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Multi-layered coarse grid modelling in 2D urban flood simulations

Albert S. Chen, Barry Evans, Slobodan Djordjević, Dragan A. Savić

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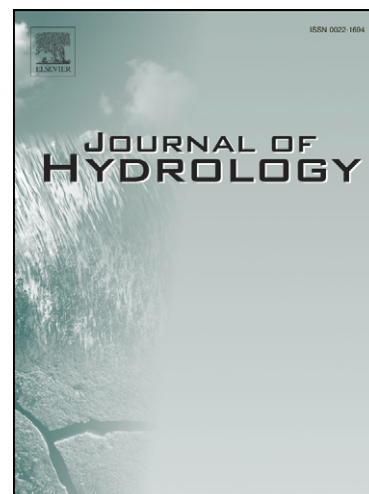
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1

Introduction

2 Urbanisation associated with economic growth, particularly in developing countries, has
3 become a strong global trend in the past half century (United Nations, 2010). Nowadays,
4 more than 50% of the world's population live in urban areas. This number is growing and
5 projections show that nearly 70% of world population will be living in urban areas by 2050.
6 Hazard risks and exposures increase rapidly in cities as a consequence of the concentration
7 of population and wealth, exhaustion of resources, and changing environmental and human
8 activities (Mitchell, 2003). In England, the Environment Agency (2009) estimated that
9 around 3.8 million properties are susceptible to surface water flooding (pluvial flooding). Due
10 to climate change, the likelihood of surface water flooding is rising because the central
11 estimate of UKCP09 (the UK Climate Projections 2009) predicted that the rainfall in winter
12 wettest days could increase by 10-30% by the 2080s over the majority of the UK (Jenkins et
13 al., 2009). The Pitt Review (Pitt, 2008) highlighted the fact that flood modelling is crucial to
14 understanding the increase of flood risk caused by climate change. This Review also
15 indicated that, although the Environment Agency has advanced understanding and models
16 for assessing the risk of flooding from rivers and coasts, the information related to surface
17 water flood risk is still limited. There has been significant research into fluvial and coastal
18 flooding and tools have been developed to analyse them, but models for pluvial flooding are
19 less advanced. Therefore, modelling and better understanding of the risk of surface water
20 flooding is needed urgently for flood risk management.

21 Two-dimensional (2D) surface flood modelling can provide abundant information about the
22 dynamics of flooding, which may improve the flood risk management. However, the
23 efficiency of 2D flood modelling has been one of the major challenges to modellers. The
24 performance of existing 2D models varies significantly depending the choice of time steps
25 and the number of iterations within each time step, the efficiency of numerical algorithms,

1 the use of multi-processing, the hardware specification and other computational overhead
2 costs for modelling (Néelz and Pender, 2010).

3 Various methodologies have been developed to improve the performance of modelling.

4 These approaches include:

- 5 • reduced-complexity models (Liu and Pender, 2010);
- 6 • simplified governing equations (Bates et al., 2010);
- 7 • parallelisation (Hankin et al., 2008; Neal et al., 2010);
- 8 • unstructured mesh (Wang et al., 2010);
- 9 • adaptive grid-based methods (Wang and Liang, 2011); and
- 10 • grid coarsening (Yu and Lane, 2006a).

11 Among these methods, unstructured mesh can effectively reduce the computing load and
12 potentially enable more efficient description of surface features, however the pre-processing
13 of terrain data is complex, especially in urban environment (the use of unstructured mesh is
14 beyond the scope of this paper).

15 On the other hand, grid coarsening appears to be the simplest approach and straightforward
16 for modelling. However, the loss of information with low resolution often leads to less
17 accurate modelling results. The efforts to rectify this problem and to regain some information
18 have included the use of: (1) sub-grid treatment (Yu and Lane, 2006b; Yu and Lane, 2011),
19 (2) porosity parameters (McMillan and Brasington, 2007), (3) multi-cell information from
20 pre-simulations (DHI Software, 2010), (4) progressive morphological filtering of raw LiDAR
21 data (Abdullah et al., 2012).

22 In urban environment, buildings occupy considerable space and their walls usually exclude
23 deluges from the interior spaces during flooding. The water flows around buildings rather
24 than into or through them, unless their entrances are left open. To characterise the physical
25 situation in overland flow modelling, using the roof elevations (whose resolution is less than

1 the building scale) in fine grids, is the simplest but computationally costly solution. When the
2 grid size is an order of magnitude greater than the building scale, the ground elevation is
3 commonly used along with *increased local roughness* for numerical simulations. However,
4 such an increase in roughness often has no objective setting criteria to follow. An alternative
5 solution is to take the average elevation of fine cells within a coarse cell as the averaged grid
6 for modelling. Nevertheless, the results are often too coarse to describe the local
7 phenomena often required in practical applications.

8 To improve the situation with coarse grid modelling, the Building Coverage Ratio (BCR) and
9 Conveyance Reduction Factor (CRF) were introduced to the 2D Urban Inundation Model
10 (UIM) to capture the building features *within* a coarse grid (Chen et al., 2008; Chen et al.,
11 2012). The application demonstrated that the use of BCR and CRFs provide good accuracy
12 of modelling results with considerably smaller computational time. However, it also indicated
13 that the approach failed to reflect the flow phenomena when a building *bisects* a coarse cell.
14 To overcome that problem, in this paper, we developed the *multi-layered approach* and
15 implemented it in the UIM to improve the accuracy of coarse grid modelling with limited extra
16 computational cost. The rest of the paper is organised as follows. The Methodology section
17 explains the details of the multi-layered flood modelling. The Applications and Discussion
18 section compares case studies using different grid coarsening approaches to the
19 benchmark of fine grid modelling. The main findings of the study are described in the
20 Conclusions.

21 **Methodology**

22 The 2D non-inertia UIM, based on the de Saint Venant equations, is adopted in the study for
23 simulating the overland flow propagation on alluvial plains with mild natural topography. The
24 parameters BCR and CRFs are applied to describe building attributes in coarse grid that
25 allow the applications to have accuracy similar to that of the fine grid modelling. The BCR

1 coefficient, $\alpha = A_b/A$ [-], represents the area ratio occupied by buildings within a
 2 computational cell, where A_b is the building area [m²] and A is the grid cell area [m²]. The
 3 CRFs, β_x and β_y , as shown in Figure 1, are the maximum occupancy ratios of buildings on
 4 the computational cell *boundaries* in the x and y directions, respectively, that flow cannot
 5 transfer through. The governing flow equations modified to account for CRFs are expressed
 6 as follows:

$$(1-\alpha)\frac{\partial d}{\partial t} + \frac{\partial[(1-\beta_x)ud]}{\partial x} + \frac{\partial[(1-\beta_y)vd]}{\partial y} = q \quad (1)$$

$$\frac{\partial(d+z)}{\partial x} + \frac{n^2 u \sqrt{u^2 + v^2}}{d^{4/3}} = 0 \quad (2)$$

$$\frac{\partial(d+z)}{\partial y} + \frac{n^2 v \sqrt{u^2 + v^2}}{d^{4/3}} = 0 \quad (3)$$

10 where, (1) is the continuity equation and (2)-(3) are the momentum equations in the
 11 horizontal Cartesian directions; d is the water depth [m]; u and v are the velocity
 12 components in the x and y directions, respectively [m/s]; z is the surface elevation [m]; n
 13 is the Manning roughness coefficient; q is the rate of water entering or leaving ground surface
 14 per unit area, comprising the excess rainfall, the upstream catchments inflows, the influent
 15 and effluent of sewer network nodes within a cell, and any overland flow drained by hydraulic
 16 facilities [m/s].

17 Details about the methodology of UIM with BCR & CRFs were discussed in a separate paper
 18 (Chen et al., 2012). The coupled BCR & CRFs enabled a representation of the available
 19 storage space within a coarse grid cell and the effective conveyance width between
 20 neighbouring cells. The modelling results showed that – rather than changing grid
 21 roughness by trial and error – this approach provided an objective way, to reflect the
 22 blockage effect induced by buildings using coarse grid modelling. Nevertheless, the BCR &

1 CRFs approach had failed to describe the regime that flow was diverted or blocked by
2 buildings that *bisect* a coarse cell (to be explained in next paragraph). To deal with the
3 situation, we propose the multi-layered approach to divide the potential storage area into
4 separate regions for modelling. In contrast, the previous BCR & CRFs approach (Chen et
5 al., 2012) is referred as the single layer approach in the following text.

6 Figure 2 shows two simple examples for BCR & CRFs applications. The channels in both
7 Figure 2-(a) and Figure 2-(b) have a width of 4 and a length of 12 fine grid cells (or a width of
8 1 and a length of 3 coarse grid cells), with the northern and southern boundaries closed, and
9 the eastern and western boundaries open. The building in Figure 2-(a) is located at the four
10 fine cells in the centre of a coarse cell, whereas the one in Figure 2-(b) occupies the four
11 cells that completely disconnect the domain into two parts. The inflow applied to the western
12 boundary traverses the channel in Figure 2-(a) but is blocked in Figure 2-(b). The single
13 layer approach generates the same BCR & CRF values for both layouts, causing the
14 building influence on surface flow identical in modelling. This misrepresentation of the
15 building layout would result in no outflow at the eastern boundary in Figure 2-(b). If the
16 domain in Figure 2-(b) is extended both northwards and southwards in coarse grid
17 modelling, as shown in Figure 3-(a), the flows from the west to the central coarse cell in the
18 fine grid modelling is separated into two routes to reach the cell in the east. The BCR &
19 CRFs in the single-layer approach cannot describe the separation of flow such that the
20 coarse grid modelling will allow the flow to propagate through the central cell from west to
21 east without any obstruction. Figure 3-(b) shows that the six possible flow paths between the
22 central cell and its four neighbours.

23 In order to describe the flow interactions comprehensively in the multi-layer approach, the
24 central cell in Figure 4-(a) is considered as the combination of two layers (Layer 0 and 1) of
25 cells as shown in Figure 4-(b) and (c). Both cells reflect the different attributes of the areas

1 that are bisected by the building within the coarse cell. Figure 4-(b) shows that the Layer 0
2 central cell has a BCR value 0.5, which means only 50% of cell area is available for flood
3 storage in the west region of the coarse cell. The CRF values at the west, north and south
4 cell boundaries are 0.0, 0.5 and 0.5, respectively, which allows water movement between
5 the Layer 0 central cell and the three neighbour cells via paths P1-P3, as shown in Figure
6 5-(a). The CRF value at the east boundary is 1.0, which prevents the flow movement from
7 any of the three boundaries to the east.

