

HST hot-Jupiter transmission spectral survey: detection of potassium in WASP-31b along with a cloud deck and Rayleigh scattering

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ABSTRACT

We present *Hubble Space Telescope* optical and near-IR transmission spectra of the transiting hot-Jupiter WASP-31b. The spectrum covers 0.3–1.7 μm at a resolution $R \sim 70$, which we combine with *Spitzer* photometry to cover the full-optical to IR. The spectrum is dominated by a cloud deck with a flat transmission spectrum which is apparent at wavelengths $>0.52 \mu\text{m}$. The cloud deck is present at high altitudes and low pressures, as it covers the majority of the expected optical Na line and near-IR H₂O features. While Na I absorption is not clearly identified, the resulting spectrum does show a very strong potassium feature detected at the 4.2σ confidence level. Broadened alkali wings are not detected, indicating pressures below ~ 10 mbar. The lack of Na and strong K is the first indication of a sub-solar Na/K abundance ratio in a planetary atmosphere ($\ln[\text{Na}/\text{K}] = -3.3 \pm 2.8$), which could potentially be explained by Na condensation on the planet's night side, or primordial abundance variations. A strong Rayleigh scattering signature is detected at short wavelengths, with a 4σ significant slope. Two distinct aerosol size populations can explain the spectra, with a smaller sub-micron size grain population reaching high altitudes producing a blue Rayleigh scattering signature on top of a larger, lower lying population responsible for the flat cloud deck at longer wavelengths. We estimate that the atmospheric circulation is sufficiently strong to mix micron size particles upwards to the required 1–10 mbar pressures, necessary to explain the cloud deck. These results further confirm the importance of clouds in hot Jupiters, which can potentially dominate the overall spectra and may alter the abundances of key gaseous species.

Key words: techniques: spectroscopic – planets and satellites: atmospheres – planets and satellites: individual: WASP-31b – stars: individual: WASP-31 – planetary systems.

1 INTRODUCTION

Hot Jupiters are gas giant planets found in tight orbits around their parent stars, with a large number now known to transit their host star and are amenable to atmospheric investigations. This wide class of exoplanets span a very large range in equilibrium temperatures, with

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most planets ranging from 1000 to 3000 K depending on the albedo and efficiency of heat transfer from the day to night side. At these temperatures, theoretical models of hot Jupiters have predominately predicted atmospheres which are dominated by water opacity in the near-IR, with the optical containing alkali features and scattering by hydrogen molecules (e.g. Seager & Sasselov 2000; Sudarsky, Burrows & Hubeny 2003; Burrows et al. 2010; Fortney et al. 2010).

For highly irradiated hot-Jupiter atmospheres, the expectation of alkali metals leads to very low predicted albedos. This expectation has generally been backed up by observations, both from the detection of Na (Charbonneau et al. 2002; Redfield et al. 2008; Sing et al. 2008, 2012; Jensen et al. 2011; Huitson et al. 2012; Zhou & Bayliss 2012; Nikolov et al. 2014b) and K (Sing et al. 2011b) atoms as well as the generally low albedos found in many hot Jupiters such as HD 209458b (Rowe et al. 2008).

The atmospheric temperatures of the hot Jupiters are close to the condensation temperature of several abundant components, including silicates and iron, making clouds and hazes a natural outcome of chemistry in much the same way as abundant H₂O, CO, and CH₄ molecules in gaseous form. The possible presence of such condensation clouds was considered early on (Seager & Sasselov 2000; Hubbard et al. 2001). According to models, condensates would weaken spectral features, or mask some of them, depending on the height of the cloud deck (Marley et al. 1999; Sudarsky et al. 2003; Fortney 2005). There is a growing body of evidence for substantial clouds and hazes in hot Jupiters, including the transmission spectra of HD 189733b WASP-12b, HAT-P-32b, and WASP-6b (Sing et al. 2011a, 2013; Gibson et al. 2013; Jordan et al. 2013; Pont et al. 2013; Nikolov et al. 2014a).

Here, we present results for WASP-31b from a large *Hubble Space Telescope* (*HST*) programme (*HST* GO-12473; P.I. Sing), consisting of an eight planet optical atmospheric survey of transiting hot Jupiters. The overall programme goals are to detect atmospheric features across a wide range of hot-Jupiter atmospheres enabling comparative exoplanetology, detect stratosphere causing agents like TiO (Hubeny, Burrows & Sudarsky 2003; Fortney et al. 2008), and detect alkali atoms as well as hazes and clouds. In the results reported so far for this survey, Huitson et al. (2013) detected H₂O in WASP-19b and found TiO was unlikely. Water was also found in HAT-P-1b (Wakeford et al. 2013) with the broad-band spectrum also showing Na I and a significant optical absorber but no K I absorption (Nikolov et al. 2014b). Finally, TiO was ruled out in the very hot planet WASP-12b and the atmosphere was found to be dominated by aerosols, with corundum a possible candidate that is particularly relevant given its high condensation temperature applicable to this very hot Jupiter (Sing et al. 2013).

WASP-31b was discovered by Anderson et al. (2011) as part of the Wide Angle Search for Planets survey. With a low mass ($0.46 M_{\text{Jup}}$) and large inflated radius ($1.55 R_{\text{Jup}}$) the planet is of particular interest to atmospheric studies as it has a very low density ($\rho_{\text{pl}} = 0.129 \rho_{\text{Jup}}$) and correspondingly low surface gravity of 4.56 m s^{-1} making the planet very favourable to transmission spectroscopy. The exoplanet orbits at 0.047 au around a F6V 6300 K low metallicity ([Fe/H] = -0.19) low activity 3–5 Gyr star, and has a nominal (zero albedo, full recirculation) equilibrium temperature of 1570 K (Anderson et al. 2011). In this paper, we present new *HST* transit observations with the Space Telescope Imaging Spectrograph (STIS) and Wide Field Camera 3 (WFC3) in spatial scanning mode, combining them with *Spitzer* photometry to construct a high signal-to-noise (S/N) near-UV to infrared transmission spectrum of WASP-31b, capable of detecting and scrutinizing atmospheric constituents. We describe our observations in Section 2,

present the analysis of the transit light curves in Section 3, discuss the results in Section 4 and conclude in Section 5.

2 OBSERVATIONS

2.1 *HST* STIS spectroscopy

The overall observational strategy for WASP-31b is nearly identical for each of the eight targets in the large *HST* programme, including the WASP-19b, HAT-P-1b, and WASP-12b which have been published in Huitson et al. (2013), Wakeford et al. (2013), Nikolov et al. (2014b) and Sing et al. (2013).

We observed two transits of WASP-31b with the *HST* STIS G430L grating during 2012 June 13 and 26, as well as one transit with the STIS G750L during 2012 July 10. The G430L and G750L data sets each contain 43 spectra, which span five spacecraft orbits. The G430L grating covers the wavelength range from 2900 to 5700 Å, with a resolution R of $\lambda/\Delta\lambda = 530\text{--}1040$ (~ 2 pixels; 5.5 Å). The G750L grating covers the wavelength range from 5240 to 10 270 Å, with a $R = 530\text{--}1040$ (~ 2 pixels; 9.8 Å). Both the STIS data were taken with a wide 52 arcsec \times 2 arcsec slit to minimize slit light losses. The visits of *HST* were scheduled such that the third and fourth spacecraft orbits contain the transit, providing good coverage between second and third contact, as well as an out-of-transit baseline time series before and after the transit. Exposure times of 279 s were used in conjunction with a 128-pixel wide sub-array, which reduces the readout time between exposures to 21 s, providing a 93 per cent overall duty cycle.

The data set was pipeline-reduced with the latest version of CALSTIS, and cleaned for cosmic ray detections with a customized procedure based on median-combining difference images following Nikolov et al. (2014b). The G750L data set was defringed using contemporaneous fringe flats. The mid-time of each exposure was converted into BJD_{TBD} for use in the transit light curves (Eastman, Siverd & Gaudi 2010).

The spectral aperture extraction was done with IRAF using a 13-pixel-wide aperture with no background subtraction, which minimizes the out-of-transit standard deviation of the white-light curves. The extracted spectra were then Doppler-corrected to a common rest frame through cross-correlation, which helped remove sub-pixel wavelength shifts in the dispersion direction. The STIS spectra were then used to create both a white-light photometric time series (see Fig. 1), and custom wavelength bands covering the spectra, integrating the appropriate wavelength flux from each exposure for different bandpasses.

Like the other targets in our *HST* programme, the STIS light curves of WASP-31 show instrument-related systematic effects primarily due to the well-known thermal breathing of *HST*, which warms and cools the telescope during the 96 min day/night orbital cycle, causing the focus to vary. The first exposure of each spacecraft orbit has also consistently been found to show significantly lower fluxes than the remaining exposures. Similar to our previous STIS analysis (Huitson et al. 2013; Sing et al. 2013; Nikolov et al. 2014b), we intended to discard the entire first orbit to minimize the effect of the breathing trend, but found for two of the three *HST* visits, a few of the exposures taken towards the end of the first orbit could be used in the analysis and fit with the same systematics model as used for the subsequent orbits. In addition, we set the exposure time of the first image of each spacecraft orbit to be 1 s in duration, such that it could be discarded without significant loss in observing time. We find that the second exposures taken for all five spacecraft orbits (each 279 s in duration) do not in general

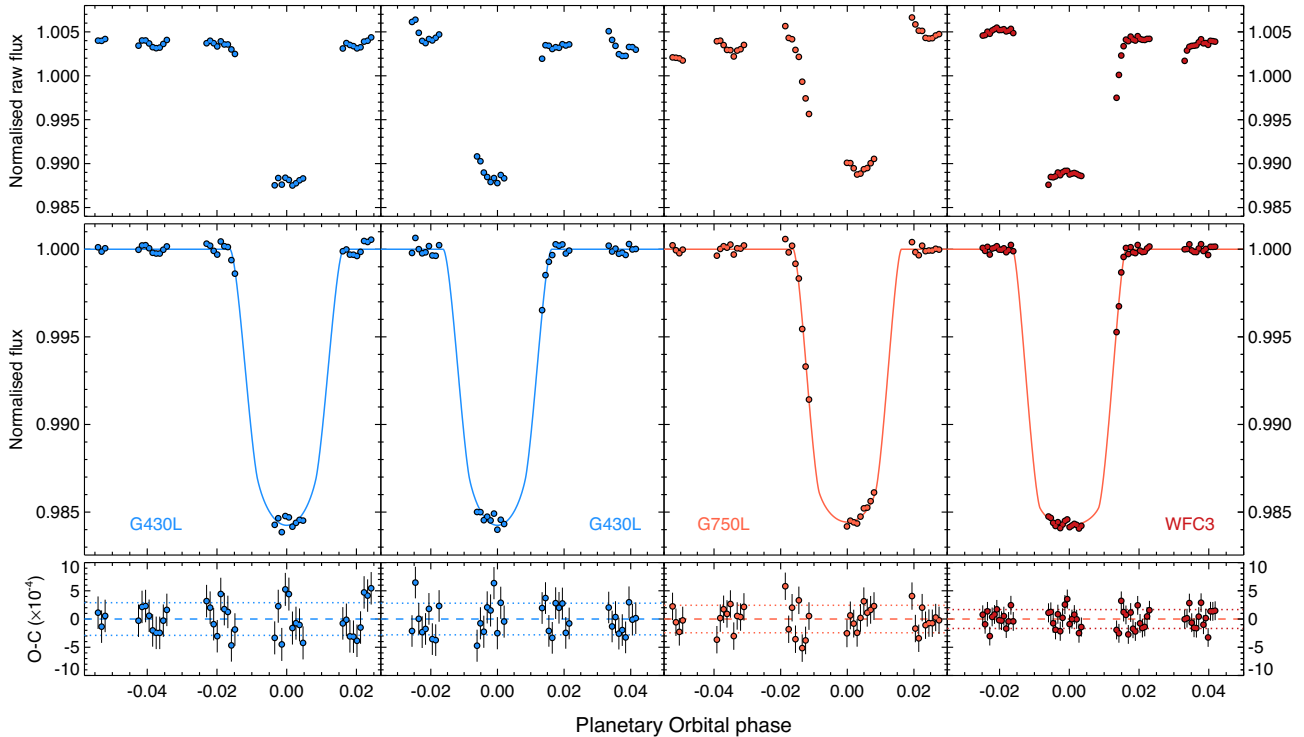


Figure 1. *HST* STIS normalized white-light curves for the three WASP-31b transits taken with the STIS G430L, STIS G750L, and WFC3. Top panels: raw light curves normalized to the mean out-of-transit raw flux. Middle panels: detrended light curves along with the best-fitting limb-darkened transit model superimposed with continuous lines. Lower panels: observed minus modelled light-curve residuals, compared to a null (dashed lines) and 1σ level (dotted lines).

show the first-exposure systematic trend, with an exception of the third orbit of the *G750L* light curve. Upon analysing several targets from the large *HST* programme, the 1-s strategy to avoid the faint exposure systematic appears to have mixed results. For both WASP-19b, WASP-12b, and here for WASP-31b the second exposures of each spacecraft orbit do not generally show the first-exposure trend as intended, though the exposures of HAT-P-1b were still affected. Though the 1-s strategy may not always be effective, especially for brighter targets, it still appears to be a recommended practice for STIS programmes requiring high photometric accuracy and long exposures as it can often save useful observing time as was usually the case here.

