

1 Timing of Neoproterozoic glaciations linked to transport-limited 2 global weathering

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9 **The Earth underwent several snowball glaciations between 1,000 and 542 Myr ago. The**
10 **termination of these glaciations is thought to have been triggered by the accumulation of volcanic**
11 **CO₂ in the atmosphere over millions of years [1,2]. Subsequent high temperatures and loss of**
12 **continental ice would increase silicate weathering and in turn draw down atmospheric CO₂ [3].**
13 **Estimates of the post-snowball weathering rate indicate that equilibrium between CO₂ input and**
14 **removal would be restored within several million years [4], triggering a new glaciation. However**
15 **the transition between deglaciation and the onset a new glaciation was on the order of 10⁷ years.**
16 **Over long timescales, the availability of fresh rock can become a limiting factor for silicate**
17 **weathering rates [5]. Here we show that when this limitation is incorporated into the COPSE**
18 **biogeochemical model [6], the stabilization time is substantially higher, >10⁷ years. When we**
19 **include a simple ice albedo feedback, the model produces greenhouse-icehouse oscillations on this**
20 **timescale that are compatible with observations. Our simulations also indicate positive carbon**
21 **isotope excursions and an increased flux of oxygen to the atmosphere during interglacials, both of**
22 **which are consistent with the geological record [7,8]. We conclude that the long gaps between**
23 **snowball glaciations can be explained by limitations on silicate weathering rates.**

24 The Neoproterozoic era (1000-542Ma) is punctuated by at least three glaciations [9], the
25 severe low-latitude Sturtian and Marinoan episodes being proposed as examples of 'Snowball Earth'
26 events [1, 10]. Figure 1 displays Neoproterozoic carbonate carbon isotope data [7], which shows a
27 quasi-periodic pattern. Negative excursions associated with glaciation appear at ~50 Myr intervals
28 between long periods of positive fractionation. The long interval between glaciations poses a puzzle
29 given the standard model of a snowball Earth being terminated by very high CO₂ and temperature.
30 The time taken to restore equilibrium after such a perturbation depends on the rate of CO₂
31 drawdown via silicate weathering, a process that would be greatly enhanced in the aftermath of
32 snowball Earth. Highly weatherable rock flour produced by glacial grinding would likely cover a large
33 surface area, and increased temperature and runoff should allow for an elevated weathering flux.
34 Linked GCM and kinetic weathering models have determined the maximum weathering rate in this
35 climate to be on the order of 10 times the modern day flux, implying a timescale of around 10⁶ years
36 to reduce atmospheric CO₂ to pre-glacial levels [4]. Based on these results, we would expect the
37 system to establish equilibrium in a time far shorter than the interglacial periods following the
38 Sturtian and Marinoan glaciations.

39 Here we propose that the timescale for CO₂ drawdown following a snowball glaciation
40 should be extended due to transport limitation of the silicate weathering process. In a transport
41 limited regime, silicate cations are completely leached from fresh regolith and therefore the rate of
42 chemical weathering depends only on the physical erosion rate [5]. Modern continental cratons are
43 transport limited, as seen by plotting the rate of denudation of silicate cations against total
44 denudation rate [11]. In such a regime, increasing temperature or runoff does not increase the rate
45 of CO₂ drawdown, because all the available silicate cations are already being processed. As global
46 temperature and humidity rises, we would expect more weathering zones to become transport-
47 limited, implying a theoretical maximum silicate weathering rate, where every available cation is
48 leached.

49 Over the Phanerozoic, the mean continental erosion rate is estimated to be $\sim 16 \text{ m Myr}^{-1}$ [12].
50 Using the average density and area of the present day continents (area = $1.5 \times 10^{14} \text{ m}^2$, density = $2.5 \times$
51 10^3 kg m^{-3}) yields a total mass of $6 \times 10^{12} \text{ kg yr}^{-1}$. Assuming a cation weight fraction of 0.08 [5], we
52 estimate a global silicate weathering rate maximum for the Phanerozoic of around $4.8 \times 10^{11} \text{ kg yr}^{-1}$.
53 This maximum transport limited rate is about 2.4 times greater than present day weathering rate
54 [13].

55 Determining the global erosion rate in the Neoproterozoic is difficult, because it depends on
56 the continental area and rate of uplift. Current estimates for Neoproterozoic uplift rates are close to
57 present day values [14], and the majority of studies agree that the total continental area was
58 probably less than it is now. Proxies for global denudation show very low values ($< 10 \text{ m Myr}^{-1}$) for the
59 early Phanerozoic, but are likely to be affected by sampling artefacts [15]. The rate of volcanic
60 degassing in the Neoproterozoic is also important, as it is the balance between CO_2 degassing and its
61 consumption rate via weathering and burial that dictates the system response time to large
62 perturbations. In carbon cycle models, degassing is usually assumed to be proportional to the
63 seafloor spreading rate. Accounting for different continental growth models, the Neoproterozoic
64 outgassing rate was probably between 1 and 5 times the present day rate [14, 16]. But smaller
65 crustal carbon content in the Neoproterozoic [17] may have decreased the CO_2 content of volcanic
66 gas by up to 20%.