8 On the contrast, Figure 4-(c) shows the Layer 1 central cell has a BCR value 0.75, which
9 represents that only 25% of coarse cell area is available for flood storage in the east region.
10 The CRF values at the north, south and east cell boundaries are 0.75, 0.75 and 0.0,
11 respectively, which allows the water movements between the Layer 1 central cell and the
12 neighbour cells via paths P4-P6, as shown in Figure 5-(b). The CRF value at the west
13 boundary is 1.0, which prevents the flow movement from any of the three boundaries to the
14 west.

15 Figure 5-(c) is the schematic presentation for the relationships between the coarse cells.
16 The central cell is divided into two smaller cells with reduced storage areas. For each time
17 step calculation, the momentum equations along flow paths between all Layer 0 cells over
18 the whole domain are firstly solved using the original UIM routine. Then, the momentum
19 equations along flow paths between Layer 0 cells and the Layer 1 central cell are solved
20 where such flow paths exist. In case of more than two layers (such as in the two case studies
21 discussed later), corresponding momentum equations would need to be solved in a similar
22 manner. Finally, the continuity equations are solved in the same sequence. Since the two
23 central cells (Layer 0 and 1) are treated separately, the flow interaction between them is not
24 permitted, which represents correctly the physical phenomenon that flow between the two
25 regions is blocked by the building.

1 The described principles for setting up the Multilayer parameters are simple. Nevertheless,
2 the calculations of the BCR & CRFs, the level of Multilayers and the linkages between cells
3 of different layers become complex if more than two layers are required. An appropriate
4 post-processing is also required to remap the modelling results back to correct positions on
5 the fine grid. All this would be a demanding task in large areas with thousands of buildings.
6 We adopted a cellular automata (CA) approach to flag out all coarse cells bisected by
7 buildings, and calculate automatically all the relevant parameters. The CA model searches
8 all non-building fine cells within a coarse cell to identify consecutive non-building areas.
9 Each identified area is indexed as a coarse cell layer and its BCR is calculated. Then, the
10 flow paths between neighbour coarse cell layers and the corresponding CRFs are
11 determined. Evans et al. (2009) proposed the original methodology of the CA model that can
12 generate BCR and CRFs for the single layer approach. The advanced version (Evans et al.,
13 2012) has been extended to the multi-layered approach and applied to the examples shown
14 in this paper.

15 **Applications and discussion**

16 **Synthetic case study**

17 The first case study was selected to be an E-shaped building on a 400m x 100m 'ski run'
18 surface, following the previous single layer BCR & CRFs application (Evans, 2010). The
19 arrangement of the building was complex enough to demonstrate the difference between
20 single layer and multi-layered approaches. The terrain consisted of three sections, as shown
21 in Figure 6, the first and the last 100m sections had a slope 0.005:1 (V:H) and the middle
22 200m section had a milder slope 0.002:1. The northern and southern boundaries were
23 closed and the eastern boundary was open. A lateral discharge, shown in Figure 7, was
24 introduced at the western boundary and distributed uniformly over a 60m central swath (30m
25 either side of the centre line bisecting the x-axis where $y = 0$). The normal flow depth was set

1 as the downstream condition at the eastern boundary. These boundary conditions were
2 applied to ensure the propagation of flow along the surface from west to east. The E-shaped
3 building with 4m height was located in the middle section of the domain and the building's
4 orientation was such that its closed face was perpendicular to the incoming surface flow.
5 Three coarsening approaches (averaged DEM, single layer and multi-layered) with 20m grid
6 resolution were compared to the benchmark. The benchmark was assumed to be the
7 simulation on a fine 1m grid with terrain elevations that include building heights, with
8 buildings positioned such that each fine grid cell is either fully or not at all covered by a
9 building. The averaged DEM took the mean of ground and roof elevations of fine cells within
10 a coarse cell as the new elevation of the coarse cell. The single layer approach adopted the
11 mean of the ground elevations of fine cells that were not occupied by buildings to represent
12 the new elevation of a coarse cell, with the calculated BCR & CRFs. The multi-layered
13 approach determined the new ground elevation of each layer based on the average
14 elevation of non-building fine cells in the layer. The individual BCR & CRFs were calculated
15 for the extra layers and flow paths.

16 Figure 8 shows the layer index and BCR values of Layer 0 of the coarse cells surrounding
17 the E-shape building. The overall layout around the building feature can be shown as the
18 schematic map shown in Figure 9. The circle size represents the available storage area, the
19 arrows represent the flow path between cells in multiple layers, the value associated with
20 each arrow represents the CRF value and the colour represents the corresponding layer
21 number as shown in Figure 8. The preservation of the building features in the 20m resolution
22 was achieved by using additional 6 grid cells and 10 pathways connecting them accordingly,
23 which is 7 pathways more than in a single-layer approach.

24 The error distribution maps of the coarse grid modelling results, as compared to the fine-grid
25 benchmark, are shown in Figure 10. The averaging with building roof height raised the

1 terrain elevation that expanded the building areas in the coarse grid. For the 20m resolution,
2 the widths of flow paths on north and south sides of building were reduced from 30m to 20m
3 each due to the over-estimated building areas, which resulted in significant blockage effect
4 on the upstream side of the building, as shown in Figure 10-(a). The errors of the single layer
5 approach in Figure 10-(b) show that the BCR & CRFs did not describe the layout where the
6 building bisected coarse cells.

7 The reasons for this are illustrated in Figure 11-(a), which shows the original building
8 alignment within 20m resolution grid in the single layer approach. Figure 11-(b) is a similar
9 setting but with gaps between buildings, and the compensation building areas were added
10 back to have equivalent BCR values in Figure 11-(a). Although the widths of flow paths on
11 cell interfaces where the 4m building walls occupied were reduced by 20% in Figure 11-(a),
12 the approach did not prevent the flow interactions between both sides of the building and
13 both settings in Figure 11-(a) and (b) had identical flow behaviour, i.e. the single layer
14 approach cannot distinguish between these two cases. Therefore, the water transferred
15 from the west side of the building directly into the inner area resulted in a large
16 underestimation error on the upstream side of the building and an overestimation on the
17 downstream side. Because the flow in the multiple layer modelling was blocked by the
18 building completely instead of having width reduced flow paths, the backwater effect
19 increased on the upstream side of the building with less overestimation of flood depths on
20 the downstream side than in the single layer case, as shown in Figure 10-(c).

21 Figure 12 shows the maximum flood depth profiles along the central line in the x direction of
22 different modelling results. The profile of the multi-layered approach is clearly much closer to
23 the benchmark model than other two approaches. As no flow is allowed through the building
24 using this method the maximum depth errors after the building are thus significantly reduced
25 when using the multilayer approach.

1 Table 1 shows the root mean squared error (RMSE) of the calculated maximum flood depths
2 for the three approaches against the benchmark model for the whole computing domain and
3 the middle section, where the building was more influential on the flow movement. These
4 results reveal that the multi-layered approach offered a significant improvement over the
5 averaged DEM and the single layer approaches.

6 Table 2 shows that the model efficiency of the multi-layer approach is good, i.e., the
7 reduction of the number of grid cells greatly reduces the computing time for coarse grid
8 modelling. As the multi-layered model requires more computing time for solving those extra
9 layers and flow paths, and remapping the coarse data back to the fine grid at selected output
10 timing, the overall running time was only slightly longer than the other two grid coarsening
11 approaches. Nevertheless, the multi-layered modelling, with the added advantage of
12 maintaining building integrity and subsequent flow-path routing, is more accurate such that
13 the minor additional time required is negligible when assessing the model performance.

14 **Real case study**

15 In the following example a 300m x 300m LiDAR tile at a 1m resolution shown in Figure 13
16 was applied to test the multiple-layered approach in real urban environment. This surface
17 model was coarsened using above-mentioned three methods to a 12m resolution. Rainfall
18 was introduced directly onto the 2D surface flow model over the whole region and – in case
19 of the multi-layered approach – into each layer simultaneously. It was assumed that any
20 rainfall that lands upon a building roof will be drained directly to a sewer and therefore will
21 not move across the surface, hence the rainfall was only applied to the surface regions
22 where there are no buildings present. For this particular simulation the duration of the input
23 rainfall was one hour and was applied at a constant intensity 60mm/h. The overall simulation
24 time was 90 minutes which allowed a 30-minute period for water movement across the
25 surface after the rainfall has stopped.

1 Figure 14 shows the maximum flood depth distribution on the 1m resolution benchmark and
2 the three coarse grid models. The pattern of water distribution reveals three areas with
3 significant ponding of surface water, which are highlighted as regions A, B and C. The
4 benchmark result, Figure 14-(a), shows that water accumulated in region A and then flew
5 through the narrow alleyway in the east section of the terrace on the north side of region A to
6 location of region B. The water in this region then propagated via two alleyways between
7 buildings to the street on the north side of the terrace that connects to region C. When the
8 built-up water depths in region B were large enough, the flow path around the south side of
9 the building next to the north-east boundary of region B was formed that allowed the surface
10 water to move towards region C.

11 Figure 14-(b) shows the averaged DEM approach not only led to the loss of alleyways
12 between buildings, it also caused the narrowing of street channels that convey surface
13 water. No flow path via narrow alleyways between buildings was formed such that more
14 water (with greater flood depths) ponded in the north-western, the south-eastern and the
15 south-western upstream areas. Less flooding occurred in the downstream areas, especially
16 region C. Meanwhile, the assumption was that rainfall falling on building roof was drained to
17 sewer system directly. In the averaged DEM approach, a cell is normally regarded as a
18 non-building cell unless it is completely occupied by buildings, such that the surface runoff
19 can flow to neighbour non-building cells quickly because of the significant difference of
20 elevations. Therefore, same flood depth covers the whole coarse cell area even though it is
21 partially occupied by buildings. Meanwhile, pre-processing to multiply the rainfall amount by
22 the non-building coverage area ratio of a cell was required to determine the rainfall input to
23 each cell.