2.2 *HST* WFC3 spectroscopy

In addition to the STIS data, observations of WASP-31b were also conducted in the infrared with WFC3 on the *HST*. Observations began on 2012 May 13 at 12:53 using the IR *G141* grism in forward spatial scan mode over five *HST* orbits. The spacial scanning is done by slewing the telescope in the cross-dispersion direction during integration in a similar manner for each exposure, which increases the duty cycle and greatly increases the number of counts obtained per exposure. We used a 256×256 pixel subarray with the SPARS25 NSAMP = 8 readout sequence, which gives exposure times of 134.35 s. Our observations were conducted with a spatial scan rate of ~ 0.15 pixels s^{-1} , where 1 pixel = 0.13 arcsec, with the final spatially scanned spectrum spanning ~ 20 pixels. The *G141* grism images contain only the first-order spectrum, which spans 143 pixels with a dispersion of 4.63 nm pixel $^{-1}$ in the direction of the *x*-axis. The resultant spectra have average count rates of about 3.8×10^4 electrons pixel $^{-1}$.

We used the ‘*ima*’ outputs from the CALWFC3 pipeline. For each exposure, *CALWFC3* conducts the following processes: reference pixel subtraction, zero-read and dark current subtraction, and a non-linearity correction; the resultant images are in units of electrons per second. For the spectral extraction, we trimmed a 152×80 box around each spectral image and the spectra were extracted using custom IDL routines, similar to IRAF’s APALL procedure, with an aperture of ± 12 pixels determined by minimizing the standard deviation of the fitted white-light curve. The aperture is traced around a computed centring profile, which was found to be consistent in the *y*-axis with an error of 0.06 pixels. Background subtraction was applied using a clean region of the untrimmed image, with background accounting for 0.4 per cent of the total flux measured in each wavelength column. Subsequent data analysis was conducted with the first orbit removed (16 exposures), as it suffers from significant thermal breathing systematic effects similar to the STIS data.

For wavelength calibration, direct images were taken in the *F139M* narrow-band filter at the beginning of the observations. We assumed that all pixels in the same column have the same effective wavelength, as the spatial scan varied in the *x*-axis direction by less than one pixel, resulting in a spectral range from 1.1 to 1.7 μm . This wavelength range is later restricted for the spectroscopic light curve fits as the strongly sloped edges of the grism response result in much lower S/N light curves.

2.3 *Spitzer* IRAC photometry

We analyse two transit observations obtained using the Infrared Array Camera (IRAC) instrument (Programme 90092 with P.I. Desert) on the *Spitzer space telescope* in the 3.6 μm and 4.5 μm channels in subarray mode (32×32 pixel, or 39 centred on the planets host). The

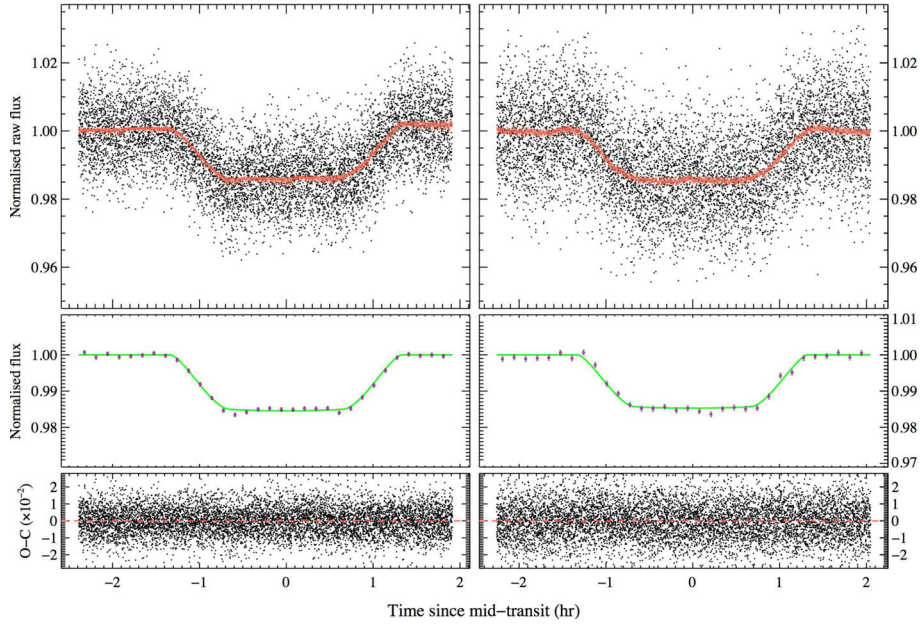


Figure 2. *Spitzer* photometry of WASP-31b for the (left) 3.6 μm and (right) 4.5 μm channels. Plotted is the raw flux along with the best fitting transit model including systematic effects (top), the flux corrected for detector trends and binned by 8 min (middle), and residuals (bottom).

3.6 μm observation was performed on UT 2013 March 9 (between 06:59 and 11:37) and the 4.5 observation was performed on UT 2013 March 19 (between 12:19 and 16:58), each transit containing 8320 images (see Fig. 2).

Photometry was extracted from the basic calibrated data files. These images are stacked in FITS data cubes, containing 64 exposures taken in a sequence which were produced by the IRAC pipeline (version S19.1.0) after dark subtraction, flat-fielding, linearization, and flux calibration. Both observations have effective integration times of 1.92 s per image.

We converted the images to photon counts (i.e. electrons) by multiplying the images by the gain and individual exposure times (FITS HEADER key words SAMPTIME and GAIN) and dividing by the flux conversion factor (FLUXCONV). Timing of each image was computed using the UTC-based Barycentric Julian Date (BJD_{UTC}) from the FITS header keyword BMJD_OBS, transforming these time stamps into BJD based on the BJD terrestrial time standard (Eastman et al. 2010). Both channels show a strong ramp feature at the beginning of the data, and we elected to trim the first 22 min of data to allow the detector to stabilize.

We performed outlier filtering for hot (energetic) or cold (low-count values) pixels in the data by examining the time series of each pixel. This task was performed in two passes, first flagging all pixels with intensity 8σ or more away from the median value computed for each frame from the 10 surrounding images. The values of these flagged pixels were replaced with the local median value. In the second pass, we flagged and replaced outliers above the 4σ level, following the same procedure. The total fraction of corrected pixels was 0.26 per cent for the 3.6 μm and 0.07 per cent for the 4.5 μm .

We estimated and subtracted the background flux from each image of the time series. To do this, we performed an iterative 3σ outlier clipping for each image to remove the pixels with values associated with the stellar point spread function (PSF), background stars or hot pixels, created a histogram from the remaining pixels, and fitted a Gaussian to determine the sky background.

We measured the position of the star on the detector in each image incorporating the flux-weighted centroiding method¹ using the background subtracted pixels from each image for a circular region with radius 3 pixels centred on the approximate position of the star. While we could perform PSF centroiding using alternative methods such as fitting a two-dimensional Gaussian function to the stellar image, previous experiences with warm *Spitzer* photometry showed that the flux-weighted centroiding method is either equivalent or superior (Beerer et al. 2011; Knutson et al. 2012; Lewis et al. 2013). The variation of the x and y positions of the stellar PSF on the detector were 0.17 and 0.18 pixels for the 3.6 μm channel and 0.76 and 0.24 pixels for the 4.5 μm channel.

We extract photometric measurements from our data following two methods. First, aperture photometry was performed with IDL routine *aper* using circular apertures ranging in radius from 1.5 to 3.5 pixels in increments of 0.1. The best result was selected by measuring the flux scatter of the out-of-transit portion of the light curves for both channels after filtering the data for 5σ outliers with a width of 20 data points.

In addition, we also performed photometry with a time-variable aperture, adjusting the size of the aperture for each image with the noise pixel parameter (Mighell 2005; Knutson et al. 2012), which is described in section 2.2.2 of the IRAC instrument handbook and has been used in previous exoplanet studies to improve the results of warm *Spitzer* photometry (e.g. Knutson et al. 2012; O’Rourke et al. 2014). The noise pixel parameter is proportional to the FWHM of the stellar PSF squared (Mighell 2005) and is defined as

$$\tilde{\beta} = \frac{(\sum_i I_i)^2}{\sum_i I_i^2}, \quad (1)$$

¹ As implemented in the IDL centroider.pro, provided on the *Spitzer* homepage.

where I_i is the intensity detected by the i th pixel. We use each image to measure the noise pixel value, applying an aperture with a radius 4 pixels, ensuring that each pixel is considered if the border of the aperture crosses that pixel. We extracted source fluxes from both channel time series for aperture radii, r , following the relation:

$$r = \sqrt{\beta a_0 + a_1}, \quad (2)$$

where a_0 and a_1 were, respectively, varied in the ranges 0.8 to 1.2 and -0.4 to $+0.4$ with a step size of 0.1.

2.4 Photometric monitoring for stellar activity

We obtained nightly photometry of WASP-31 to monitor and characterize the stellar activity over the past three observing seasons with the Tennessee State University Celestron 14-inch (C14) Automated Imaging Telescope (AIT) located at Fairborn Observatory in Arizona (see e.g. Henry 1999; Eaton, Henry & Fekel 2003). The AIT uses an SBIG STL-1001E CCD camera and exposes through a Cousins R filter. Each nightly observation consisted of 4–10 consecutive exposures on WASP-31 and several comparison stars in the same field of view. The individual nightly frames were co-added and reduced to differential magnitudes in the sense WASP-31 minus the mean brightness of six constant comparison stars. Each nightly observation has been corrected for bias, flat-fielding, pier-side offset, and for differential atmospheric extinction.

A total of 227 successful nightly observations (excluding a few isolated transit observations) were collected between 2011 October 31 and 2014 January 28. The individual observations are plotted in the top panel of Fig. 3 and summarized in Table 1. The standard deviations of single observations, with respect to their corresponding seasonal means, range between 0.0031 and 0.0038 mag for the three observing seasons (Table 1; column 4). This is near the limit of our measurement precision with the C14, as determined from the constant comparison stars in the field. The seasonal means given in column 5 agree to within a standard deviation of only 0.001 mag. Since we do not standardize the ensemble differential magnitudes, this is probably consistent with the absence of year-to-year variability.

