

1 **Semi-supervised Clustering Approach for Pipe Failure Prediction with Imbalanced Dataset**

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7 **Abstract**

8 In recent years, machine learning (ML) approaches have been widely used for water pipe condition
9 assessment and failure prediction. These methods require a considerable amount of data from water
10 distribution networks (WDNs). Imbalance and short data, either asset or failure data, compromise the
11 model's prediction performance. In this research, with the presence of only two years of failure data in
12 a real WDN, three ML methods, XGBoost, random forest and logistic regression, were utilised to
13 prioritise the asset rehabilitation. To address the issue of imbalance data, a novel method of semi-
14 supervised clustering was proposed to leverage the domain knowledge in combination with
15 unsupervised learning to divide the dataset into homogeneous categories and enhance the classification
16 accuracy. The introduced approach presented a higher performance in comparison with well-known
17 data science class imbalance treatment techniques. Furthermore, analysis of the results indicated that
18 classification evaluation metrics struggled to practically assess the effectiveness of various methods.
19 To tackle this, an economic indicator was proposed to rank the pipes for rehabilitation based on their
20 cost and likelihood of failure (LoF). Preventive maintenance using the results of an economic indicator,
21 reduces the number of failures with a small fraction of the total replacement cost. Moreover, another
22 indicator was developed to consider the consequence of the failures and LoF, simultaneously. This
23 indicator mitigates the flow capacity reductions in WDNs caused by failures, in a cost-effective manner.
24 The result of this study provides asset managers with a powerful tool to prioritise assets for
25 rehabilitation.

27 **Practical Application**

28 In recent years, machine learning (ML) algorithms have gained popularity for assessing water pipe
29 conditions and predicting failures. However, their effectiveness relies on substantial data from water
30 distribution networks (WDNs). Challenges arise with limited (imbalanced) data, affecting prediction
31 accuracy. This study focuses on a specific WDN with only two years of failure data, aiming to identify
32 priority assets for rehabilitation. Three ML methods (XGBoost, random forest, and logistic regression)
33 and a novel semi-supervised clustering approach were employed. This method combines expert
34 knowledge with traditional techniques, significantly improving predictive accuracy. By applying ML
35 algorithms within these homogenous clusters, predictive accuracy was enhanced notably. Two novel
36 metrics were introduced for prioritising pipe rehabilitation: one combining failure likelihood and
37 replacement costs, and the other evaluating pipes based on their significance within the WDN and
38 associated rehabilitation expenses. These models empower asset managers to optimise pipe replacement
39 budget allocation and enhance the network performance.

40 **Keywords:** water distribution network; pipe failure prediction; semi-supervised clustering; class
41 imbalance; machine learning.

42

43 **Introduction**

44 Water distribution networks (WDNs) are essential for providing safe drinking water in adequate
45 quantity. However, maintaining WDNs and reducing water loss have become top priorities. The
46 sustainability of the infrastructure for water supply is crucial for the continuous delivery of water. One
47 of the major obstacles that hinders the proper functioning of water supply systems is pipe bursts. Pipe
48 bursts result from intricate interactions among various factors, such as pipe intrinsic, environmental,
49 and operational factors, which contribute to the degradation and eventual failure of pipes (Barton et al.,
50 2019; Philip and Aljassmi, 2020, Dawood et al., 2020). Accurate and timely prediction of pipe failure
51 can reduce the economic, environmental, and social impacts of bursts (Hekmati et al., 2020). This can

52 help water utilities to move from reactive maintenance to predictive. In recent years, pipe condition
53 assessment has gained attention from asset managers in prioritising rehabilitation (Rifaai et al., 2022).

54 Failure of water pipes is a complex problem that is affected by a variety of static, and dynamic factors.
55 The knowledge and understanding of the factors that lead to pipe failure would allow utility companies
56 to create efficient management and maintenance plans for water distribution networks. Static factors,
57 such as pipe material, diameter, thickness, installation date, quality of workmanship during
58 manufacturing and transportation, and type of soil under which the pipe is buried, do not change over
59 time and have the potential to affect a pipe's structural stability. Age-related structural deterioration and
60 corrosion to pipelines increase the likelihood of failure (Barton et al., 2019). The type of soil in which
61 pipes are laid may affect how they will deteriorate (Rajani et al., 1996). Barton et al. (2020) found that
62 water pipe failures are strongly associated with the presence of clay soils in the vicinity.

63 Dynamic factors differ from static factors in that they vary with time. Pressure fluctuations in WDN,
64 pipeline corrosion, water quality, and transient events are examples of dynamic factors that cause pipe
65 deterioration. Pressure fluctuations can cause stress in pipes, which can lead to leaks and breakages in
66 WDN (Martínez-Codina et al., 2015; Marsili et al., 2020). In high pressure locations, utilities install
67 pressure reduction valves (PRVs) to reduce the risk of pipe failure (Kabasha and van Zyl., 2020; Jara-
68 Arriagada and Stoianov, 2021). Corrosion is another dynamic factor that affects the deterioration of
69 pipes; in particular, the corrosion rate of Ductile iron (DI) pipes significantly influences their failure
70 rate (Wasim et al., 2018). Low water quality can result in mineral accumulation and corrosion, which
71 can restrict water flow and harm pipe walls (Monfared et al., 2021). Dynamic factors also include
72 environmental factors and weather conditions, such as temperature and rainfall data, which are grouped
73 with other environmental parameters that influence the deterioration of water pipes (Kakoudakis et al.,
74 2018). According to some studies, dry seasons may increase the number of leaks and breakdowns in
75 the water pipelines (Wols and van Thienen, 2014; Jara-Arriagada and Stoianov, 2021).

76 Many researchers have examined a broad range of approaches for pipe failure prediction (Scheidegger
77 et al., 2005; Giraldo-Gonzalez and Rodriguez, 2020; Robles-Velasco et al., 2020). Generally, failure
78 prediction methods can be categorised as deterministic, probabilistic and machine learning (ML)

79 models. Deterministic models are useful for predicting failure rates in WDN or a group of pipes due to
80 simplicity and low data requirement. Probabilistic models can effectively predict the time to failure and
81 probability of failure by incorporating randomness in their predictions (Barton et al., 2022). Unlike
82 other models, machine learning (ML) models depend on data to learn and can easily adapt, resulting in
83 improved accuracy in prediction tasks (Lazar et al., 2019). Probabilistic and deterministic models are
84 both statistical models which employ available historical failure data to forecast pipe failures utilising
85 corresponding factors (Rajani and Kleiner, 2001). Statistical models rely on pre-defined models that are
86 based on prior knowledge of the system being studied, while ML methods can automatically learn and
87 adapt to the data, allowing them to detect complex patterns and relationships that may be missed by
88 statistical models. ML approaches such as Artificial Neural Networks (ANN), and tree-based models
89 like Decision Trees (DT), Random Forrest (RF), and Boosted trees have recently been used to predict
90 pipe failure. Tree-based models have been examined in various studies, showing significant prediction
91 capability (Robles-Velasco et al., 2023).

92 The abovementioned methods require different types of data from pipes (diameter, length, material,
93 etc.), the network (pressure, flow, etc.), and environment surrounding the pipe (weather conditions, soil
94 properties, etc.). The inadequacy of appropriate data in the water industry for pipe failure prediction is
95 a widespread challenge (Scheidegger et al., 2013). This issue stems from unavailability of information
96 on previously failed pipes, leading to an imbalance data for training a model.

97 Class imbalance happens in datasets where one or more classes (majority) have a much larger number
98 of instances than other classes (minority). This is a well-recognized issue in the field of data science,
99 particularly in the context of classification (Kulkarni et al., 2020). Throughout the evolution of ML
100 models, the challenge of class imbalance has been taken into consideration, leading to the development
101 of various strategies over time to effectively address this issue (Akintola et al., 2022). The main
102 difficulty with class imbalance is the classifier's tendency to assign all data to the majority class. Some
103 techniques have been proposed to overcome the problem of class imbalance. These include
104 oversampling, undersampling, and class weights, among others (Burez et al., 2009; Liu et al., 2022).
105 Although these techniques may improve the classifier's prediction capability when dealing with

106 imbalanced data, they also have some limitations. Undersampling can omit potentially valuable
107 information that could be crucial for developing rule classifiers, and the sample selected by random
108 undersampling may be biased and not an accurate representation of the overall population.
109 Oversampling could result in overfitting because it reproduces minority class data. Another technique
110 for dealing with imbalanced datasets is class-weighting. The idea is to penalise the classifier for
111 misclassifying the minority class by assigning a higher weight, while simultaneously decreasing the
112 weight for the majority class (Zhu et al., 2018).

113 Clustering is another technique to identify strong correlations between the variables and the desired
114 outcome for ML algorithms. As pipes with similar features are likely to experience comparable failures,
115 clustering results in groupings of data that are similar to one another. These techniques utilise a group
116 of classifiers, instead of a single one, which incorporate different failure patterns (Kakoudakis et al.
117 2017; Wols et al., 2019, Chen and Guikema, 2020). This paper proposes two major novelties:

118 1) The novel clustering approach proposed in this paper concentrates on employing the domain
119 knowledge in the field of water distribution networks. In other words, the clustering not only follows
120 an un-supervised mathematical algorithm, but also relies on the insights of an expert around factors
121 influencing the failures in a WDN, presenting a “semi-supervised” approach.

122 2) The paper argues that the common evaluation metrics for failure prediction models are not suitable
123 for WDN, so two novel models are proposed to a) properly rank the pipes for rehabilitation based on
124 their likelihood of failures and consequence of failures; and b) practically assess the performance of
125 various prediction models by considering the cost of replacement for both correct and incorrect
126 predictions.

127

128 **Case study and data preparation**

129 To examine the performance of the proposed approaches, they were applied to entire WDNs of a utility
130 company in the UK. The asset data includes the pipe characteristics, i.e., length, diameter, installation
131 date, elevation, and the categories of the soil types where the pipes are buried. The network consists of

132 32,842 km of pipelines with nearly 400,000 assets. The database contains 18,432 failure events. The
133 dataset on failures comprises information regarding the pipes that failed, along with the date on which
134 each failure occurred. Pipe failures were only recorded for 26 months, starting from August 2019 to the
135 end of October 2021. This dataset is imbalanced as it is not a good representative of the pipe failure
136 history.

137 Fig. (1) presents the percentages of different pipe materials in terms of length and failures in the case
138 study. As shown in Fig. (1-a), 17% and 20% of the WDN are made of asbestos cement (AC) and cast
139 iron (CI) pipes, respectively. Also, 26% and 31 % of the failures occurred in the AC and CI pipes,
140 respectively, which implies a high rate of failure in these materials (Fig. 1-b). This could be because of
141 their higher ages, compared with the PVC and Polyethylene (PE) pipes. The PE pipes have only 26%
142 of the failures, while they form 43% of the length of the network.

143 As expected, there is a relationship between the used pipe materials and the installation history (Fig. 2-
144 a). CI pipes are the oldest ones that are still in service at many locations. From the 1930s, AC pipes
145 were introduced to the market and their share of the entire network increased until PVC, and PE pipes
146 took over the water industry until today. As shown in Fig. (2-b), the majority of the pipes have diameters
147 less than 200 mm. Although pipes with diameters up to 2500 mm exist in the WDN, only those with
148 diameters less than 500 mm are shown in Fig. (2-b) due to their absolute majority.