24 Figure 14-(c) shows that the single layer approach produced closer modelling result than the
25 averaged DEM one to the benchmark. The flood depth only represents the flow condition of

1 non-building area within a coarse cell. However, it also yielded a significant underestimation
2 in surface depths within region A as a result of further erroneous (with respect to benchmark
3 model) flow routing through previously obstructed alleyways (to be discussed later). Similar
4 situation occurred for the water moving from region B to downstream region C. The water
5 transferred from region B to the street on the north directly such that the flow path around the
6 south side of the building next to region B was not formed. This resulted in greater flood
7 depths and extent than other two grid coarsening approaches in region C.

8 Figure 14-(d) shows that the multi-layered approach had by far closest modelling result to
9 the benchmark model. Multiple flood depths within a coarse cell are obtained for all
10 separated non-building areas. The alleyway in the east section of the buildings on the north
11 side of region A allowed the flow propagating from region A to region B. The water in region
12 B further flew to the street on the north side via the alleyways between buildings, as well as
13 bypassing the south side of the building next to region B. The representations of buildings
14 and the patterns of flow movements were better described in the multi-layered approach
15 than in the other two grid coarsening approaches.

16 Figure 15-(a) shows the detailed maximum flood depths near the alleyways in the west
17 section of the buildings (the outlined area next to region A in Figure 14) on the north side of
18 region A. Three alleyways with widths less than 1m were represented as blocked in the
19 benchmark model due to the resolution of terrain data.

20 In the coarse grid modelling, the representations of the two cells highlighted in Figure 15-(b),
21 15-(c) and 15-(d) resulted in significant differences of results. In the averaged DEM
22 approach, as shown in Figure 15-(b), the alleyways between buildings were completely lost,
23 as discussed above, and the whole section was modelled as single terraced house.

1 In the single layer approach, as shown in Figure 15-(c), the flow was allowed to move from
2 one cell boundary to any other boundary of the highlighted cells because neither side had
3 CRF=1 and the internal blockage was not considered.

4 In the multi-layered approach, as shown in Figure 15-(d), the non-building areas of the
5 top-right highlighted cell was divided into five layers for modelling. The setting prevented the
6 flow transferring from the south and the east sides to the north and west sides. The
7 bottom-left highlighted cell was modelled as two layers and the flow interactions among the
8 north, east and south sides were possible in the same layer. Nevertheless, the layer of its
9 north neighbour cell can only interact with the highlighted cell such that the flow movement
10 via the alleyway was also blocked, which was the same as in the benchmark model.

11 Figure 16 shows the detailed maximum flood depth in the region B, which is outlined in
12 Figure 14. In the benchmark model, as mentioned earlier and shown in Figure 16-(a), the
13 surface water left region B either via the two alleyways in the west section of buildings on the
14 north or bypassing the south side of the building on the east.

15 Figure 16-(b) shows that the averaged DEM approach completely stopped the flow
16 interaction between region B and the street on the north, therefore, less flooding occurred
17 along the street.

18 In the single layer approach, as shown in Figure 16-(c), the flow was allowed to move across
19 the highlighted cells from region B to the street on the north. Therefore, simulated flood
20 depths in region B were smaller.

21 For the multi-layered approach, as shown in Figure 16-(d), the two alleyways affected
22 modelling results in the same manner as in the benchmark. Each of the two highlighted cells
23 were modelled as two separated layers that forbid the direct flow interaction between region
24 B and street on the north. More water was trapped in region B and then the flow path

1 bypassing the south side of the building was formed. Consequently, the overall modelling
2 result was much similar to the benchmark one.

3 Although three alleyways shown in Figure 15 were blocked in the benchmark model, it is
4 clear that the modelling result may not be correct because they were not properly described
5 in the terrain data. The alleyways narrower than the resolution of terrain data are likely to be
6 blocked, especially when their orientation is not parallel/orthogonal to the grid axes. Further
7 study to clear up such alleyways from the terrain data would be necessary to provide better
8 modelling.

9 **Conclusions**

10 The originally developed multi-layered approach to regular grid 2D urban flood modelling
11 has been presented in this paper. Through implementation of BCR and CRF coefficients and
12 the accordingly modified flow equations, this method enables computation of flows
13 separated by buildings within a coarse grid cell. Automatic generation of layers and
14 calculation of BCR and CRFs using a cellular automata based flagging has been
15 implemented and tested in conjunction with the modified UIM model.

16 Through the comparisons on two case studies (a synthetic and a real one), it has been
17 shown that the multi-layered approach gives results much closer to a high-resolution
18 benchmark than the single layer model (whilst the latter is in turn much more accurate than
19 the simple DEM-averaging approach). The increased accuracy of the multi-layered
20 approach comes at only insignificantly increased computational cost. Therefore, this
21 approach lends itself for 2D modelling on a coarse grid with a good balance between
22 accuracy and computational speed. In practical applications, a desired (or “optimal”) choice
23 of the coarse grid size can easily be identified through error analysis in numerical
24 experiments similar to those presented in this paper.

1 The implementation of the multi-layered approach in conjunction with any other raster grid
2 based 2D model would require a modification of flow equations to include additional layers
3 and CFRs, however that is fairly straightforward. Without the modifications of other authors'
4 models – i.e. on the basis of our research alone – it is not possible to conclude if and to what
5 extent the multi-layered approach is superior to known improvements of coarse grid
6 modelling mentioned in the introduction. However, it is anticipated that the improvement
7 offered by our approach may be at least as good as sub-grid treatment, porosity parameters
8 or multi-cell information. This expectation – that is yet to be checked – is based on the fact
9 that multi-layered model is very flexible due to efficient automatic generation of layers and
10 calculation of BCR & CRFs, and it is realistic in the sense that it explicitly treats pathways
11 separated by buildings within a grid cell.

12 In conclusion, with the introduction of multiple layers, the possibility of a much faster 2D
13 surface flow modelling on a coarse grid – with nearly a fine-grid accuracy – can be efficiently
14 achieved. In other words, larger scale urban inundation can be simulated within time that a
15 high resolution model would require on a much smaller limited extent of urban area.

16 The real case study results highlighted, however, that some narrow alleyways not
17 represented properly due to LiDAR data resolution need additional attention in modelling.

18 Potentially, the problem can be solved if higher resolution of terrain data is made available.

19 However, the multi-layered approach can extract key features and model the detailed flow
20 movement even without using finer grid resolution, which would require creation of pathways
21 and CRFs different from the one described in this paper. In real urban environment,
22 infrastructure such as flyovers, underground passages, bridges, etc., also alters the
23 propagation of surface runoff. The multi-layered methodology can be efficiently used to
24 describe multiple flow paths that cross over each other within a cell such that the complex
25 flood propagation phenomena can be modelled.

1

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5

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46 in flood inundation modelling. *Hydrological Processes*, 25(1): 36-53.
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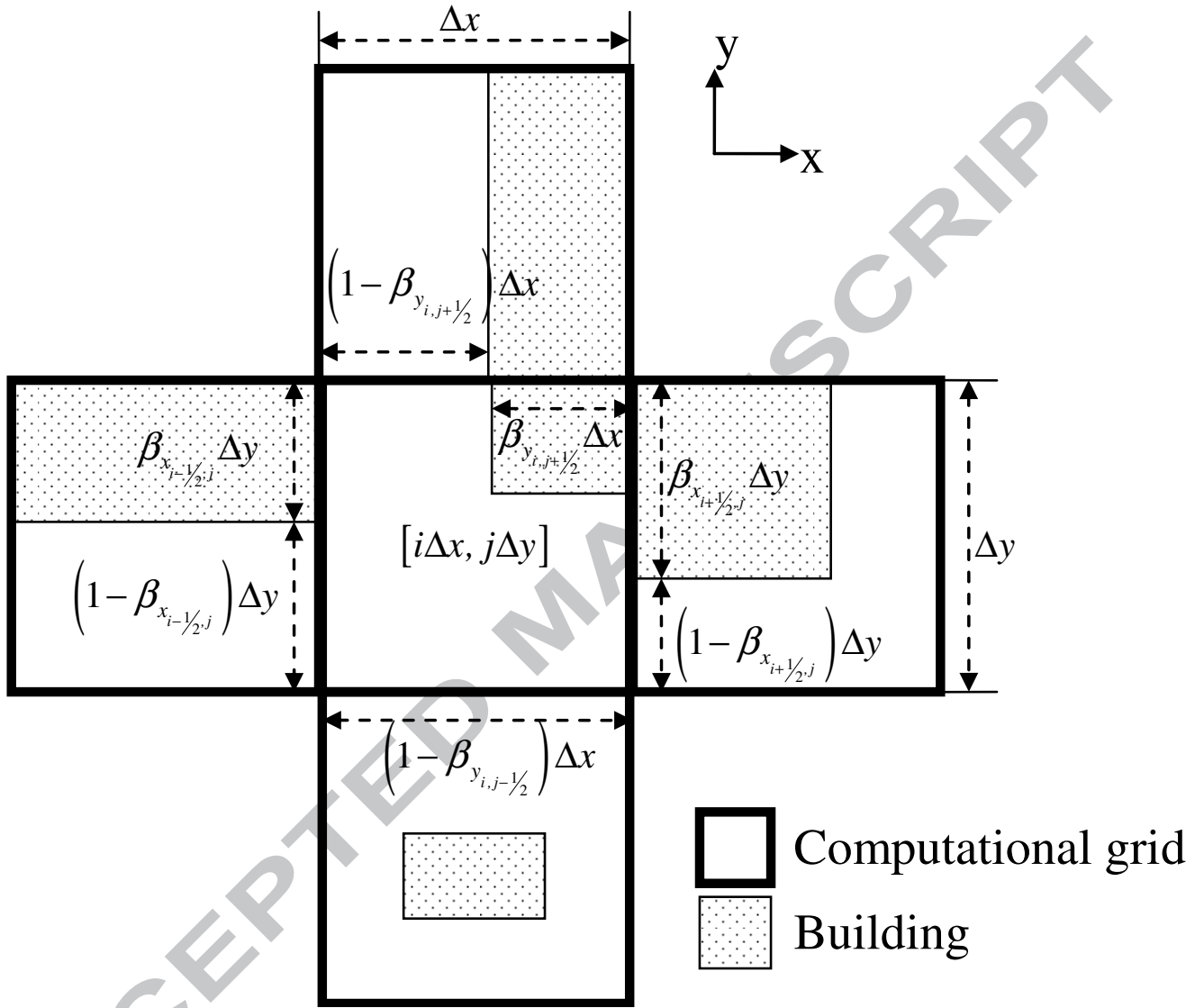
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4 Figure 1. The determination of the CRFs for a computational grid based on the building

5 alignments within itself and its neighbourhood grids at cell boundaries.

