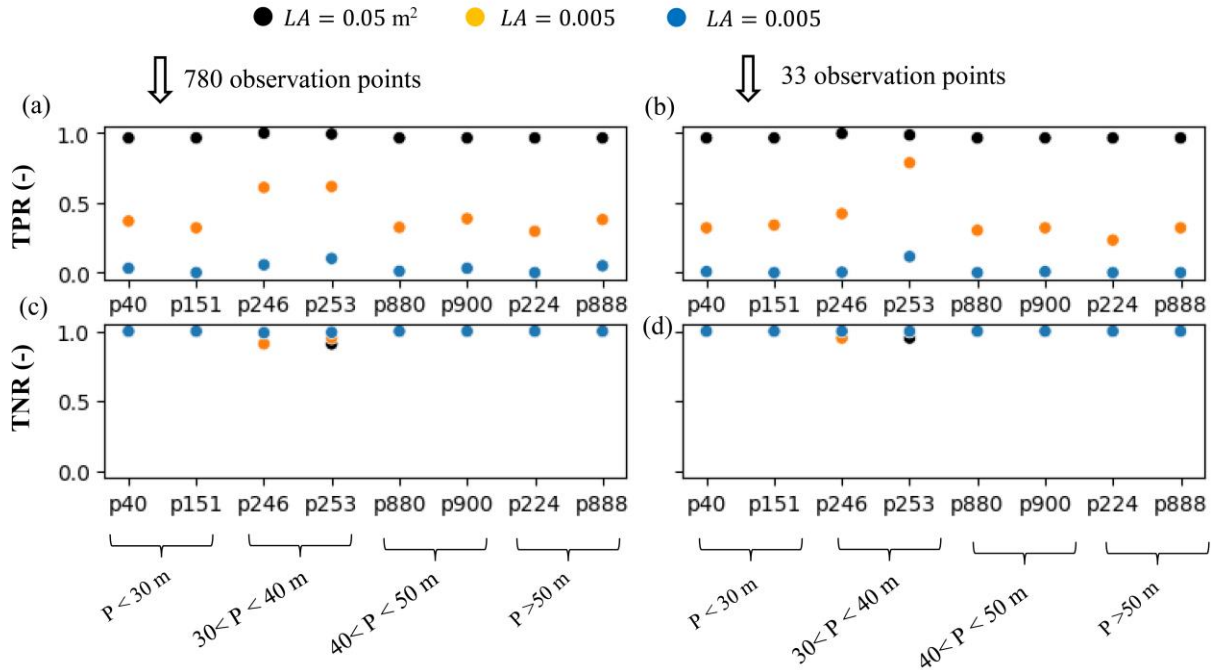
516 for $LA = 0.0005 \text{ m}^2$. Detail analysis of the $SSIM_0$ time series for the hypothetical single leak scenarios
 517 (an example of which was presented in **Fig.10**) shows that the detectable threshold representing
 518 the minimum detectable leak rate is between $0.0001\text{-}0.0005 \text{ m}^2$ for the various scenarios. The
 519 maximum standard deviation of TPR is observed for the middle value of leak rate ($LA = 0.005$
 520 m^2). The TNR is generally high for all scenarios (**Fig. 13c, d**). Comparison of TPR and TNR values
 521 obtained from incorporating 780 (**Fig. 13a, c**) and 33 (**Fig. 13b, d**) OPs, shows a minor difference
 522 between the two, with the average TPR for 780 OPs 0.02 higher than 33 OPs. The average ACC
 523 across all scenarios is 0.91 and 0.90 for 780 and 33 OPS, respectively.
 524



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 526 **Fig. 13.** TPR and TNR for various hypothetical leak scenarios.
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 529 **Fig. 14** compares TPR and TNR values obtained for leaks in various locations. Based on this figure,
 530 there seems to be no correlation between the leak location or pressure range and the associated
 531 TPR and TNR. This is observed for both 780 and 33 OPs.