149 Characteristics of the WDN are briefly demonstrated in Table (1). Most failures occurred in the CI pipes
150 (5586 failures) and the pipes with diameters between 100 and 200 mm (10,167 failures). In terms of the
151 number of failures per length of the pipes, the CI and AC pipes have failure rates significantly higher
152 than the others. For this reason, only these two pipe materials have been used to develop a failure
153 prediction model in this research. The higher the diameter, the lower the failure rate. Nonetheless, the
154 large diameter pipes were not eliminated from the database, due to their high consequence of failure.
155 Also, by increasing the age of the assets, the failure rate increased. Interestingly, the failure rate in 50-
156 100 year old pipes was not much less than those with over 100 years of age. Overall, the failure rate of
157 the WDN was 25.9 failures/100 km/year. The number of failures per asset could present the level of
158 class imbalance in the data. In this case study, the overall failure percentage was 4.6, while the highest

159 values correspond to AC and CI pipes with 7.2 and 6.9 percent. On the other hand, only a few assets in
160 the dataset experienced failure more than once. As a result, the time to failure cannot be calculated for
161 most of them, therefore, being failed or not failed was assigned as a binary variable to each asset. In
162 summary, the dataset suffers from highly imbalanced data, which should be treated in a proper manner,
163 to achieve a reasonable prediction capability.

164 In this WDN, district metered areas (DMAs) have been divided into discrete pressure areas (DPAs),
165 and pressure was measured by taking readings at critical measurement points (CMPs), which were
166 situated at the highest elevation of each DPA and also at pressure reducing valves (PRVs) every 15
167 minutes. Due to missing records, the average time series of pressure measurements were shorter than
168 26 months. To summarise the pressure data, the statistical values of time series were extracted for each
169 CMP, including the mean pressure, median pressure, pressure range, 5th and 95th percentile of pressure,
170 and minimum and maximum pressures (Fig. 3). Based on Akaike Information Criteria (AIC)
171 (Bozdogan, 1987), mean pressure, median pressure and 95th percentile of pressure were selected as
172 representatives of pressure time series data for each asset. Digital records of each asset's average
173 elevation were included in the dataset. In the absence of a hydraulic model for the WDN, pressure
174 measurements were compensated using elevation data to give an estimation of the static pressure head
175 in each asset.

176 To find the main factors influencing pipe failure, a correlation analysis was carried out (Fig. 4). The
177 results show that there are weak correlations between failures, and pipe intrinsic factors (diameter, age,
178 length, and elevation), environmental factors (soil type), and operational factors (pressure). The highest
179 correlation coefficients belong to length (0.16), age (0.05) and 95th percentile of pressure (0.03),
180 respectively, which implies a weak one-to-one relationship between independent variables and the
181 target variable. All of the available covariates were utilised in training the machine learning models,
182 except the standard deviation of the pressure, which was eliminated due to a very low correlation
183 compared to the other factors.

184

185 **Methodology**

186 This paper mainly concentrates on presenting a novel approach for grouping the data into clusters,
187 employing the knowledge of the experts in the field of water distribution networks. In other words, the
188 clustering approach both follows a well-known un-supervised algorithm, i.e., K-Means, and utilises the
189 insights of an expert around factors influencing the failures in a WDN, presenting a “semi-supervised”
190 approach. To evaluate the effectiveness of the proposed method, a failure prediction model is developed
191 by combining the common clustering and classification methods. Then, the model is enhanced using
192 the proposed clustering method.

193 This section describes various components of the failure prediction model. First, a set of strategies for
194 dealing with imbalanced data, e.g., under-, over-sampling, and class weight, are examined and the best
195 performing one is selected. Then, the K-Means algorithm and the proposed clustering methods, i.e.,
196 domain knowledge and hybrid clustering, are discussed. Once the dataset is categorised into
197 homogeneous clusters, the selected class imbalanced treatment method is applied on each cluster, then
198 three well-known classifiers were introduced and employed to predict the failures in pipes. The section
199 wraps up by introducing new metrics to distinguish various solutions for pipe rehabilitation. These
200 metrics assess the solutions from economic and failure consequence points of view. Fig. (5) presents
201 the flowchart of the failure prediction model developed in this study.

202 **Treating imbalanced data**

203 Given that no failure occurred for the majority of the pipes, and that the pipe failure data collection
204 period was too short to create an accurate prediction model, the database clearly displays class
205 imbalance. The consequence will be poor performance in predicting the minority class, which is crucial
206 for pipe failure prediction models. In such a case, ML algorithms will focus on the majority class (not
207 failed pipes) and neglect the minority class (failed pipes) (Liu et al., 2022).

208 Some methods were proposed for class imbalance situations, which were applied to the dataset in this
209 study while training the model. These include random under-, over-sampling, synthetic minority
210 oversampling technique (SMOTE), and class weight.

211 The random undersampling method randomly removes a group of majority classes, and continues until
212 the numbers of each class are balanced. In this strategy the model trains itself with less data than normal,
213 which may result in the removal of important information from the dataset.

214 The random oversampling technique involves randomly duplicating additional data from minority
215 classes until the populations of all classes are balanced. This may result in overfitting and poor
216 performance of the model when classifying unseen data.

217 The Synthetic Minority Oversampling technique (SMOTE) uses the K-nearest neighbour algorithm to
218 select a point from the minority class and its K neighbours. It then places synthetic points randomly on
219 the line connecting the two points. The minority and majority classes are balanced by repeating this
220 process. Despite not duplicating, SMOTE might prevent overfitting, but as a drawback, this approach
221 has the potential to create artificial data that lacks an accurate representation of the minority class, which
222 could compromise the performance of ML models.

223 Class weights technique assigns higher weight to the minority class and lower weight to majority class.
224 Unlike the oversampling and undersampling approaches, the number of members in the minority and
225 the majority classes does not change by the class weights technique, i.e., it deals with class imbalance
226 data without removing valuable data or introducing artificial data.

227 **Clustering the data**

228 A classifier can be trained on a homogenous set of data to reach an acceptable prediction ability. When
229 data is not homogeneous, it can be divided into smaller clusters, and a classifier could be trained for
230 each cluster. This approach may lead to higher prediction capability for water assets (Chen and
231 Guikema., 2020; Abokifa and Sela, 2023).

232 In this study, the CI and AC pipes have different structural characteristics (Barton et al., 2019), so assets
233 with the same material type are considered in the same group and the clustering process is applied for
234 each group, separately.

235 **K-Means clustering**

236 In general, clustering might be used to generate collections of datapoints of pipes aggregated due to
237 similar pipe attributes. As a popular unsupervised machine learning algorithm, K-Means clustering
238 could be employed. A target value for k, which denotes the number of centroids, must be established in
239 K-Means clustering. Centroids are the areas that indicate the clusters' centres. The K-Means algorithm
240 finds k centroids, keeps the centroids as minimal as possible, and then assigns each data point to the
241 closest cluster. K-Means clustering was applied in earlier research showing a potential performance
242 improvement in pipe failure prediction (Kakoudakis et al., 2018; Gonzalez et al., 2020).

243 In this study, three variables of diameter, age, and length are used to generate clusters by the K-Means
244 clustering method. Length and age of the pipes had the highest correlations with failures, as mentioned
245 in Fig. (4), so, they were considered as explanatory features for the failures, and were selected for
246 clustering. Moreover, the diameter of the pipes which is an inherent feature of the pipes, available for
247 every water utility, was selected as another clustering variable. The optimal number of clusters, k, for
248 the datasets is selected from the best F1-score value after classification. F1-score is defined along with
249 other evaluation metrics in Section 3.4. As an unsupervised clustering method, K-Means generates
250 clusters in each of which the classifier has the same prediction capability as un-clustered data. If the
251 clustering is performed considering the target value, it could result in a more efficient classification.

252 **Domain Knowledge clustering approach**

253 In this research, in addition to the K-Means method, a new clustering has been proposed by using the
254 domain knowledge. In this way, the cumulative number of failures is depicted as a function of
255 independent variables and the clustering is conducted based on the graph variations. For example, the
256 variation of cumulative number of failures with age is shown in Fig. (6) for the AC and CI pipes. In this
257 case, 7 ranges of the asset ages are determined for the CI pipes as low failure (regions 1, 3, 5, and 7)
258 and high failure ages (regions 2, 4, and 6) (Fig. 6-b). A high failure region demonstrates a significant
259 jump in the number of failures along a limited range of the ages. This approach leads to a semi-
260 supervised clustering method which creates homogeneous clusters according to both independent and
261 target covariates.

262 The same clustering has been done for the other clustering variables of diameter and length. Some
263 clusters were found to be too small to train a classifier. Therefore, some small neighbouring clusters
264 were merged to form larger ones. Finally, the overall number of clusters for the AC and CI assets
265 reached 20 and 22, respectively. Then, the classifiers were trained for 70% of the assets (training set)
266 in each cluster, and the models were validated using the 30% of the assets (testing set).

267 **Hybrid clustering**

268 To further improve the prediction capability of the classifiers, K-means clustering was done after
269 domain knowledge clustering. Initially, all assets with similar material were divided into domain
270 knowledge clusters, then some clusters were divided into smaller sub-clusters using the K-means
271 method. This was only applied to large clusters, and tiny clusters were not divided into smaller sub-
272 clusters. To obtain the optimum number of sub-clusters, each cluster was divided into 2-10 sub-clusters,
273 and the best number of sub-clusters in each cluster was selected based on the maximum F1-score of the
274 classifier (Eq. 6). This could result in a higher number of sub-clusters in larger clusters. The total
275 number of sub-clusters can vary, for different materials and classifiers.

276 **Classification**

277 After clustering the data, classifiers can be used to predict pipe failure in WDN assets. Classifiers are
278 machine learning tools which can be trained by a fraction of data to identify the membership of unseen
279 data to a certain class. Many classifiers have been used in different fields. In this study, LR, RF and
280 XGB are used to predict the failure of water pipes.

281 **Logistic Regression (LR)**

282 Logistic regression (LR) is a well-known statistical approach that fits samples into a logistic function.
283 Among statistical models, LR-based failure prediction models are considered as one of the best
284 performers (Barton et al., 2022). Since hyperparameter optimisation is not required, it is easy to apply
285 for multiple models (Jara-Arriagada and Stoianov, 2020). For a classification task, this approach gives
286 each sample the labels of 0 or 1. In order to ascertain the likelihood of falling into a particular category,
287 the findings are analysed using the equation below (Cox and Snell, 1989):

$$p = \frac{1}{1 + e^{-(w_0 + \sum_{i=1}^m w_i x_i)}} \quad (1)$$

288 where; p is the probability of failure for each sample; x_i is the covariates vector for the i -th feature;
289 w_i is the weight of i -th feature that will be tuned during the training process; and w_0 is the constant
290 bias. Some variables were presented in a categorical format, as an instance, soil type has 6 categories.
291 In this study, to handle categorical variables, the method of generating dummy variables was employed
292 to convert categorical data into a quantitative form. The use of dummy variables allowed for the
293 representation of discrete independent variables with multiple strata relative to a reference stratum
294 (Akinsomi et al., 2013). Once weights are determined, the classification result, y of each sample can
295 be achieved by Eq. 1, in which the threshold is usually set as 0.5 for binary classification. $y = 0$ if
296 $p \leq threshold$ and $y = 1$ if $p > threshold$. Due to the high range of values in pressure and asset
297 length, Log transformation was applied to achieve better predictions.

