1 2	Is Bursting More Effective than Spiking in Evoking Pituitary Hormone Secretion? A Spatiotemporal Simulation Study of Calcium and Granule Dynamics		
3			
4	Alessia Tagliavini ¹ , Joël Tabak ^{2,3} , Richard Bertram ² , Morten Gram <u>Pedersen¹</u>		
5			
6	¹ Department of Information Engineering, University of Padua, Padua, Italy		
7 8	² Department of Mathematics and Program in Neuroscience and Molecular Biophysics, Florida State University, Tallahassee, FL 32306, USA		
9	³ Exeter University Medical School, Biomedical Neuroscience, Exeter, UK		
10			
11	Corresponding author:		
12	Morten Gram Pedersen,		
13	Department of Information Engineering, University of Padua,		
14	Via Gradenigo 6/B, 35131 Padua, Italy.		
15	Email: pedersen@dei.unipd.it		
16			
17	Running head:		
18	Pituitary secretion evoked by bursting and spiking		
19			
20	Author contributions:		
21	Conceived research: RB, MGP		
22	Performed research: AT, JT		
23	Prepared figures: AT		
24	Wrote and edited manuscript, and approved final version: AT, JT, RB, MGP		
25			
26 27	Keywords: electrical activity; exocytosis; Ca ²⁺ oscillations; mathematical modeling; dynamic clamp.		

28 ABSTRACT

Endocrine cells of the pituitary gland secrete a number of hormones, and the amount of hormone 29 released by a cell is controlled in large part by the cell's electrical activity and subsequent Ca²⁺ 30 influx. Typical electrical behaviors of pituitary cells include continuous spiking and so-called 31 pseudo-plateau bursting. It has been shown that the amplitude of Ca^{2+} fluctuations is greater in 32 bursting cells, leading to the hypothesis that bursting cells release more hormone than spiking 33 34 cells. In this work, we apply computer simulations to test this hypothesis. We use experimental recordings of electrical activity as input to mathematical models of Ca^{2+} channel activity. 35 buffered Ca²⁺ diffusion, and Ca²⁺-driven exocytosis. To compare the efficacy of spiking and 36 bursting on the same cell, we pharmacologically block the large conductance potassium (BK) 37 current from a bursting cell, or add a BK current to a spiking cell via dynamic clamp. We find 38 that bursting is generally at least as effective as spiking at evoking hormone release, and is often 39 considerably more effective, even when normalizing to Ca²⁺ influx. Our hybrid 40 experimental/modeling approach confirms that adding a BK-type K^+ current, which is typically 41 associated with decreased cell activity and reduced secretion, can actually produce an increase in 42 hormone secretion, as suggested earlier. 43

44

45

47 INTRODUCTION

Endocrine cells of the pituitary gland (i.e., melanotrophs, lactotrophs, somatotrophs, 48 thyrotrophs, corticotrophs, and gonadotrophs) secrete a number of hormones and are regulated 49 by the hypothalamus (30). These hormones act on other endocrine glands and other tissues 50 including the brain to regulate physiological and behavioral aspects of growth, metabolism, 51 water balance, and reproduction (7). The endocrine pituitary cells contain a wide variety of ion 52 channels and are electrically excitable, and hormone secretion occurs due to an elevation in the 53 intracellular Ca^{2+} concentration that often accompanies electrical activity (29). Common 54 behaviors of the cells include continuous spiking - typically observed in luteinizing hormone-55 secreting gonadotrophs under basal conditions – and a form of bursting known as pseudo-plateau 56 bursting often observed in prolactin-secreting lactotrophs, growth hormone-releasing 57 58 somatotrophs, and ACTH-secreting corticotrophs, where the burst duration is at most a few seconds and the spikes that ride on the elevated voltage plateau are very small (9, 10). Each 59 electrical event brings Ca^{2+} into the cell, and this Ca^{2+} is responsible for exocytosis of hormone-60 filled granules. Simultaneous measurements of both electrical activity and Ca²⁺ concentration 61 have established that the amplitude of Ca^{2+} fluctuations is greater in a bursting cell than in a 62 spiking cell (30) leading to the hypothesis that bursting cells release more hormone than spiking 63 cells (8, 9). Experimentally exploring this hypothesis will require simultaneous measurements of 64 electrical activity and release from single cells. The aim of this report is to use computer 65 simulations to explore the hypothesis that pseudo-plateau bursting evokes more secretion than 66 67 continuous spiking.

