The Impact of Climate Change on Agriculture: Nonlinear Effects and Aggregation Bias in Ricardian Models of Farmland Values
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The Impact of Climate Change on Agriculture: Nonlinear Effects and Aggregation Bias in Ricardian Models of Farmland Values

Carlo Fezzi, Ian Bateman

Abstract: Ricardian (hedonic) analyses of the impact of climate change on farmland values typically assume additively separable effects of temperature and precipitation with model estimation being implemented on data aggregated across counties or large regions. We use a large panel of farm-level data to investigate the potential bias induced by such approaches. Consistent with the literature on plant physiology, we observe significant nonlinear interaction effects, with more abundant precipitation acting as a mitigating factor for increased heat stress. This interaction disappears when the same data are aggregated in the conventional manner, leading to predictions of climate change impacts that are significantly distorted.

JEL Codes: C14, C23, Q54

Keywords: Aggregation bias, Agriculture, Climate change, Ricardian analysis, Semiparametric models

There is growing policy concern regarding the potential impact of climate change on agriculture as variation in temperature and precipitation significantly affect crop and livestock production (e.g., IPCC 2014). Different approaches have been
used to try to quantify this effect (see Mendelsohn and Dinar [2009, chap. 3] for a review). Early works focused on biophysical crop models simulating the impact of changes in weather on plants’ growth and input requirements (e.g., Adams et al. 1990; Kaufmann and Snell 1997). These techniques include only limited behavioral responses in farmers’ adaptation to climate change and, therefore, may risk overestimating negative impacts. More recent studies derive the effect of climate on crop yield (Schlenker and Roberts 2009; Welch et al. 2010; Lobell, Schlenker, and Costa-Roberts 2011) or farm profits (e.g., Deschênes and Greenstone 2007, 2012) by fitting statistical or econometric models to time series, cross-sectional, or panel data. There are strengths and weaknesses in each of these approaches: for example, while panel models can include location-specific fixed effects to absorb possible time-invariant omitted variables, identification rests on random year-to-year weather shocks, which are different from permanent shifts in climate (Fisher et al. 2012).

Among the economic analyses, the Ricardian (or hedonic) method, introduced by Mendelsohn, Nordhaus, and Shaw (1994), has gained considerable prominence. In recent years, this approach has been applied to various countries across the globe, including the United States (e.g., Schlenker, Hanemann, and Fisher 2005, 2006), Brazil (Timmins 2006), Germany (Lang 2007), Latin America (Seo and Mendelsohn 2008), and Africa (Seo et al. 2009). The Ricardian method is based on the notion that, in a competitive market, the value of farmland reflects the discounted sum of the expected future profits that can be derived from it (Ricardo 1817). Estimation is typically implemented using data aggregated over counties or large regions. By regressing land prices on climatic measures and a set of exogenous control variables, this technique estimates the impact of climate on farmers’ expected incomes by relying on the cross-sectional variation observed in the current climate. This model is most commonly estimated using cross-sectional data as climate has not changed enough over time to allow the identification of its effect in any given location.

The major advantage of the Ricardian approach is that it automatically captures adaptation, since farmers adjust inputs and outputs to match local conditions. Three major drawbacks are (a) the implicit assumption of fixed prices, (b) possible omitted variables (an issue that typically affects all cross-sectional analyses), and (c) potential aggregation bias. Of these issues, fixed prices, set at the global level, are a common assumption in most studies that use a partial-equilibrium setting. Similarly, omitted variables, while not amenable to direct testing, tend to be of a lesser concern given the robustness of the observed relationship across years and settings (e.g., Schlenker et al. 2006). In contrast, data aggregation may conceal nonlinear effects and farm-level heterogeneity resulting in biased parameters and subsequent predictions (e.g., Theil 1954). Maybe surprisingly, almost all prior studies have employed county- or regional-level data (e.g., Mendelsohn et al. 1994; Schlenker et al. 2005, 2006; Mendelsohn and Reinsborough 2007; Lang 2007; Seo and Mendelsohn 2008; Seo
et al. 2009), but none have yet tested the effect of the aggregation process on the parameter estimates and on the resulting projections of climate change impacts.¹

In light of these issues, this study makes three main contributions to the literature. First, we test for aggregation bias by comparing the estimates resulting from a unique panel of farm-level data with those obtained after aggregating the same data to the conventional county level in order to replicate previous findings. This test reveals a strong aggregation bias in both the coefficient estimates and in the resulting projections of climate change impacts. Second, in line with the literature on plant physiology (e.g., Monteith 1977; Morison 1996), our farm-level analysis estimates a significant interaction effect between precipitation and temperature in determining land values. This effect, typically ignored in previous Ricardian studies, disappears when the same data are aggregated at the county level. Third, we test for functional form misspecification by estimating the first semiparametric Ricardian model on farm-level data. In our application this flexible functional form model does not yield results that are significantly different from those obtained using the simpler, parametric model.

Aggregation bias is a long-standing issue in econometrics, recognized since the seminal works by Theil (1954), Grunfeld and Griliches (1960), and Feige and Watts (1972). While in linear models this issue can be resolved by using appropriate weights, in nonlinear specifications the aggregation process typically produces biased coefficients and predictions (Lewbel 1991; Garderen, Lee, and Pesaran 2000; Imbs et al. 2005). As Ricardian analyses typically use aggregated information and report strong nonlinear climatic effects, it is of interest to test whether these results are robust to aggregation bias. We compare farm-level and county-level approaches to assess the suitability of aggregate data by (a) evaluating the parameter estimates of the climatic variables and by (b) measuring the predicted impact of climate change on agriculture. Such a comparison exposes strong aggregation bias with severe implications for predictions: on average, climate change impacts estimated on aggregated data differ by a factor of three compared with those derived from farm-level information. Our results also indicate that this bias is most probably caused by the fact that aggregated data do not adequately represent the fine variation in local climate experienced by each farm within a county.

Since farmland values are the discounted sums of future profits, any factor that affects crop productivity and yield should also affect farmland values. Crop research

¹. To our knowledge, the only Ricardian model estimated on farm-level data so far is the one presented by Schlenker, Hanemann, and Fisher (2007). Other papers used farm-level information on yield (e.g., Welch et al. 2010) or farm revenues (e.g., Mendelsohn and Dinar 2009; Wang et al. 2009), but the standard Ricardian approach requires farmland value data (analyses of farm net revenues are sometimes referred to as semi-Ricardian approaches; McKinsey and Evenson 1998).
has shown that plant yield response to weather and climate is highly nonlinear and includes significant interaction effects between temperature and precipitation (e.g., Hillel and Rosenzweig 2010; Welch et al. 2010). Surprisingly, most Ricardian studies (e.g., Mendelsohn et al. 1994; Schlenker et al. 2005, 2006) do not document such an interaction but rather assume the impact of temperature and precipitation to be additively separable. Additive effects are at odds with plant physiology, since increased heat generates higher demand for water in crop development (e.g., Monteith 1977; Morison 1996). Our farm-level analysis reconciles the Ricardian approach with the literature on plants and crops growth by confirming a significant interaction effect: precipitation is more valuable when temperatures are high. Similarly, temperature has a positive effect on land value only if there is enough precipitation to prevent possible droughts. We observe only the interaction effect in our farm-level data set, again highlighting the importance of using micro-level data. This result is robust in a variety of settings, including different data sets, climate definitions, and estimation methods.

A related issue is that Ricardian analyses typically assume climatic effects to have simple quadratic forms (e.g., Mendelsohn et al. 1994; Schlenker et al. 2005, 2006). However, previous research has shown that in hedonic models restrictive parametric specification can rarely be justified a priori (e.g., Cropper et al. 1988; Ekeland, Heckman, and Nesheim 2002, 2004) and that semi- and nonparametric alternatives can provide several advantages (Anglin and Gencay 1996; Parmeter, Henderson, and Kumbhakar 2007; Bontemps, Simioni, and Surry 2008). In addition, findings reported by Deschénes and Greenstone (2012) seem to indicate that the predicted impacts of climate change on farm profits are heavily dependent on the functional form assumed for the climatic and control variables. Therefore, we test for functional form misspecification arising from omitted nonlinear effects by estimating a semi-parametric farm-level Ricardian model. Compared with the parametric regression, this approach provides a superior fit and reveals an even stronger interaction between rainfall and temperature. However, climate change impact predictions are not significantly different from those obtained using the simpler specification.