298

299 **Random Forest (RF)**

300 The RF algorithm is a supervised classification technique in machine learning, which could be used for
301 classification and regression. It has attracted growing interest in pipeline failure prediction (Liu et al.,
302 2022; Snider et al., 2023). As RF produces several trees for the decision-making process, it performs
303 better than decision trees (Piryonesi et al., 2021). Among ML algorithms, this technique is more stable
304 in the presence of outliers and in very large data sets (Menze et al., 2009). The Gini impurity criteria
305 index is used to evaluate the variable importance, which is an implicit feature selection carried out by
306 RF using a heuristic search technique (Ceriani and Verme, 2012). Based on the impurity reduction
307 concept, the Gini index evaluates the predictive importance of variables in regression or classification.
308 In a binary split, the following formula is used to calculate a node's Gini index (Strobl et al., 2007):

$$Gini(n) = 1 - \sum_{j=1}^2 (p_j)^2 \tag{2}$$

309 where; p_j is the relative frequency of class j in node n . To achieve optimal binary node splitting, it
310 is necessary to maximise the Gini index. The Gini index can be used to rate the significance of features
311 for a classification task.

312 **XGBoost**

313 Extreme Gradient Boosting (XGB) algorithm is an efficient technique that combines the prediction of
314 several weak tree models linearly (Chen and Guestrin, 2016). Due to its high speed and ability to handle
315 data with minimal pre-processing, XGB has become a popular choice for working with large datasets.
316 One notable feature that differentiates XGB from other boosting algorithms is its use of variable
317 weights, which makes it more prone to overfitting. To tackle this, it uses a regularisation process to
318 smooth the final learnt weight and avoid overfitting (Chen et al., 2019; Liu et al., 2022). Similar to other
319 machine learning models, XGB requires hyperparameter optimization to fine tune its performance.
320 Given the substantial size of the dataset in this study, XGB was selected as the preferred model. The
321 general prediction output of the model is given as:

$$O_i = G(\mathbf{X}_i) = \sum_{j=1}^t g_j(\mathbf{X}_i) \quad (3)$$

322 where; \mathbf{X}_i are the model features, t is the number of iterations and $g_k(\mathbf{X}_i)$ is the output function of
 323 each tree model.

324 **K-fold cross validation**

325 Usually, a subset of data not included in model training (unseen dataset) is used to test the model
 326 performance. Cross validation (CV) is a way to evaluate the efficacy of ML models. In this process, the
 327 dataset is divided into k folds, and the model utilises a new fold for training and testing on each iteration
 328 (Hoang Lan Vu et al., 2022). The ML should present comparable performance when running on each
 329 fold. In this study, five data subsets (folds) were randomly selected, and evaluation metrics were
 330 compared for each fold.

331 **Prediction performance metrics**

332 The classification models motioned above produce a continuous probability value between 0 and 1
 333 indicating the likelihood of a pipe failure. To classify whether a pipe will fail or not, the continuous
 334 probability value will need to undergo a threshold analysis. By using a threshold, the model can assign
 335 a label of 0 or 1, indicating whether the pipe is predicted to fail or not. The correctly categorised pipes
 336 are represented by "True positive" (TP) and "True negative" (TN) in a confusion matrix. False positives
 337 (FP) are samples that have not failed, but have been predicted to have failed, whereas false negatives
 338 (FN) are pipes that have failed in reality, but were categorised as not failed by the model. A threshold
 339 value must be chosen to maximise the model predictive performance.

340 After categorizing the prediction results, five metrics are utilised in this study to evaluate the
 341 performance of the models as given in Eq. (4) to Eq. (7).

$$Precision = \frac{\sum TP}{\sum (TP + FP)} \quad (4)$$

$$Recall = \frac{\sum TP}{\sum (TP + FN)} \quad (5)$$

$$F1-Score = \frac{2 \times Precision \times Recall}{(Precision + Recall)} \quad (6)$$

$$Accuracy = \frac{\sum (TP + TN)}{\sum (TP + FN + TN + FP)} \quad (7)$$

$$Specificity = \frac{\sum TN}{\sum (TN + FP)} \quad (8)$$

342 A higher recall value indicates that more failure samples in the test dataset were correctly detected by
 343 the model, while a higher precision value indicates that the majority of the predicted values are indeed
 344 failure samples. Low recall and low accuracy values will result in missing and replacing non-failed
 345 assets, respectively, which will increase investment costs. The harmonic means of precision and recall
 346 are calculated, as *F1-score*. Usually, the best threshold to determine the positive and negative samples
 347 is selected in a way to maximise the F1-score.

348 The Receiver Operating Characteristics (ROC) curve has been extensively utilised to compare
 349 classifiers (Debón et al., 2010; Rubles-Velasco et al., 2020; Fan et al., 2022). ROC describes the
 350 relationship between the rate of FP and TP in different thresholds as a curve. The area under the ROC
 351 curve could be extracted as a metric of evaluation. However, this metric may sometimes be misleading
 352 in datasets with high class imbalance. Precision-Recall curve (PRC) was recommended as a suitable
 353 substitute and, also the area under the PRC is calculated as a performance metric (Saito and Rehmsmeier
 354 2015; Davis and Goadrich, 2006). As the PRC only considers the number of correct and wrong
 355 predictions, it does not take into account of the economic and consequence aspects of the predictions.
 356 Therefore, in this research, further economic and consequence analyses are proposed to shed light on
 357 the prediction capability of models using various techniques for dealing with imbalanced datasets.

358

359 **Evaluation models**

360 In many cases, when categorizing a dataset into two or more distinct classes, all the members of the
361 dataset are considered equivalent from the decision maker's point of view. For example, when a medical
362 test kit is designed to predict a disease in a group of people, it may make correct or wrong predictions.
363 In this case, making a correct/wrong prediction for a patient is similar to the other ones, because all of
364 the patients have the same value to the predictor. Therefore, only the number of TP, FP, TN, and FN
365 predictions could be counted and used in the evaluation of the prediction model. Failure prediction in a
366 WDN is rather different. Each pipe has its length, diameter, location, etc. Therefore,
367 rehabilitation/failure of a certain pipe could have cost/consequences different from the others. As an
368 example, replacing a long pipe with a large diameter is much more expensive than a short pipe with a
369 small diameter. Failure in a large diameter pipe could result in more customers being cut from the WDN.
370 Therefore, only counting the number of correct predictions is not enough to assess the capabilities of a
371 failure prediction model, and the cost and consequence of predictions should be taken into account.

372 **Likelihood of failure analysis**

373 To evaluate the results of failure prediction models, the likelihood of failure (LoF) calculated by
374 classifiers (XGB, RF, and LR) was studied. In traditional classification methods, a threshold for LoF
375 (usually 0.5) is selected and the predicted LoF is compared with the threshold. In this way, all assets
376 can be categorised into two binary groups (failed/not failed). In this research, predicted LoFs are used
377 to sort all assets according to their priority for rehabilitation. Such a list of assets can be used by water
378 utility companies for long-term rehabilitation of the water pipes.

379 To evaluate the benefits of the prediction model, variations of the cumulative reduction in the number
380 of failures are presented as a function of cumulative cost of rehabilitation. The cost of rehabilitation is
381 calculated based on the diameter and length of the pipes, considering a 10% replacement of the entire
382 length for each pipe. This presentation outlines the relationship between failure reduction and
383 rehabilitation cost. It highlights the amount of investment required to achieve a specific level of failure

384 reduction, as well as the amount of failure reduction that can be achieved with a given rehabilitation
385 budget.

386 **Economic analysis**

387 Similar to the likelihood of failure analysis, economic analysis is performed to find the economic
388 options for pipe rehabilitation. To take the cost of rehabilitation into account, a new metric is defined,
389 as:

$$eco_i = \frac{LoF_i}{cost_i} \quad (9)$$

390 where; LoF_i is the likelihood of failure of the i -th pipe predicted by the classifier; and $cost_i$ is the cost
391 of rehabilitation for the i -th pipe. Using this metric, the pipes with higher LoF and lower cost could be
392 prioritised for rehabilitation. A graph presenting the cumulative reduction in a number of failures
393 against the corresponding rehabilitation cost can show the efficacy of each method. In an ideal model,
394 a high number of failures should be captured by a low rehabilitation cost. This analysis helps the asset
395 managers to reduce the number of failures with smaller rehabilitation budget.

396 **Consequence analysis**

397 In addition to rehabilitation cost, it is also crucial to consider the consequences of the pipe failures. The
398 size of pipe diameter can indicate the number of customers supplied by a pipe. So, the diameter of each
399 pipe is taken as an indicator to approximate the consequences of a failure. The following metric is
400 defined to prioritise the pipes with higher LoF and a higher consequence of failure:

$$consequence_i = LoF_i \times d_i \quad (10)$$

401 in which, d_i is the diameter of the i -th pipe. In essence, rehabilitation of a pipe with high LoF results
402 in saving a certain amount of capacity in the WDN. A larger diameter pipe can save more capacity than
403 smaller diameter pipes. An ideal model selects the pipes with high LoF and high consequence to
404 rehabilitate. To evaluate the performance of the models in predicting the pipe failures with higher
405 consequence, the cumulative flow saved by each model is depicted against the corresponding costs.

406 This analysis allows the decision makers to prioritise the pipes with higher likelihood of failure and
407 consequence for rehabilitation.

408

409 **Results**

410 **Using under- and over- sampling, SMOTE and class weight**

411 Different techniques were employed to address class imbalance in the training datasets of the AC and
412 CI pipes. The impact of these techniques was subsequently analysed on the test dataset. The number of
413 assets in the training dataset for AC and CI are 46,747 and 56,963, and the number of failures are 3342
414 and 3910, respectively. Initially, the data was used as-is to perform an imbalance analysis without
415 altering the number of assets or failures. This was considered the baseline model (Figs. 7- a & d). In
416 Fig. (7), class 0 (blue) and class 1 (red) indicates not failed and failed pipes, respectively. High density
417 of blue dots indicates the class imbalance, in which the majority of the assets were not failed.

418 Next, random undersampling was applied to both the AC and CI training datasets. This technique
419 randomly reduces the number of majority samples in order to balance with the minority class. As a
420 result, the number of assets in the AC training dataset was reduced from 46,747 to 3342 while the
421 number in the CI training dataset was reduced from 56,963 to 3,910 (Figs. 7- b & e).

422 In the next step, the number of minority samples increased due to the utilisation of oversampling
423 techniques, such as random oversampling, and SMOTE, on the AC and CI train datasets. In this case,
424 number of failed assets increased from 3342 to 46,747 and 3910 to 56,963 in the AC and CI datasets,
425 respectively. The results of the SMOTE technique are graphically presented on the AC and CI datasets
426 in Figs. (7- c & f), respectively. In these figures, the same density of blue and red dots shows a balanced
427 dataset.

428 The class weighting method was also used on the AC and CI datasets. Although the quantity of samples
429 from the majority and minority classes will not vary in class weighting, the importance of the minority
430 class will be considered by penalising any incorrect predictions in this class.