67 In figure 2, we use a modified version of the COPSE biogeochemical model [6] (see
68 supplementary information) to investigate the effect of a weathering rate cap on the time taken to
69 return to steady state after the suggested snowball exit concentration of 0.3 atm CO_2 [1, 2] is
70 imposed. Silicate weathering rate is fixed at a prescribed maximum value, W_{max} , which is defined
71 relative to the present day rate. We find that choice of W_{max} has a strong effect on the system:
72 Assuming the Phanerozoic average erosion rate ($W_{max}=2.4$) yields a stabilisation time of $\sim 10^7$ years,
73 even for conservative estimates of the CO_2 degassing rate D . A lower erosion rate, and/or a higher

74 degassing rate increases the stabilisation time greatly. For further model runs we let global
75 weathering follow a simple kinetic equation as described by Berner [18], but asymptote to W_{max} as
76 the kinetic weathering rate approaches the transport-limited value, placing a cap on global
77 weathering rates. The choice of kinetic weathering function, and the nature of the transition to W_{max}
78 has negligible effect on results as the rate remains at W_{max} until CO_2 is very close to the stable level.

79 An important consideration for this work is weathering of rock flour left on the surface after
80 a snowball glaciation, which would be expected to increase weathering kinetics as in the quaternary
81 glacial cycle [19]. Global weathering fluxes would not become limited by transport of fresh rock until
82 the flour produced during the glaciation had been completely leached. Le Hir et al [4] assume a thin
83 soil profile following a snowball, due to evidence of persistent weathering during glaciation [20].
84 Following their estimate of a 25cm reactive upper layer¹⁷, we derive a weatherable equivalent of $\sim 10^{17}$
85 moles C (see supplementary information).

86 Figure 3 shows model sensitivity to the initial quantity of rock flour. Here we allow a global
87 weathering rate of 10 times present day when rock flour is present [4], switching to the transport
88 limited equation once a specified amount of carbon has been buried, analogous to the abundance of
89 glacial flour. We find that a weatherable equivalent on the order of 10^{20} moles C is required to
90 significantly affect stabilisation time; we use a increased reactive layer depth of 2.5m (10^{18} mol C
91 equiv.) for future model runs, due to uncertainty in estimation.

92 Our results indicate that the sequence of deep glaciations in the Neoproterozoic could be
93 the result of a change of state in the long-term carbon-climate system to a regime which exhibits
94 self-sustaining oscillations. If there was a long period in which global steady state temperature
95 remained below the value required to trigger a snowball glaciation, this would be manifest as an
96 oscillatory regime, with snowball glaciations alternating with warm phases. Such a temperature
97 forcing may well be attributed to the continental configuration at this time. It has been shown that
98 the position of the continents at low latitudes at 750Ma, along with the prevalence of basaltic

99 lithologies, could provide the necessary cooling to trigger the first snowball event [21]. It is thought
100 that the continents would have remained near low latitudes until 600Ma [22], after which they begin
101 to drift to higher latitudes, relaxing the forcing.

102 To investigate this possible mechanism we parameterise a runaway ice-albedo feedback in
103 our model by imposing a change in albedo when temperature falls below a given value T_{crit} .
104 Assuming the classic snowball scenario [23], we choose $T_{crit} = 283K$ and allow deglaciation at 263K.
105 Because deglaciation begins in the tropics, it is assumed to occur at lower temperature than is
106 required for the ice sheets to initially advance. Throughout this work we assume a solar constant for
107 650Ma (1298 Wm^{-2} [24]), broadly representing the timeframe of interest. This allows glaciation at
108 $\sim 150\text{ppm CO}_2$, close to other estimates [21].

109 We impose the described cooling scenario in the model, adding a parameter ρ to represent
110 enhancement of kinetic weathering. This follows the treatment of vascular plant colonisation in the
111 Phanerozoic COPSE model runs [6], acting as a multiplier on the kinetic weathering rate equation. To
112 trigger oscillations we increase ρ by a factor of three for a period of 150Myrs. The magnitude of this
113 enhancement is roughly analogous to the increase in basaltic surface area and mid-latitude runoff
114 calculated in ref [21]. For present day CO_2 degassing rate ($D = 1$), we require $W_{max} = 1.4$ to produce a
115 rough analogue of the Neoproterozoic record. This parameter choice is shown in figure 4. Assuming
116 a higher CO_2 degassing rate shortens glacial duration and allows for larger values of W_{max} to produce
117 the observed timing, in line with figure 2.

118 We use output from the CO2SYS model [25] to approximate the atmospheric fraction of
119 total ocean and atmosphere CO_2 , assuming that there is gas exchange between atmosphere and
120 ocean during glaciation [1]. The total solubility of CO_2 is higher in cold water than warm water,
121 therefore deglaciation causes a large transfer of CO_2 from ocean to atmosphere.