2. Mendelsohn and Reinsborough (2007) and Seo et al. (2009) do include interaction effects but represent climate using temperature and precipitation during the months of January, April, July, and October, rather than degree days and precipitation in the growing season as recommended by Schlenker et al. (2006) and extensively applied thereafter (e.g., Deschénes and Greenstone 2007, 2012; Lang 2007; Schlenker et al. 2007; Fisher et al. 2012). An issue with using monthly averages is that the high cross-sectional correlation that characterizes these variables significantly limits the interpretability of the resulting interaction terms (in our sample, for instance, the correlations between the average temperature in October with the one in January, April, and July are, respectively, 0.93, 0.97, and 0.91).
Our empirical application covers farms located in Great Britain (GB). While GB is smaller than the spatial extent of other Ricardian analyses, its geographic position (surrounded to the south by the Gulf Stream and to the north by sub-Arctic waters) generates a diversity of micro-climates, yielding a wide range of variation in temperature and precipitation. Obviously, heterogeneity in climate is necessary to obtain precise estimates. Focusing on a narrow spatial scale that has significant variation in climate is even preferable as other, potentially confounding, variables are more homogeneous. In the extreme, having identical farms that only differ in climate would be the best-case scenario for identifying the effect of climate on land values. Limited spatial scale can therefore be considered an advantage rather than a constraint on the analysis. However, the major benefit arising from focusing on GB is the availability of accurate local climate measurements derived by one of the most dense weather station networks in the world, comprising 540 temperature and 4,400 rainfall stations (Perry and Hollis 2005). Comparison with the PRISM data (Di Luzio et al. 2008) used in the most recent Ricardian analyses (Deschênes and Greenstone 2012; Fisher et al. 2012) reveals that the number of temperature stations per square mile is roughly twice that of the United States while the number of precipitation stations is more than 20 times higher. Given that precipitation and (to a lesser extent) temperature are notoriously highly variable over space (e.g., Baigorria, Jones, and O’Brien 2006; Mendelsohn et al. 2007), this substantial increase in accuracy is crucial for obtaining precise estimates of the farm-level climatic conditions and to effectively test for aggregation bias. Conversely, a sparse network of weather stations would introduce measurement error in local climatic values, thereby undermining the superiority of farm-level estimates over their county-level counterparts.

1. THE DATA
This analysis integrates multiple sources of information expressed at different spatial scales to generate a database covering the whole of GB. These data are detailed throughout the remainder of this section.

Land Value Data
Data on land value are derived from the Farm Business Survey and the Scottish Farm Accounts Survey panels which, sampled annually, include information on the physical characteristics and economic performance of farm businesses throughout Great Britain. Farms are retained in the sample for several years, with only 10% of them being replaced in each survey. The two Farm Surveys (FS) include a specific figure for land value, which excludes buildings and other improvements used for agriculture (it includes, however, the value of buildings and dwellings older than 30 years) and reflects the expected sale value assessed by professional farmland sales agents based on agricultural land sales taking place in the area where the farm is
located. Since these estimates are not revised each year, we discard from the analysis all records for which the farmland value does not change from the previous year, as this indicates that the value has not been updated over that period. Therefore, while most Ricardian models are based purely on cross-sectional information, our data are an unbalanced panel, which includes both spatial and time variation in farmland price. The FS also contains the location of the farm on a $10 \times 10$ km grid square basis, which we use to link farm value to environmental and climatic characteristics. In this analysis we consider 10 years of FS data, from 1999 to 2008, consisting of approximately 2,500 farm records each year. Farms included in the panel comprise a variety of land uses, including arable crops, livestock pasture, and forestry. Eliminating farms smaller than 30 hectares (ha) as well as those for which the land value or the location are missing leaves about 9,500 observations for analysis.

**Climatic Variables**

Temperature and precipitation are represented by the $5 \times 5$ km grid cell data available from the UK Meteorological Office archive (Met Office, http://www.metoffice.gov.uk/). As previously mentioned, these data are derived from one of the most dense networks of weather stations in the world, which includes, on average, one temperature station every $20 \times 20$ km (540 stations) and one rainfall station every $7 \times 7$ km (4,400 stations). The process used to derive the $5 \times 5$ km grid climate data published by UK Met Office is based on multiple regressions with inverse distance-weighted interpolation and takes into account geographic and topographic factors, validated by randomly excluding 10% of the stations and predicting for their values (Perry and Hollis 2005). This approach yields an out-of-sample root mean square error (RMSE) of 0.36°C for the monthly mean temperature (3.5% of the mean value) and of 16 mm (3.6%) for the total monthly precipitation. This strong

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3. Therefore, it is a function of both the discounted value of agricultural production and the potential for other uses such as urban development. In our model we control for this latter factor by including a semiparametric function of population density as explanatory variable.

4. As an example, consider a farm that is surveyed in the years 2000–2005. The farmland value is estimated to be £1,000 per hectare in year 2000, £1,500 in 2001, 2002, and 2003, and £1,800 in 2004 and 2005. In this case we include in the analysis only the records relative to years 2000, 2001, and 2004. However, as a robustness test we also estimate the model including the years in which the farmland value remains constant showing that the results remain essentially unchanged.

5. In farms with only a small amount of owned land, farmland price per hectare can be significantly inflated when the property contains buildings or houses older than 30 years, since their value is included in the farmland price. This effect will be obviously diluted in large farms. Therefore, to reduce this source of noise in the data we eliminate all farms in which the owned land is smaller than 30 hectares. In the robustness tests section, however, we also report the estimates obtained by including all farms and show that our findings remain consistent.
predictive performance reassures us of the ability of the $5 \times 5$ km climatic data to accurately represent the local conditions faced by the individual farmers within our sample. This feature is essential to effectively test for aggregation bias. Data collected on a sparser network of weather stations, in fact, would introduce measurement error in local temperature and precipitation values, undermining the superiority of farm-level estimates over their county-level counterparts.

As per Deschénes and Greenstone (2012) and Fisher et al. (2012), for each observation we calculate climatic variables as averages over the 30-year period 1971–2000. Temperature has been included in Ricardian models as monthly or seasonal averages (Mendelsohn et al. [1994] and Seo et al. [2009] consider average temperature in the month of January, April, July, and October) or as the number of degree days in the growing season between 5.5°C and 32°C (Schlenker et al. 2006; Deschénes and Greenstone 2007, 2012; Fisher et al. 2012). The concept of degree days is derived from the agronomic literature and reflects the fact that plant growth is linear in temperature only within a certain range, with temperatures below this interval being irrelevant for crop development and temperatures above that threshold being potentially harmful. Schlenker et al. (2006) show how this strategy is superior to including monthly averages, mainly because temperatures in different months can be highly correlated with each other (e.g., in our climatic data the correlation of the average temperature in October with the one in January, April, and July are, respectively, 0.93, 0.97, and 0.91). As in previous contributions, we consider only the degree days during the main growing season, defined for GB as the months from April to September. To derive degree days, we use the common assumption that, during the day, temperature ($temp$) follows a sinusoidal function (Schlenker and Roberts 2006):

$$temp = 0.5[temp_{\text{max}} - temp_{\text{min}}]\sin(\chi) + temp_{\text{min}} + 0.5[temp_{\text{max}} - temp_{\text{min}}],$$

where $\chi$ is defined between $-1/2\pi$ and $3/2\pi$ and $temp_{\text{min}}$ ($temp_{\text{max}}$) is the minimum (maximum) temperature within the day. Since data on the minimum and maximum temperature in each day of the year are not available, we use average monthly minimum and maximum temperature to compute the number of degree days. For con-

6. This is, not surprisingly, just an approximation. Recent literature (e.g., Schlenker and Roberts 2006) shows how the effect of temperature on yield can present nonlinearities even within the two thresholds. However, since the objective of a Ricardian analysis is not to analyze crop growth but to understand the effect of climate on land value, the linearity assumption to compute degree days still constitutes a reasonable approximation.

7. We do not use the approach developed by Thom (1966), commonly implemented on US data, because his formula is based on the average monthly temperature and its standard deviation. On the other hand, we have information on the average monthly minimum temperature and the average monthly maximum temperature. This latter information provides a better representation of the GB climate (Hitchin 1983).
sistency with previous analyses and also following the standard in GB (e.g., UK Met Office, http://www.metoffice.gov.uk/) we employ 5.5°C as our lower threshold. Considering the upper threshold after which temperatures become harmful, recent studies on crop yield (e.g., Schlenker and Roberts 2009) suggest that 32°C may be too high and that a value of 29°C/30°C may better represent crop development. In any case, the relatively cold climate characterizing GB’s growing season makes this latter threshold not relevant for our study. In fact, our highest recorded monthly average temperature is 27.31°C in July 1983, which is well below even the most conservative threshold of 29°C. Note that this is not the highest 1971–2000 climatic average, but the highest monthly average within this time span (the highest monthly 30-year average in our data is barely 23°C, occurring in the month of July).

Considering rainfall, as in previous studies we include the total precipitation in the growing season. Finally, as the $5 \times 5$ km grid of climatic data and the $10 \times 10$ km grid of farm location data share the same origin, we convert degree days and precipitation from $5 \times 5$ km to $10 \times 10$ km grid squares to match the resolution of the farm location data by using arithmetic averages. Figure 1 illustrates the climatic variability in our data, plotting the map of degree days and precipitation and including also county boundaries.