431 **Clustering by the K-Means method**

432 The K-Means method was also employed to cluster the data. In each pipe material, the assets were
433 divided into 2-20 clusters based on age, diameter and length. The best number of clusters, usually less
434 than 10 in this case study, was selected based on the maximum F1-score achieved by each classifier. In
435 this way, the optimum number of clusters could be different from one classifier to another. The optimum
436 number of clusters of the K-Means method for AC, and CI pipes are presented in Tables (2) and (3),
437 respectively. The optimum numbers of clusters for the XGB, RF, and LR classifiers were 9, 6 and 5, in
438 the AC pipes and 3, 10, and 3, in the CI pipes, respectively. Fig. (8) presents the clustering of the AC
439 pipes into 5 and 9 clusters, and the CI pipes into 3 and 10 clusters.

440 **Clustering by domain knowledge and hybrid approaches**

441 Using the domain knowledge clustering approach, the datasets of each pipe material were divided into
442 homogeneous clusters. This approach clusters data points by analysing the relationship between the
443 number of failures and key pipe features (e.g., age, diameter, and length), looking for patterns in their
444 variations. This results in semi-supervised clustering. Using this approach, the dataset of AC and CI
445 pipes were divided into 20 and 22 clusters, respectively. Then, the classifiers were run on each cluster
446 to predict the failures.

447 Each domain knowledge cluster was further divided into smaller sub-clusters by the K-Means method.
448 A larger cluster could then be divided into more sub-clusters than a small one. The optimum number of
449 sub-clusters in each cluster was selected based on the F1-score of the classifiers, i.e., the total number
450 of sub-clusters could be different with each classifier. For example, the number of sub-clusters for XGB,
451 RF, and LR were 59, 58, and 50, in the AC pipes, and 67, 47, and 58 in the CI pipes, respectively.

452 **ML evaluation metrics for classifiers**

453 The performance of the ML models was evaluated using ML performance indicators. The performance
454 metrics of the classifiers for the AC and CI pipes are shown in Tables (2) and (3), respectively. As
455 shown in the tables, when no treatment was utilised for imbalanced data, all classifiers had the highest

456 accuracy and specificity metrics. However, since these classifiers do not accurately predict the minority
457 class, these metrics may not be a reliable indicator of their prediction ability.

458 The values of precision, recall, and F1-score for the pipes are also included in Tables (2) and (3).
459 Precision and recall represent different aspects of prediction capability, and therefore, both metrics
460 should be considered simultaneously when evaluating a machine learning model. For both material
461 types, all classifiers demonstrated a slight improvement in the F1-score (i.e., the harmonic average of
462 precision and recall) when employing the hybrid clustering technique. As outlined in the methodology,
463 Tables (2) and (3) present the AUC of ROC as a distinct measure of prediction performance for AC and
464 CI pipes, respectively. The undersampling approach yielded the highest AUC-ROC values for the
465 majority of classifiers, including XGB for AC pipes (Table 2) and XGB for CI pipes (Table 3). Other
466 techniques had lower values due to class imbalance. AUC-PRC is an additional metric that is shown in
467 Tables (2) and (3) for AC and CI pipes, respectively. As AUC-PRC values are very similar to each
468 other, relying solely on them to make decision can be difficult. Therefore, decision-makers should
469 consider alternative parameters that are more explainable for pipeline failure prediction.

470 **LoF analysis**

471 As mentioned in Section 3.5.1, all assets in the test set were sorted according to their LoF predicted by
472 each classifier. The percent of reduction in the number of failures is presented as a function of
473 rehabilitation cost for the AC and CI pipes, using the three classifiers (Fig. 9). For each classifier, the
474 results of different methods are presented. For AC pipes, in the XGB classifier, hybrid, SMOTE, and
475 domain knowledge based approaches yielded the best performance. In RF, hybrid, K-Means and domain
476 knowledge based approaches made the best predictions. In LR, the results of the hybrid, K-Means, and
477 imbalance data approaches provided the best performance and they were very close to each other.
478 Overall, RF-hybrid model showed the best performance, such that by spending 10% of the total
479 rehabilitation cost, 18% of the failures could be reduced.

480 For CI pipes, in the XGB classifier, SMOTE, K-Means, and hybrid models showed the highest failure
481 reduction in pipes. In RF, K-Means and hybrid yielded the best predictive models. In LR, the predictions

482 are no more accurate than if they were randomly selected. Spending 10% of the whole rehabilitation
483 cost, the XGB-SMOTE and RF-Class weight models were able to reduce the failure in CI pipes by 16%.
484 In most cases, models without clustering (imbalance data, undersampling, oversampling, SMOTE, and
485 class-weight) showed weak performance in predicting the failure. Also, there were considerable
486 differences between the models, so the best model to predict the failure should be selected carefully.
487 The hybrid and domain knowledge based models showed acceptable performance, compared to the
488 others.

489 **Economic analysis**

490 To minimise the cost of rehabilitation and improve the efficacy of budget allocation, an economic
491 analysis was carried out, in which the assets were sorted based on their value of $\frac{LoF}{cost}$, instead of LoF
492 solely (Fig. 10). The results show that in all cases, different models yielded similar performance, hence
493 it is challenging to select one as the best model. Comparing the results of Fig. (10) and Fig. (9), indicates
494 a significant increase in performance of the Economic model. To better elucidate the distinction between
495 pipe replacement through Economic Analysis and reliance solely on the *LoF*, Table (4) demonstrates
496 that employing the *LoF* for pipe rehabilitation in the case study WDN for AC and CI pipes with a
497 budget allocation of £5 million captures 24.9% and 19.9% of failures, respectively. Similarly, utilising
498 *eco* indicators to rank the AC and CI pipe for replacement at the same cost captures 34.7% and 32.6%
499 of failures, respectively.

500 Upon increasing the budget to £10 million, using the LoF for pipe rehabilitation in AC and CI pipes
501 captures 46.5% and 38.2% of failures in the WDN, respectively. Similarly, employing *eco* indicators
502 enhances the failure capture rate to 62.6% for AC pipes, and 57.6% for CI pipes.

503 This notable increase in failure capture highlights that the utilisation of *eco* indicator for pipe
504 replacement yields a greater proportion of failures captured compared to relying solely on the *LoF*,
505 especially within a specific budget allocation for replacement.

506

507 **Consequence analysis**

508 In consequence analysis, all assets were sorted according to their ($LoF \times diameter$). Total flow saved
509 by pipe rehabilitation was plotted against rehabilitation cost (Fig. 11). For AC pipes, in the XGB and
510 RF classifiers, hybrid model was considerably better than the other models, with domain knowledge
511 and K-Means in the next places. In LR, hybrid, and K-Means showed the best prediction capability. For
512 CI pipes, in XGB, K-Means and hybrid had higher flow capacity savings. In RF and LR, the hybrid
513 model outperformed the other models.

514 The difference between the results of the models is enough to encourage the decision makers to examine
515 all models and select the best one. Overall, the results demonstrate that the hybrid model, which uses
516 semi-supervised clustering, has the highest ability in prioritising the assets for rehabilitation. Similarly,
517 the clustering models outperformed the non-clustering models.

518

519 **Conclusion**

520 In this paper, a WDN with highly imbalanced data was studied to develop a failure prediction model.
521 During 26 months of pipe failure data collection period, only 18,000 failures were recorded within
522 400,000 assets, representing a failure rate of about 4 % among all assets. This presented a significant
523 challenge for training classifier models. To improve the performance of the classifiers, various
524 approaches of handling imbalanced data from literature were employed. Among the methods used,
525 class-weight showed a better performance than undersampling, oversampling, and SMOTE, so it was
526 used for further analyses.

527 Moreover, clustering was used to improve the prediction capability. Creating smaller clusters of
528 homogeneous data enabled classifiers to more easily establish the relationship between the covariates
529 and target values. Two new clustering methods were proposed: Domain knowledge based clustering
530 and hybrid clustering which is based on domain knowledge clustering and K-Means methods.

531 Domain knowledge and hybrid clustering provide a new means of clustering, called “semi-supervised”
532 clustering, in which the samples are categorised based on the relationship between the target variable
533 and independent covariates. In this paper, semi-supervised clustering was applied on the training dataset
534 and the resulting model was subsequently evaluated on the test dataset to assess the performance of the
535 model. Running the classifiers on these clusters resulted in a slight improvement over unsupervised
536 clusters. The results show that the proposed hybrid clustering approach outperforms the other clustering
537 methods.

538 Evaluation of the three machine learning methods, namely XGB, RF and LR, revealed that their results
539 did not significantly differ from each other. However, implementing diverse measures to address the
540 issue of imbalanced data improved the accuracy of failure prediction. It can be concluded that focusing
541 on the techniques for handling imbalanced data may prove more effective than employing complex and
542 computationally-intensive machine learning models.

543 While conventional metrics have been used to compare various models, they were found unsuitable for
544 evaluating failure prediction models in WDNs. This is because these metrics only take the number of
545 true and false predictions into account, without considering their significance to decision makers. In
546 this paper, economic analysis and consequence analysis are proposed to rank the pipes for rehabilitation
547 considering their replacement cost and consequence of failure. The methodologies embedded in
548 economic analysis and consequence analysis evaluate the failure prediction models in a practical
549 manner to enhance pipe rehabilitation strategies. These analyses can provide insight into the reduction
550 in failures and increase in flow capacity in a WDN, as a result of certain level of investment in asset
551 rehabilitation.

552

553 **Data Availability Statement**

554 d. Some or all data, models, or code generated or used during the study are proprietary or confidential
555 in nature and may only be provided with restrictions. All case study data is owned by the utility company
556 and is subject to a non-disclosure agreement (NDA), thereby limiting its availability for public

557 dissemination. Requests for non-commercial usage of the scripts will be evaluated on a case-by-case
558 basis.

559

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563

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710

Table 1. Characteristics of the case study WDN.