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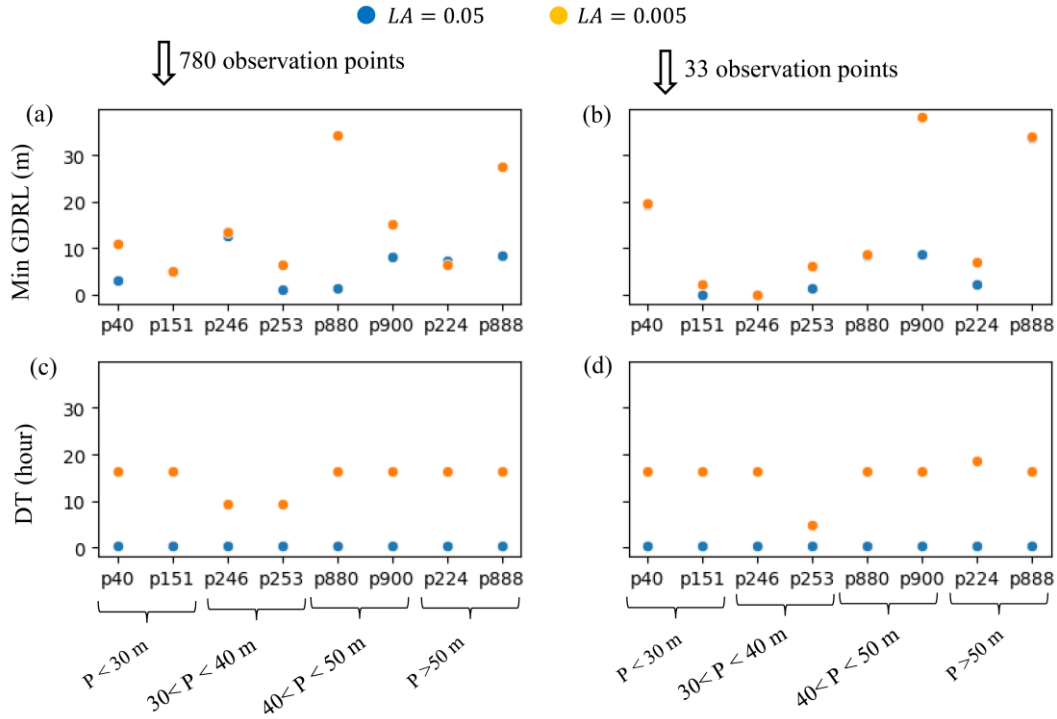
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Fig. 14. TPR and TNR for leaks in various locations. The associated pressure ranges are shown for each leak location.

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Fig. 15 provides the DT and minimum GDRL ($GDRL_{min}$) values obtained for various leak locations and two different leak rates. It can be seen that DT is significantly lower for the larger leak rate. For $LA = 0.005 \text{ m}^2$, DT is constantly below 17 hours, and for $LA = 0.05 \text{ m}^2$ DT is generally less than an hour. $GDRL_{min}$ for the larger leak rate is equal to or less than the associated values of the smaller leak, indicating that, as expected, larger leaks can more accurately be localized. For LA equal to 0.05 and 0.005 m^2 , $GDRL_{min}$ is lower than 11 and 35 m, respectively. There is no correlation between leak location and either DT or $GDRL_{min}$.

547



548
 549 **Fig. 15.** GDRL and DT for leaks in various locations. The associated pressure ranges are shown for each
 550 leak location.
 551