Figure 1. Degree days and rainfall during the growing season in Great Britain. $10 \times 10$ km grid squares, Met Office climate 1971–2000 data corresponding to the growing season (April–September). White lines indicate county (NUTS3) limits.
Environmental and Other Control Variables

Besides climate, several other factors can significantly influence farmland values. Considering soil characteristics, we include soil texture as the share of fine (clay share between 35% and 60%), medium fine (clay <35% and sand <15%), medium (clay between 18% and 35% and sand >15% or clay between 18% and 35% and sand <65%), coarse (clay <18% and sand >65%) and peaty soils, and the depth to rock. These variables are derived from the 1 km grid square data given in the European Soil Database (ESDB) maintained by the European soil data center (http://eusoils.jrc.ec.europa.eu/). We also include average slope (derived from the Ordnance Survey, Digital Terrain Model, http://www.ordnancesurvey.co.uk/oswebsite/), representing the suitability of land for machinery operations, and population density (computed from 1990 and 2000 census data, http://casweb.mimas.ac.uk/) to capture the opportunity value of converting land to residential use, distance to markets and the availability of amenities or off-farm work for the members of the farmer’s family. Finally, to capture the impact of location-specific policies we include the share of each 10 km grid square classified as National Park, Nitrate Vulnerable Zone (NVZ), or Environmentally Sensitive Areas (ESA) in each year. NVZs, established in 1996 and extended in 2003 and 2008 to cover more than 70% of English farmland, are designed to reduce surface and groundwater nitrate contamination by imposing certain restrictions on the agricultural activities of farms within their boundaries (e.g., limiting the amount of fertilizer to be used on fields, regulating the storage of organic manure, etc.). ESAs, introduced in 1987 and extended in subsequent years, are intended to safeguard and enhance areas of high landscape, wildlife, or historic value. Unlike NVZs, participation in ESA schemes is voluntary, and farmers receive monetary compensation for engaging in environmentally friendly farming practices, such as converting arable land to permanent grassland, establishing hedgerows, and so forth.

Farm-Level Data Descriptive Statistics

Descriptive statistics for these variables are reported in table 1. The distribution of farmland values appears to be highly skewed with a long right tail, which could support a lognormal distribution as, for example, implemented by Schlenker et al. (2006). Considering rainfall levels, although GB covers a relatively modest area compared to those analyzed in other Ricardian studies (e.g., United States, Brazil), its location between the warm waters of the Gulf Stream to the West and the cold climates of Scandinavia to the East means that it exhibits a wide range of precipitations across the growing season (from 244 mm to 1,434 mm). This range actually exceeds that reported for the rainfed US counties (from 332 mm to 982 mm) analyzed by Schlenker et al. (2006). Indeed, accounting for irrigation (Schlenker et al. 2005) is not necessary in GB, since most farmland is rainfed (less than 1% of the farms in our sample use any irrigation at all). Furthermore, temperatures rarely reach particularly
high values, with total degree days in the growing season ranging between 654 day °C and 1,639 day °C.

Aggregation
In order to obtain units of aggregation comparable with those examined in previous Ricardian studies, we aggregate our farm-level values to the official “third level” Nomenclature of Territorial Units for Statistics (NUTS) areas as defined by the European Union (which roughly correspond to GB counties). Their size varies considerably, ranging from about 40 km² to more than 10,000 km², with an average of 1,814 km² (for comparison, the average area of US counties is about 3,000 km²). We assign each farm to a county based on its spatial location and compute the aggregated land values as farmland-area weighted averages. Similarly, we aggregate climatic and control variables using as weights the amount of agricultural land within each 10 km grid square included in a county. This leads to over 30 farm records for each county (with an average of 11 farms in each year per county) and a total of 848 aggregated observations.
Descriptive Statistics of the Climatic Variables Aggregation

The statistics reported in table 2 measure the impact of the aggregation process on the accuracy of the climatic variables. The upper part of the table reports the subdivision of the total variability (sum of squares) in within-counties and between-counties variation. The higher the within-county variation, the greater is the share of climate variability lost through the aggregation process. The within-county variation for degree days and temperature is, respectively, 20% and 37% of the total variation, indicating that both variables vary considerably at this level. In line with the previous literature, precipitation appears to be the most spatially variable climatic factor (e.g., Mendelsohn et al. 2007; Auffhammer et al. 2013). The between-county statistics, reported in the middle of table 2, denote the variation in climate retained in the aggregated data, represented as county-level averages. Considering degree days, the values range between 756 day °C and 1,611 day °C (with a mean of 1,290 day °C), which is very similar to that observed for farm-level data. However, precipitation during the growing season presents a minimum value of 275 mm and a maximum of 811 mm, which is considerably lower than the highest value observed on the farm-level data (1,434 mm). Again, this can be explained by the high spatial variability of rainfall, which causes some of the extreme values observed in farm-level data to be lost in county-level statistics. The lower section of table 2 reports within-county sta-

Table 2. Descriptive Statistics of the Climatic Variables Aggregation

<table>
<thead>
<tr>
<th>Sum of Squares</th>
<th>Within</th>
<th>Between</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>Degree days (×10,000 day °C)</td>
<td>971 (19.6%)</td>
<td>3,994 (80.4%)</td>
<td>4,965</td>
</tr>
<tr>
<td>Precipitation (×10,000 mm)</td>
<td>636 (37.4%)</td>
<td>1,065 (63.6%)</td>
<td>1,701</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Between-county statistics:</th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean precipitation (mm)</td>
<td>400.80</td>
<td>275.70</td>
<td>811.00</td>
</tr>
<tr>
<td>Mean degree days (day °C)</td>
<td>1,290.00</td>
<td>756.90</td>
<td>1,605.00</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Within-county statistics:</th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Range of precipitation (mm)</td>
<td>157.50</td>
<td>2.09</td>
<td>1,075.00</td>
</tr>
<tr>
<td>Range of degree days (day °C)</td>
<td>230.40</td>
<td>1.00</td>
<td>801.70</td>
</tr>
</tbody>
</table>

Note.—Statistics refer to climatic conditions calculated as the weather average from year 1970 to year 2000 ( indicate the sample mean). The sum of squares relates to both within- and between-county variation. Between-county statistics denote the climatic conditions observed on aggregated county-level data expressed as the average climate for each county. Within-county statistics indicate the loss of climatic variability due to the aggregation process, represented as the range of variation of climate within counties.
tistics, indicating the heterogeneity in climate that is concealed by the aggregation, represented as county-level ranges of variation. Within the average county, degree days and precipitation vary by about 230 day °C and 150 mm, respectively. This loss of climatic information is substantial and corresponds, in turn, to about 22% and 15% of the range of values observed across the entirety of GB. In addition, there is also considerable variation around this mean, with some counties presenting a relatively homogeneous climate while others exhibit strong heterogeneity.

2. METHODOLOGY

2.1. The Ricardian Model

The Ricardian approach assumes that each farmer allocates land among different activities in order to maximize net revenues. Consequently, in a competitive market, farmland price equals the expected present value of the future stream of income derived from land. We assume that farms are atomistic and that input demand is small enough to not influence input prices. By the same token, idiosyncratic weather shocks do not influence the exogenous output prices since the quantity produced in GB is not large enough to affect the global market. The Ricardian approach does not model farmers’ land allocations, input, and output choices explicitly, but rather estimates the overall value of each land characteristic by specifying the hedonic, reduced form model:

\[ V_t = f(p, z, g), \]

where \( V_t \) is the farmland value per hectare in year \( t \), \( p \) = input and output prices expectations, \( z \) = climatic variables, \( g \) = all other exogenous factors, including soil types, terrain, and so forth, and \( f(.) \) is a functional form unknown a priori. As in most hedonic models, economic theory provides little guidance regarding the shape of this relation.

2.2. Testing for Aggregation Bias and Omitted Nonlinearities

Virtually all Ricardian analyses have translated equation (1) into an empirically tractable model by assuming a linear or semi-log specification with a quadratic formulation for the climatic variables (here degree days, \( dd \), and precipitation, \( prec \)) and a linear function for all other determinants. Findings reported by Schlenker et al. (2006) suggest that a log-transformation of the dependent variable outperforms a linear specification, since the distribution of land values is nonnegative and typically highly skewed. Estimation is normally implemented on data aggregated over counties or larger regions. As a starting point, we open our analysis by replicating such a conventional model, which has been implemented in the majority of Ricardian studies so far. This hedonic equation (model A) is specified as:

\[ \ln V_{ct} = \beta_0 + \beta_1 prec_c + \beta_2 dd_c + \beta_3 prec_c^2 + \beta_4 dd_c^2 + \gamma^t g_{ct} + d_{ct} + u_{ct}, \]
where $c$ indicates the county, $t$ indicates the time at which expectations are taken, $\beta_0, \ldots, \beta_4$ and $\gamma$ are the county-level parameters to be estimated, and $u_{c,t}$ is a residual component which we define as being the sum of a county-specific random effect and a residual, both normally distributed and uncorrelated ($u_{c,t} = \alpha_c + \varepsilon_{c,t}$). In our framework the vector $g_{c,t}$ includes population density ($d_{pop}$ and $d_{pop}^2$; see Schlenker et al. 2006), depth to rock ($d_{tr}$), slope, soil texture shares, National Park ($s_{park}$), ESA ($s_{esa}$), and NVZ ($s_{nvz}$) shares. As in most Ricardian models, price and other potential omitted variables are accounted for by including regional fixed effects (for England, Wales, and Scotland) and yearly fixed effects, represented by the term $d_{c,t}$.