		Length (km)	Number of assets	Number of failures	Failure rate (failure/100km/year)	Failure percentage
Materials	AC	5637.6	66782	4775	39.09	7.15
	CI	6423.5	81375	5586	40.14	6.86
	PV	4943.5	53005	2268	21.17	4.28
	PE	13870.2	172825	4784	15.92	2.77
	DI	1149.2	14304	546	21.93	3.82
	other	818.5	10072	473	28.41	4.70
Diameters	D≤ 100 mm	13170.9	167275	7040	24.67	4.21
	100<D≤200	16332.0	200842	10167	28.73	5.06
	D>200	3339.5	30246	1225	16.93	4.05
Ages	age≤20	7224.0	92570	2375	15.17	2.57
	20<age≤50	13549.3	159630	6078	20.70	3.81
	50≤age<100	9608.1	114651	7927	38.08	6.91
	age>100	2461.0	31512	2052	38.48	6.51
Total WDN		32842.4	398363	18432	25.90	4.63

Table 2. Performance metrics of the classifiers in AC pipes

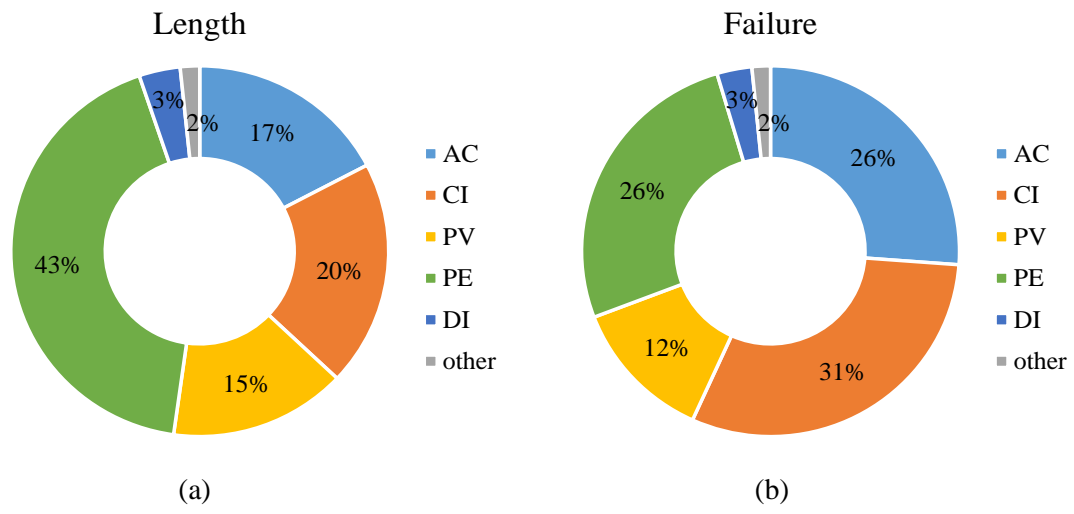
Classifier	Method	Total number of clusters	Precision	Recall	F1-score	Accuracy	Specificity	AUC_PR	AUC_ROC
XGB	Imbalanced	1	0.375	0.002	0.004	0.928	1.000	12.8	66.6
	Undersampling	1	0.146	0.326	0.201	0.896	0.920	12.2	78.8
	Oversampling	1	0.140	0.317	0.194	0.893	0.918	11.7	76.8
	SMOTE	1	0.101	0.526	0.170	0.792	0.803	10.0	76.0
	Class Weight	1	0.120	0.401	0.184	0.747	0.773	11.8	63.2
	K-means clustering	9	0.117	0.495	0.190	0.698	0.714	12.0	55.9
	Domain knowledge clustering	20	0.138	0.375	0.202	0.787	0.819	11.0	62.0
	Hybrid clustering	59	0.144	0.379	0.209	0.796	0.827	11.8	62.0
RF	Imbalanced	1	0.167	0.006	0.012	0.927	0.998	11.1	62.6
	Undersampling	1	0.135	0.302	0.186	0.893	0.918	11.6	78.0
	Oversampling	1	0.127	0.289	0.176	0.891	0.916	10.4	75.1
	SMOTE	1	0.105	0.471	0.172	0.816	0.831	10.1	75.7
	Class Weight	1	0.134	0.503	0.212	0.732	0.749	13.3	66.9
	K-means clustering	6	0.126	0.541	0.204	0.699	0.711	13.9	61.2
	Domain knowledge clustering	20	0.139	0.397	0.206	0.781	0.811	11.0	63.0
	Hybrid clustering	58	0.146	0.408	0.215	0.788	0.817	12.3	63.0
LR	Imbalanced	1	0.389	0.010	0.019	0.928	0.999	13.7	65.4
	Undersampling	1	0.162	0.343	0.220	0.902	0.925	13.1	78.2
	Oversampling	1	0.161	0.344	0.219	0.901	0.924	13.1	78.4
	SMOTE	1	0.152	0.362	0.214	0.893	0.915	13.0	78.2
	Class Weight	1	0.156	0.390	0.223	0.806	0.838	13.8	67.5
	K-means clustering	5	0.145	0.437	0.218	0.775	0.801	14.0	62.9
	Domain knowledge clustering	20	0.165	0.341	0.222	0.829	0.867	12.0	65.0
	Hybrid clustering	50	0.163	0.365	0.226	0.822	0.857	12.6	65.0

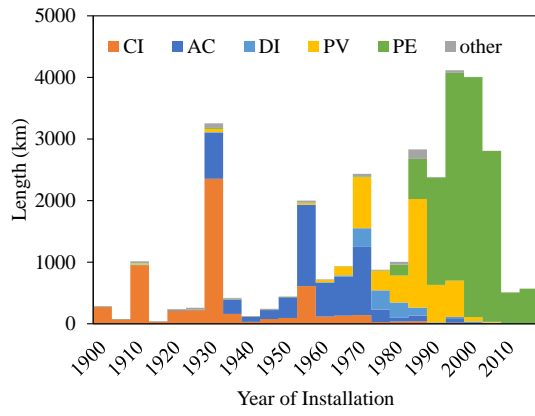
Table 3. Performance metrics of the classifiers in CI pipes

Classifier	Method	Total number of clusters	Precision	Recall	F1-score	Accuracy	Specificity	AUC_PR	AUC_ROC
XGB	Imbalanced	1	0.083	0.001	0.003	0.928	0.998	13.6	66.8
	Undersampling	1	0.132	0.425	0.202	0.879	0.896	12.0	80.3
	Oversampling	1	0.122	0.383	0.186	0.879	0.897	11.4	78.1
	SMOTE	1	0.107	0.420	0.170	0.852	0.869	9.5	77.1
	Class Weight	1	0.138	0.454	0.212	0.768	0.791	13.2	67.5
	K-means clustering	3	0.138	0.392	0.204	0.790	0.819	13.6	68.4
	Domain knowledge clustering	22	0.129	0.421	0.198	0.766	0.791	11.0	64.0
	Hybrid clustering	67	0.148	0.399	0.216	0.802	0.831	11.0	64.0
RF	Imbalanced	1	0.231	0.007	0.014	0.930	0.998	11.9	65.3
	Undersampling	1	0.125	0.354	0.184	0.887	0.907	11.0	78.9
	Oversampling	1	0.120	0.330	0.177	0.889	0.910	10.2	76.3
	SMOTE	1	0.100	0.440	0.163	0.837	0.852	9.4	76.3
	Class Weight	1	0.157	0.359	0.218	0.824	0.858	14.3	69.1
	K-means clustering	10	0.131	0.464	0.204	0.752	0.773	12.3	62.8
	Domain knowledge clustering	22	0.141	0.406	0.209	0.790	0.818	11.0	65.0
	Hybrid clustering	47	0.154	0.423	0.226	0.801	0.829	12.0	65.0
LR	Imbalanced	1	0.152	0.004	0.008	0.930	0.998	12.6	66.7
	Undersampling	1	0.147	0.370	0.210	0.900	0.920	12.4	79.3
	Oversampling	1	0.148	0.372	0.211	0.900	0.920	12.5	79.3
	SMOTE	1	0.145	0.383	0.211	0.896	0.916	12.3	78.8
	Class Weight	1	0.150	0.362	0.212	0.816	0.849	13.4	68.1
	K-means clustering	3	0.140	0.462	0.214	0.768	0.790	14.2	69.7
	Domain knowledge clustering	22	0.142	0.391	0.209	0.796	0.826	11.0	66.0
	Hybrid clustering	58	0.168	0.357	0.228	0.834	0.869	12.0	64.0

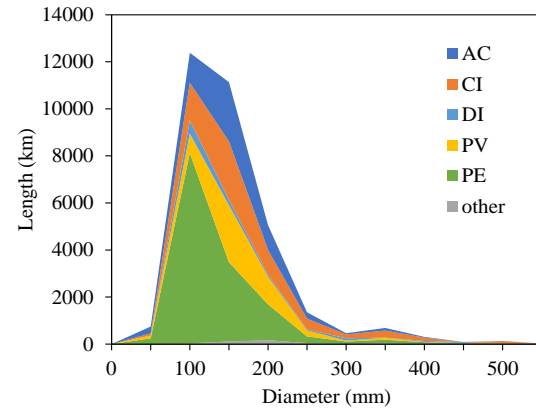
Table 4. Reduction in number of failures by spending £5 million and £10 million for pipe replacement, through *LoF* and *economic* analysis.

Budget Pipe material	£5 million		£10 million	
	AC	CI	AC	CI
<i>LoF</i>	24.9%	19.9%	46.5%	38.2%
<i>eco</i>	34.7%	32.6%	62.6%	57.6%

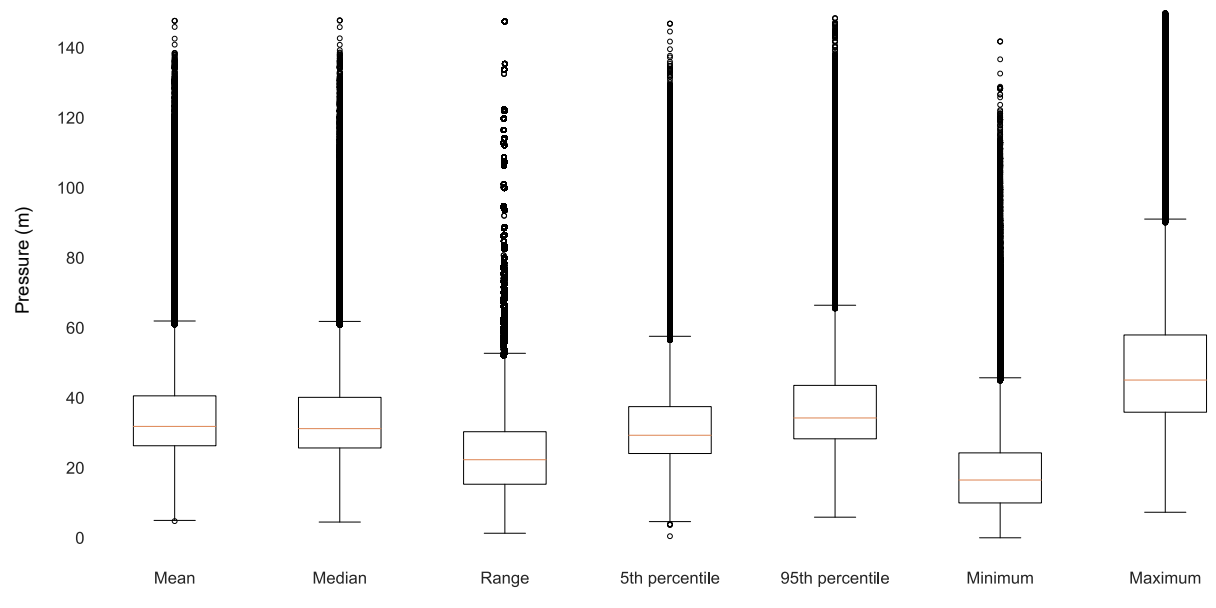




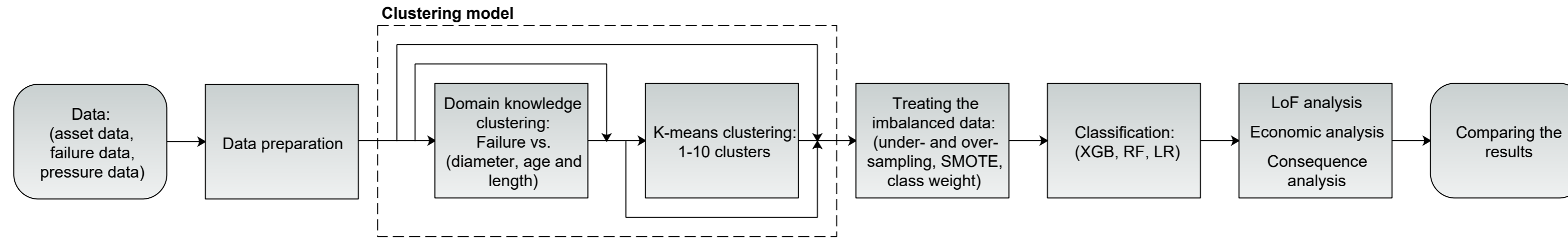
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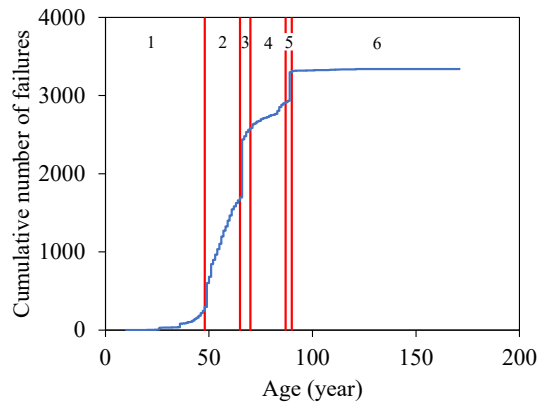