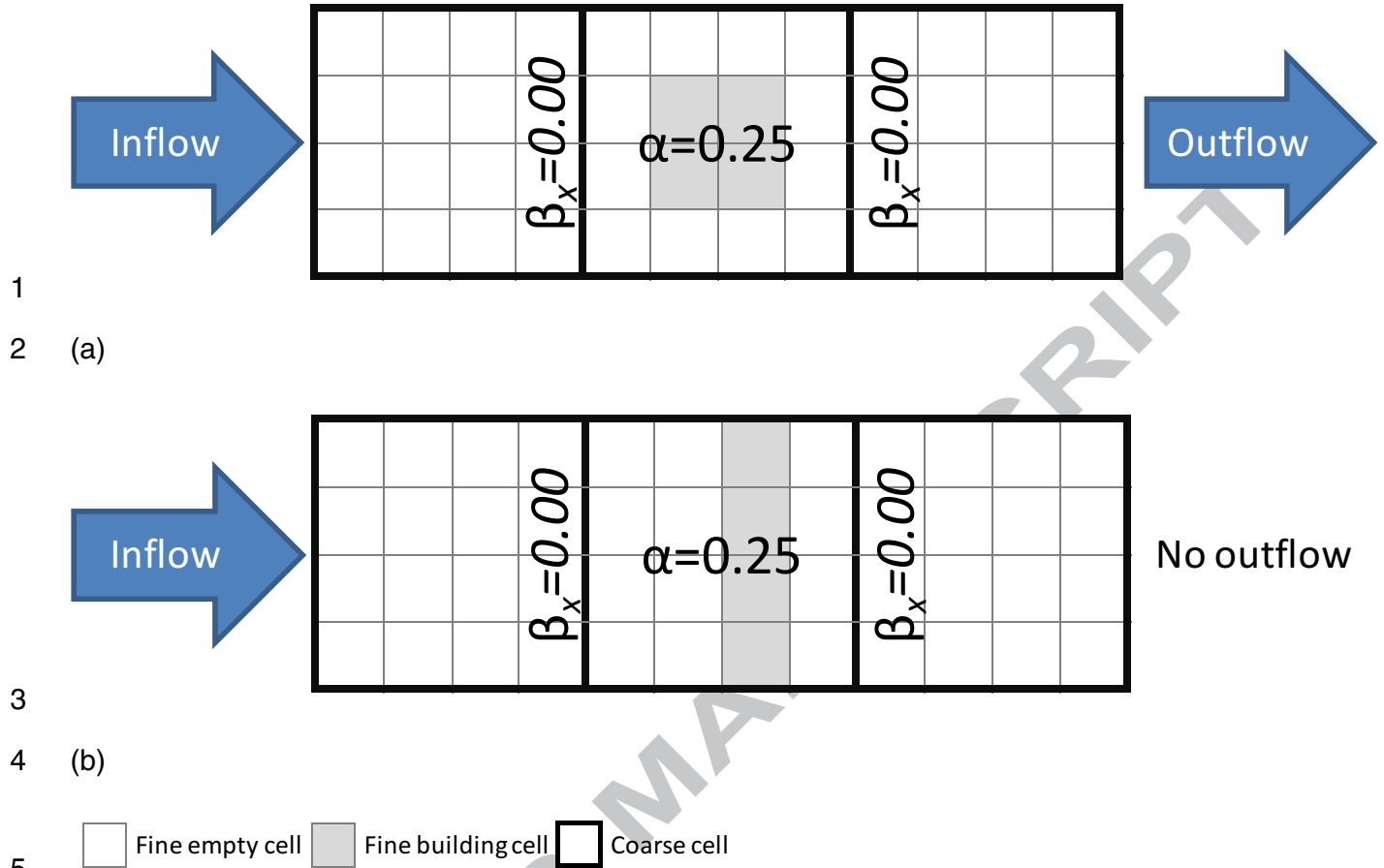
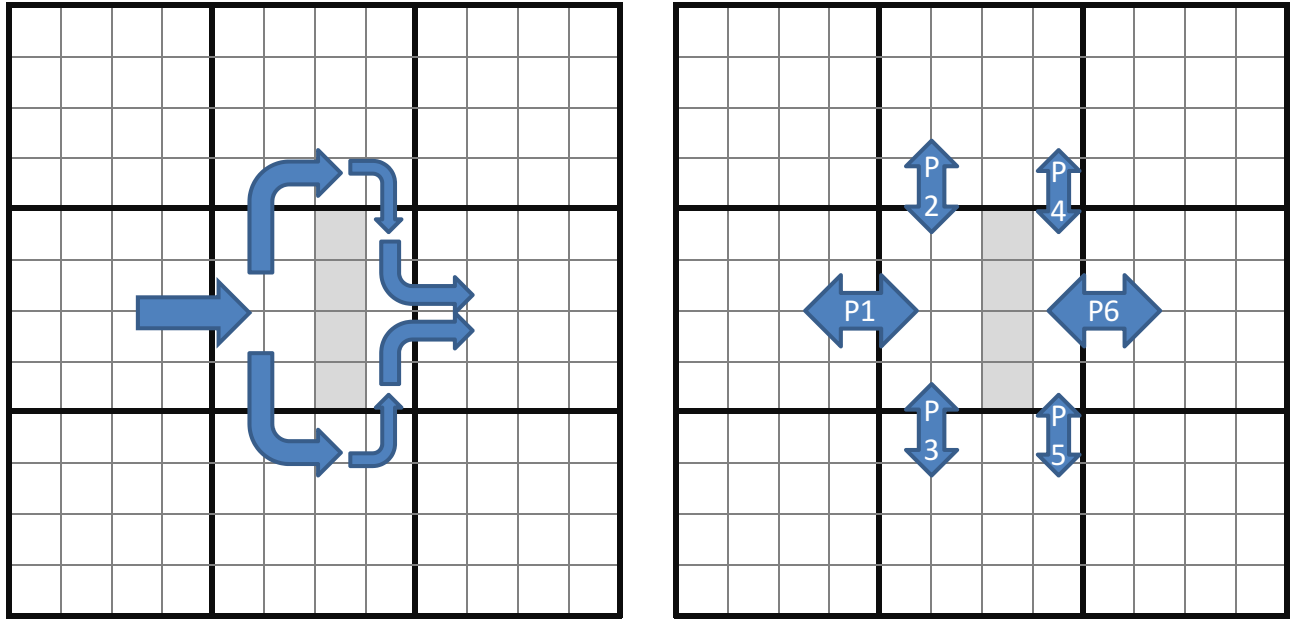


Figure 2. Different building layouts within a coarse cell result in same BCR and CRFx values

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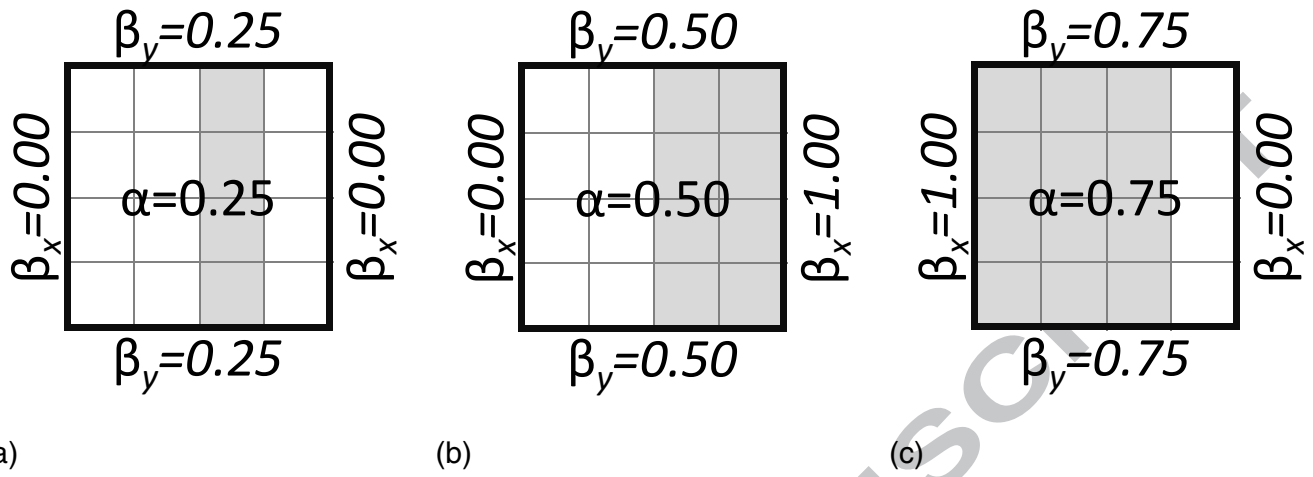


(a)

(b)