This quadratic approximation with additively separable climatic effect (on the logarithmic scale) has been implemented in most applications (see Mendelsohn and Dinar [2009] for a review) because it allows the identification of “optimal” crop-growing conditions while maintaining simplicity in estimation. In this specification, climatic effects are multiplicative. For example, the marginal effect of precipitation is

$$\frac{\partial V_c}{\partial \text{prec}_c} = V_c(\beta_1 + 2\beta_3 \text{prec}_c).$$

This effect, therefore, depends on all the variables that determine the land value $V_c$. However, this formulation does not encompass all interactions among climatic variables. In fact, the sign of the marginal effect (3) depends solely on the term $\beta_1 + 2\beta_3 \text{prec}_c$, which contains only the parameters of precipitation itself, and none of those relating to other variables. This means that the optimal amount of rainfall will not depend on the level of temperature, and vice versa. This constraint might not necessarily be valid. For instance, agronomic experiments have shown that warmer conditions typically lead to an increase in crop requirements for water (e.g., Morison 1996).

The simplest approach to relaxing the assumption of additively separable climatic effects is to include an interaction term to equation (2), allowing the effect of precipitation and temperature to be mutually dependent. Therefore, we estimate our second specification (model B) as

$$\ln V_{c,t} = \beta_0 + \beta_1 \text{prec}_c + \beta_2 d_{dd} + \beta_3 \text{prec}_c^2 + \beta_4 d_{dd}^2 + \beta_5 \text{prec}_c d_{dd} + \gamma' g_{c,t} + d_{c,t} + u_{c,t},$$

There are good theoretical reasons to believe that even simple nonlinear relations, such as those represented by equations (2) and (4), are not robust to the aggregation process. In fact, even under very stringent conditions, recovering the farm-level parameters using a county-level regression would require the inclusion of squares and cross-products of the explanatory variables and very complex functional forms (Van Garderen et al. [2000] provide a few examples). Given that most Ricardian analyses have been implemented on aggregated data, it is important to investigate the size of any bias inherent in such approaches and its implication for the prediction of climate change impacts.
The simplest approach to test for aggregation bias is to reestimate model (4) using the same data, but disaggregated at the farm level, examining whether parameters and climate change impacts predictions are significantly different from those obtained with county-level data. The resulting specification (model C) can be written as

\[
\ln V_{i,j,t} = \alpha_0 + \alpha_1 \text{prec}_{i,j} + \alpha_2 \text{dd}_{i,j} + \alpha_3 \text{prec}^2_{i,j} + \alpha_4 \text{dd}^2_{i,j} + \alpha_5 \text{prec} \text{dd}_{i,j} + \xi' g_{i,j,t} + d_{j,t} + u_{i,j,t},
\]  

where \(i\) indicates the farm, \(j\) the 10 km grid square, \(\alpha_0, ..., \alpha_5\) and \(\xi\) are the farm-level parameters to be estimated, and all other terms are defined previously. We specify the residual component to include both a farm-level and a 10 x 10 km cell-specific random effect (\(u_{i,j,t} = w_j + \alpha_{i,j} + \varepsilon_{i,j,t}\)), to take into account that farms located within the same area may share common unmodeled factors that may significantly affect their land value. This is also a simple approach to account for spatial autocorrelation by allowing the residuals of the farms located within the same cell to be correlated with each other.\(^8\)

A drawback of this latter approach (and of any other strict parameterization) is that it constrains the effects to assume very specific functional forms. In such a model, climatic impacts are forced to be quadratic and their interaction is assumed to be linear. While these might be reasonable approximations, there is no theoretical justification underpinning such a rigid structure, which is mainly adopted for ease of estimation. Therefore, it is worth investigating possible functional form misspecification by using a more flexible model. Here we represent the relationships of interest via smooth functions, deriving an additive mixed model (AMM) which is our most general and last specification (model D):

\[
\ln V_{i,j,t} = f(z_{1,t}; z_{2,t}) + s_1(g_{i,j,t}) + \ldots + s_h(g_{i,j,t}) + d_{j,t} + u_{i,j,t},
\]  

In this model the joint effects of temperature and precipitation are encompassed by a multidimensional smooth function \(f(\cdot)\), which allows the estimation of flexible nonlinear relationships and interaction effects. The control variables are also included via smooth functions, \(s_1(\cdot), \ldots, s_h(\cdot)\), to capture possible nonlinear relations. How-

\(^8\) An alternative approach is using cluster robust standard errors, as implemented, among others, by Fisher et al. (2012) and Deschénes and Greenstone (2012). While this approach can be easily implemented for model C, to the best of our knowledge there is no established approach for deriving robust errors for additive models estimated via penalized likelihood (model D). Therefore, for ease of comparison we present the simplest specification with farm- and cell-specific random effects for both models. In the robustness test section, however, we present further specifications for model C. In addition to using cluster robust standard errors at the cell level, we also allow a stronger spatial autocorrelation by adding a further random effect term, grouping together clusters of nine cells. Results remain essentially unchanged.
ever, to maintain simplicity in the interpretation and avoid the well-known curse of dimensionality, their effects are assumed to be additively separable. The marginal effects of rainfall can be derived as

$$\frac{\partial V_i}{\partial \text{prec}} = V_i \frac{\partial f(\text{prec}, \text{dd})}{\partial \text{prec}}.$$  

(7)

Note that the sign of this marginal effect is a function of both precipitation and temperature. As a result, the model encompasses, in a flexible form, the interaction effects among all climatic factors. This is a very general specification and encompasses model C as a special case. Comparing the estimates from the two models allows us to test for omitted nonlinear relations.

3. EMPIRICAL APPLICATION

3.1. Estimation Results

We estimate models A (eq. [2]), B (eq. [4]), C (eq. [5]), and D (eq. [6]) via restricted maximum likelihood (REML). Here A, B, and C are standard linear regression models with random effects. Model D is implemented by representing the smooth functions as natural cubic splines, which fit third degree polynomial functions between a set of knots located between the range of values of each explanatory variable. The number and the location of the knots effectively determine the flexibility of each smooth function. We estimate the optimal number of knots (i.e., the optimal amount of smoothing) directly from the data by following the approach illustrated by Ruppert, Wand, and Carroll (2003) and Wood (2006), who suggest representing the smoothing splines as random effects (details are in the appendix, available online). This approach automatically reduces the smooth functions of the variables for which the optimal fit does not include any nonlinearity to standard linear forms. In the extreme, a model in which none of the nonlinear relationships are supported by the data will be reduced directly to a standard linear regression during estimation. The optimal level of nonlinearity of each smooth function is indicated by the “effective degrees of freedom” (EDF). The higher the EDF, the more nonlinear is the estimated function. An EDF equal to 1 suggests that the best smooth function representation is linear.

The parameter estimates and diagnostics of the four models are presented in table 3. The first column reports the coefficients of model A: the standard Ricardian regression based on county-averaged data. The estimated effect of degree days is always positive (with the quadratic effect being nonsignificant) and the effect of precipitation is negative with a quadratic shape. This is not entirely surprising, given the relatively wet and cold conditions that characterize GB. The coefficients of the control variables have intuitive signs. Better physical environments (lower slope and deeper soils) translate into higher land values. Finally, while not reported in the table to preserve space, the yearly fixed effects are also significant, highlighting the presence
## Table 3. Parameter Estimates and Diagnostics

<table>
<thead>
<tr>
<th></th>
<th>Model A:</th>
<th>Model B:</th>
<th>Model C:</th>
<th>Model D:</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>County Level</td>
<td>County Level</td>
<td>Farm Level</td>
<td>Farm Level</td>
</tr>
<tr>
<td></td>
<td>No Climatic</td>
<td>Climatic</td>
<td>Climatic</td>
<td>Semiparametric</td>
</tr>
<tr>
<td>Interaction</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Climate variables:</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Precipitation (prec)</td>
<td>.580 (.801)</td>
<td>.639 (.790)</td>
<td>−.583 (.233)*</td>
<td>. . .</td>
</tr>
<tr>
<td>prec^2</td>
<td>−7.756*** (2.130)</td>
<td>−10.299*** (2.561)</td>
<td>.253 (.559)</td>
<td>. . .</td>
</tr>
<tr>
<td>Degree days (dd)</td>
<td>1.217*** (.313)</td>
<td>1.112*** (.315)</td>
<td>.692*** (.122)</td>
<td>. . .</td>
</tr>
<tr>
<td>dd^2</td>
<td>−1.138 (1.125)</td>
<td>−1.125 (1.112)</td>
<td>−1.676*** (4.34)</td>
<td>. . .</td>
</tr>
<tr>
<td>dd × prec</td>
<td>. . .</td>
<td>−4.567 (2.633)</td>
<td>2.741** (1.022)</td>
<td>8.606***</td>
</tr>
<tr>
<td>Control variables:</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Slope</td>
<td>.045 (.031)</td>
<td>.057 (.031)</td>
<td>−.026** (.008)</td>
<td>1.000***</td>
</tr>
<tr>
<td>Depth to rock</td>
<td>−.001 (.002)</td>
<td>−.001 (.002)</td>
<td>−.000 (.000)</td>
<td>1.895</td>
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<tr>
<td>Pop. density</td>
<td>.091 (.217)</td>
<td>.139 (.216)</td>
<td>.398*** (.100)</td>
<td>3.751***</td>
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<tr>
<td>(dpop)</td>
<td>−.058 (.115)</td>
<td>−.081 (.114)</td>
<td>−.201*** (.059)</td>
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<tr>
<td>Share park</td>
<td>.747*** (.256)</td>
<td>.710** (.254)</td>
<td>.175** (.059)</td>
<td>.191** (.060)</td>
</tr>
<tr>
<td>Share NVZ</td>
<td>.012 (.049)</td>
<td>.011 (.049)</td>
<td>−.033* (.013)</td>
<td>−.031* (.013)</td>
</tr>
<tr>
<td>Share ESA</td>
<td>−.410*** (.174)</td>
<td>−.403* (.171)</td>
<td>.027 (.045)</td>
<td>.011 (.045)</td>
</tr>
<tr>
<td>Fixed effects</td>
<td>Yes***</td>
<td>Yes***</td>
<td>Yes***</td>
<td>Yes***</td>
</tr>
<tr>
<td>Soils shares</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes***</td>
<td>Yes***</td>
</tr>
<tr>
<td>Random effects:</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>County</td>
<td>.234</td>
<td>.230</td>
<td>. . .</td>
<td>. . .</td>
</tr>
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<td>Cell</td>
<td>. . .</td>
<td>. . .</td>
<td>.279</td>
<td>.271</td>
</tr>
<tr>
<td>Farm</td>
<td>. . .</td>
<td>. . .</td>
<td>.403</td>
<td>.402</td>
</tr>
<tr>
<td>Residuals</td>
<td>.274</td>
<td>.273</td>
<td>.184</td>
<td>.184</td>
</tr>
<tr>
<td>Model fit:</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>LogLik</td>
<td>−233.09</td>
<td>−229.71</td>
<td>−2,045.58</td>
<td>−1,966.49</td>
</tr>
<tr>
<td>AIC</td>
<td>523.18</td>
<td>519.43</td>
<td>4,153.16</td>
<td>3,998.97</td>
</tr>
<tr>
<td>BIC</td>
<td>660.79</td>
<td>660.70</td>
<td>4,375.02</td>
<td>4,235.24</td>
</tr>
</tbody>
</table>