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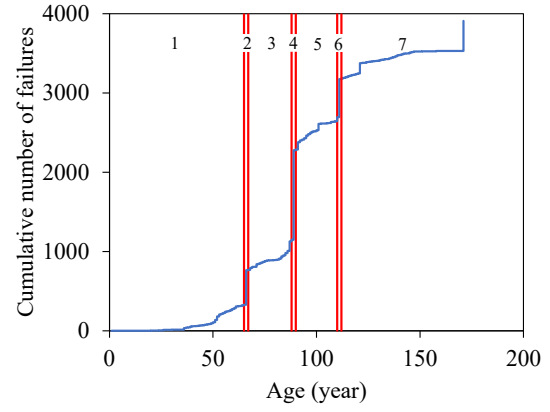


	Diameter	Age	Length	Elevation	Soil Type	Pressure Mean	Pressure Median	Pressure SD	Pressure Range	Pressure 5th percentile	Pressure 95th percentile	Pressure Min	Pressure Max	Failures
Diameter	1	0.113	0.03	0.019	-0.011	0.041	0.044	-0.008	0.009	0.042	0.039	0.024	0.019	-0.014
Age	0.113	1	-0.006	0.082	0.006	0.01	0.017	-0.028	-0.011	0.01	0.01	0.007	-0.019	0.054
Length	0.03	-0.006	1	-0.004	-0.016	0.046	0.043	0.02	0.021	0.043	0.047	0.025	0.04	0.163
Elevation	0.019	0.082	-0.004	1	0.295	0.258	0.271	-0.1	-0.044	0.268	0.246	0.248	0.089	0.027
Soil Type	-0.011	0.006	-0.016	0.295	1	0.074	0.083	-0.067	-0.036	0.076	0.072	0.085	0.006	0.012
Pressure Mean	0.041	0.01	0.046	0.258	0.074	1	0.986	0.07	0.135	0.99	0.992	0.815	0.647	0.03
Pressure Median	0.044	0.017	0.043	0.271	0.083	0.986	1	0.03	0.11	0.976	0.977	0.82	0.6	0.03
Pressure SD	-0.008	-0.028	0.02	-0.1	-0.067	0.07	0.03	1	0.675	0.032	0.109	-0.17	0.55	0.005
Pressure Range	0.009	-0.011	0.021	-0.044	-0.036	0.135	0.11	0.675	1	0.091	0.176	-0.221	0.725	0.011
Pressure 5th percentile	0.042	0.01	0.043	0.268	0.076	0.99	0.976	0.032	0.091	1	0.966	0.843	0.628	0.028
Pressure 95th percentile	0.039	0.01	0.047	0.246	0.072	0.992	0.977	0.109	0.176	0.966	1	0.78	0.659	0.031
Pressure Min	0.024	0.007	0.025	0.248	0.085	0.815	0.82	-0.17	-0.221	0.843	0.78	1	0.406	0.018
Pressure Max	0.019	-0.019	0.04	0.089	0.006	0.647	0.6	0.55	0.725	0.628	0.659	0.406	1	0.02
Failures	-0.014	0.054	0.163	0.027	0.012	0.03	0.03	0.005	0.011	0.028	0.031	0.018	0.02	1