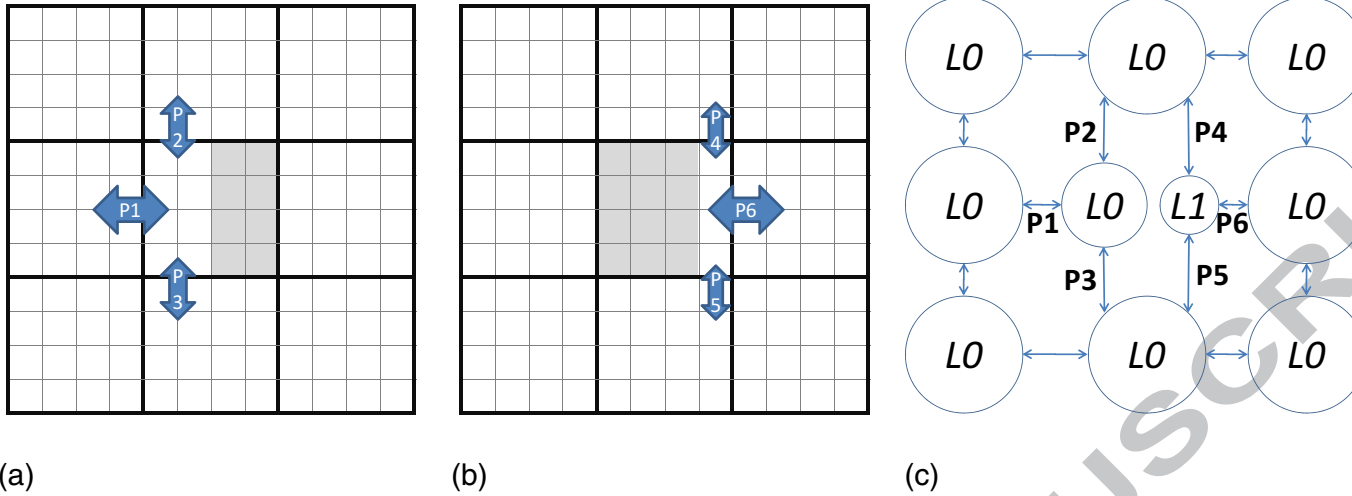
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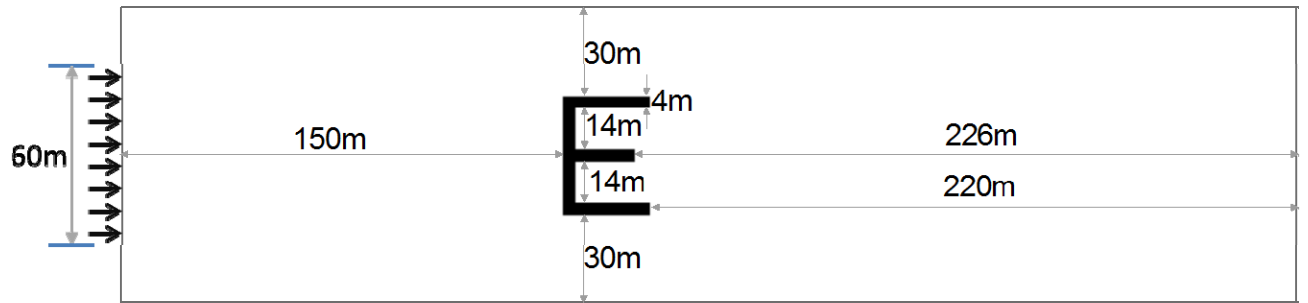


2 Figure 4. (a) The central coarse cell in Figure 3 is represented by the multi-layered cells of
 3 (b) Layer 0 and (c) Layer 1

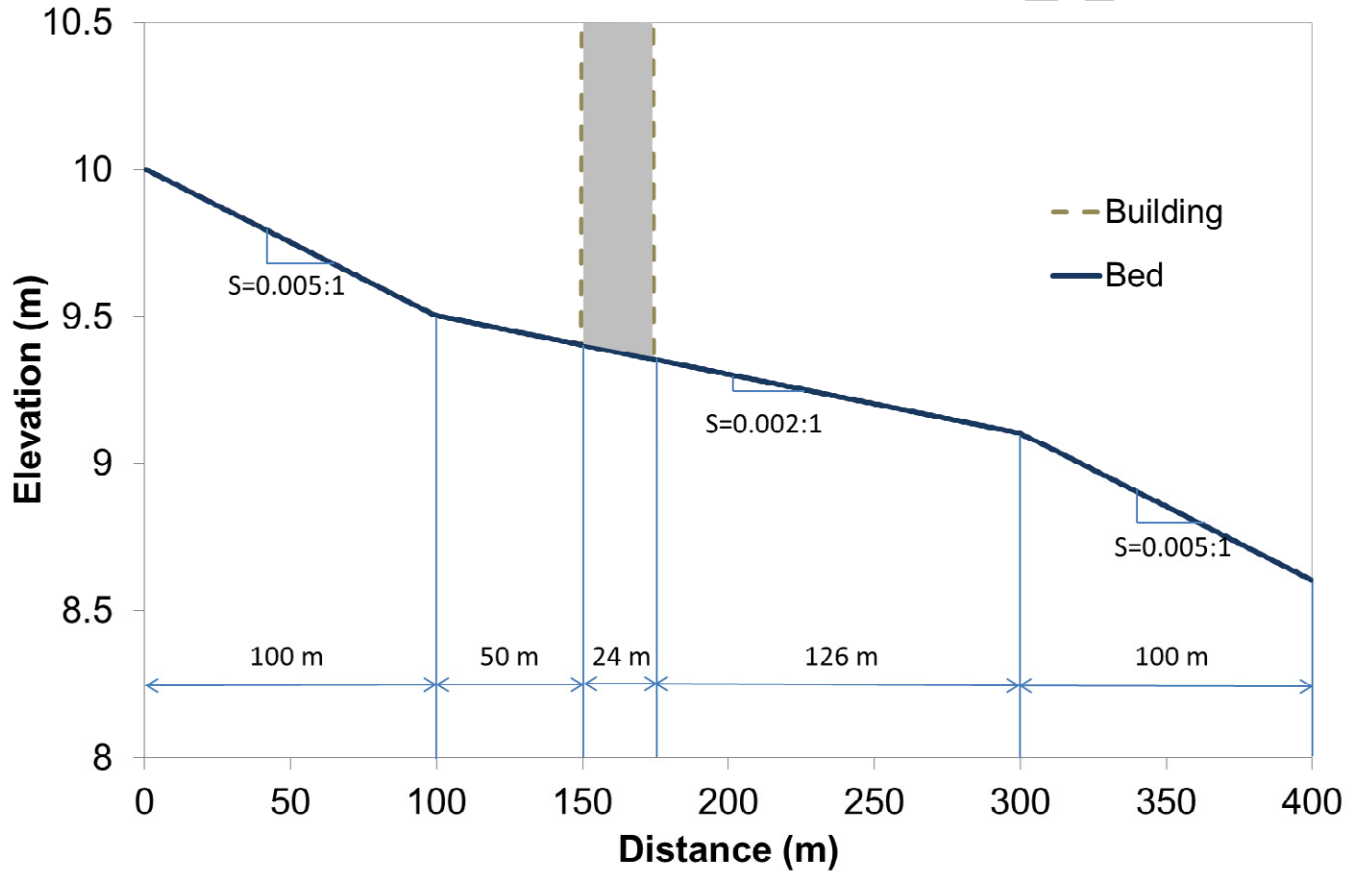
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2 Figure 5. (a) The Layer 0 central cell used for describing the flow paths between the central cell and its west, north and south
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 4 neighbour cells.



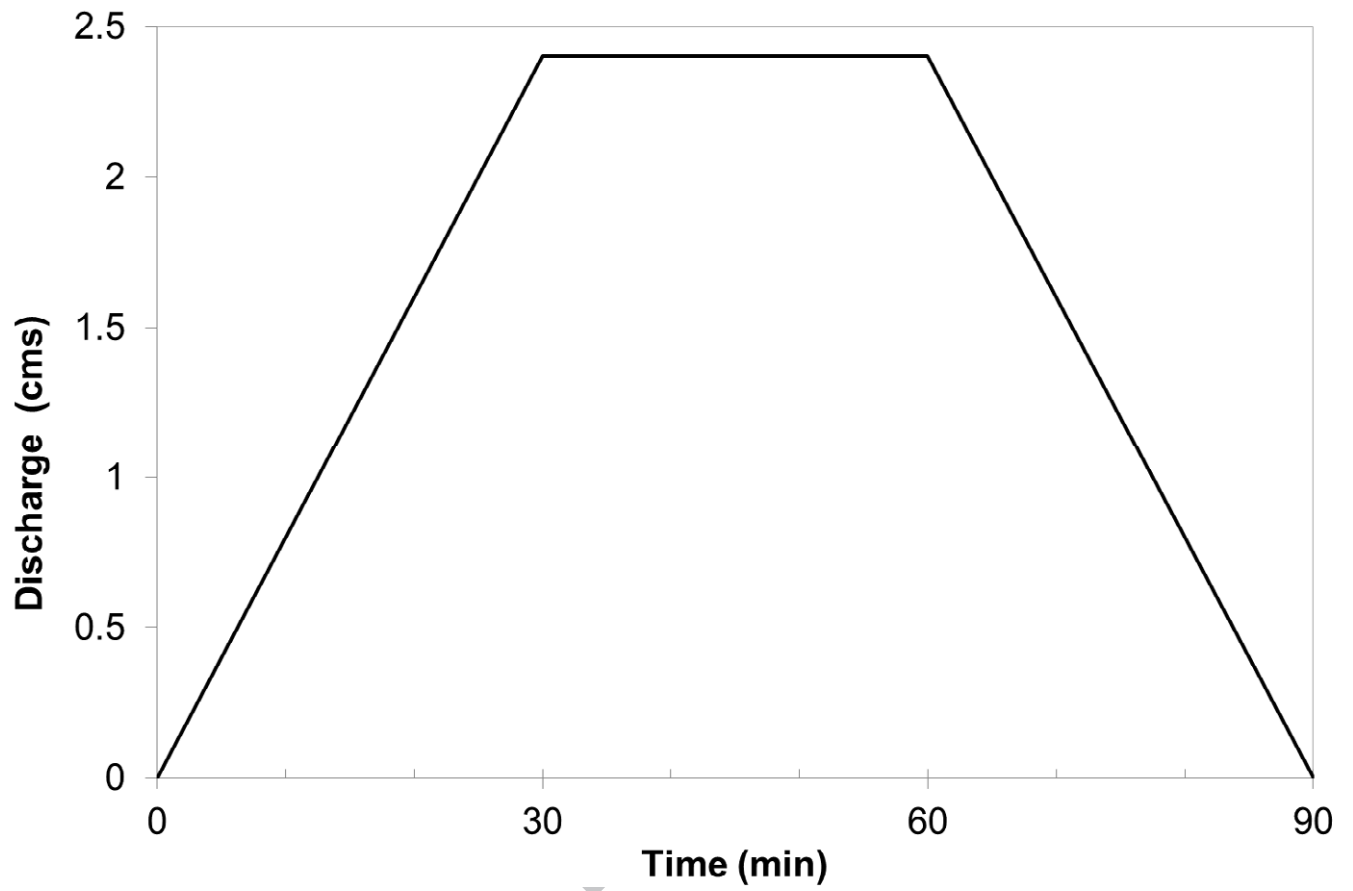
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3 Figure 6. The plain view (up) and the longitudinal elevation profile (down) along the central

4 line of the 2D case study.