Note.—Models A and B are estimated on county averages with 848 observations for a total of 102 counties. Models C and D are estimated on farm data with 9,506 observations for a total of 3,283 farms in 1,361 cells of 10 km square. All models estimated with restricted maximum likelihood. Yearly fixed effect and Scotland and Wales dummy variables statistically significant but not reported in the table to preserve space. In models A, B, and C the table reports the coefficient estimate (with standard error in parentheses) and the significance calculated with an approximate t-value conditional on the random effects (details in Pinheiro and Bates 2000). In model D the table reports the “effective degree of freedom” and the significance calculated with an approximate F-test (details in Wood 2006). In models A, B, and C precipitation and degree days are centered to the population means to reduce multicollinearity, and precipitation, degree days, and population density are divided by 1,000 to increase readability of the coefficients. LogLik = (restricted) log-likelihood, AIC = Akaike information criterion, BIC = Bayesian information criterion.

* Significant at the .05 level.
** Significant at the .01 level.
*** Significant at the .001 level.
of important differences among the (deflated) land values in different years, reflecting evolutions in market conditions, policy, and technology.\(^9\) Also the regional fixed effects are significant.

Model B, presented in the second column, also employs aggregated county-level data to test whether the interaction effect between degree days and precipitation is significant. The approximate \(t\)-test is \(-1.73\), with approximate \(p\)-value of \(.086\), which does not reject the null hypothesis of no interaction at the standard 5% level. In addition, the negative sign of the corresponding coefficient is counterintuitive. Previous crop studies (e.g., Monteith 1977; Morison 1996) demonstrated that the amount of water required for plant development increases with temperature, implying a positive rather than a negative interaction. Altogether, we conclude that county-level estimates suggest predominantly additive climatic effects, with a strong quadratic component for precipitation and without a significant interaction between precipitation and temperature. Overall, taking into account the wet and cold British climate, these conclusions are in line with those reported by previous Ricardian analyses (see Mendelsohn and Dinar [2009, chap. 7] for a review).

*Parameter Estimates and Diagnostics*

These results obtained on aggregated data are, however, overturned when individual farm records are analyzed. As the estimates of model C (third column) show, rainfall and degree days present strong nonlinear effects, with one quadratic term and the interaction term being highly statistically significant. The interaction is positive: consistent with the agronomic literature, the optimal amount of rainfall increases with temperature. Interestingly, the quadratic effect of precipitation is no longer significant, indicating that in model B some of the variation attributed to the interaction may have been captured by the quadratic coefficient.\(^{10}\) The estimates of the semiparametric model D, reported in the last column of table 3, are in line with those provided by the parametric model C. The EDF of the bivariate smooth function of temp-

\(^9\) While significant, yearly variation does not account for a large part of the variability in land values which, as one may expect, is mainly related to cross-sectional heterogeneity. For instance, in model A (county level) the share of the variation captured by the yearly fixed effects is only 2.5% of the total variation captured by the model, while in model C (farm level) this rises but only to about 6.5%.

\(^{10}\) We also tried to estimate a farm-level model with no interaction effect. In such a model the quadratic parameter of precipitation is still not significant. This indicates that the cause of this difference in statistical significance cannot be attributed to possible collinearity between the quadratic term and the interaction term but it is actually caused by the aggregation process. Results are not reported in table 2 to preserve space but are available from the authors upon request.
perature and precipitation is equal to 8.61, indicating strong nonlinear effects and interactions. For comparison, the bivariate smooth function corresponding to the climatic effects estimated in model C (i.e., two quadratic effects with a linear interaction term) would have an EDF equal to 5.11.

Figure 2 provides a graphical representation of the estimates produced by the semiparametric model. The left-hand panel represents with iso-value lines the joint effects of the climatic variables on land price. We only draw such contours for values of degree days and temperature observed within the estimation sample, as represented in the scatter plot in the right-hand panel. For example, in GB there are no areas with both relatively high temperature and high precipitation and, therefore, the top-right corner of the left-hand plot is blank. Furthermore, the distribution of the climatic variables appears to be highly skewed, with most farms located in areas characterized by relatively high temperature ($dd > 1,300$) and low precipitation ($prec < 500$). Therefore, the upper-left parts of the contour graphs are the most relevant for climate change predictions in GB (the next section shows how our sample of farms is representative of the overall conditions in the country). The contour plot shows a clear interaction effect. In the colder areas ($dd < 1,200$), abundant precipitation reduces agricultural land values, while in warmer areas ($dd > 1,400$) the crop requirement for water increases and the effect of rainfall becomes positive. Therefore, beyond a certain level, higher temperatures increase land values only if there is enough precipitation to prevent heat-related stress. This means that there is not a generalized, ideal level of temperature that defines the best crop-growing conditions (as implied in previous Ricardian studies) but, rather, that optimal temperature levels vary with the availability of precipitation. Similarly, the optimal level of precipitation depends on the level of temperature.

This interaction effect is analyzed in greater detail through the next two figures. Figure 3 represents the estimated impact of precipitation on land value for two levels of temperature. When temperature is low ($dd = 1,100$, left-hand panel), we

11. We cannot compare models C and D via a likelihood ratio test since the two models are not nested. However, the log-likelihood, the Akaike information criterion (AIC) and the Bayesian information criterion (BIC), reported at the end of table 3, suggest that the semiparametric specification provides a better fit. Ignoring this nonlinearity also comes at the cost of increasing the unmodeled spatial autocorrelation, which is reflected in the higher value of the cell-specific random component of model C compared to that of model D. This is consistent with Kostov’s (2009) findings, which show that flexible functional forms can significantly reduce residual spatial autocorrelation in farmland price modeling. While model D is more flexible, model C provides more robust predictions when applied outside the range of the data used for estimation. Therefore, we view the two models as complementary rather than competitive and we retain both for climate change impact projections.
Figure 2. The effect of temperature and precipitation on the logarithm of land price: contour plots with iso-value lines (left) and observed climate data (right). Left panel shows the estimated effect of precipitation and degree days on the logarithm of land value according to the semiparametric model D. Right panel shows the scatter plot of the values of precipitation and degree days within the farm-level sample.

Figure 3. The effect of precipitation on the logarithm of farmland value for different levels of temperature. Left panel shows the estimated effect of precipitation when temperature is low (1,100°C degree days in the growing season). Right panel shows the estimated effect of precipitation when temperature is high (1,500°C degree days in the growing season). Solid line = mean estimate according to the semiparametric model D; dotted line = ±1 standard error.
observe a strong negative effect of high precipitation that can be attributed to soil waterlogging, delayed ploughing and sowing, or to the negative effect that excess soil moisture can have on plant growth (e.g., IPCC 2014). However, as temperature increases, the relationship with rainfall becomes more moderate and in the warmest areas \((dd = 1,500,\) right-hand panel) higher precipitation has a positive effect on land values across the entire range of observed data. Moving to consider the effect of temperature, figure 4 represents the impact of degree days for two different levels of precipitation. In areas where rainfall is relatively low \((300 \text{ mm, left-hand panel})\) the positive effect of warmer temperatures on plant growth is offset by the increase in drought risk such that the resulting net effect on land value is not significant. However, in areas of higher precipitation \((500 \text{ mm, right-hand panel})\), increased water availability protects plants from heat stress, allowing temperature to have a strong and positive effect on land value.