The approach that we use is to directly measure electrical spiking and bursting patterns 68 from pituitary cells and use these data as input to mathematical models of Ca^{2+} channel activity, 69 Ca^{2+} diffusion and binding to buffer, and finally Ca^{2+} -driven exocytosis. The model parameters 70 are set according to prior data and models, but one major unknown factor is the geometrical 71 arrangement of Ca²⁺ channels and docked granules at the plasma membrane. We consider the 72 secretion response to stochastic single channels as well as small clusters of stochastic channels, 73 and vary the distance of the channels from the release sites. Our objective is to determine how 74 these factors affect the differential secretion evoked by spiking electrical activity vs. bursting 75 76 electrical activity.

77 We find that bursting is typically more effective at evoking secretion than is continuous spiking. When bursting is induced in a spiking gonadotroph by injecting a BK-type K^+ current 78 79 with dynamic clamp, our model simulations suggest that the burst pattern is generally at least as effective as continuous spiking at evoking hormone release, and is often considerably more 80 effective. We demonstrate that the degree of superiority of bursting over spiking depends on the 81 channel configuration, which would likely vary from cell-to-cell. We also demonstrate that the 82 bursting reappearing in an endogenously bursting pituitary cell, after previously 83 pharmacologically blocking the native BK current and subsequently adding a BK current using 84 dynamic clamp, is superior at evoking secretion than the pharmacologically induced spiking 85 behavior. Thus, we demonstrate with this hybrid experimental/modeling approach that adding a 86 87 K^+ current, which is typically associated with decreased cell activity and reduced secretion, can actually produce an increase in hormone secretion, as suggested earlier (9). 88

89

90 METHODS

91 The inputs to our mathematical models are voltage time courses recorded from a rat gonadotroph or from a GH4C1 lacto-somatotroph cell. We use traces consisting of continuous 92 spiking patterns, and traces of fast pseudo-plateau bursting caused by adding a BK-type current 93 to a spiking cell with the dynamic clamp technique. Each of these traces is fed into a 94 mathematical model consisting of stochastic Ca²⁺ channels coupled to reaction-diffusion 95 equations that describe Ca^{2+} transport through the cell. Finally, the computed Ca^{2+} concentration 96 is used to drive an exocytosis model based on Ca^{2+} binding to granules, granule fusion with the 97 membrane, and resulting hormone release. 98

99

100 <u>EXPERIMENTAL</u>

GH4C1 cells were maintained in culture conditions in supplemented F10 medium (Sigma-Aldrich, St-Louis, MO) according to established procedures (35). Primary pituitary cells were obtained from diestrous female rats (Sprague Dawley, aged 3-6 months) using enzymatic dispersion of pituitary fragments (33). Animal procedures were approved by the Florida State University Animal Care and Use Committee. Cells were cultured in supplemented M199
medium (Invitrogen, Carlsbad, CA) for one day before being used for patch clamp experiments.
Gonadotrophs were identified by their larger size and by their typical rhythmic
hyperpolarizations in response to 1 nM gonadotropin-releasing hormone (Bachem, Torrance,
CA) applied at the end of the experiment (38).

During the patch-clamp experiments, cells were superfused with Hepes-buffered saline (138 mM NaCl, 5mM KCl, 10 mM D-glucose, 25 mM HEPES, 0.7 mM Na₂HPO₄, 1 mM MgCl₂, 2 mM CaCl₂) at room temperature. Patch pipettes (resistance 6-9 MOhm) were filled with solution containing 90 mM KAsp, 60 mM KCl, 10 mM HEPES, 1 mM MgCl₂ with the addition of 120 g/ml amphotericin B. Usually, access resistance decreased below 50 MOhm within 10 minutes following seal (> 5 GOhm) formation. BK channels were blocked by bath application of 100 nM iberiotoxin (Tocris).

117

118 DYNAMIC CLAMP

119 Membrane potential was recorded in current clamp (bridge mode) and output from the 120 patch amplifier (Multiclamp 700B, Molecular Devices, Sunnyvale, CA) was read through an 121 analog to digital acquisition card (DAQ) on a PC running the software QuB with a dynamic 122 clamp module (22). Membrane potential (*V*) was used to compute the current going through the 123 BK channels, $I_{BK} = g_{BK} f(V_K - V)$, with *f* obtained by integrating

124
$$au_{BK} \frac{df}{dt} = f_{\infty}(V) - f$$

in real time using the forward Euler method (22), with *dt* average = 54 μ s, maximum = 100 μ s, and the steady state BK channel activation given by

127
$$f_{\infty}(V) = \left[1 + \exp((v_f - V)/s_f)\right]^{-1}$$
.