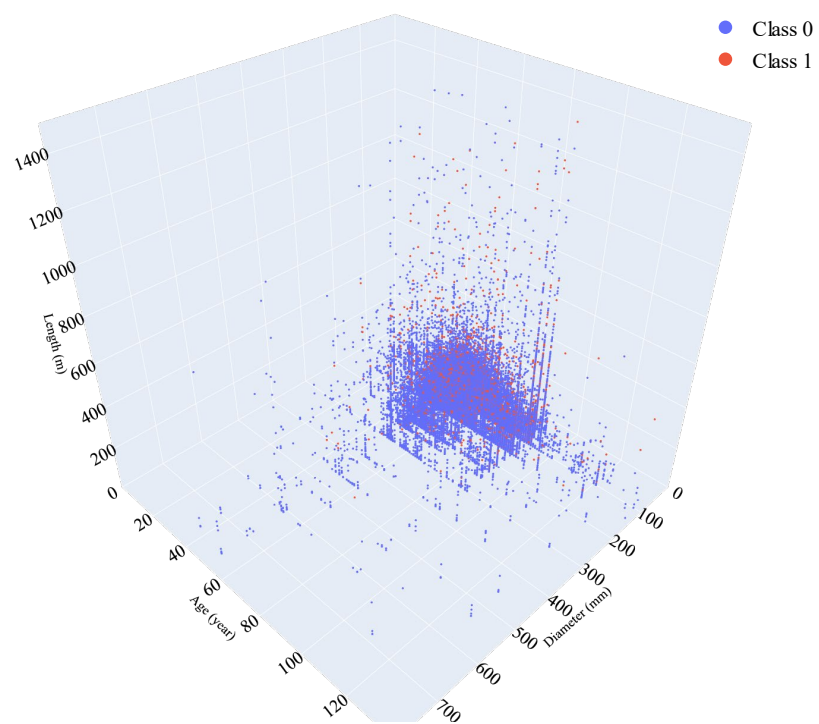




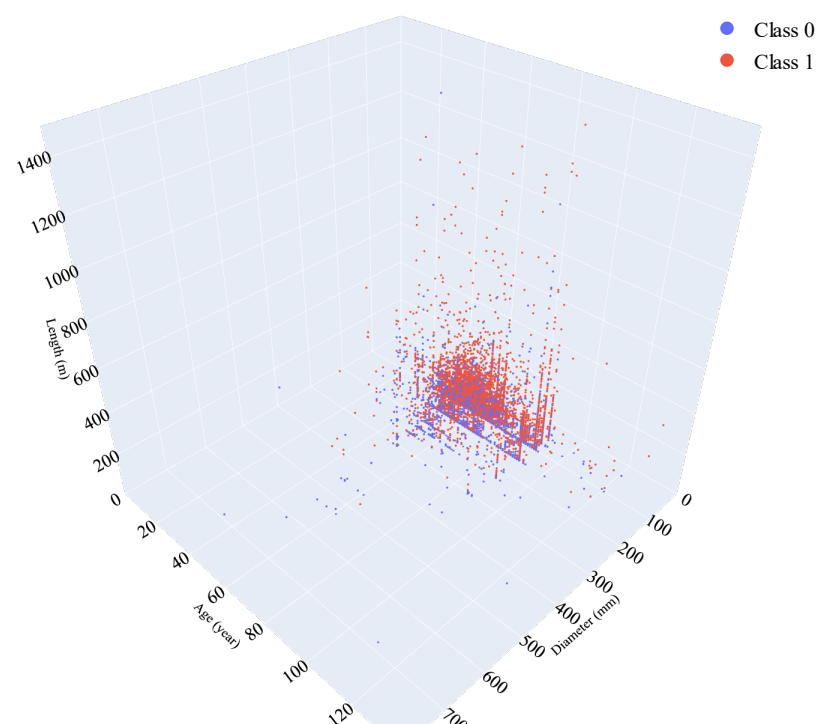
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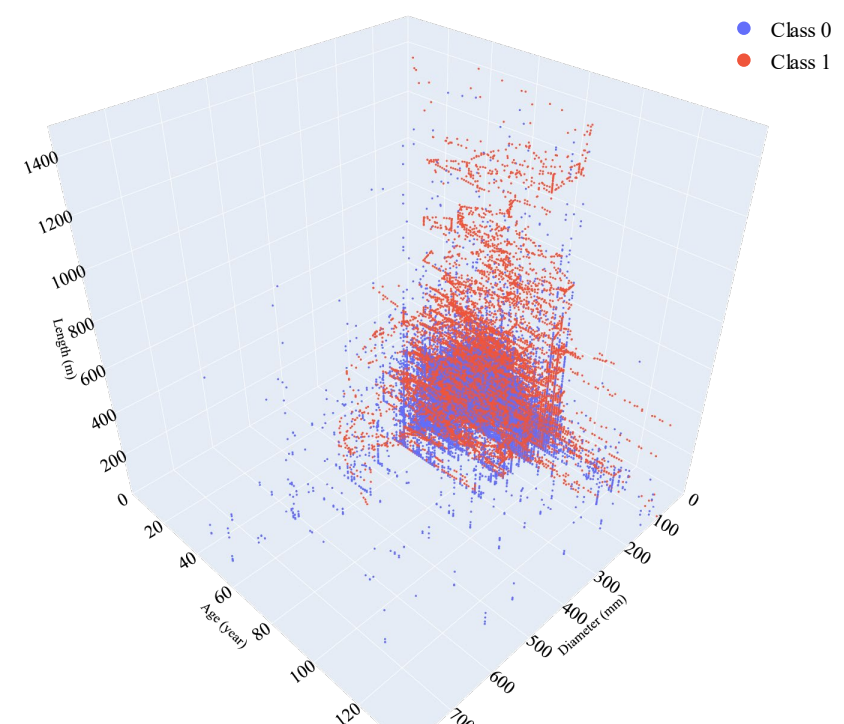
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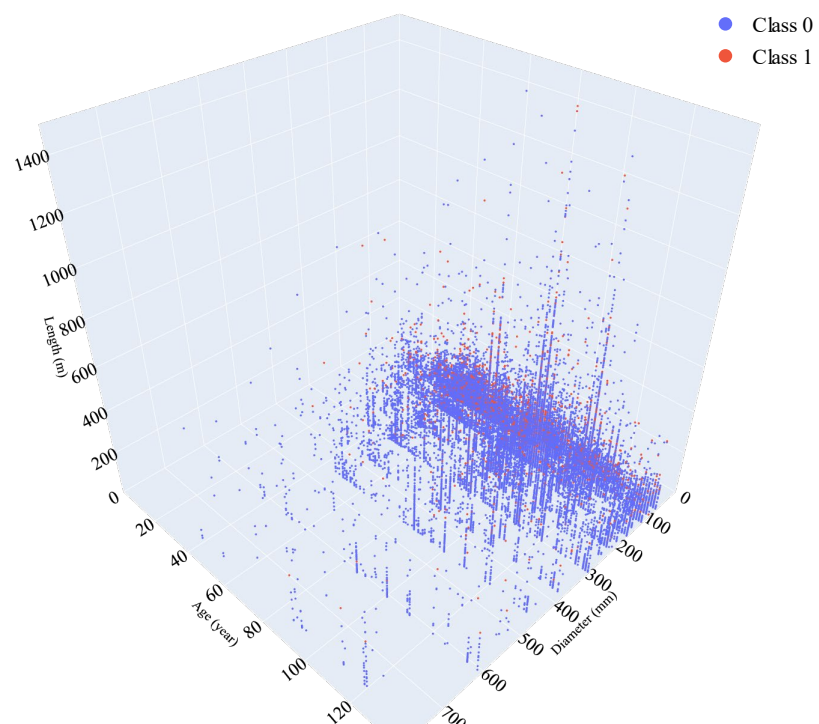
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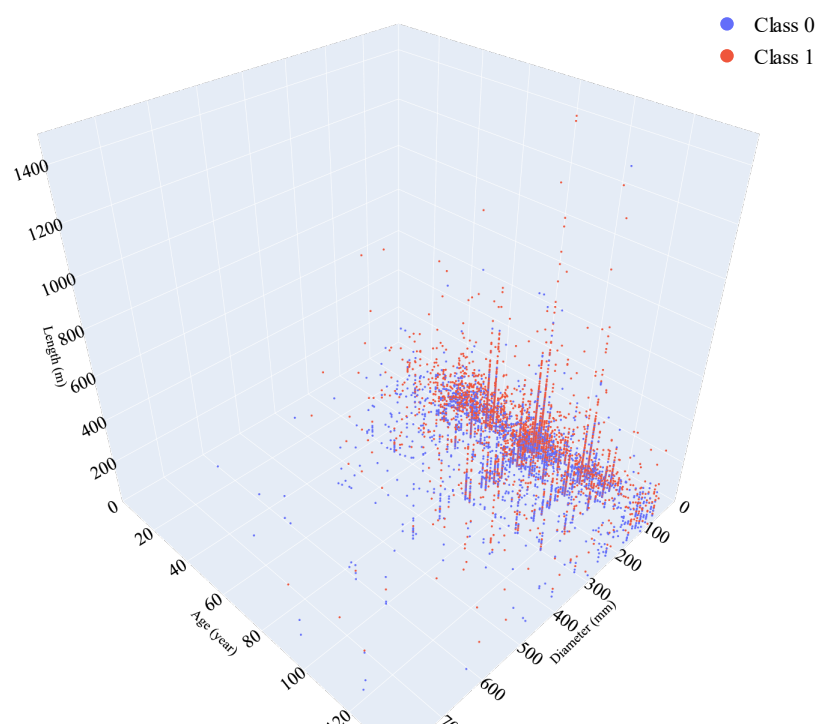
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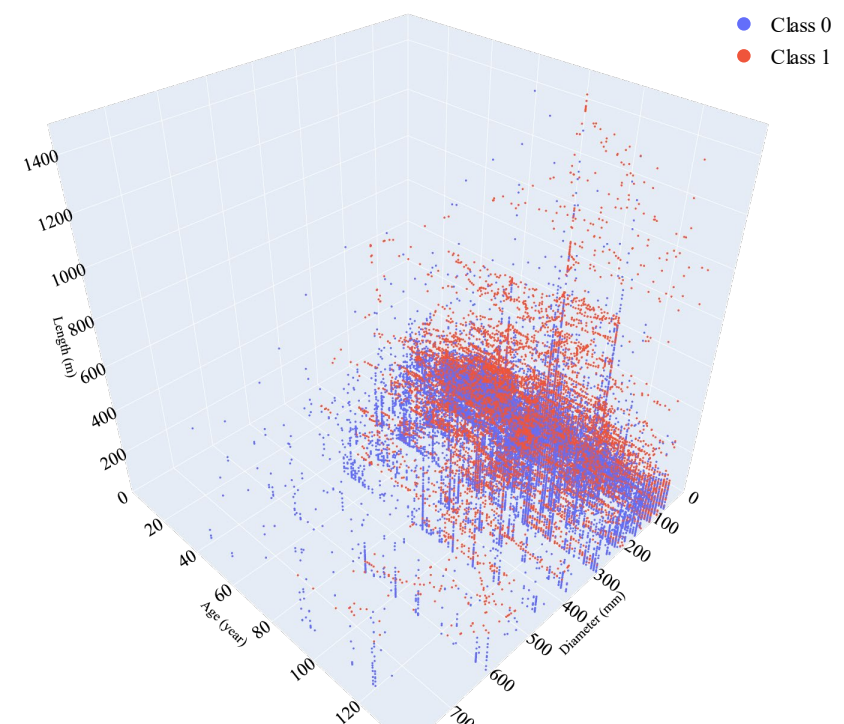
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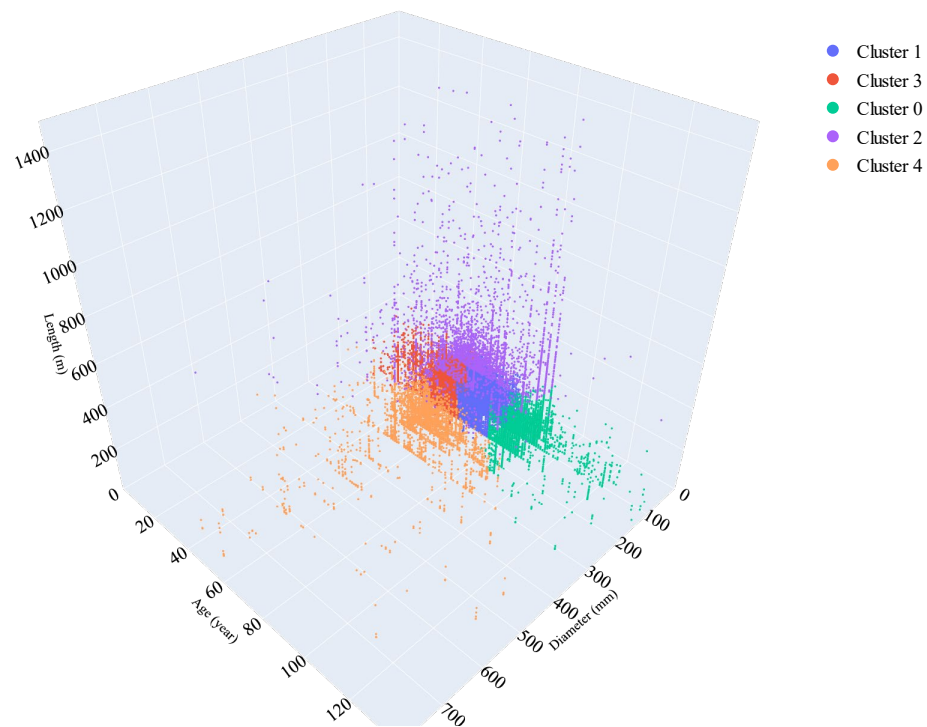
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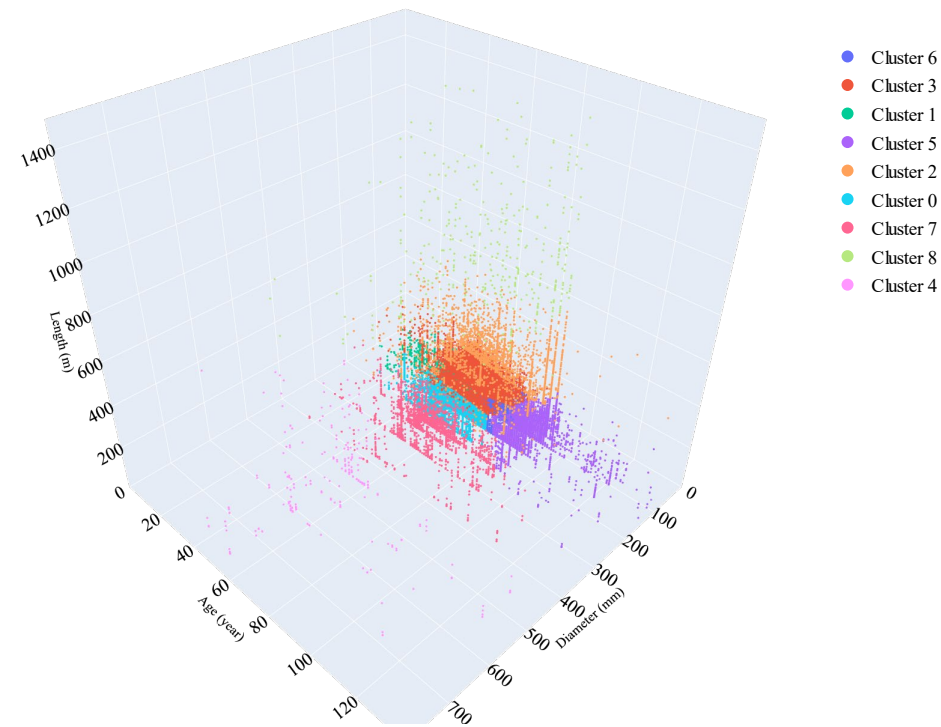
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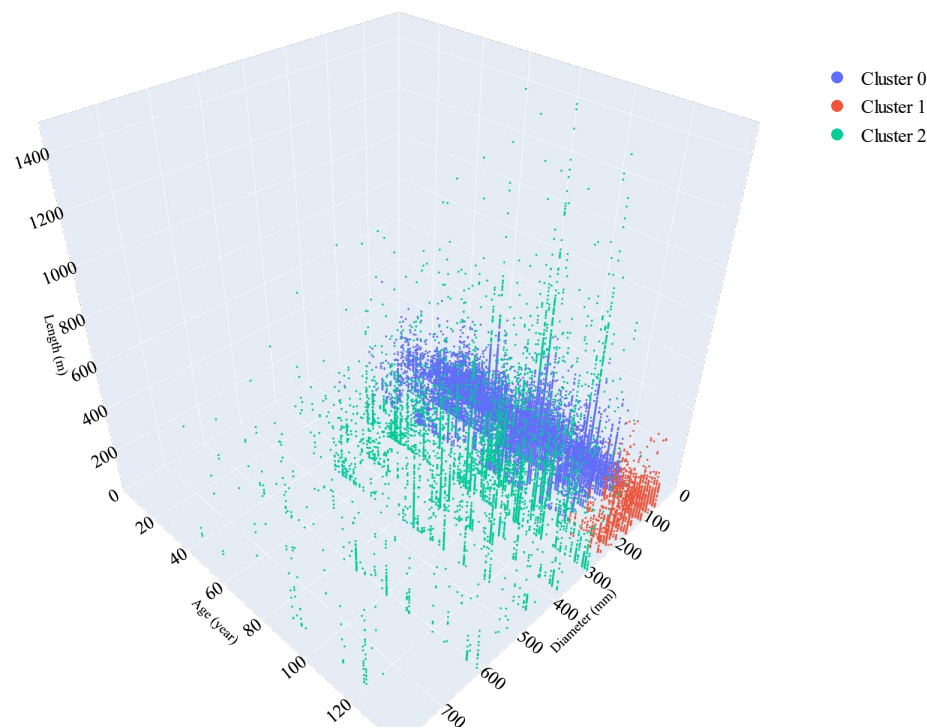
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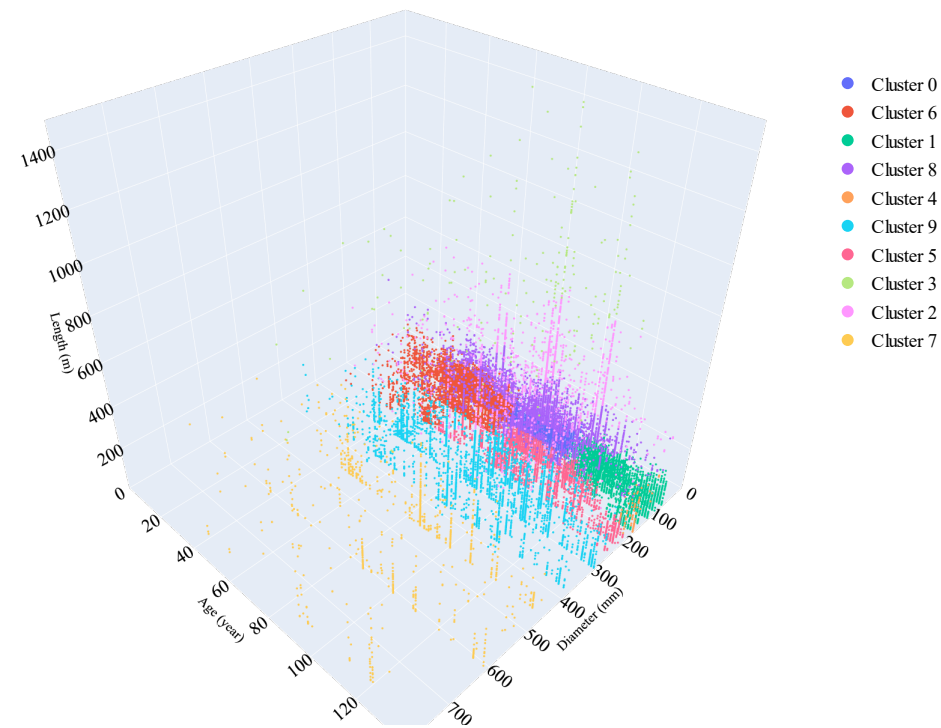
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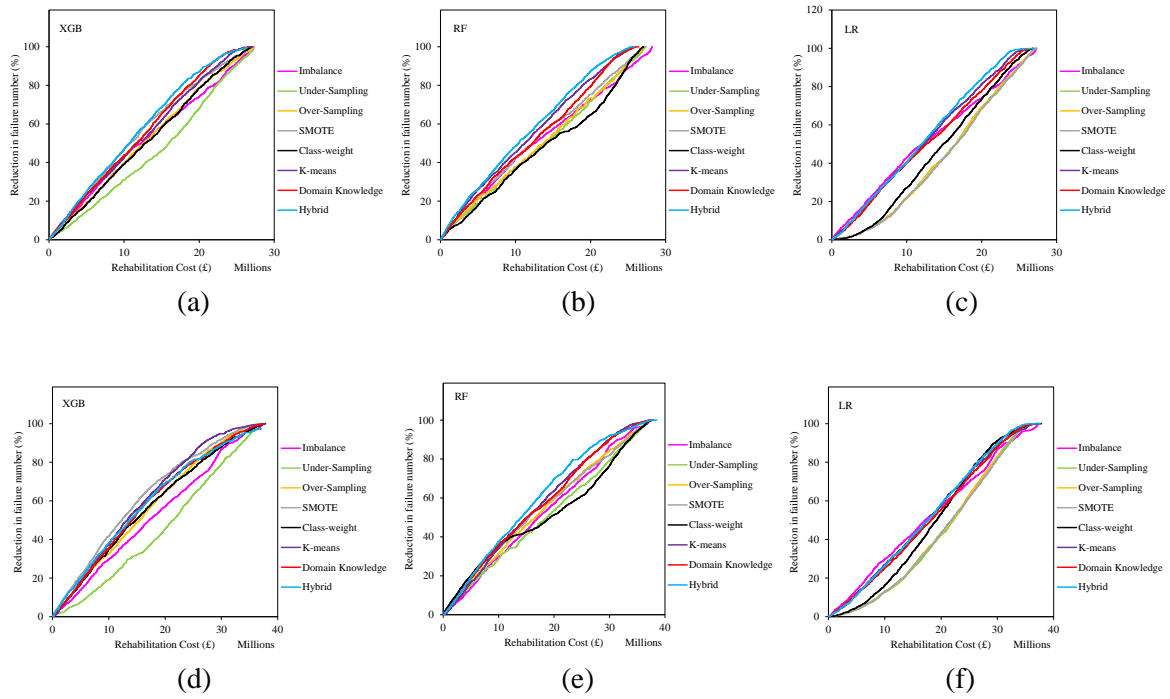
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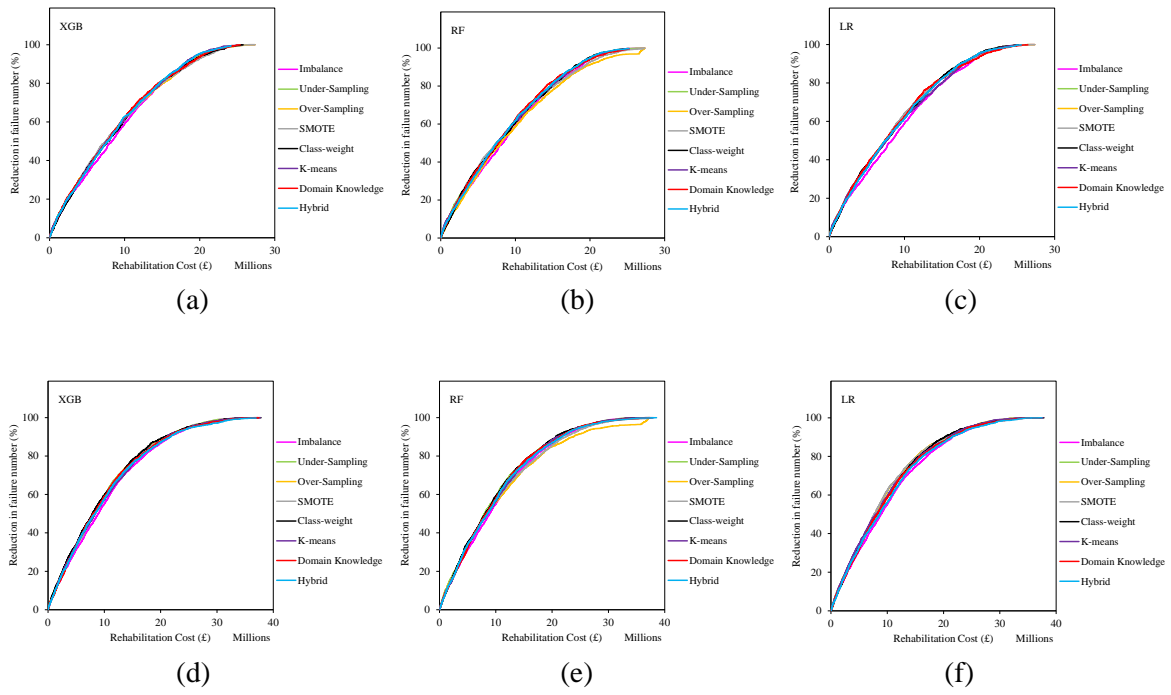