Overall, the interaction effect between temperature and rainfall, which is positive and significant in the farm-level analyses, completely disappears (or even becomes negative) in county-level estimates. The main reason for the attenuation of this effect is that the aggregated county-level data ignore the heterogeneity in climate faced by individual farms within a county. Since both temperature and rainfall patterns are expected to vary as a result of climate change, this aggregation bias may have significant implications for climate change predictions. Such a hypothesis is tested in the

![Figure 4](image)

**Figure 4.** The effect of temperature on the logarithm of farmland value for different levels of precipitation. *Left panel* shows the estimated effect of temperature when precipitation is low \((300 \text{ mm in the growing season})\). *Right panel* shows the estimated effect of precipitation when temperature is high \((500 \text{ mm in the growing season})\). *Solid line* = mean estimate according to the semiparametric model \(D\); *dotted line* = ±1 standard error.
next section, which compares the projected climate change impacts derived from each of our four Ricardian regression models. However, we first report a series of checks to test whether our farm-level results are stable and robust to possible omitted-variable bias and to examine whether our aggregation bias evidence is consistent across specifications, data, and climate definitions.

3.2. Robustness Tests
We open this subsection by undertaking some robustness analyses on our farm-level estimates, testing for omitted variable bias and parameter stability. We then move to consider alternative Ricardian models to show that our aggregation bias findings are robust to a range of specifications and data definitions.

Concerns about potential omitted cross-sectional variables in Ricardian analyses have been raised by Deschênes and Greenstone (2007, 2012), among others. A panel fixed-effect estimator is not applicable here, since it would eliminate not only the potential bias but also all the cross-sectional variation upon which the parameters of the Ricardian model hinge. Ricardian analyses represent climate (as opposed to weather), through long-term averages of temperature and rainfall which, even in long panels, present a time variability that is almost negligible compared to the cross-sectional (spatial) variability. This means that fixed-effect estimators, intended to eliminate potential time-invariant omitted variables, cannot be implemented in this context because they would also remove the crucial spatial variation in climate. A second, related issue, concerns the distortions in the land market that various agricultural policies tend to create (e.g., Barnard et al. 1997). For instance, crop and environmental payments could be capitalized into the land price and, if correlated with climatic variables, introduce a bias in their coefficient estimates.

We address both issues by testing whether the parameters of degree days and precipitation are stable over time. If cross-sectional and time-varying omitted variable bias were a problem, then these coefficients should exhibit significant temporal variation, reflecting changes in agricultural prices and policies over time. Our sample provides a particularly rigorous basis for such a test as the 10 years covered by our data saw agricultural policies in GB change markedly, as a result of various reforms to the EU Common Agricultural Policy. These policy developments culminated with the introduction of decoupled single farm payments in 2005, replacing the system of area-based crop-specific subsidies in place since 1992. Input and output prices also changed dramatically during this period, with, for instance, cereal prices more than doubling during the period from 2007 to 2008.

These transformations have different effects across locations. For instance, an increase in the price of cereals may boost the arable area and revenues in lowland farms, while impinging negatively on upland sheep and beef farms through high feed-stuff prices. Similarly, many policies are area specific. NVZs, for example, have been significantly expanded in recent years. Therefore, evaluating parameter stability over
time is not simply a check against time-varying omitted variables but rather a stricter test for spatial effects varying over time. If these effects are correlated with climate, one would expect the smooth functions of temperature and precipitation to present significant variation over time in such unstable market conditions. To investigate this hypothesis, we choose the first year in our sample (1999) as a baseline and test for parameter stability comparing one year at a time via pairwise F-tests (Pinheiro and Bates 2000). Since the distribution of this test is only approximated, we compute it via 500 bootstrap repetitions. We test our final and more flexible specification, model D, and in order to use the standard inference for random-effect models, we define the spline bases of the model a priori and implement unpenalized estimation via REML. To attain a level of flexibility comparable to the optimal one selected by the penalized likelihood, we choose natural cubic splines with 4 knots for population density and 16 knots for the joint function of precipitation and rainfall, while all other variables are modeled as linear terms. Table 4 reports the results: none of the pairwise instability tests is significant at the 5% level. This is consistent with the null hypothesis of parameter invariance which, therefore, we find no evidence to reject. Overall, these results reassure us about the robustness of our climate impact estimates to omitted variable bias such as changes in prices and agro-environmental policies.

**Pairwise Stability Tests**

We now test whether the evidence of aggregation bias is consistent across different data, models, and aggregation methods. For each alternative specification, table 5 reports the interaction coefficients between precipitation and temperature estimated on county-level (model B) and farm-level data (model C). Since the two models have the same structure and variables, any difference in the parameter estimates can be attributed to the aggregation process. For comparison, the first row reports the coefficients of the original specification. In the second row we test the effect of using a different aggregation method. Rather than taking area-weighted averages of the land value of all farms located in each county, we use simple, unweighted averages. As can be seen, the aggregation bias becomes even larger, with the interaction effect remaining negative but now growing stronger and significant. This is not unexpected,

12. This F-test is conditional on the estimates of the random effects and it is only approximated. Nevertheless, it is the most appropriate in our context since, as shown by Pinheiro and Bates (2000), likelihood ratio tests should not be used for the significance of fixed parameters in random effect models. To obtain the empirical distribution of this test we use a bootstrap procedure specifically designed to take into account the hierarchical structure of random effect models, that is, we resample residuals hierarchically at the cell, farm, and observation levels (see Carpenter, Goldstein, and Rasbash 2003).
given that not taking into account the relative size of the properties can produce aggregated data that are less representative of the original population.

**Parameter Estimates according to Alternative Specifications**

The third row of table 5 reports the results obtained using a different climate specification. Rather than calculating climate as the average weather between the years 1971 and 2000, we follow Schlenker et al. (2006) and define climate as the average weather in the 30 years preceding each observation (e.g., for 2005 data the climate is defined as the average between the years 1975 and 2004). This means that we introduce some temporal variation that allows climate to change somewhat from year to year in each cell or county. The resulting coefficients are very similar to those in the baseline approach, suggesting that our conclusions are robust to different definitions of climate.

In the fourth row of table 5 we reestimate the models including all observations in which the farmland value is not updated in that year. Such an approach might be justifiable if replicated entries reflect periods over which owners do not perceive significant changes in their property value (as opposed to a failure to update value changes). While the magnitude of some of the climate coefficients appears to slightly increase, the results are consistent with the baseline specification in that we observe a

<table>
<thead>
<tr>
<th>Years</th>
<th>$F$-test</th>
<th>$p$-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>1999 and 2000</td>
<td>0.58</td>
<td>0.802</td>
</tr>
<tr>
<td>1999 and 2001</td>
<td>1.76</td>
<td>0.084</td>
</tr>
<tr>
<td>1999 and 2002</td>
<td>1.19</td>
<td>0.296</td>
</tr>
<tr>
<td>1999 and 2003</td>
<td>1.75</td>
<td>0.088</td>
</tr>
<tr>
<td>1999 and 2004</td>
<td>1.12</td>
<td>0.258</td>
</tr>
<tr>
<td>1999 and 2005</td>
<td>1.64</td>
<td>0.084</td>
</tr>
<tr>
<td>1999 and 2006</td>
<td>1.57</td>
<td>0.092</td>
</tr>
<tr>
<td>1999 and 2007</td>
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<td>0.258</td>
</tr>
<tr>
<td>1999 and 2008</td>
<td>1.14</td>
<td>0.314</td>
</tr>
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</table>

Note.—Test on model D (see table 3) estimated only on those farms that are present in both years, with 4 knots for population density and 16 knots for the joint effect of rainfall and temperature. The approximated $F$-statistics test the stability of the climate parameters from one year to the other and are conditional on the random-effect estimates, as suggested in Pinheiro and Bates (2000). Approximated $p$-values calculated with 500 bootstrap repetitions maintaining the hierarchical structure of the data following the approach introduced by Carpenter, Goldstein, and Rasbash (2003).
Table 5. Interaction Effect between Precipitation and Temperature according to Alternative Specifications