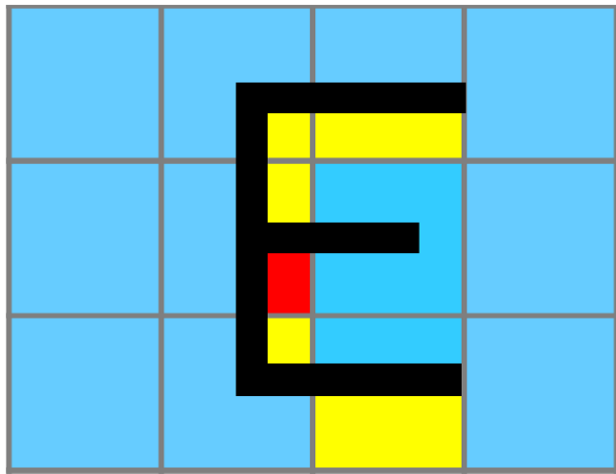


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2 Figure 7. Lateral flow input at $x=0$

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■ Layer 0 ■ Layer 1 ■ Layer 2 ■ Building

| | | | |
|------|------|------|------|
| 0.00 | 0.25 | 0.50 | 0.00 |
| 0.00 | 0.50 | 0.14 | 0.00 |
| 0.00 | 0.25 | 0.70 | 0.00 |

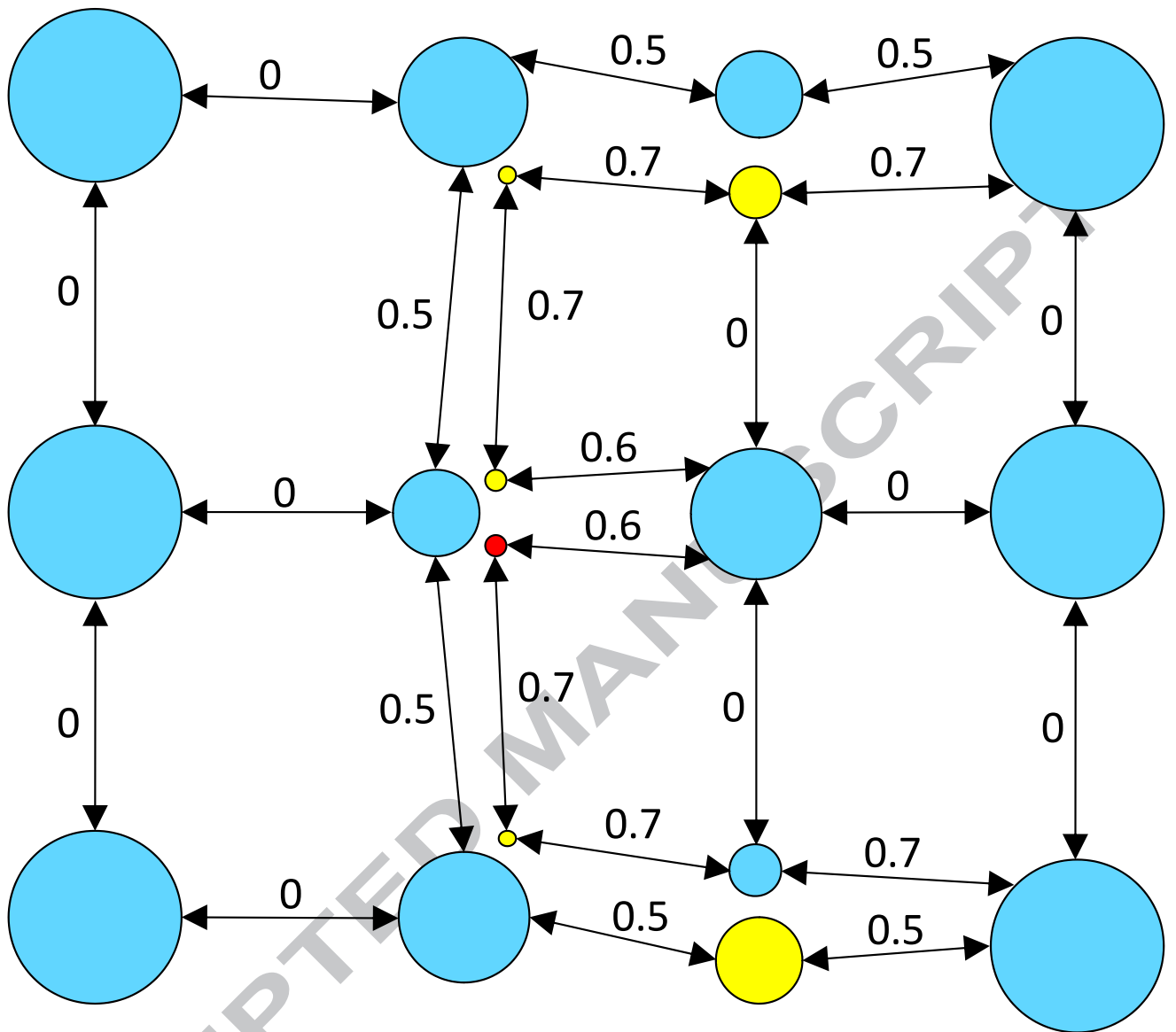
(a)

(b)

2 Figure 8. Grid plain view of (a) multiple layers and (b) BCR for Layer 0 using the

3 multi-layered

approach



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2 Figure 9. Multi-layered concept map of the section shown in Figure 8

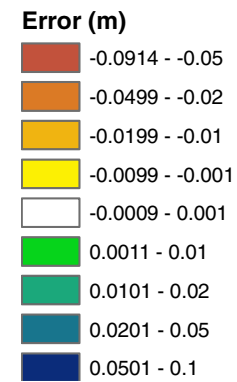
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(a) Averaged DEM