We performed a periodogram analysis of the composite data set in the top panel of Fig. 3 after first normalizing the data by translating the second and third observing seasons to have the same mean as the first season. To first order, this removes low-amplitude, long-term variability in WASP-31 or the comparison stars as well as any uncorrected year-to-year systematic errors. A frequency spectrum of the normalized data set, computed as the reduction in variance of the data versus trial frequency, is plotted in the middle panel of Fig. 3. Trial frequencies ranged between 0.005 and 0.95 c/d, corresponding to a period range between 1 and 200 d. The result suggests low-amplitude brightness variability with a period of 8.6 ± 0.1 d. This is consistent with the stellar rotation period of 7.9 ± 0.7 d predicted by Anderson et al. (2011) from their observed $v \sin i$ and computed stellar radius R_* . Therefore, we take 8.6 d as the stellar rotation period made visible by rotational modulation in the visibility of weak surface features.

The three-year normalized data set is plotted in the bottom panel of Fig. 3, phased to the rotation period of 8.6 d. A least-squares sine fit gives a peak-to-peak amplitude of 0.0031 ± 0.0006 mag. Thus, while we find probable low-amplitude rotational modulation in stellar brightness, we find no evidence for significant variability above the noise at or near the planetary orbital period (corresponding to a frequency of 0.2936 c/d in Fig. 1). A least-squares sine fit of the

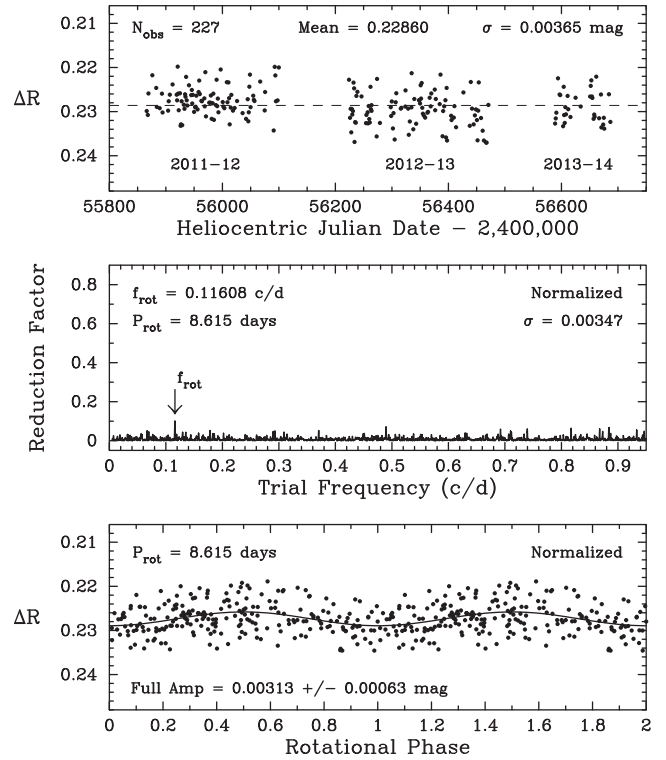


Figure 3. Top: the composite nightly Cousins R -band photometric data set of WASP-31 from the 2011–2012, 2012–2013, and 2013–2014 observing seasons, acquired with the C14 AIT at Fairborn Observatory. The data within each observing season scatter from night to night with a standard deviation between 0.003 and 0.004 mag. This is the approximate limit of our measurement precision. The scatter of the yearly means is only 0.001 mag. Middle: the frequency spectrum of the composite data set, normalized to the first seasonal mean, suggests low-amplitude variability at about 8.6 d. Bottom: the normalized data set phased to the 8.6 d period, which we interpret as the stellar rotation period. A least-squares sine fit to the 8.6-d rotation period gives a peak-to-peak amplitude of 0.003 mag.

Table 1. Summary of WASP-31 AIT photometric observations.

Observing season	N_{obs}	Date range HJD–2400000	Sigma (mag)	Seasonal mean (mag)
2011–2012	95	55866–56099	0.003 16	$0.227\ 30 \pm 0.000\ 32$
2012–2013	98	56224–56470	0.003 79	$0.229\ 74 \pm 0.000\ 38$
2013–2014	34	56589–56686	0.003 45	$0.228\ 93 \pm 0.000\ 59$

normalized data to the orbital period gives a peak-to-peak amplitude of only 0.0014 ± 0.0006 mag. Since the 8.6-d stellar rotation period and the 3.4-d planetary orbital period are well separated, the radial velocity variations are clearly due to planetary reflex motion with very little jitter caused by surface activity (e.g. Queloz et al. 2001; Paulson et al. 2004).

In addition, we also measure a low stellar activity for WASP-31 as determined by the Ca II H & K lines, where we find an activity index of $\log(R'_{\text{HK}}) = -5.4$ using archival High Accuracy Radial Velocity Planet Searcher (HARPS) spectra.

From equation 5 of Sing et al. (2011a), activity levels of 0.0031 mag limits the effects of the photometric variability on the measured planet-to-star radius contrast to $0.000\ 18 R_p/R_*$. With low levels of stellar activity, we conclude their effects on measuring WASP-31b's transmission spectrum are minimal. A low-activity star in this case is particularly advantageous for transmission

spectroscopy, as it minimizes or eliminates any potential uncertainty in the interpretation of the transmission spectrum across the spectral regime and from different data sets and epochs.

3 ANALYSIS

3.0.1 STIS white-light curve fits

Our overall analysis methods are similar to the *HST* analysis of Sing et al. (2011a, 2013), Huitson et al. (2013) and Nikolov et al. (2014b), which we also describe briefly here. The light curves were modelled with the analytical transit models of Mandel & Agol (2002). For the white-light curves, the central transit time, inclination, stellar density, planet-to-star radius contrast, stellar baseline flux, and instrument systematic trends were fit simultaneously, with flat priors assumed. The period was initially fixed to a literature value, before being updated, with our final fits adopting the value from Section 3.1. Both *G430L* transits were fit simultaneously with a common inclination, stellar density, and planet-to-star radius contrast. The results from the *G430L* and *G750L* white-light curve fits were then used in conjunction with literature results to refine the orbital ephemeris and overall planetary system properties (see Section 3.1).

To account for the effects of limb-darkening on the transit light curve, we adopted the four parameter non-linear limb-darkening law, calculating the coefficients with ATLAS stellar models ($T_{\text{eff}} = 6250$, $\log g = 4.5$, $[\text{Fe}/\text{H}] = -0.2$) following Sing (2010). Varying the stellar model within the known parameter range has a negligible effect on the output limb-darkening coefficients and fit transit parameters.

As in our past STIS studies, we applied orbit-to-orbit flux corrections by fitting for a fourth-order polynomial to the photometric time series, phased on the *HST* orbital period. The systematic trends were fit simultaneously with the transit parameters in the fit. Higher order polynomial fits were not statistically justified, based upon the Bayesian information criteria (BIC; Schwarz 1978). The baseline flux level of each visit was let free to vary in time linearly, described by two fit parameters. In addition, for the *G750L* we found it justified by the BIC to also linearly fit for two further systematic trends which correlated with the x and y detector positions of the spectra, as determined from a linear spectral trace in *IRAF*.

The errors on each data point were initially set to the pipeline values, which is dominated by photon noise but also includes readout noise. The best-fitting parameters were determined simultaneously with a Levenberg–Marquardt least-squares algorithm (Markwardt 2009) using the unbinned data. After the initial fits, the uncertainties for each data point were rescaled based on the standard deviation of the residuals and any measured systematic errors correlated in time (‘red noise’), thus taking into account any underestimated errors in the data points.

The red noise was measured by checking whether the binned residuals followed a $N^{-1/2}$ relation, when binning in time by N points. In the presence of red noise, the variance can be modelled to follow a $\sigma^2 = \sigma_w^2/N + \sigma_r^2$ relation, where σ_w is the uncorrelated white noise component, and σ_r characterizes the red noise (Pont, Zucker & Queloz 2006). We find that the pipeline per-exposure errors are accurate at small wavelength bin sizes, which are dominated by photon noise, but are in general somewhat underestimated at larger bin sizes. For the *G750L* white-light curve we find our light curve precision achieves $1.3 \times$ the photon noise value with the scatter of the residuals measured at 201 ppm, while the *G430L* achieves 1.6 times the photon noise value with the residual scatter

276 ppm. We do not find any evidence for remaining systematic errors, as both *G430L* STIS white-light curves as well as the *G750L* curve give $\sigma_r = 0$. A few deviant points were cut at the 3σ level in the residuals.

The uncertainties on the fitted parameters were calculated using the covariance matrix from the Levenberg–Marquardt algorithm, which assumes that the probability space around the best-fitting solution is well described by a multivariate Gaussian distribution. Previous analyses of other *HST* transit observations (Berta et al. 2012; Line et al. 2013; Sing et al. 2013; Knutson et al. 2014b; Nikolov et al. 2014b) have found this to be a reasonable approximation. We then compared these uncertainties to the results of an MCMC analysis (Eastman, Gaudi & Agol 2013), which does not assume any functional form for this probability distribution. In each case, we found equivalent results between the MCMC and the Levenberg–Marquardt algorithm for both the fitted parameters and their uncertainties. Inspection of the 2D probability distributions from both methods indicate that there are no significant correlations between the systematic trend parameters and the planet-to-star radius contrast.

3.0.2 WFC3 white-light curve fits

WFC3 is now being used extensively for transiting exoplanet work (Berta et al. 2012; Gibson et al. 2012; Deming et al. 2013; Huitson et al. 2013; Mandell et al. 2013; Swain et al. 2013; Wakeford et al. 2013; Knutson et al. 2014a; Kreidberg et al. 2014). The data quality appears mainly affected by detector persistence, which causes a ramp-effect at high count levels and *HST* thermal-breathing variations. Thus far, parametrized methods and various common-mode techniques have been employed to handle the systematics, which largely appear repeatable orbit-to-orbit.

Our WFC3 white-light curve transit shows small intra-orbit and orbit-to-orbit trends (see Fig. 1). We fit for the systematics errors similarly as the STIS data, adopting a fourth-order polynomial of the *HST* orbital phase, a baseline flux allowed to vary linearly in time, and a first-order shift along the y -axis detector position as measured through cross-correlation. We found similar transit depths with the divide-OOT method (Berta et al. 2012) but found larger overall noise properties, with the BIC favouring the parametrized method ($\Delta\text{BIC} = 27$, see Fig. 4).

We find our white-light curve precision achieves about 1.47 times the photon noise value with the scatter of the residuals measured at 157 ppm. There is no evidence for remaining systematic errors, as we estimate a value of $\sigma_r = 0$ from the binning technique. With these precision levels, the near-IR transit depth is measured to about a 53 ppm accuracy.

3.0.3 Spitzer light curve fits

We analyse the $3.6 \mu\text{m}$ and $4.5 \mu\text{m}$ channel light curves following standard procedures for warm *Spitzer*. First, we normalize the light curves in flux so that the out-of transit data are equal to unity. We employ the analytical transit models of Mandel & Agol (2002) adopting the non-linear limb-darkening law computed for the spectroscopic stellar parameters of the target (see Table 2). To correct the *Spitzer* systematic effects, we used a parametric model of the form

$$f(t) = a_0 + a_1x + a_2x^2 + a_3y + a_4y^2 + a_5xy + a_6t, \quad (3)$$

where $f(t)$ is the stellar flux as a function of time, x and y are the positions of the stellar centroid on the detector, t is time and a_0 to a_6

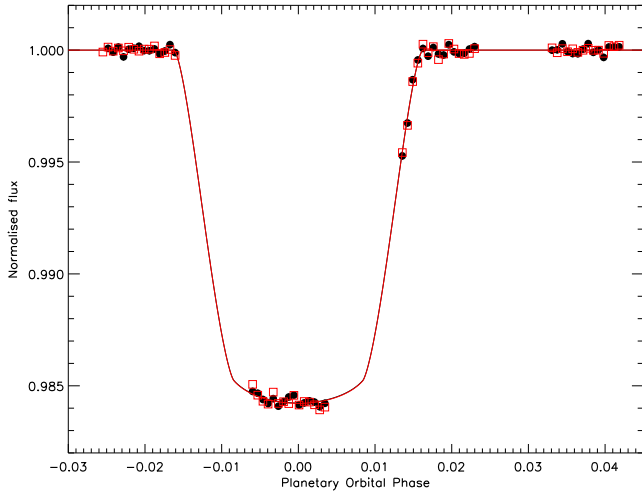


Figure 4. *HST* WFC3 detrended white-light curves along with the best-fitting limb-darkened transit models for the cases of detrending with a polynomial of the *HST* orbital phase (black circles) and the divide-OOT method (red squares). The vertical extent of the plotted symbols reflects the flux uncertainty.