552 4.4.2. Real-time Leak Detection for a One-Year Dataset

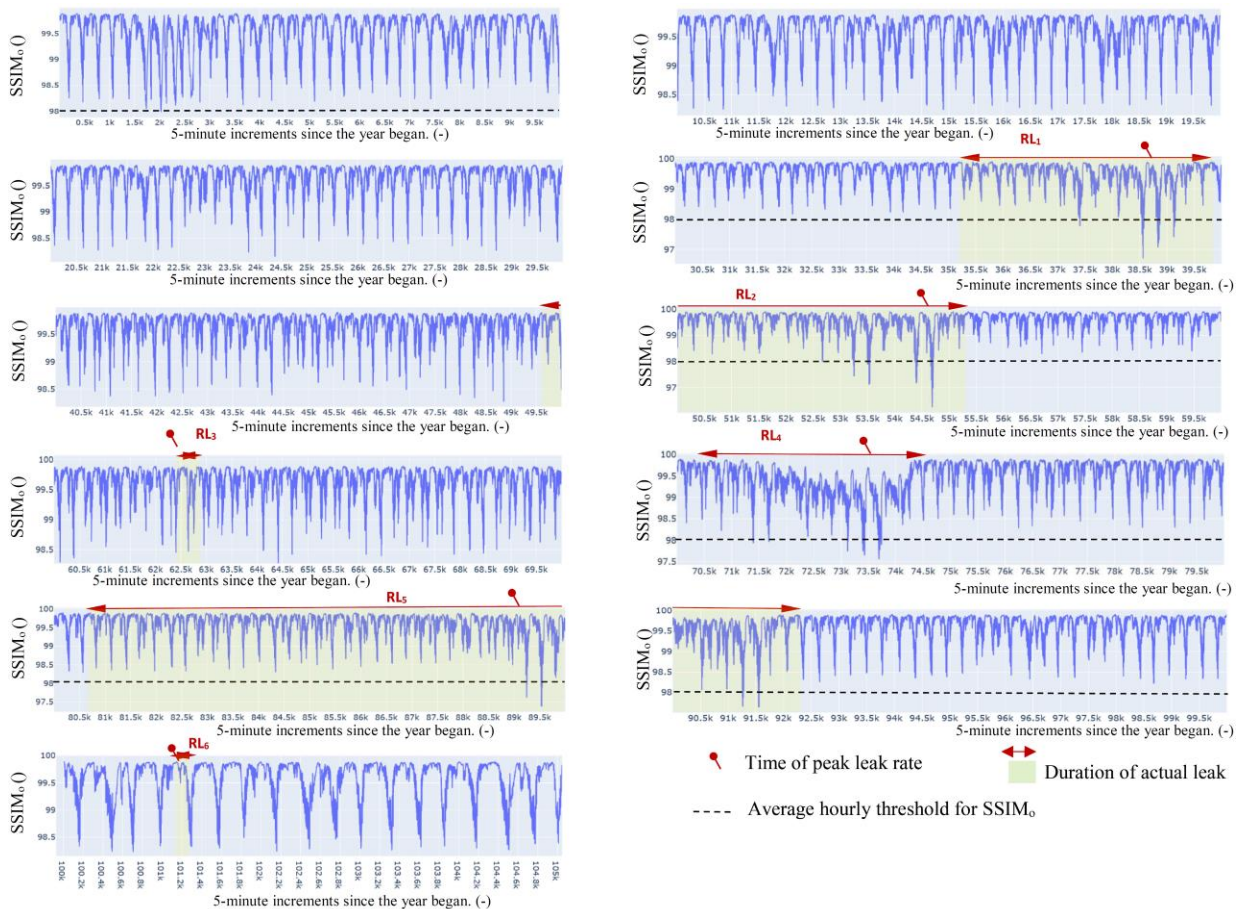
553 Six real-time leaks in the L-Town WDN provided by the *Battle of Leakage Detection and Isolation*
 554 *Methods* (BattLeDIM) (Vrachimis et al., 2022), are also assessed. These leaks occur at different
 555 times during the year 2018 (with no concurrency) and involve a gradual increase in the outflow
 556 rate. The leak locations and magnitudes are presented in **Table 2**. All six leaks have smaller peak
 557 values of leak rate compared to the hypothetical scenarios described in the previous sub-section.
 558 A single one-year EPANET simulation is performed by incorporating these leaks, and the results
 559 are used to create pairs of demand-pressure images for each 5-minute time step. Only 33 OPs (of
 560 the sensor locations) are employed to create the pressure images. These images are incorporated
 561 in the LD&L algorithm, and the resulting $SSIM_0$ time series for the entire year is presented in **Fig.**
 562 **16**. Except for the leak RL_6 (which has the shortest duration among the six leaks), the other five
 563 leaks (RL_1 to RL_5) are detected by the proposed methodology. Generally, leak detection only
 564 becomes possible near the peak leak rate. For the entire year, the accuracy of leak detection is
 565 70%. $GDRL_{min}$ ranges between 160 to 185 m for the five identified leaks.

566 **Table 2.** Summary of the real-time leak detection scenarios.