<table>
<thead>
<tr>
<th>Specification</th>
<th>County-Level (Model B)</th>
<th>Farm-Level (Model C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(1) Base specification (only farms bigger than 30 ha, climate 1971–2000, area-weighted aggregation)</td>
<td>-4.57 (2.63)</td>
<td>2.74** (1.02)</td>
</tr>
<tr>
<td>(2) Different aggregation method (aggregating data by using unweighted arithmetic averages)</td>
<td>-8.10** (2.75)</td>
<td>. . .</td>
</tr>
<tr>
<td>(3) Different climate specification (climate calculated as the average weather in the 30 previous years)</td>
<td>-.23 (2.46)</td>
<td>3.91*** (.87)</td>
</tr>
<tr>
<td>(4) Including not updated values (including observations in which the land value is not updated in that year)</td>
<td>-.92 (2.85)</td>
<td>3.16** (.99)</td>
</tr>
<tr>
<td>(5) Including also small farms (including all farms bigger than 5 ha)</td>
<td>-4.55 (2.77)</td>
<td>2.59* (1.08)</td>
</tr>
<tr>
<td>(6) Including all farms (including all farms, even farms smaller than 1 ha)</td>
<td>-1.69 (3.47)</td>
<td>.73 (1.39)</td>
</tr>
<tr>
<td>(7) Larger spatial autocorrelation (including an additional random effect term grouping nine 10 km cells)</td>
<td>. . .</td>
<td>2.56* (1.27)</td>
</tr>
<tr>
<td>(8) Non-Gaussian errors and more general correlation (model estimated using cluster-robust covariance matrix at the cell level)</td>
<td>. . .</td>
<td>2.94* (1.47)</td>
</tr>
<tr>
<td>(9) Generalized residuals and larger spatial correlation (model estimated using cluster-robust covariance matrix at the country level)</td>
<td>. . .</td>
<td>2.94 (2.31)</td>
</tr>
<tr>
<td>(10) Excluding covariates 1 (eliminating from the model the strongest control variable: population density)</td>
<td>-4.36 (2.60)</td>
<td>2.69** (1.03)</td>
</tr>
<tr>
<td>(11) Excluding covariates 2 (eliminating from the model population density, depth to rock, and slope)</td>
<td>-3.36 (2.54)</td>
<td>2.92** (1.02)</td>
</tr>
<tr>
<td>(12) Excluding areas with the most favorable climate (eliminating all farms for which $dd &gt; 1,400$ and $prec &gt; 350$)</td>
<td>-4.90 (2.87)</td>
<td>3.65** (1.16)</td>
</tr>
<tr>
<td>(13) Excluding large counties (eliminating the largest county in each one of the three GB countries)</td>
<td>-5.22 (2.64)</td>
<td>4.08** (1.11)</td>
</tr>
<tr>
<td>(14) Using county-level climate (using county-level climate data on farm land value data)</td>
<td>. . .</td>
<td>.34 (1.18)</td>
</tr>
</tbody>
</table>

Note.—Coefficients estimated via restricted maximum likelihood (REML) and defined as in table 3. Standard errors conditional to the random effects in parentheses.

* Significant at the .05 level.
** Significant at the .01 level.
*** Significant at the .001 level.
strong, positive, and significant interaction effect on farm-level observations and no interaction on county-level data.

Rows 5 and 6 of table 5 report results obtained by broadening the farm sample to include very small farms. Recalling section 2, the rationale behind limiting our analysis to properties larger than 30 ha is that our definition of farmland value includes the value of buildings and houses older than 30 years. While this is not a problem for large farms, very small properties with old household buildings can present a significantly inflated farmland value per hectare. However, as shown in the fifth row, including all farms larger than 5 ha (3,801 farms) does not significantly affect the estimated climatic coefficients. The sixth row shows that even encompassing all properties in the FS sample (4,044 farms), including those smaller than 1 ha, does not change the sign and the magnitude of the coefficients, although the interaction effect becomes nonsignificant because the additional noise introduced the data.

In row 7 of table 5 we allow for a stronger spatial autocorrelation in the farm-level model, including an additional random effect term grouping together clusters of nine 10 × 10 cells (total area: 900 km²). While the magnitude of some of the interaction coefficient slightly decreases, the parameter is still positive and significant at the 5% level.

In row 8 we allow for a more general form of spatial correlation, departing from the normality assumption typical of random effect models. We estimate the model with ordinary least squares but calculate the standard errors using a cluster-robust covariance matrix at the cell level as in Fisher et al. (2012) and Deschénes and Greenstone (2012). Again, results are consistent with the base specification. Finally, in row 9 we combine departure from normality with an even larger spatial autocorrelation, using a cluster-robust covariance matrix at the county level. While allowing a very general structure of the residuals generates large standard errors because of the relatively high collinearity between rainfall and temperature, results remain essentially unchanged.

Even though the stability tests reported in table 4 showed no bias arising from omitted spatial effects varying over time, it still possible that some omitted and time-constant variables may be affecting our estimates. As explained above, fixed effects cannot be used to address this concern as they would remove most of the climatic variation on which the estimation of the temperature and precipitation coefficients depends. However, we can examine whether the climate parameters vary if some of the control variables we have in the model are removed. If results are stable, we may expect that they will also be robust to unobserved variables. In row 10 of table 5, we report our estimates after removing population density, and in row 11 after additionally excluding the depth to rock and slope variables. Results show that, even without these important control variables, the climatic coefficients remain very stable in both farm-level and county-level specifications.
Since the effect of precipitation is positive for a limited part of our sample (circa $dd > 1,400$), one may wonder if this is due to some omitted variable that is correlated with the locations characterized by high precipitation and high temperature. To address this issue, we removed from the sample all farms for which $dd \geq 1,400$ and $prec \geq 350$ (290 farms in total, almost 10% of our sample). Most of these farms are located in the Southwest of England and in the South of Wales. Climatic parameters, reported in row 12 of table 5, again remain consistent, with a positive and significant interaction on farm-level data and a negative and borderline significant effect on county-level models.

One may wonder if the aggregation bias is mainly driven by the presence of some large and climatically heterogeneous counties. To test this issue, in row 13 we re-estimate our models after eliminating all farms located within the largest counties in England (North Yorkshire), Wales (Southwest Wales), and Scotland (Caithness, Sutherland, Ross, and Cromarty). These counties include 377 farms, corresponding to about 12% of our data. The results on both farm-level and county-level data are not significantly different from those obtained using the full sample.

All the robustness tests confirm the presence of aggregation bias. While farm-level results, in line with the literature on plant physiology, estimate a significant interaction effect between temperature and precipitation in determining land profitability, county-level analyses provide a different picture with essentially precipitation and temperature being additively separable. Is this bias caused by grouping together properties with different land values, or by the cruder representation of climate? In order to answer this question, in row 14, which completes table 5, we report the estimates of a farm-level model that represents climate using the values of rainfall and precipitations calculated for the aggregated data, that is, county-level weighted averages. The resulting coefficients are indeed biased and similar to those estimated on aggregated data with, in particular, the interaction effect being nonsignificant and the quadratic precipitation term being strongly significant (latter term not reported in the table to preserve space but available upon request). This shows that not taking into account the important within-county variation in climate (previously illustrated in table 2) may well be the main cause of the bias we detect on the models estimated on aggregated data.

4. CLIMATE CHANGE IMPACT PREDICTIONS

We combine the estimates presented in the previous section with the recently released UK Climatic Projections 2009 (UKCIP09; UKCIP 2009, ukclimateprojections.defra.gov.uk) to project the impact of climate change on agriculture in GB and to test whether aggregation bias has any implication for predictions. Specifically, we use the UKCIP09 projected changes in monthly average minimum temperature, maximum temperature, and precipitation in the medium level emission scenario (corresponding to the SRES A1B in the IPCC Special Report on Emissions Scenarios;
for the climate in the years 2020–49. These data are available on 25 × 25 km grid squares covering the entire United Kingdom. As suggested by Auffhammer et al. (2013), we derive the values of degree days and precipitation in the climate change scenarios by applying projected changes to a historical baseline. Here we use the 10 × 10 km Met Office historical averages for the years 1961–90, which are the baseline climatic conditions identified by the UKCIP09.

To derive the impact of climate change, we predict log-agricultural land price under both the baseline (1961–90) and the climate change scenario (2020–49). The only difference between the two scenarios is climate: all other determinants (soil, population density, etc.) are kept constant at their 2008 values, the last year of our farm data. Consequently, we do not consider other factors that are likely to change in the future, such as technology, prices, land use, and population. Therefore, our results are intended to estimate how climate will affect agriculture ceteris paribus and should not be interpreted as predictions of the future. Table 6 reports descriptive statistics for the climatic and environmental determinants in the baseline and climate change scenarios. The ranges of the exogenous variables are similar to those of the data used for estimation (see table 1), indicating that our FS sample is representative of the overall environmental conditions in Great Britain.

**Descriptive Statistics of the Climatic and Environmental Variables**

Compared to the baseline, the UKCIP 2020–49 medium emission climate change scenario is characterized by both higher temperatures and lower precipitation dur-

| Table 6. Descriptive Statistics of the Climatic and Environmental Variables |
|----------------|-------------|-----------|---|---|
| Units          | \( \bar{x} \) | \( s(x) \) | Min | Max |
| Baseline (1960–90): |
| Degree days (day °C) | 1,164.0 | 251.8 | 367.4 | 1,645.0 |
| Precipitation (mm) | 450.7 | 169.0 | 250.8 | 1,504.0 |
| Climate change projections (UKCIP 2020–49): |
| Degree days (day °C) | 1,424.0 | 276.1 | 571.6 | 1,948.0 |
| Precipitation (mm) | 395.8 | 188.3 | 158.6 | 1,444.0 |
| Control variables: |
| Depth to rock (dm) | 6.4 | 3.5 | .0 | 14.0 |
| Slope (°) | 4.4 | 3.6 | .0 | 24.7 |
| Pop. density (pop/Km²) | 226.4 | 434.6 | 8.0 | 4,924.0 |

Note.—\( \bar{x} \) indicates the sample mean, \( s(x) \) the sample standard deviation. Data refer to 10 km grid square cells for Great Britain, including only cells in which there is some agricultural land. Control variables are assumed to remain constant between the two scenarios.
ing the growing season. The highest value of degree days is 1,948, still considerably below 2,400: the threshold identified by Schlenker et al. (2006) as the level at which temperature begins to have a negative effect on land values. Therefore, we can extrapolate our model estimates with sufficient confidence. However, to test the robustness to these out-of-sample projections, we also compute climate change impacts using a “constrained” scenario, in which all combinations of rainfall and temperature are restricted to be within the range used for estimation. For example, in this “constrained” scenario we set to 1,700 the maximum value for degree days and to 240 mm the minimum quantity of precipitation. While we calculate predictions from the parametric specifications (models A, B, and C) using both the “unconstrained” and “constrained” climate change scenarios, we use only the latter for the semiparametric regression (model D) since the bidimensional smooth function of degree days and precipitation is potentially erratic when applied outside the range of values used for estimation, generating unreliable results when used out of sample.