Table 2. Transit timing for WASP-31b.

Epoc	BJD _{TBD}	BJD error	Notes
-200	2455192.6895	0.0003	Anderson et al. (2011)
-84	2455587.7719	0.0014	Dragomir et al. (2011)
55	2456061.19042	0.000 49	<i>HST</i> WFC3
68	2456105.46683	0.000 37	<i>HST</i> G430L
72	2456119.08991	0.000 41	<i>HST</i> G750L
143	2456360.90835	0.000 32	<i>Spitzer</i> 3.5 μm
146	2456371.12637	0.000 43	<i>Spitzer</i> 4.6 μm

are the free parameters in the fit (Désert et al. 2009; Todorov et al. 2013). Inclusion of the quadratic and cross-position terms were justified by the BIC ($\Delta\text{BIC} = 69$). Our results are not sensitive to the inclusion of the cross-term a_5xy , though it did help to reduce the correlated noise in channel 2.

The fits using both the time-variable and constant aperture methods examined were examined, including the root-mean-square residual after fitting the light curves from each channel as well as the white and red noise components measured using the wavelet method (Carter & Winn 2009). We found the 3.6 μm channel favoured the time-variable aperture while the 4.5 μm channel favoured a constant aperture (see Fig. 2), with both methods giving consistent transit depths for each channel. To compare with the *HST* transmission spectra, we set the transit ephemeris and system parameters to the values found in Section 3.1 and re-fit the light curves. We find residual red noise in both channels, which is comparable to the binned white noise on the transit-duration time-scale. We estimate values for σ_r of 212 and 346 ppm for channels 1 and 2, respectively, using either the binning or wavelet techniques, which we account for in the final quoted error bars.

3.1 System parameters and transit ephemeris

We used the central transit times of the *HST* and *Spitzer* data along with the transit times of Anderson et al. (2011) and Dragomir et al.

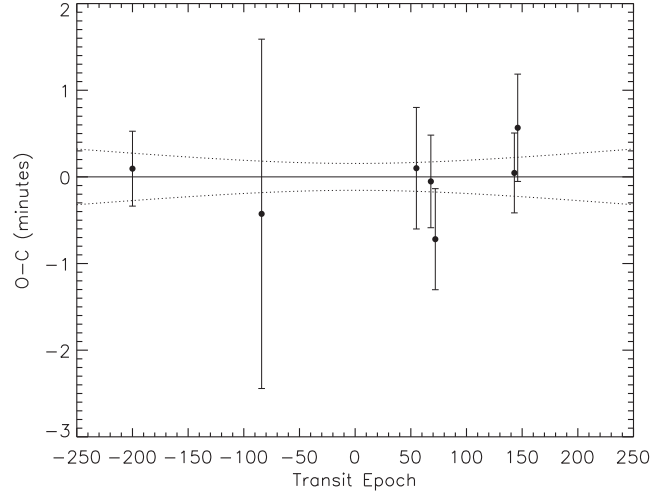


Figure 5. O–C diagram for the transit times of WASP-31 using the transits listed in Table 2 and a linear ephemeris. The 1σ error envelope on the ephemeris is plotted as the dotted lines.

(2011) to determine an updated transit ephemeris. The transit times are listed in Table 2, shown in Fig. 5 and fit with a linear function of the period P and transit epoch E ,

$$T(E) = T(0) + EP. \quad (4)$$

We find a period of $P = 3.405\,886\,00 \pm 0.000\,000\,78$ (d) and a mid-transit time of $T(0) = 2455873.86662 \pm 0.00011$ (BJD). A fit with a linear ephemeris is a good fit to the data, having a χ^2 of 2.5 for 5 degrees of freedom (dof).

We also refined the transit parameters for the inclination, i , and stellar density, ρ_* , using the white-light curve fits of the *G750L* and *G430L*, in conjunction with the two *Spitzer* light curves and the values of Anderson et al. (2011). Given that all our measurements were highly consistent (within the errors) with both each other and with those of Anderson et al. (2011), we computed the weighted mean value of both the inclination, semimajor axis to stellar radius ratio, and the stellar density finding values of $i = 84.67 \pm 0.11$, $a/R_* = 8.19 \pm 0.10$, and $\rho_* = 0.895 \pm 0.033$ (cgs), respectively.

3.2 Transmission spectrum fits

We extracted various wavelength bins for the STIS *G430L*, *G750L*, and WFC3 *G141* spectra, to create a broad-band transmission spectrum and search for the expected narrow-band Na and K features (see Figs 6–9). In these transit fits, we fixed the transit ephemeris, inclination, and stellar density to the results from Section 3.1. The parameter R_p/R_* was allowed to fit freely, as well as the baseline flux and model parameters describing the instrument systematic trends. The limb-darkening parameters were fixed to the model values, with the four non-linear coefficients for each bin individually calculated from the stellar model, taking into account the instrument response (see Table 3). Given our overall lack of ingress or egress data, we were not able to perform a sensitive test of the stellar limb-darkening as was done on WASP-12A (Sing et al. 2013).

As done for WASP-12b (Sing et al. 2013), we handled the modelling of systematic errors in the spectral bins by two methods. We allowed each light curve to be fit independently with a parametrized model and also separately fit the spectral bins by removing common-mode trends from each spectral bin, before fitting for residual trends with a parametrized model containing fewer free parameters. For

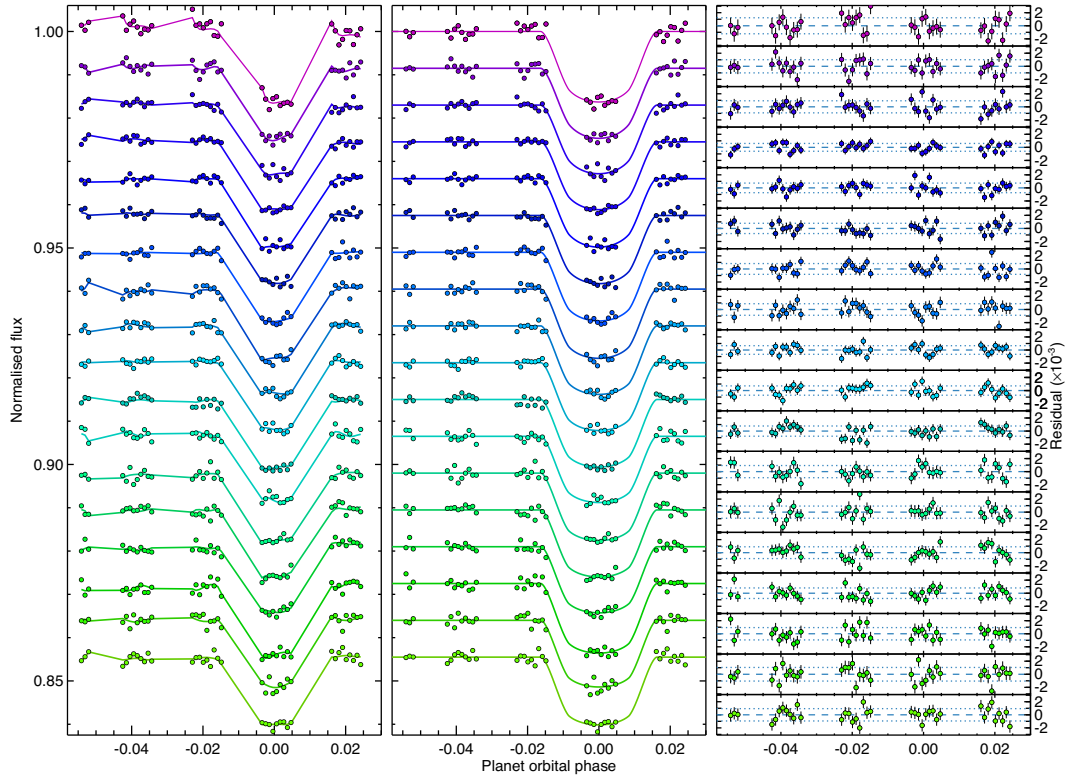


Figure 6. *HST* STIS *G430L* spectral bin transit light curves for visit 15. Left: light curves for the *HST* STIS *G430L* spectral bins with the common-mode trends removed, overplotted with the best-fitting systematics model. The points have been offset in relative flux, and systematics model plotted with connecting lines for clarity purposes. The light curves are ordered in wavelength, with the shortest wavelength bin shown at the top and longest wavelength bin at the bottom. Middle: light curves fully corrected for systematic errors, with the best-fitting joint transit model over-plotted. Right: residuals plotted with 1σ error bars along with the standard deviation (dotted lines).

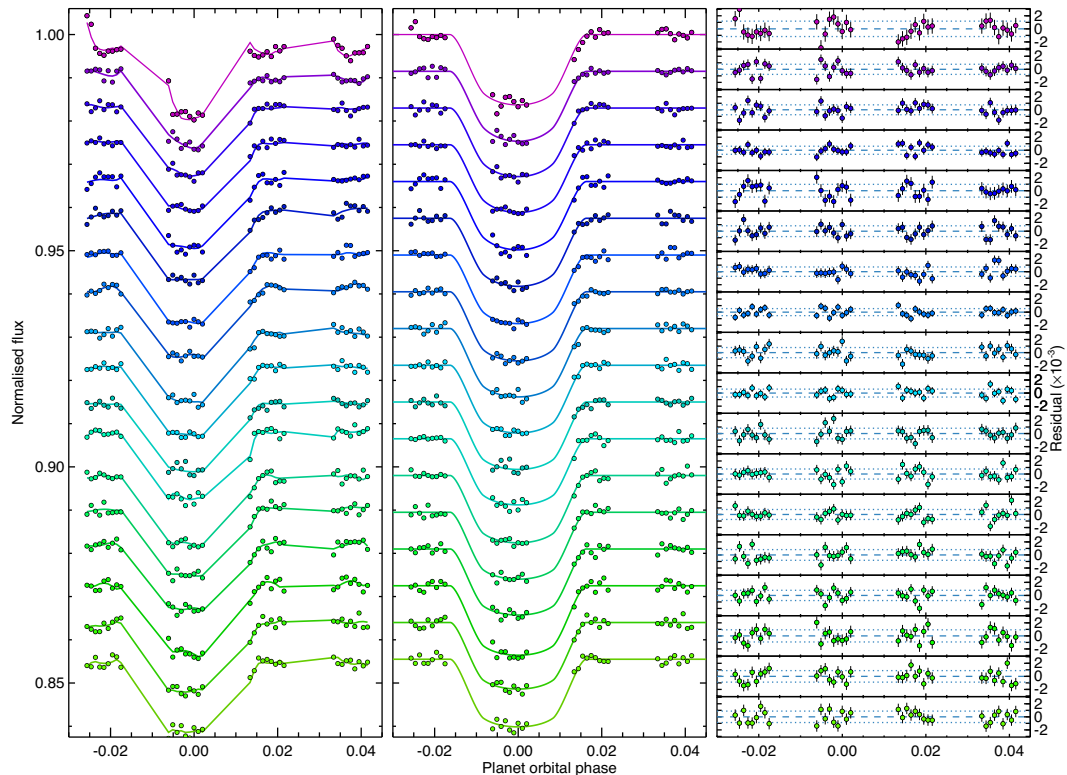


Figure 7. The same as Fig. 6, but for the *G430L* spectral bins of visit 16.