122 The solid line for $\delta^{13}\text{C}$ shows the isotopic fractionation of marine carbonates, assuming the
123 fractionation effect on burial takes into account the equilibrium fractionation between oceanic and
124 atmospheric carbon, and a dependence on temperature, as in the full COPSE model [6]. The dashed
125 line shows an alternative solution where fractionation effects are constant. Both treatments yield a
126 continued positive fractionation during the interglacial period due to elevated burial of light organic
127 carbon, due in turn to sustained above-average nutrient fluxes from weathering. Higher assumption
128 of W_{max} increases nutrient delivery and therefore also increases fractionation. Low productivity
129 during glaciations causes a negative excursion. We do not expect a simple model such as this to
130 replicate exactly the isotope record. Negative excursions preceding glaciation are not reproduced by
131 our model, and may be due to direct temperature effects on productivity, which are not included.
132 Our aim is to demonstrate that the extended period of system disequilibrium following a snowball
133 glaciation should contribute to prolonged positive excursions in $\delta^{13}\text{C}$, and more complex analysis is
134 required to fully understand the Neoproterozoic carbon cycle.

135 With the imposition of a suitable long term maximum weathering rate, oscillations in this
136 simple carbon – climate model can provide a qualitative fit to the sequence of glaciations and carbon
137 isotope variations in the Neoproterozoic. The globally transport limited scenario presents a
138 prolonged period of elevated primary productivity, which would support suggested increases in
139 oxygen concentration and phosphorous deposition over this time [7, 8, 26-29]. There is evidence for
140 phosphorous deposition after the Marinoan glaciation but not after the Sturtian.

141 It is important to note that the mechanism we describe relies on a particular interpretation
142 of the Neoproterozoic period, namely the Snowball Earth hypothesis [1, 10]. It is possible that the
143 Neoproterozoic actually contained more frequent smaller glaciations, which would not terminate via
144 a high CO_2 ‘super greenhouse’. Due to our long timeframe for CO_2 drawdown, our prediction is
145 highly testable, with for example one recent study proposing a rapid decline in CO_2 following the

146 Marinoan glaciation [30]. Further work to establish the duration of any post-glacial greenhouse may
147 thus enable validation or falsification of mechanisms to explain these fascinating events.

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230 **Author Contributions:**

231 BM and AJW suggested the study. BM wrote the model, results were analysed by BM and AJW.

232 Discussion with CG helped improve the method. RB and TML contributed to the manuscript.

233 **Competing financial interests statement**

234 The authors declare that they have no competing financial interests.

235 **Figure captions**

236 **Figure 1: $\delta^{13}\text{C}$ record for the late Neoproterozoic.** Isotopic composition of carbonates from ref. [7].

237 The vertical grey bars from left to right denote the Sturtian, Marinoan and Gaskiers glaciations.

238

239 **Figure 2: Phase portrait: stabilisation time versus maximum weathering rate, W_{max} .** Here we

240 assume an initial CO_2 concentration of 0.3 atmospheres, and fix the global weathering rate at W_{max} .

241 The three lines show different choices of the relative CO_2 degassing rate, D . W_{max} is defined relative

242 to present day silicate weathering rate, with the grey vertical line showing our estimate of $W_{max} = 2.4$

243 for the Phanerozoic. Increasing the weathering rate enhances nutrient delivery and therefore

244 increases the organic burial fraction, allowing stability when W_{max} is somewhat smaller than D ,

245 providing $W_{max} > 1$. See supplementary information for full model description.

246

247 **Figure 3: Stabilisation time after 0.3 atm CO_2 perturbation for different initial abundances of rock**

248 **flour. a, Rock flour consumed. b, Silicate weathering rate. c, Atmospheric CO_2 concentration.** Here

249 R_{max} denotes the maximum amount of carbon (in moles) that can be drawn down via weathering of

250 glacial rock flour before it is depleted. This figure shows the situation where $D = 1$, $W_{max} = 2.4$. The

251 grey vertical line shows the stabilisation time when no flour is present (as in fig2). The second drop

252 in weathering rate here occurs as CO_2 returns to a stable concentration.

253 **Figure 4: Cyclic solution when steady state temperature is forced below the ice-albedo runaway**
254 **value for 150Myr.** Here we let $D = 1$ and $W_{max} = 1.4$ to produce glacial timing on the order observed
255 in the Neoproterozoic. **a**, The imposed kinetic weathering enhancement (ρ) is shown in grey; in black
256 is the weathering rate relative to present. **b**, Total atmosphere/ocean carbon (grey), and
257 atmospheric CO_2 (black). **c**, Temperature alongside snowball entry/exit thresholds. **d**, Model $\delta^{13}\text{C}$,
258 solid line shows temperature/ CO_2 dependent fractionation [6], dashed line shows solution when
259 fractionation effects are constant.