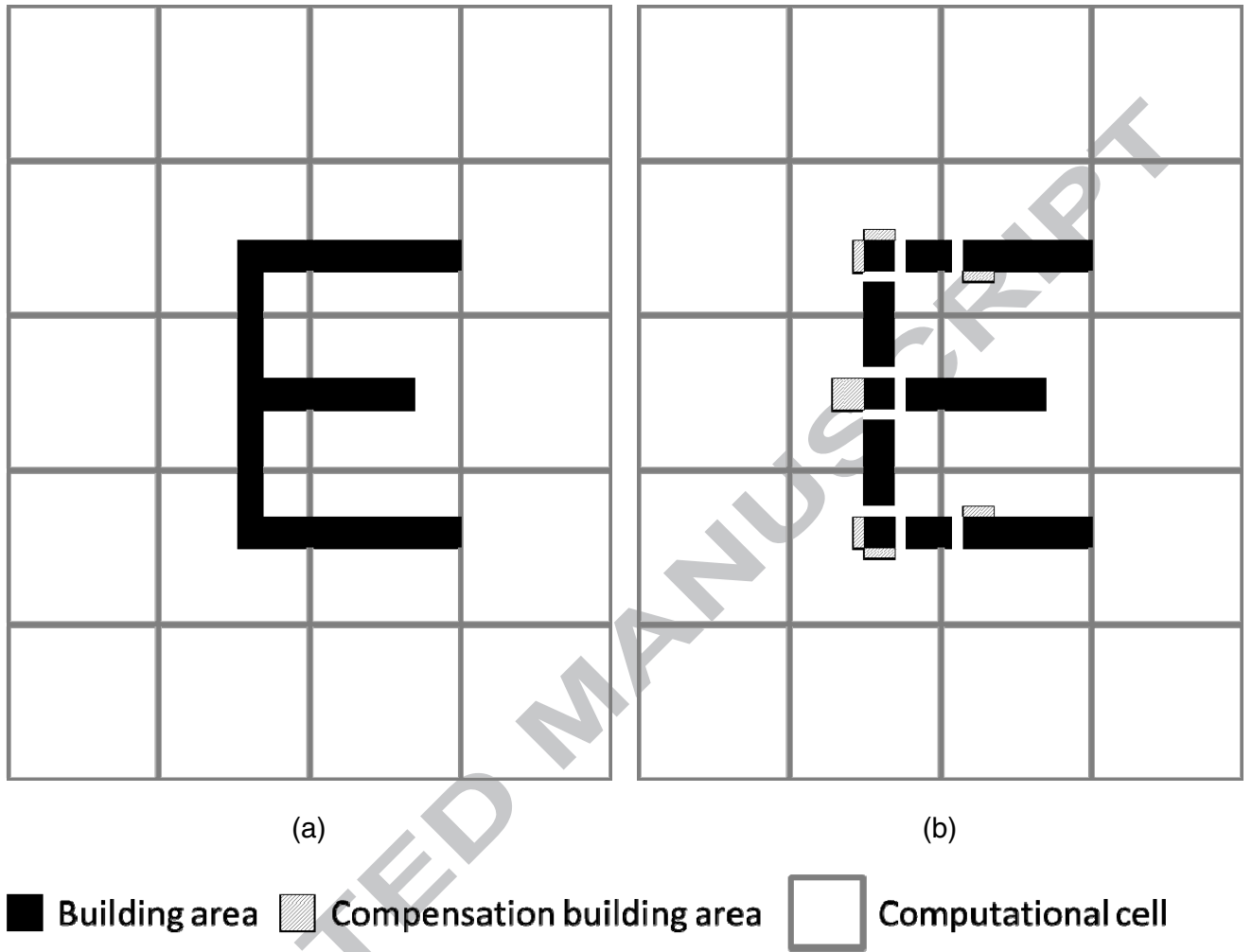
(b) Single layer



(c) Multi-layered

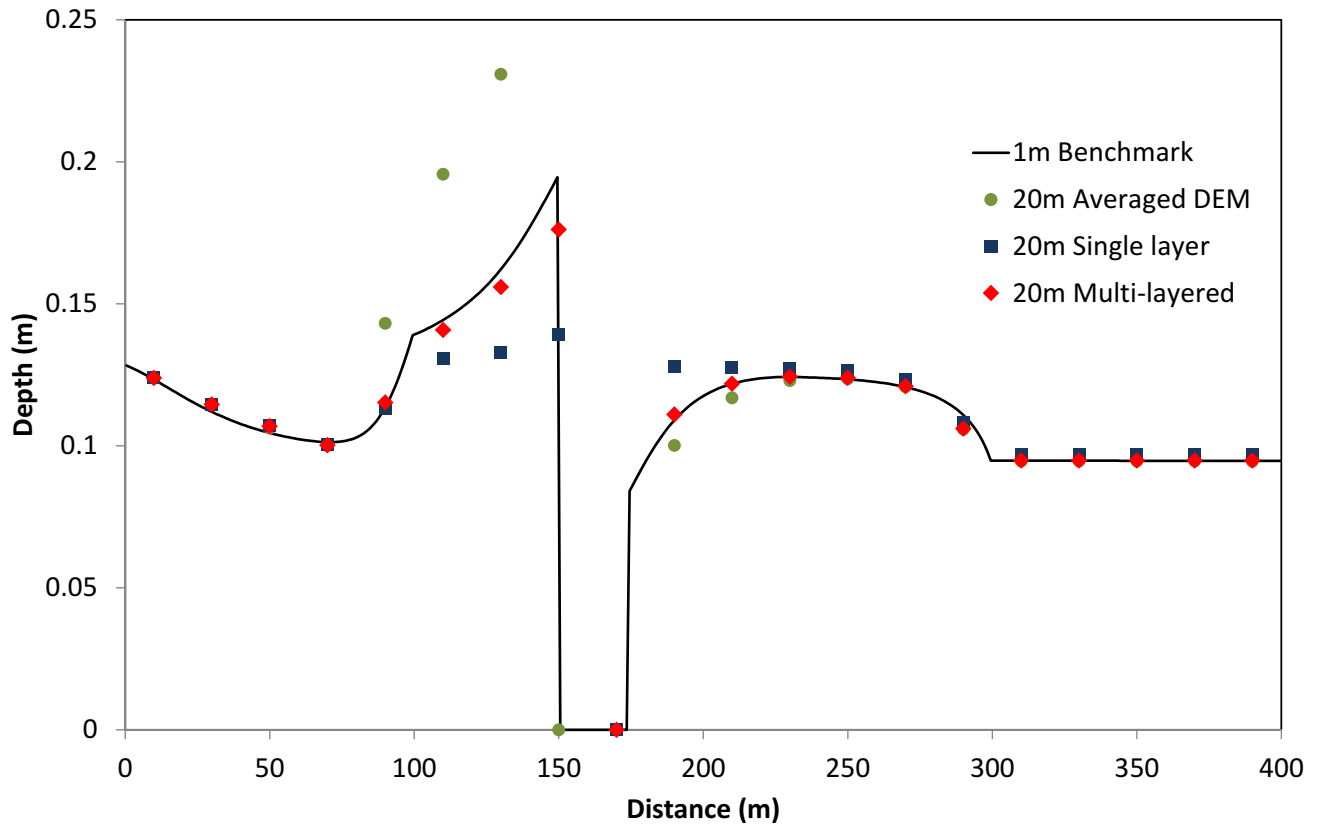
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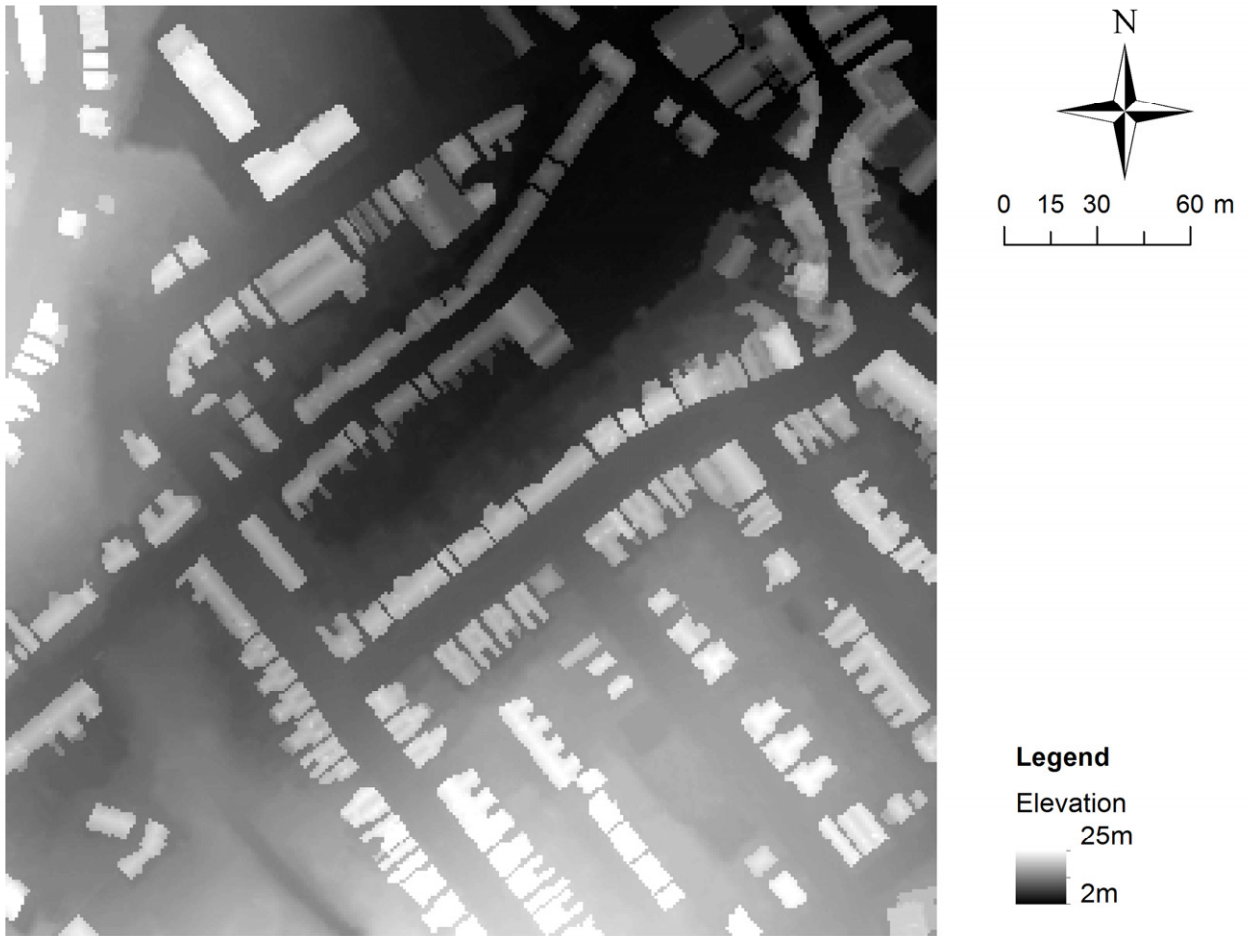
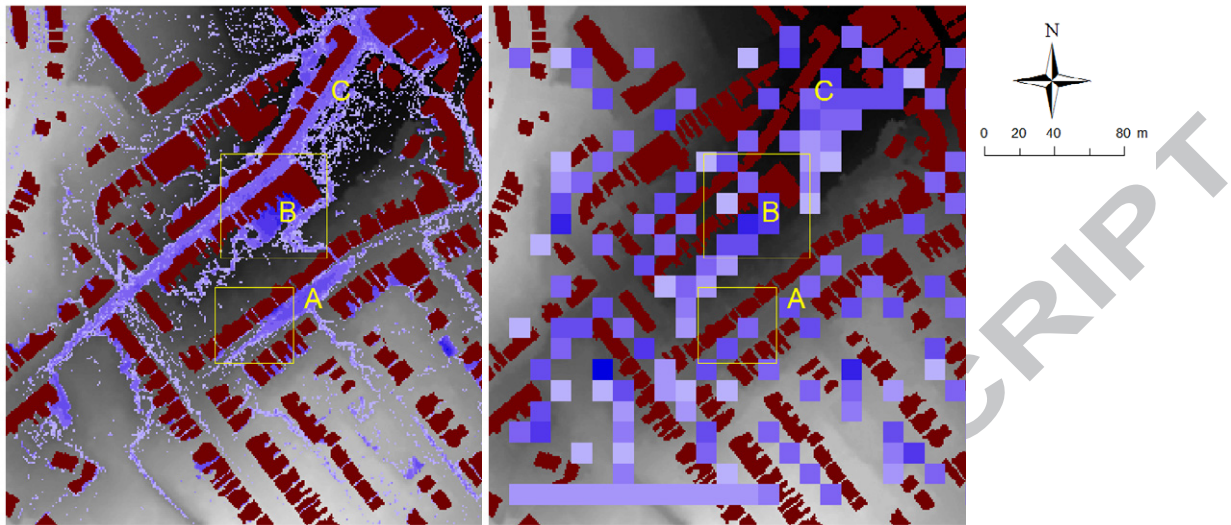


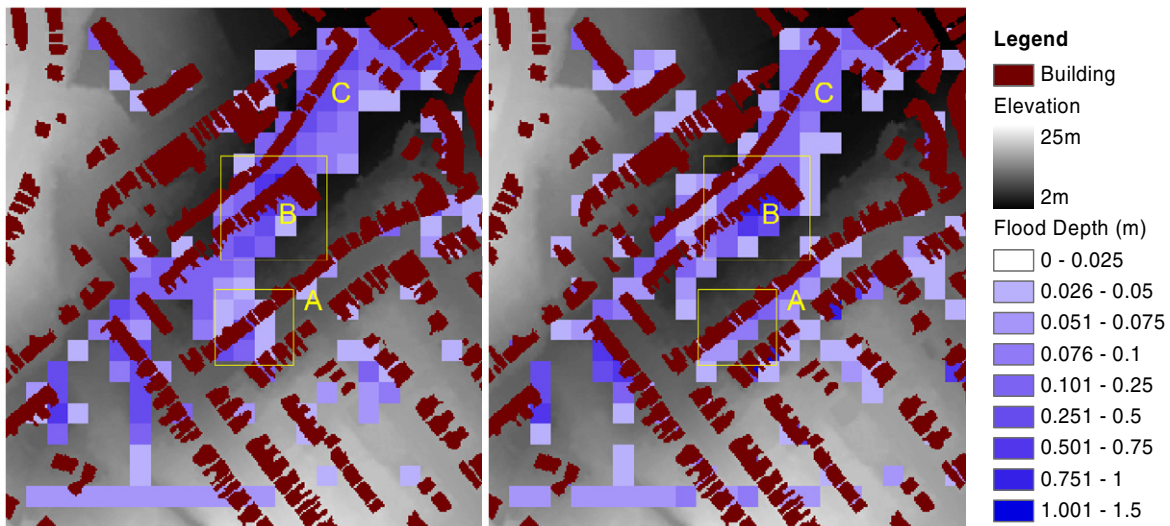
Figure 13. The terrain elevation with building height from LiDAR data for the real case study