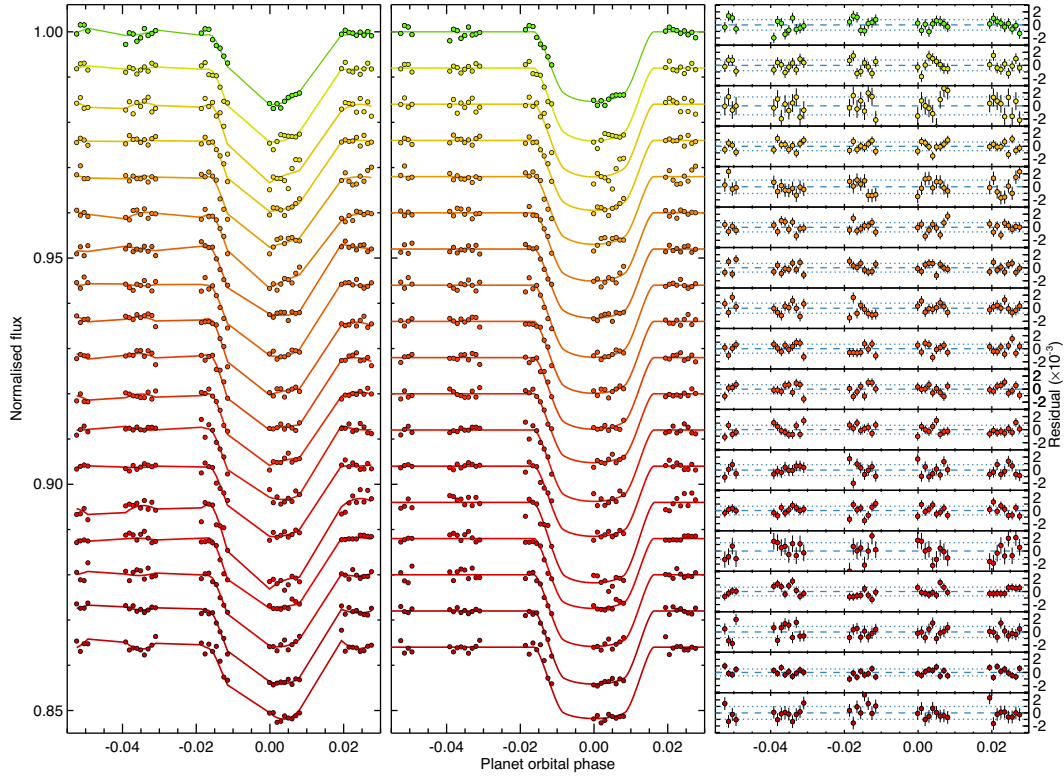


Figure 8. The same as Fig. 6, but for the *G750L* spectral bins.

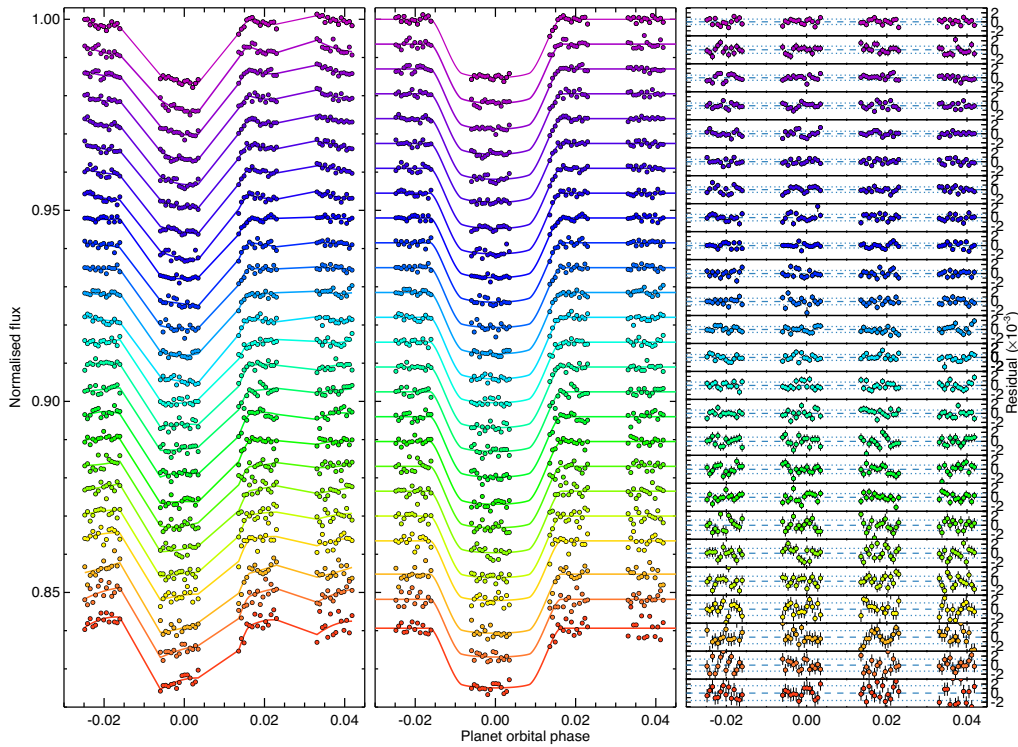


Figure 9. The same as Fig. 6, but for the WFC3 *G141* spectral bins.

both the STIS and WFC3, removing the common trends significantly reduces the amplitude of the observed systematics, as these trends are observed to be similar wavelength-to-wavelength across a detector. The two methods give very similar results, though we

choose the common-mode method to quote our subsequent results as it produces slightly higher overall S/N with more dof. The ΔBIC values are on average lower for the common-mode method by 10.5 for the *G430L* light curves, 13.1 for *G750L* light curves, and 25.7

Table 3. WASP-31b broad-band transmission spectral results and non-linear limb-darkening coefficients for the STIS *G430L*, *G750L*, WFC3 *G141*, and *Spitzer* IRAC.

$\lambda(\text{\AA})$	R_p/R_*	c_1	c_2	c_3	c_4
2900–3700	0.128 25 ± 0.001 49	0.3403	0.6641	−0.0625	−0.0907
3700–3950	0.128 52 ± 0.001 11	0.3957	−0.0018	0.9565	−0.4757
3950–4113	0.127 01 ± 0.001 06	0.2129	0.7661	−0.0385	−0.0737
4113–4250	0.125 98 ± 0.000 77	0.2136	0.8688	−0.1927	−0.0317
4250–4400	0.126 89 ± 0.001 03	0.4479	−0.2031	1.1499	−0.5530
4400–4500	0.126 33 ± 0.001 01	0.2837	0.6062	0.0919	−0.1409
4500–4600	0.126 53 ± 0.000 91	0.1778	1.1859	−0.7235	0.1887
4600–4700	0.127 04 ± 0.000 85	0.2336	1.0124	−0.5540	0.1291
4700–4800	0.126 22 ± 0.000 88	0.2531	0.9945	−0.5675	0.1259
4800–4900	0.125 59 ± 0.000 83	0.2632	0.9362	−0.4808	0.0835
4900–5000	0.125 29 ± 0.000 97	0.3486	0.7057	−0.2924	0.0280
5000–5100	0.124 01 ± 0.001 08	0.3328	0.7698	−0.3730	0.0554
5100–5200	0.125 18 ± 0.001 07	0.4177	0.4396	0.0065	−0.0924
5200–5300	0.124 71 ± 0.001 09	0.3246	0.8223	−0.4701	0.0936
5300–5400	0.123 90 ± 0.001 01	0.3897	0.5857	−0.2007	−0.0098
5400–5500	0.127 07 ± 0.001 16	0.3873	0.5986	−0.2214	−0.0062
5500–5600	0.124 31 ± 0.001 22	0.3640	0.6822	−0.3215	0.0315
5600–5700	0.125 28 ± 0.001 14	0.3673	0.7158	−0.4132	0.0757
5700–5800	0.124 34 ± 0.001 37	0.4070	0.5534	−0.2195	0.0001
5800–5878	0.127 13 ± 0.001 37	0.3774	0.6655	−0.3623	0.0542
5878–5913	0.127 02 ± 0.002 29	0.4276	0.4659	−0.1253	−0.0414
5913–6070	0.124 46 ± 0.001 13	0.3873	0.6505	−0.3927	0.0743
6070–6200	0.122 40 ± 0.001 77	0.4058	0.5806	−0.3146	0.0386
6200–6300	0.122 92 ± 0.001 22	0.4304	0.4956	−0.2242	0.0027
6300–6450	0.123 65 ± 0.001 13	0.4582	0.3866	−0.1029	−0.0503
6450–6600	0.126 11 ± 0.001 29	0.4111	0.5841	−0.3151	0.0084
6600–6800	0.126 09 ± 0.001 14	0.4590	0.3784	−0.1053	−0.0506
6800–7000	0.125 85 ± 0.001 13	0.4657	0.3399	−0.0804	−0.0525
7000–7200	0.123 42 ± 0.001 14	0.4961	0.2114	0.0595	−0.1054
7200–7450	0.125 61 ± 0.001 38	0.4941	0.2119	0.0391	−0.1013
7450–7645	0.124 52 ± 0.001 12	0.4953	0.2053	0.0076	−0.0779
7645–7720	0.133 38 ± 0.002 00	0.5184	0.1285	0.0841	−0.1041
7720–8100	0.124 22 ± 0.001 38	0.5115	0.1318	0.0783	−0.1059
8100–8485	0.125 84 ± 0.001 42	0.5043	0.1541	0.0361	−0.0841
8485–8985	0.127 06 ± 0.000 86	0.5166	0.0389	0.1599	−0.1358
8985–10300	0.125 51 ± 0.001 62	0.5165	0.0417	0.1293	−0.1206
11340–11540	0.123 40 ± 0.000 78	0.4324	0.3175	−0.3283	0.0956
11540–11740	0.124 20 ± 0.001 02	0.3932	0.4846	−0.5483	0.1904
11740–11940	0.125 36 ± 0.000 73	0.4458	0.2965	−0.3251	0.0941
11940–12140	0.125 64 ± 0.000 75	0.4645	0.2109	−0.2184	0.0507
12140–12340	0.125 87 ± 0.000 68	0.4574	0.2195	−0.2376	0.0664
12340–12540	0.124 03 ± 0.000 66	0.4180	0.4200	−0.5092	0.1784
12540–12740	0.125 30 ± 0.000 77	0.4263	0.4442	−0.5611	0.1938
12740–12940	0.125 86 ± 0.000 84	0.4589	0.3528	−0.5107	0.1923
12940–13140	0.124 74 ± 0.000 68	0.4270	0.4563	−0.6173	0.2321
13140–13340	0.124 42 ± 0.000 87	0.4253	0.4880	−0.6681	0.2545
13340–13540	0.125 01 ± 0.000 86	0.6197	−0.4348	0.4174	−0.1567
13540–13740	0.126 45 ± 0.000 87	0.4314	0.5228	−0.7475	0.2933
13740–13940	0.126 61 ± 0.000 76	0.4524	0.4801	−0.7299	0.2940
13940–14140	0.125 65 ± 0.000 93	0.4788	0.4154	−0.6779	0.2773
14140–14340	0.125 73 ± 0.000 93	0.4815	0.4623	−0.7680	0.3219
14340–14540	0.124 63 ± 0.001 19	0.4997	0.4165	−0.7444	0.3207
14540–14740	0.125 48 ± 0.001 24	0.5228	0.2094	−0.4124	0.1611
14740–14940	0.127 87 ± 0.001 03	0.5299	0.3487	−0.6754	0.2930
14940–15140	0.126 46 ± 0.001 44	0.5531	0.3286	−0.6973	0.3124
15140–15340	0.126 48 ± 0.001 36	0.6050	0.1936	−0.5897	0.2824
15340–15540	0.126 51 ± 0.001 38	0.6699	0.3129	−0.9263	0.4493
15540–15740	0.124 46 ± 0.001 77	0.6603	0.0663	−0.5009	0.2625
15740–15940	0.123 87 ± 0.001 90	0.6583	0.0797	−0.5063	0.2577
15940–16140	0.122 41 ± 0.001 72	0.6465	0.1055	−0.5546	0.2837
16140–16340	0.124 47 ± 0.001 90	0.7357	−0.0020	−0.4485	0.2387
36000	0.124 29 ± 0.001 31	0.3632	−0.1314	0.0949	−0.0435
45000	0.121 34 ± 0.001 75	0.4514	−0.5278	0.5414	−0.2073

for the WFC3 light curves. With the common-mode method, we reach average precisions of 88 per cent the photon noise limit with the *G430L*, 92 per cent for the *G750L*, and 72 per cent with the WFC3 with no significant red-noise detected in any of our spectral bins. The transmission spectral results for both *HST* and *Spitzer* are given in Table 3 and shown in Fig. 10.