The predicted impacts of climate change on farmland values derived from our four models are reported in Table 7. To provide a meaningful summary of grid squares or counties with different agricultural areas and land values, the percentage changes are weighted by the baseline total value of agricultural land in each cell or county. The county-level regressions (model A and B) predict strong and positive impacts of expected climate change on the rural sector, with an overall increase of about 20% in GB farm values compared to baseline levels. By applying a 5% discount rate (as per Mendelsohn et al. 1994), this translates into an increase in total GB farm net revenues of £1 billion per annum. Furthermore, according to model B (county-level with interaction effect), the first decile of the predicted changes corresponds to an increase of around 12% and the last decile to an increase of 32%, indicating that almost all counties will be significantly better off as a result of projected climate change. Model A (county level with no interaction) presents a slightly more heterogeneous picture, with the first decile predicted to experience almost no change in value and gains rising to about 45% for the last decile.

13. We compute the total agricultural area within each square or county using 1 km grid data from the Land Cover Map 2000 (LCM2000, http://www.ceh.ac.uk/LandCoverMap2000.html), produced by the Centre for Ecology and Hydrology. LCM2000 is a parcel-based classification of satellite image data showing land cover for the entire United Kingdom. We include in agriculture the land classified as (a) arable and horticultural, (b) improved grassland, (c) semi-natural rough grass and bracken, and (d) mountain heath and bog. This definition somewhat overestimates the amount of agriculture in GB, resulting in a total of about 19 million hectares rather than the 17 million presented in the official statistics (e.g., http://www.defra.gov.uk/statistics/). Therefore, we rescaled the agricultural area in each cell or county by multiplying it by a factor of 0.9 to match with the official GB total.
In contrast to the aggregated, county level analyses, the estimates provided by the farm-level models (models C and D) are considerably less optimistic. Model C predicts a mean increase in farm value ranging between 6% and 8% (which is lower than the first decile predicted by model B) with large areas experiencing losses and the first decile now indicating a loss of between 12% and 20%, depending on the climate change scenario. These results are not significantly different from those obtained using our most flexible regression, model D, which suggests that climate change will induce a diverse set of impacts on agricultural land values ranging from a lower decile loss of 5% to an upper decile increase of almost 40% with a mean value around +7%, comparable to an annual rise in net revenues of about £400 million.

Figure 5 presents maps of the spatial distribution of farmland value changes derived from models B and C. These models use the same specification with both including quadratic functions of degree days and precipitation and an interaction effect, but they differ in that model B is estimated on county data, while model C employs farm data. Consistent with the statistics reported in table 7, model B predicts a somewhat uniform increase in land values throughout GB, driven by the warmer and drier climate. In contrast, model C projects spatially heterogeneous impacts with the wetter areas of Scotland, Wales, and the North of England being significantly better off and the dry lowland of the Southeast of England being the
main loser. The main rationales for this loss are the higher temperature and reduced precipitation, which can lead to water deficiency and less favorable farming conditions, ultimately lowering land values. Not surprisingly, the motivation for this difference in predictions between farm-level and county-level models can be found in the interaction effect between temperature and rainfall. Recalling figures 2 and 3, precipitation in farm-level models can have either a negative or a positive effect on land values depending on the level of temperature. While the warmer
growing season projected in this climate change scenario can boost yields, it can also increase crop water demand and reduce drought tolerance. County-level models do not capture the interaction effect between temperature and precipitation and, therefore, erroneously project lower rainfall and higher temperatures to always have positive impacts on land values.

Finally, in figure 6 we present box plots of the distribution of the change in total GB farm net revenues according to different models, computed via 5,000 Monte Carlo repetitions. Results compare county-level against farm-level estimates using a variety of specifications among the ones reported in table 5, with each permutation investigated using both the unconstrained and constrained climate predictions. Specifically, we plot the results using the baseline model (row 1 in table 5), a different aggregation method (row 2), using a different climate definition (row 3), including the observations for which the farmland value was not updated (row 4), including a larger spatial autocorrelation (row 7), and using an even larger (county-level) and more general autocorrelation specification (row 9).

The box plots clearly illustrate the bias introduced by aggregation. None of the mean impacts predicted by the county-level models fall within the confidence intervals of any of the impacts predicted by the farm-level models. County-level models indicate a strong and unequivocally positive impact of climate change. Despite the confidence intervals being quite large, all predictions are significantly different from zero. In contrast, the farm-level estimates reveal that the overall net effect is most likely to be much smaller and, according to some specifications, this impact may not even be significantly different from zero. In comparison, restricting the climate change conditions to remain within the boundaries of the estimation sample (“constrained” climate scenario) as opposed to using the original UKCIP temperature and precipitation values (“unconstrained” climate scenario) has a small effect on results. Overall, these findings show that the aggregation has not only affected the parameter estimates, as shown in the previous section, but has also led to climate change impact projections that are significantly distorted.

5. CONCLUDING REMARKS

Both Fisher et al. (2012) and Deschénes and Greenstone (2012) conclude their analyses by pointing out that, despite the growing literature, a consensus on the potential economic impact of climate change on agriculture still remains far from being achieved. This paper contributes to the debate by highlighting two significant issues that have been previously overlooked: aggregation bias and interactions between temperature and precipitation. We present a Ricardian analysis of farmland values using a unique, 10-year panel of more than 3,000 farms located in GB, a country characterized by one of the most dense weather station networks in the world. This allows us to accurately represent the local climatic conditions affecting each farm in our sample. We compare this analysis with conventional models estimated on data
Figure 6. Estimated total impact of climate change on GB agriculture in the 2020–49 UKCIP medium emission scenario in different model specifications. The box plots represent confidence intervals for the change in total GB annual farm net revenues, calculated with 5,000 Monte Carlo repetitions. The gray box indicates the first and third quartile, the whiskers the 90% confidence interval. The models include interaction effects, are estimated on county-level data (model B) and farm-level data (model C), and are based on five different specifications reported in table 5 (rows 1, 2, 3, 4, and 7, in parentheses). "unconst." indicates the unconstrained climate change scenario; "constr." indicates the constrained climate change scenario.
averaged across counties, demonstrating that a significant bias afflicts climatic coefficients based on aggregated data. While our county-level regressions appear to confirm the assumption of additive climatic effects implemented in previous Ricardian studies, our farm-level analyses reveal important interactions between precipitation and temperature in determining land values. Consistent with the literature on plant physiology, which shows that the crop requirement for water increases with temperature, we find that higher precipitation is more valuable when temperatures are high. Accordingly, higher temperatures increase land values only if there is enough precipitation to prevent the risk of drought. This interaction effect becomes statistically insignificant when we analyze the same data aggregated over counties. These findings are consistent across different data, models, and aggregation methods. Ignoring this interaction has significant implications for climate change impact projections which are severely distorted by aggregation bias.

We also test for functional form misspecification by estimating a semiparametric model based on penalized splines. The results do not appear to be significantly different from those obtained using the simpler, quadratic regression with interaction. Although farmland values have changed considerably in the 10 years included in the analysis, our estimates remain remarkably robust. As observed by Schlenker et al. (2006) and Fisher et al. (2012), we find that the fundamental dependence of agricultural incomes on climatic conditions is independent of government policies and crop prices.

One possible explanation for the aggregation bias is measurement error (e.g., Auffhammer et al. 2013). As shown in this paper, aggregated data fail to account for the fine-scale variations in the local climate affecting single farms and erroneously assume counties to be climatically homogenous units. On this point, using county-level climate averages with farm-level land value data still produces biased coefficients. Unfortunately, in most countries weather station networks are not dense enough to provide the accurate local climate measures (in particular regarding precipitation) required for extensive farm-level analyses. Our findings are consistent with previous research (e.g., Sinclair 2011) in showing that local patterns of precipitation play a fundamental role in understanding the impact of climate change on agriculture. They also highlight the importance of collecting weather data accurate enough to truthfully represent local climatic conditions. While aggregation bias could be less significant in countries where climate presents less local variation (or where the agricultural sector is more homogeneous), the fact that previous county-level analyses ignored the interaction effect between precipitation and temperature may cast some doubt on the validity of their conclusions. This is an empirical question that could be worth investigating in the future by, for example, analyzing farm-level statistics for enterprises located close to weather stations, in order to generate more precise information on the corresponding climate.
Obviously, the usual caveats of Ricardian analyses apply here also. Prices, population, and other drivers are assumed to remain constant between the scenarios. The impact of changes in the length of the growing season or variation in intraseasonal precipitation patterns are not taken into account. Finally, possible beneficial effects of increased CO₂ fertilization on crop growth are also not included, though some recent research suggests that those may be much smaller than previously believed (Long et al. 2006).

REFERENCES


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