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(a) Benchmark

(b) Averaged DEM



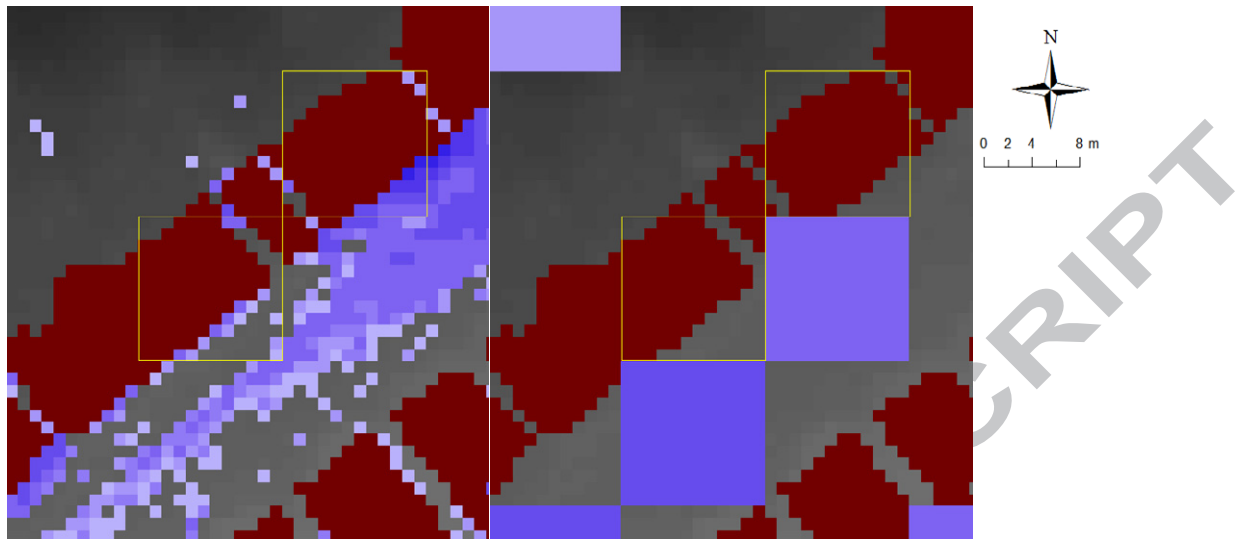
(c) Single layer

(d) Multi-layered

2 Figure 14. The maximum flood depth for the benchmark and the three grid coarsening

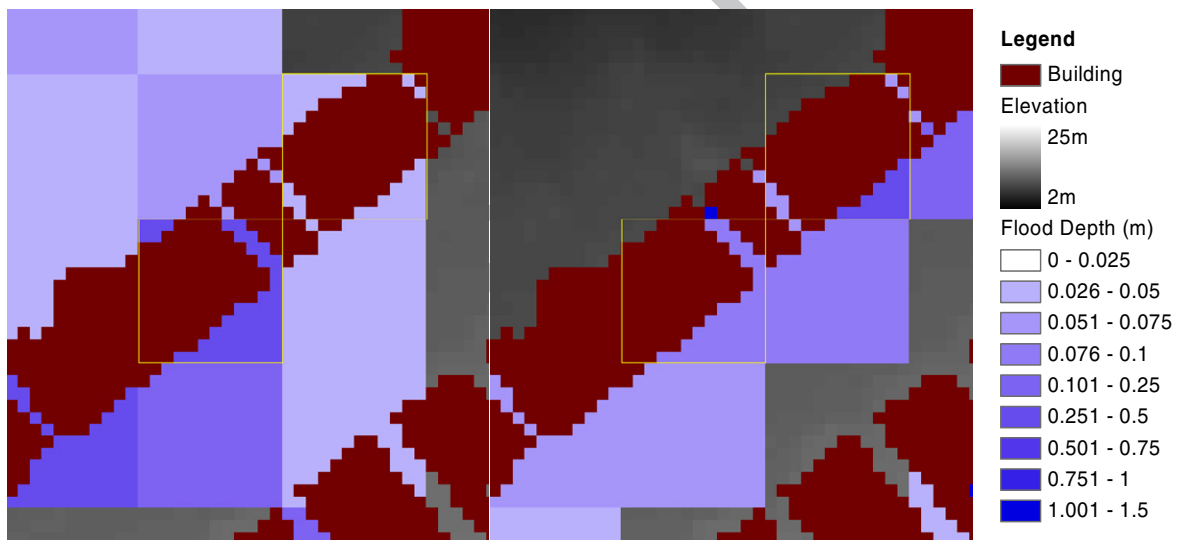
3 models of the real case study

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(a) Benchmark

(b) Averaged DEM



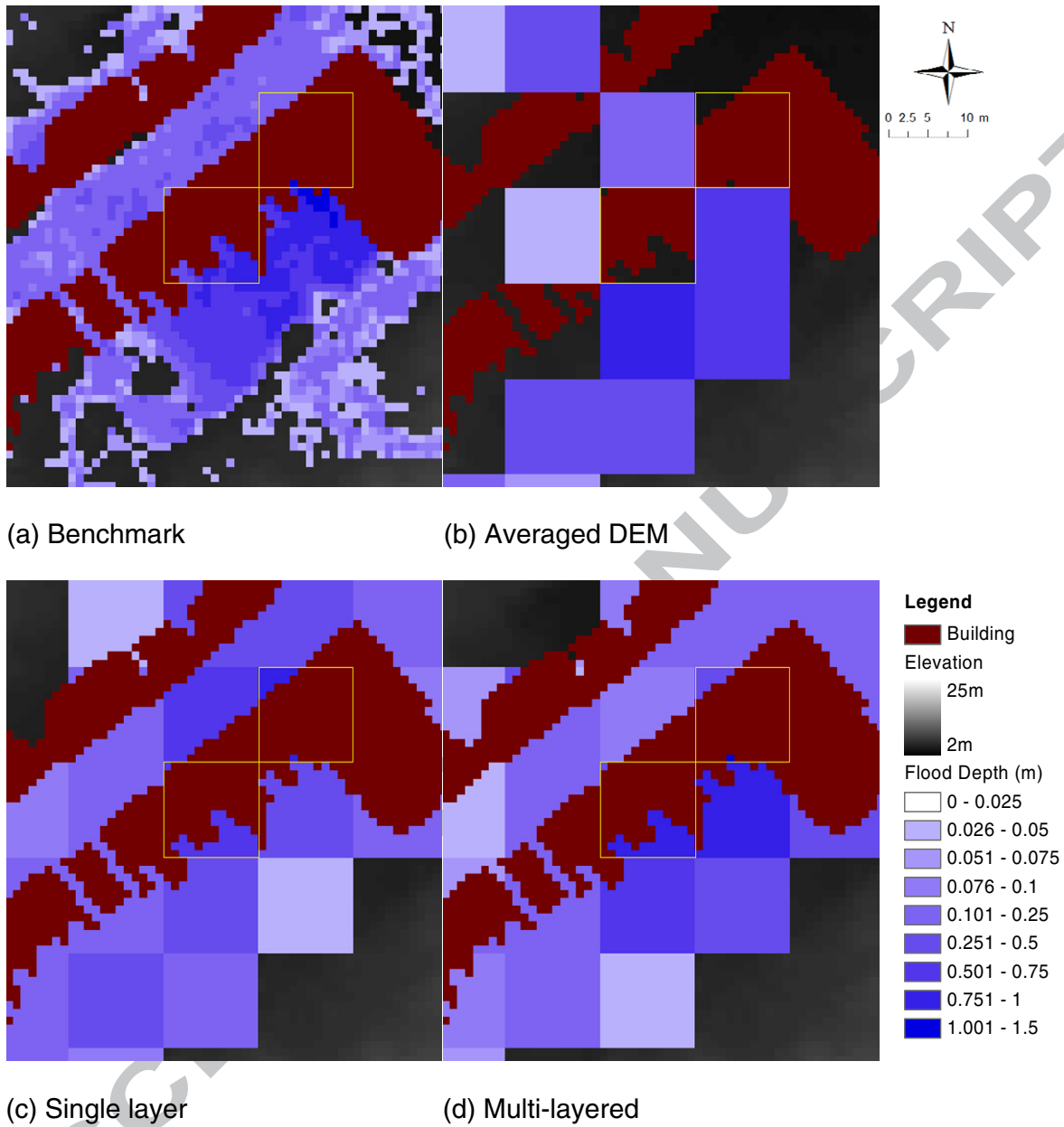
(c) Single layer

(d) Multi-layered

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3 models of in the upstream end of region A shown in Figure 13

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2 Figure 16. The maximum flood depth for the benchmark and the three grid coarsening

3 models of in the region B shown in Figure 13

1

2

3 Table 1. The RMSE for the overall domain and middle section for the synthetic case study
4 for the averaged DEM, the single layer and the multi-layered models against the benchmark

| | Averaged DEM | Single layer | Multi-layered |
|--------------------------|--------------|--------------|---------------|
| Overall domain RMSE (mm) | 38.2 | 15.0 | 6.0 |
| Middle section RMSE (mm) | 53.0 | 20.6 | 5.7 |

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1 Table 2. Model properties and computing time of the synthetic case study for the
2 benchmark, the averaged DEM, the single layer and the multi-layered models

| | Benchmark | Averaged DEM | Single layer | Multi-layered |
|-----------------|-----------|--------------|--------------|---------------|
| Grid resolution | 1m | 20m | 20m | 20m |
| No of cells | 40,000 | 100 | 100 | 106 |
| Computing time | 27,004s | 2.4s | 1.2s | 2.7s |

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3 Research Highlight

4 ➤ Multi layers are used to represent separate parts of a coarse cell bisected by
5 buildings.

6 ➤ The building coverage ratio (BCR) represents the storage area occupied by buildings.

7 ➤ The conveyance reduction factor (CRF) reflects the confined flow paths.

8 ➤ Each layer has its own BCR and CRF parameters to describe building situations.

9 ➤ The model can improve modelling accuracy with limited extra computational cost.

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