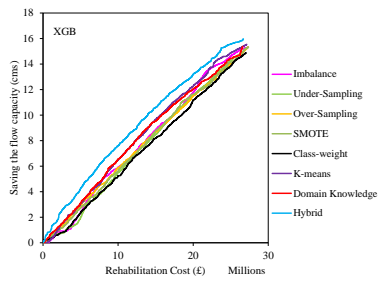
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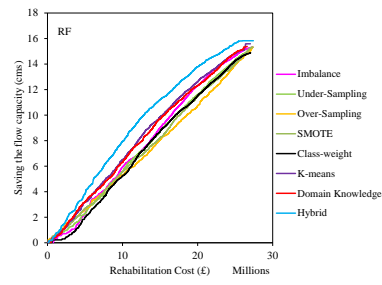
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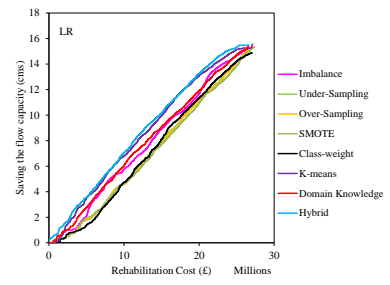




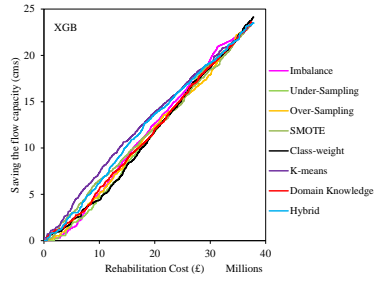
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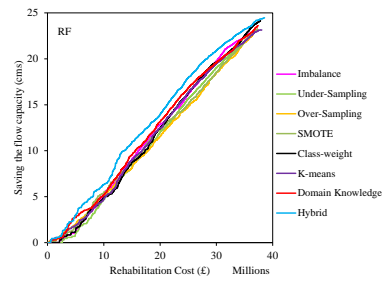
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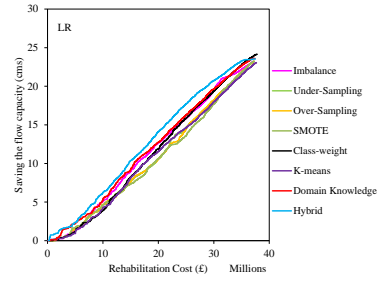
(c)



(d)



(e)



(f)

Fig. 1. Distribution of pipe materials based on (a) length; and (b) number of failures.

Fig. 2. Distribution of pipes in the case study WDN based on (a) age; and (b) diameter.

Fig. 3. Statistical metrics of pressure in the case study WDN.

Fig. 4. Correlation matrix for covariates in the case study.

Fig. 5. Flowchart of the proposed failure prediction model in this study.

Fig. 6. Cumulative number of failures vs. age of assets for (a) AC pipes; and (b) CI pipes.

Fig. 7. Presentation of dataset for AC (a-c) and CI (d-f) pipes; untreated (a and d), undersampled (b and e) and oversampled by SMOTE (c and f).

Fig. 8. Different clustering of asset data by K-Means method for (a-b) AC pipes; and (c-d) CI pipes.

Fig. 9. Reduction in failure versus rehabilitation cost based on LoF predicted by classifiers for (a-c): AC pipes; and (d-f) CI pipes.

Fig. 10. Reduction in failure versus rehabilitation cost based on economic analysis model for (a-c): AC pipes; and (d-f) CI pipes.

Fig. 11. Saving the flow capacity of the WDN versus rehabilitation cost based on consequence analysis model for (a-c): AC pipes; and (d-f) CI pipes.