4 DISCUSSION

WASP-31b has a zero-albedo equilibrium temperature of $T_{\text{eq}} = 1570$ K, and is highly inflated with a radius of $R_p = 1.55R_{\text{Jup}}$, mass of $M_p = 0.48M_{\text{Jup}}$, and a surface gravity of $g = 4.56 \text{ m s}^{-2}$ (Anderson et al. 2011). At these temperatures, cloud-free solar-abundance models predict significant optical absorption by Na and K atoms, covering most of the optical spectrum with pressure-broadened line wings, with the near-IR dominated by H_2O (Burrows et al. 2010; Fortney et al. 2010).

With a very low surface gravity, WASP-31b has large predicted transmission spectral features, which can be estimated from the analytical relation for the wavelength-dependent transit-measured altitude $z(\lambda)$ of a hydrostatic atmosphere found in Lecavelier des Etangs et al. (2008),

$$z(\lambda) = H \ln \left(\frac{\varepsilon_{\text{abs}} P_{\text{ref}} \sigma(\lambda)}{\tau_{\text{eq}}} \sqrt{\frac{2\pi R_p}{kT\mu g}} \right), \quad (5)$$

where ε_{abs} is the abundance of dominating absorbing species, T is the local gas temperature, μ is the mean mass of the atmospheric particles, k is Boltzmann's constant, P_{ref} is the pressure at the reference altitude, $\sigma(\lambda)$ is the absorption cross-section, and $H = kT/\mu g$ is the atmospheric scaleheight. For WASP-31b, the scaleheight is estimated to be 1220 km at 1550 K (or $0.0014 R_p/R_*$), which gives expected Na, K, and H_2O transmission spectral features which are $\sim 0.006 R_p/R_*$ in amplitude. Our transmission spectrum compares very favourably to these predicted signals, as our average per-bin precisions are $0.0011 R_p/R_*$, which is less than one scaleheight.

4.1 Interpreting the transmission spectrum

The broad-band transmission spectrum of WASP-31b seen in Fig. 10 has three distinct features: a significant blueward slope shortwards of $\sim 0.6 \mu\text{m}$, a largely flat spectrum longwards of about $0.6 \mu\text{m}$

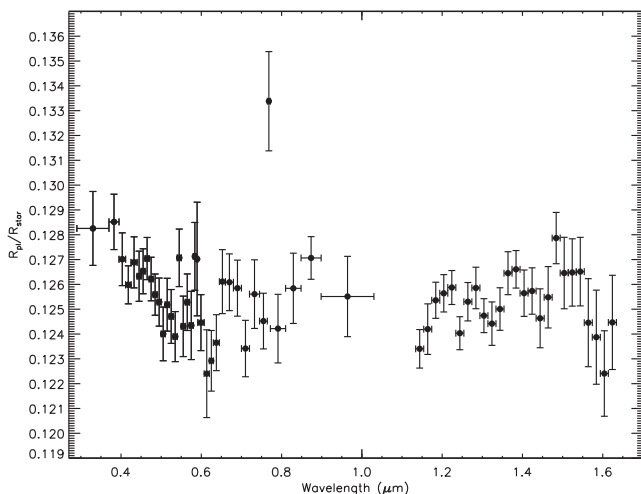


Figure 10. Combined *HST* STIS, *HST* WFC3 transmission spectrum of WASP-31b.

which extends through the red-optical out to infrared wavelengths, and a strong but narrow K line core. We compare these spectral features to both analytic models and those from the modelling suites of Burrows et al. (2010) and Fortney et al. (2010).

The models from Fortney et al. (2008, 2010) include isothermal models as well as those with a self-consistent treatment of radiative transfer and chemical equilibrium of neutral and ionic species. Chemical mixing ratios and opacities assume solar metallicity and local thermochemical equilibrium accounting for condensation and thermal ionization but no photoionization (Lodders 1999; Lodders & Fegley 2002; Freedman, Marley & Lodders 2008).

The models from Burrows et al. (2010) and Howe & Burrows (2012) use a 1D day-side TP profile with stellar irradiation, in radiative and thermochemical equilibrium. Chemical mixing ratios and opacities assume solar metallicity and local chemical equilibrium accounting for condensation and thermal ionization but no photoionization, using the opacity data base from Sharp & Burrows (2007) and the equilibrium chemical abundances from Burrows & Sharp (1999) and Burrows et al. (2001).

4.1.1 A cloud deck

The large pressure-broadened alkali features predicted by models with a clear atmosphere are not seen in the data (see Fig. 11) and cloud-free solar-abundance models can be ruled out. A 1500 K isothermal model from Fortney et al. (2008), which contains large pressure-broadened alkali line wings, gives a poor fit with a χ^2 value of 51.0 for 20 dof when fit to the optical *HST* STIS data between the wavelengths of 0.52 and $0.9 \mu\text{m}$ (excluding the potassium core). A flat line gives a better fit to the data, at 5σ confidence, with a χ^2 value of 25.9 for 20 dof

The H_2O bandhead features predicted by cloud-free models in the WFC3 spectra are also not detected, though the data are clearly of sufficient quality to have detected such a feature (see Fig. 11). In particular, a 1500 K isothermal model predicts a broad $\Delta R_p/R_* = 0.0058$ amplitude H_2O feature between 1.25 and $1.425 \mu\text{m}$, while the WFC3 spectra does not significantly deviate from a flat spectrum beyond the precision level of the data points which average $0.0011 R_p/R_*$ per spectral bin. Moreover, the 1500 K isothermal model dominated by molecular H_2O in the near-IR gives

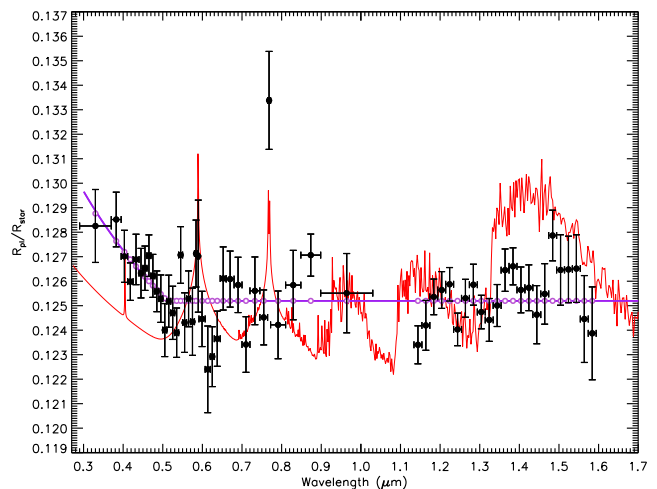


Figure 11. Plotted is the broad-band transmission spectral data along with atmospheric models including a 1500 K cloud-free solar-abundance model (red) and a Rayleigh scattering and cloud-deck model (purple).

χ^2 value of 112 for 24 d.o.f when fit to the WFC3 data, compared to a χ^2 value of 34 for 24 dof for a flat line. Thus, a water dominated atmosphere can be ruled out at 8.8σ confidence.

There is not a significant difference in the overall measured radius between the four transits of the WFC3, STIS *G750L*, and *Spitzer* data sets. A single flat line fitting these the 47 data points for wavelengths longer than $\sim 0.52 \mu\text{m}$ (excluding the Na and K lines) results in a χ^2 value of 59.8 for 46 dof and $R_p/R_* = 0.12519 \pm 0.00015$.

Approximations to hazy or cloudy atmospheres were generated varying the Fortney et al. and Burrows et al. isothermal models with either an artificially added Rayleigh scattering component, simulating a scattering haze, or a cloud deck simulated by a grey flat line at different altitudes. In these models, the artificial hazes and clouds cover up some but not all of the expected atomic and molecular gaseous species.

While a flat line is a good fit to the flat portions of the transmission spectrum, a low-amplitude water feature does slightly improve the χ^2 quality of the fit. A cloudy Fortney et al. model gives a χ^2 value of 31.2 for 23 dof (fitting for the altitude of the cloud deck and overall model altitude) when compared to the WFC3 data, compared to a flat line χ^2 of 34.2 for 24 dof. In addition, when fit to the STIS, WFC3 and *Spitzer* data for wavelengths $> 0.52 \mu\text{m}$ (excluding the Na and K lines) the cloudy Fortney et al. model gives our best fit to those data with a χ^2 of 56.61 for 44 and a $R_p/R_* = 0.12497 \pm 0.00014$.

4.1.2 Rayleigh scattering and a cloud deck

The data shortwards of $\sim 0.55 \mu\text{m}$ shows a significant blueward slope, indicative of Rayleigh scattering (see Fig. 10). To further characterize and assess the significance of the slope, we fit the near-UV transmission spectrum assuming an atmospheric opacity with an effective extinction (scattering+absorption) cross-section which follows a power law of index α , i.e. $\sigma = \sigma(\lambda/\lambda_0)^\alpha$ following Lecavelier des Etangs et al. (2008). With this assumption, the slope of the transmission spectrum is then proportional to the product αT given by

$$\alpha T = \frac{\mu g}{k} \frac{d(R_p/R_*)}{d \ln \lambda}. \quad (6)$$

However, compared to previous studies of HD 189733b and WASP-12b where this analytic method was a useful diagnostic of the observed transmission spectral slope (Lecavelier des Etangs et al. 2008; Sing et al. 2013), it is not immediately apparent in WASP-31b where the blueward near-UV slope transitions to a flat spectrum. This ambiguity can have an effect on the inferred slope (and derived temperatures) as including more of the flat portions of the spectrum will decrease the measured slope, lowering the inferred temperatures.

We elected to fit a two-component model which included both a power-law cross-section at short wavelengths, and a flat spectrum at longer wavelengths, with the transition wavelength, λ_T , between the two freely fit (see Fig. 11). Excluding only the Na and K line cores from the full transmission spectrum, this model gave a good fit to the 59 data points (χ^2 of 65.4 for 56 dof), with $\lambda_T = 0.510 \pm 0.031 \mu\text{m}$ and $\alpha T = -9284 \pm 3240 \text{ K}$. The uncertainty in λ_T increases the error in measuring αT by about 40 per cent. The result is compatible with Rayleigh scattering, $\alpha = -4$, which results in estimated temperatures of $2300 \pm 800 \text{ K}$. While the derived temperature may appear too high to be associated with most condensates, we note that given the large error it is still within the 1σ uncertainty of the zero-albedo equilibrium temperature ($T_{\text{eq}} = 1570 \text{ K}$) where

condensates from Fe and Mg are found. This two-component model, simulating a short-wavelength Rayleigh haze and a long-wavelength cloud deck, results in a much better χ^2 fit compared to a simple flat line over the same wavelength range (χ^2 of 87.17 for 57 dof). Thus, the presence of a near-UV Rayleigh slope is significant at about 4σ confidence.

4.1.3 Potassium

In addition to measuring the broad-band transmission spectrum, we also searched the STIS data for narrow-band signatures, notably the line cores of the Na I and K I D lines and the H_α line. No significant absorption was found for either Na I or H_α . We quote a 34 \AA wide bin across the Na line in our transmission spectrum for comparison purposes (see Table 3), choosing this width based on the HAT-P-1b Na detection (Nikolov et al. 2014b).