Scenario	RL_1	RL_2	RL_3	RL_4	RL_5	RL_6
Leak position	p232	p673	p866	p183	p158	p427
Leak area at the peak (m ²)	0.00032	0.00024	0.00031	0.00041	0.00028	0.00031
Leak type	incipient	incipient	abrupt	incipient	incipient	abrupt
Start (date, time, time step)	2018-05-01, 02:35, 35,167	2018-06-20, 15:45, 49,725	2018-08-03, 07:00, 62,292	2018-08-28, 10:35, 69,535	2018-10-06, 02:35, 80,671	2018-12-15, 13:00, 100,956
End (date, time, time step)	2018-05-17, 09:20, 39,856	2018-07-10, 10:25, 55,421	2018-08-03, 11:00, 62,340	2018-09-15, 17:30, 74,802	2018-11-15, 13:35, 92,323	2018-12-15, 17:00, 101,004
Peak (date, time, time step)	2018-05-12, 16:05, 38,497	2018-07-06, 15:45, 54,333	2018-08-03, 07:00, 62,292	2018-09-10, 02:45, 73,185	2018-11-10, 02:35, 88,867	2018-12-15, 13:00, 100,956
Mean daily discharge (m ³ /hour)	4.11	3.01	3.98	5.27	3.6	3.99

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Fig. 16. SSIM_o time series a one-year simulation based on the real-time leaks of L-Town

571 **5. Conclusion**

572 Previous studies in different settings have shown that GANs are a promising tool for anomaly
573 detection and localization (Xia et al., 2022). Due to their ability in mapping complex non-linear
574 relationships, robustness in presence of uncertainty, and adaptability to limited data, GANs can
575 theoretically overcome many key challenges of LD&L. In this paper, we exploit the use of a
576 particular GAN architecture and develop an LD&L methodology around it. Our key contributions
577 can be summarized as follows:

- 578 • We develop a conditional GAN architecture based on pix2pix to predict the pressure
579 distribution resulting from a known demand distribution in the context of image-to-image
580 translation. The GAN model is trained using hydraulic model-generated data of leak-free
581 conditions and learns a discriminative boundary around the normal, leak-free instances.
582 New data instances that don't belong to this normal class are identified as anomalous.
- 583 • We propose the use of the SSIM index for LD&L. In this framework, the SSIM index is
584 computed over the entire pressure distribution image for leak detection, and a local estimate
585 of SSIM is employed for leak localization.
- 586 • We analyze the effectiveness and accuracy of the proposed methodology using the L-Town
587 WDN case study. Besides the six real-time leaks provided by BattLeDIM, several
588 hypothetical leak scenarios are also defined and analyzed to assess the minimum detectable
589 leak, and the correlation between leak rate and location with key metrics such as TPR,
590 TNR, ACC, DT, and GDRL.

591 The L-Town benchmark problem has several key underlying assumptions, allowing for simplified
592 modeling and LD&L. However, these assumptions may not reflect the actual circumstances in a
593 WDN. Specifically, the assumptions include (1) the network's homogeneity, where pipes, nodes,
594 and other components are assumed to have similar properties and behave uniformly; (2) the
595 absence of leaks or defects at the start of the simulation; and (3) a fully-piped network, which does
596 not include open channels, and (4) no changes in pipe characteristics and system configuration
597 over time. Additionally, in developing our LD&L methodology, we assume that both demand
598 uncertainty and measurement error are normally distributed, which may or may not reflect the
599 actual circumstances in a WDN. Although the normal distribution is commonly used in this
600 context, there are other distribution models, such as the lognormal, gamma, and Weibull
601 distributions, which are also widely used to model demand uncertainty or measurement error in

602 WDNs. The choice of distribution should be based on the data and the specific needs of the
603 analysis.

604 Various architectures of GANs, such as f-AnoGAN (Schlegl et al., 2019), BiGAN (Kaplan and
605 Alptekin, 2020), etc., have been proposed for anomaly detection and localization in other settings,
606 and we suggest future studies consider these various architectures to improve LD&L in WDNs.

607 Future investigations could focus on exploring the robustness of GAN-based methods across
608 different operational scenarios and evaluating the impact of the WDN's size and complexity on the
609 accuracy of the method. Additionally, conducting a comprehensive analysis of the effect of
610 simultaneous leaks and observation location on the model's accuracy and reliability may also be a
611 valuable avenue for further research.

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