While no significant Na I absorption was detected, there is a strong K line evident in the data (see Fig. 11). Searching both on and around the wavelength range of the K I doublet (with line centres at 7664 and 7699 \AA), we measured the transit depth in various bin sizes ranging from one resolution element ($\sim 10 \text{ \AA}$) up to several hundred \AA , comparing the transit depths to the surrounding continuum regions and that of the white-light curve. We find a radius of $R_p/R_* = 0.1334 \pm 0.0020$ in a 78 \AA band (7645 and 7720 \AA) which encompasses the K I doublet gives an optimal detection, which is larger than the white-light radius at 4.2σ confidence ($\Delta R_p/R_* = 0.0086 \pm 0.0020$). A confirmation of the K I detection is provided by the fact that each line of the potassium doublet is also individually detected, with a band from 7645 to 7683 \AA giving radius of $R_p/R_* = 0.1342 \pm 0.0027$ and a band from 7683 to 7720 \AA giving a radius of $R_p/R_* = 0.1325 \pm 0.0032$. No significant signals were detected outside the 7645 to 7720 \AA region confining the potassium feature to a 78 \AA region, as wider bins dilute the measured potassium absorption depth. In addition, no other similar features rising to significant levels above the broad-band continuum are seen at any other wavelengths in the *G750L* data.

4.2 Limits on the pressure level of the cloud deck

The pressure level of the broad-band spectrum can potentially be constrained by the shape of the potassium line and the presence (or lack) of pressure-broadened wings. The maximum expected pressures probed would correspond to the near-UV slope being due to gaseous H_2 Rayleigh scattering, which following the fits from Section 4.1.2 and Lecavelier des Etangs et al. (2008) would put the cloud deck radius of $R_p/R_* = 0.12497$ at pressures of 40 mbar. However, this scenario is unlikely due to the lack of pressure-broadened K wings, and the fact that both Na and H_2O would have to both have sub-solar abundances depleted by about a factor of 100 to hide both features.

To further constrain the pressures and abundances, we model the alkali metal lines following Burrows, Marley & Sharp (2000), Iro, Bézard & Guillot (2005), and Huitson et al. (2012). Statistical theory predicts the collisionally broadened alkali line shapes which vary as $(\nu - \nu_0)^{-3/2}$ outside of the impact region, which lies between the line centre frequency ν_0 and a detuning frequency $\Delta\sigma$ away from ν_0 . The power-law line shape is then truncated by an exponential cutoff term of the form $e^{-q h(\nu - \nu_0)/kT}$, where h is Planks constant and q a parameter of order unity. For the potassium doublet, we estimate $\Delta\sigma$ following Burrows et al. (2000) using

$$\Delta\sigma = 20(T/500 \text{ K})^{0.6} \text{ cm}^{-1}. \quad (7)$$

Assuming a 1570 K equilibrium temperature for WASP-31b gives a detuning frequency of 23 Å from the K line centres. The K doublet is spaced by 34.1 Å, giving a total impact region encompassing the two doublets which is 80.1 Å wide (7641.6 to 7722 Å).

Within $\Delta\sigma$ of the line centre in the impact region, we use a Voigt profile, $H(a, u)$, which is defined in terms of the Voigt damping parameter a and frequency offset u . The frequency offset is calculated as $u = (\nu - \nu_0)/\Delta\nu_D$, where $\Delta\nu_D$ is the Doppler width given by $\Delta\nu_D = \nu_0/c\sqrt{2kT/\mu_K}$, with c the speed of light and μ_K the mean molecular weight of potassium. The damping parameter is given by $a = \Gamma/(4\pi\Delta\nu_D)$, where the transition rate Γ is calculated as follows:

$$\Gamma = \gamma + \Gamma_{\text{col}}, \quad (8)$$

where γ is the spontaneous decay rate and Γ_{col} is the half-width calculated from classical impact theory. Assuming a van der Waals force gives $\Gamma_{\text{col}} = 0.14(T/2000)^{-0.7} \text{ cm}^{-1} \text{ atm}^{-1}$ for K (Burrows et al. 2000; Iro et al. 2005). The cross-sections for both the sodium and potassium doublets in the impact region are then calculated as,

$$\sigma(\lambda) = \frac{\pi e^2}{m_e c} \frac{f}{\Delta\nu_D \sqrt{\pi}} H(a, u), \quad (9)$$

where f is the absorption oscillator strength of the spectral line, m_e is the mass of the electron and e the electron charge. With the cross-sections, the transmission spectrum is then calculated with equation (5).

In addition to the cloud-free solar-abundance models which can be ruled out at high confidence (see Section 4.1.1), we further test for the presence of collisionally broadened wings by using the Rayleigh and cloud analytic model from Section 4.1.2, fixing both T and λ_T while adding a potassium line and adjusting P_{ref} via the Rayleigh slope opacity. This also tests the hypothesis that the near-UV slope is due to gaseous H_2 Rayleigh scattering (as opposed to aerosols), but a low-altitude cloud is still present. With a solar abundance of potassium and assuming H_2 Rayleigh scattering, the model gives a fit with a χ^2 of 71.3 with 60 dof. The model reproduces the height of the K core measurement and still contains significant collisional broadening as the presumed low-altitude cloud does not fully cover the broadened alkali wings. Assuming instead the Rayleigh scattering is from an aerosol (residing at higher altitudes and lower pressures) and maintaining the amplitude of the potassium line gives a χ^2 of 65.2 for 60 dof, with the model lacking significant collisionally broadened wings. In conjunction with the results of Section 4.1.1, pressure-broadened potassium wings can be fully excluded from cloud-free models, and further at about the 98 per cent confidence level for the case of H_2 Rayleigh scattering with a low-altitude cloud. We note that this result can be expected from statistical theory, as the width of the potassium line calculated assuming pressures of zero in equation (8) (i.e. only natural broadening) match very well with the measured width of the potassium line.

We estimate the maximum pressure level of the cloud deck by raising the Rayleigh scattering opacity and K abundance by the minimum amounts needed to maintain the K line amplitude and produce a sufficiently narrow width. A cloud deck at pressures below about 10 mbar reduce the broadening such that the model gives a $\Delta\chi^2$ of 1 compared the best-fitting model, which corresponds to a minimum aerosol opacity which is about 4 times that of gaseous H_2 .

As the 1.4 μm H_2O feature is strong, the pressure level of the cloud deck estimated by the lack of alkali broadened wings (10 mbar) would still not be sufficient to cover H_2O at the mixing

ratios predicted when assuming chemical equilibrium and solar abundances. Based on the Fortney et al. and Burrows et al. models, we estimate that a cloud deck at pressures of about 1 mbar would be needed to cover all but the very peak of the 1.4 μm H_2O feature at mixing ratios assuming solar-abundances.

4.3 The Na/K abundance ratio

Transmission spectra can provide robust measurements of the abundance ratio between Na and K, which following equation (5) gives

$$\frac{\varepsilon_{\text{Na}}}{\varepsilon_{\text{K}}} = \frac{\sigma_{\text{K}}}{\sigma_{\text{Na}}} \exp\left(\frac{z_{\text{Na}} - z_{\text{K}}}{H}\right), \quad (10)$$

making the ratio dependent on the relative opacities of the species in question, the measured altitude difference between the two species, and the scaleheight of the atmosphere. A reliable measurement of the abundance ratio is particularly useful for WASP-31b, as the source of the Rayleigh scattering is unknown as is the absolute value of P_{ref} thereby the absolute abundances are unknown. However, the relative abundance ratio is not dependent upon P_{ref} and thereby can still be measured.

To measure the relative abundances, we fit an analytic model which included Rayleigh scattering, a cloud deck as well as Na and K (see Fig. 12). We also included the small H_2O feature from the cloudy Fortney et al. model as found in Section 4.1.1 as it provided the best fits, though very similar results were obtained by removing the opacity of H_2O and fitting the entire infrared wavelength region with a flat line. Fitting for the alkali abundances, T , λ_T and the baseline radius while setting P_{ref} below 10 mbar gives our best-fitting overall model to all 61 data points, with a χ^2 of 63.0 for 56 dof. We find a Na to K abundance ratio² of $\ln[\text{Na}/\text{K}] = -3.3 \pm 2.8$ which is sub-solar compared to the solar value being $\ln[\text{Na}/\text{K}]_{\odot} = +2.8$ (Asplund et al. 2009). The uncertainty in the abundance ratio is dominated by the uncertainty in the Na line core measurement, which could benefit greatly from higher resolution data clearly separating any Na signatures from the surrounding clouds.

With the K line included in the fit, the fit temperature increases somewhat to $T = 2470 \pm 590$ K. At the high altitudes probed in the K line core, the presence of a thermosphere is possible and may be responsible for the high measured temperatures, as has been found in HD 189733b and HD 209458b using the Na line (Vidal-Madjar et al. 2011; Huitson et al. 2012). However, the errors on the retrieved temperatures are still high which limits the current interpretation.

A sub-solar value for the Na to K abundance ratio is surprising, and to the best of our knowledge has not yet been seen in any planetary atmosphere. A variety of physical processes could in principle alter the abundances, though a Na/K ratio < 1 is in any case still difficult to explain. While the alkali metals are easily ionized, which could dramatically alter their measured neutral abundances, photoionization favours depleting K I over Na I presumably making it a difficult mechanism to explain the observed ratio. Condensation of Na could also potentially play a role in reducing its abundance, and would be consistent with the presence of a cloud deck or higher altitude scatterer. However, the expectations from current chemical models predict Na to condense at temperatures near ~ 1000 K (Lodders 1999) which is lower than the expected temperatures of WASP-31b, though a large day/night temperature contrast could be

² We quote logarithmic abundance values in base e rather than the more common base 10 given the exponential relationship to the measured values of z .

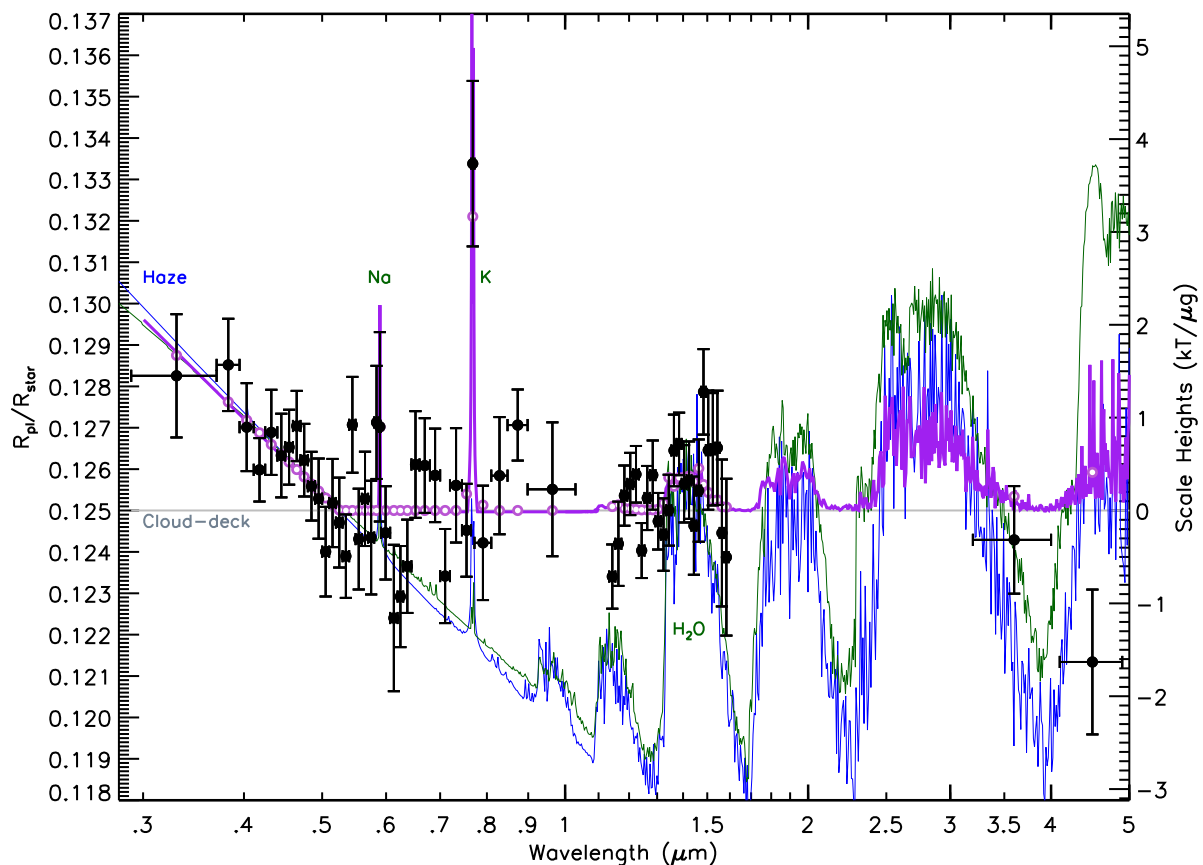


Figure 12. Plotted is the broad-band transmission spectral data along with atmospheric models. Two solar-composition models containing a scattering haze are shown from the modelling suits of Burrows et al. (green) and Fortney et al. (blue). Our best-fitting model is also plotted (purple) containing a Rayleigh scattering haze, a grey cloud deck at low pressures, non-pressure broadened Na and K features, and an obscured H₂O feature. The band-averaged model points are indicated with open circles.

present, making for a Na cold-trap on the night side while K is not likely to condense out at temperatures exceeding ~ 800 K. This explanation of condensing Na but not K is very specific: the planet has to have a specific temperature regime so that Na₂S condenses but not KCl, which requires only a ~ 200 K lower temperature. Finally, we speculate that the large element-to-element metallicity variations could be primordial in nature, or altered after formation from accretion processes.

While the absolute abundances in WASP-31b are unknown, as P_{ref} is unknown, limits on the pressure can in principle provide bounds on the K abundance. A cloud deck pressure level of 10 mbar or lower, required to hide the pressure-broadened alkali wings, corresponds to a minimum K abundance of $\ln[\epsilon_K] = -14.77 \pm 0.86$, indicating a super-solar K abundance (solar $\ln[\epsilon_K]_{\odot} = -16.05$). The K abundance would be a factor of ~ 10 higher if the cloud deck is instead at 1 mbar, required to hide a solar-abundance of H₂O.

4.4 Cloud properties and vertical mixing

A broad-band transmission spectrum can give valuable constraints on aerosol particle sizes. Obtaining a flat spectrum out to wavelengths of several microns requires a particle size of at least ~ 1 μm ; small particles of, e.g. ~ 0.1 μm or less would become transparent in the IR and thus would be inefficient at scattering the radiation, as necessary to produce a flat spectrum. The presence of

Rayleigh scattering can also give constraints, as scattering occurs when the particle size is less than the wavelength of light probed. In the WASP-31b transmission spectrum, there are two distinct possible scattering slopes in the data, the near-UV to blue slope as discussed in Section 4.1.2, and second possible (though fairly flat) slope in the IR as the 4.5 μm channel exhibits the smallest radii in our spectrum (at $\sim 2\sigma$ significance).

To further estimate the possible particle sizes allowed in the data, we computed a series of transmission spectra assuming an opacity dominated by a single size aerosol calculated with Mie theory, and compared it with the transmission spectrum. As the cloud and haze composition cannot be easily identified, we explored a variety of plausible materials, including Al₂O₃, CaTiO₃, Fe₂O₃, MgSiO₃, and a Titan tholin (Sing et al. 2013). We find a single particle size does not give a good quality fit to the broad-band spectrum, and two distinct particle sizes are needed, a larger particle size for the cloud deck and a smaller size particle for the higher altitude haze layer. For the condensate materials explored, we find cloud particle sizes between 0.52 and 1 μm are needed to fit the flat transmission spectrum between 0.52 to 3.6 μm and the small radius at 4.5 μm . Fitting for the data < 0.52 μm , we find haze particle sizes of 0.02 to 0.1 μm can reproduce the near-UV to blue optical scattering slope, with condensates containing lower values for the imaginary part of the refractive index (like MgSiO₃ or Fe-poor Mg₂SiO₄ silicates) giving larger particle sizes.

Our results can also place important constraints on the vertical mixing rate in the atmosphere of WASP-31b. As discussed

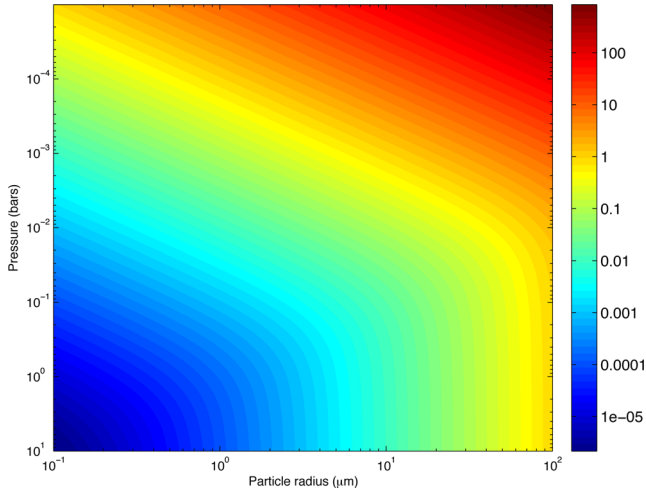


Figure 13. Downward settling velocity (colour scale, m s^{-1}) for spherical atmospheric particles as a function of particle radius and pressure, assuming an H_2 atmosphere with a temperature of 1570 K and gravity of 4.56 m s^{-2} , appropriate to WASP-31b (see equations 3–7 of Parmentier, Showman & Lian 2013). Stokes flow holds at high pressure and leads to settling velocities that depend on particle size but not pressure. Mean-free-path effects become important at low pressure, where settling velocity scales as approximately one over pressure. Here, we have assumed a particle density of 3000 kg m^{-3} (appropriate to silicate) and the gas viscosity appropriate to hydrogen from Rosner (2000); see Parmentier et al. (2013) for more details.

previously, a flat spectrum requires the presence of cloud or haze particles down to the 10-mbar level (based on the absence of the potassium line wings) or potentially even up to the 1-mbar level (based on the weakness of the water spectral feature). Fig. 13 shows the expected particle settling velocity for conditions relevant to WASP-31b as a function of particle radius and pressure, based on Stokes–Cunningham theory. The regime in the bottom portion of the plot corresponds to Stokes flow, where settling velocity is approximately independent of pressure. The regime at the top corresponds to that where the mean-free path becomes significant compared to the particle size, such that the continuum approximation breaks down and gas-kinetic effects are important; in this regime, the settling velocity for a particle of a given size scales approximately with the inverse of pressure. The figure shows that the settling velocity of $1\text{-}\mu\text{m}$ particles is 0.01 m s^{-1} at 10 mbar and 0.1 m s^{-1} at 1 mbar.

Given these estimates of settling velocity, it is interesting to estimate the effective atmospheric eddy diffusivities that would be necessary to loft such $1\text{-}\mu\text{m}$ particles to 1–10 mbar pressures, as necessary to cause a flat transmission spectrum. Parmentier et al. (2013) considered an idealized 1D diffusion model with downward transport due to particle settling being balanced by upward transport due to mixing by atmospheric motions (see equation 10 in Parmentier et al. 2013). An order-of-magnitude consideration of this equation suggests that, crudely, to keep particles of a given size lofted to a given altitude, one requires an eddy diffusivity of order $K_{zz} \sim H w_{\text{settle}}$, where H is the atmospheric scaleheight and w_{settle} is the particle settling velocity (e.g. as shown in Fig. 13). Given the $\sim 1000\text{-km}$ scaleheight expected on WASP-31b and the settling velocities quoted above, we estimate that the necessary atmospheric mixing corresponds to $K_{zz} \sim 10^4 \text{ m}^2 \text{ s}^{-1}$ to loft $1\text{-}\mu\text{m}$ particles to 10 mbar and $K_{zz} \sim 10^5 \text{ m}^2 \text{ s}^{-1}$ to loft them to 1 mbar. These estimates are consistent with the more detailed analysis presented in Parmentier et al. (2013).

Determining whether the atmospheric circulation on WASP-31b can generate sufficient mixing to induce $K_{zz} \sim 10^4\text{--}10^5 \text{ m}^2 \text{ s}^{-1}$ is not trivial and will require detailed 3D numerical simulations for this planet, which is a task for the future. Nevertheless, Parmentier et al. (2013) made such estimates for HD 209458b, which has a similar effective temperature to WASP-31b. Because the incident starlight drives the vertical mixing, we might expect that planets with similar incident stellar irradiation, such as WASP-31b and HD 209458b, should exhibit similar profiles of the vertical mixing rate. Parmentier et al. (2013) showed that, interestingly, K_{zz} is *not* well represented by the product of the scaleheight and the rms vertical velocity of the atmospheric motions (as has sometimes been assumed in the literature). They fit diffusion models to their 3D simulations of the atmospheric circulation to obtain the vertical profile of the effective diffusivity: $K_{zz} \approx (5 \times 10^4 / \sqrt{P_{\text{bar}}}) \text{ m}^2 \text{ s}^{-1}$, where P_{bar} is the pressure in bar. This equation suggests that the effective eddy diffusivity should be $\sim 5 \times 10^5 \text{ m}^2 \text{ s}^{-1}$ at 10 mbar and $\sim 2 \times 10^6 \text{ m}^2 \text{ s}^{-1}$ at 1 mbar. These values exceed the estimates we made above for the diffusivity required to mix $\sim 1\text{-}\mu\text{m}$ particles to pressures of 1–10 mbar. Thus, it appears physically plausible that the circulation will indeed be sufficiently strong to mix particles upward to pressures of 1–10 mbar, as necessary to explain our flattened spectrum.

5 CONCLUSION

We have presented *HST* and *Spitzer* observations totalling six transits of WASP-31b, which cover the full-optical to infrared spectral regions. The resulting exoplanet transmission spectrum is unique, showing several atmospheric features not yet seen in conjunction including potassium line cores and no detectable sodium, a flat optical to near-IR slope indicative of a cloud deck, and Rayleigh scattering at short wavelengths. The potassium feature is strong (detected at 4.2σ confidence) though lacks significant pressure broadened wings, which we find limits the pressures probed to 10 mbar or less. Weak sodium and strong potassium lines indicate the peculiar possibility of a sub-solar $[\text{Na}/\text{K}]$ abundance ratio below one, which is difficult to explain though may point towards Na condensation or large element-to-element metallicity variations from formation/accretion processes.

The transmission spectrum is flat longwards of $0.52 \mu\text{m}$, indicative of a high altitude broad-band cloud deck which covers the expected optical Na and near-IR H_2O features. However, despite containing a substantial cloud(s) the broad-band transmission spectrum is not flat, and a 4.2σ significant slope is observed at wavelengths shortwards of $0.52 \mu\text{m}$, consistent with Rayleigh scattering by small sub-micron size haze particles.

WASP-31b joins a growing group of hot-Jupiter exoplanets with evidence for clouds and hazes. Clouds and hazes are now seen to be important atmospheric features in hot Jupiters across a wide range of effective temperatures, including the hottest planets like WASP-12b and much cooler planets like HD 189733b. Moreover, at temperatures near 1570 K, WASP-31b has an equilibrium temperature close to the mean for known hot Jupiters, implying atmospheric clouds and haze signatures are not confined to the extremes of hot-Jupiter parameter space.

We highlight the importance of wide wavelength coverage for exoplanet transmission spectra, as short-wavelength data can be highly sensitive to the cloud properties and the blue-optical data were necessary in this case to detect aerosol scattering features.

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