128 The calculated BK current was injected back into the cell through the same DAQ. The parameter 129 values were: $g_{BK} = 0.5 - 1$ nS; $\tau_{BK} = 5 - 10$ ms; $v_f = -15$ mV; $s_f = 1$ mV. 130

131 <u>MODELLING</u>

132 GEOMETRY

To model data from pituitary cells we represented a single cell by a sphere with a 133 diameter of 13 µm (5). Based on whole-cell calcium conductance of ~1.5-2 nS (10), and single 134 channel conductance ~ 20 pS (13), we assumed that a cell possesses 75 functional L-type Ca²⁺ 135 channels. In our simulations we considered two different configurations for the channel 136 distribution over the sphere surface: channels were either uniformly distributed and each release 137 site affected by a single channel, or there were clusters composed of 5 channels, and each release 138 site affected by a single cluster. In the single channel case, Ca^{2+} diffusion was computed in a 139 conical region with base radius of 1.5 µm (Fig. 1a), a radius obtained by dividing the sphere 140 surface into 75 circular areas, one for each channel. This radius corresponds to an inter-channel 141 distance of $\sim 3 \mu m$, in agreement with (11). The single channel conductance was set to 20 pS 142 (13). In the case of channel clusters, Ca^{2+} diffusion was simulated in a conical region with a base 143 radius of 3.3 µm, corresponding to dividing the sphere surface into 15 circular areas. In both 144 cases, the Ca²⁺ current source was located at the base center of the conical region. We 145 implemented no-flux boundary conditions for Ca²⁺ and buffers on the sides of the cone. This 146 assumption means that Ca^{2+} flowing out of the conical region equals the flux into the cone from 147 adjacent regions, or in other words, that the Ca^{2+} channels in adjacent cones contribute to Ca^{2+} 148 levels in the cone of study exactly as the Ca²⁺ channel or cluster under study influences the 149 adjacent regions. Because of the conical geometry, the full 3-dimensional problem was reduced 150 to a 2-dimensional problem, using rotationally symmetric spherical (r,θ) coordinates, thus 151 reducing the computational requirements. Since the granules participating in hormone secretion 152 are located just below the membrane (14), we focused our attention on the submembrane Ca^{2+} 153 profiles along the plasma membrane. 154

155

[Figure 1]

156

158 SINGLE CHANNEL CURRENT

For the single Ca^{2+} channel, we assumed three states with kinetic mechanism described by (28)

$$C \bigsqcup_{\beta}^{\alpha} O \bigsqcup_{k_{-}}^{k_{+}} B,$$
(1)

161 where the states are closed (*C*), open (*O*), and blocked or inactivated (*B*).

162 The rate constants $\alpha(V)$ and $\beta(V)$ were determined by $\alpha = m_{\infty}/\tau_m$, $\beta = 1/\tau_m - \alpha$ (12) using a steady-163 state activation function m_{∞} and time constant τ_m obtained from experiments. Based on data from 164 GH3 cells (5, 11), which have Ca²⁺ channel characteristics similar to GH4 cells (5), and in 165 agreement with Sherman et al. (28), we set $\tau_m = 1.25$ ms. The steady-state activation function was

$$m_{\infty} = \frac{1}{1 + \exp[(V_m - V) / s_m]},$$
(2)

with $V_m = -4$ mV and $s_m = 7$ mV (11). With regards to channel inactivation, some types of Ca²⁺ channels are inactivated by Ca²⁺, while others exhibit voltage-dependent inactivation. We found that fixed rate constants $k_{-}=0.018$ ms⁻¹ and $k_{+}=0.0324$ ms⁻¹ were sufficient to match inactivation experimentally observed in (11). The stochastic channel dynamics (1) was simulated as realizations of the discrete-state continuous-time Markov chain with transition probabilities for a small time step Δt described by

$$\begin{bmatrix} O(t+\Delta t)\\ C(t+\Delta t)\\ B(t+\Delta t) \end{bmatrix} = \begin{bmatrix} 1-(\beta+k_{+})\Delta t & \alpha\Delta t & k_{-}\Delta t\\ \beta\Delta t & 1-\alpha\Delta t & 0\\ k_{+}\Delta t & 0 & 1-k_{-}\Delta t \end{bmatrix} \begin{bmatrix} O(t)\\ C(t)\\ B(t) \end{bmatrix}.$$
(3)

Monte Carlo simulations were performed and the single-channel open-state O(t) was used to compute the single-channel current as

$$I_{sc}(t) = g_{sc}O(t)(V(t) - V_{Ca})$$
(4)

where g_{sc} is the single channel conductance. In the cluster case, the total current is simulated by summing 5 independent realizations of a single channel current (I_{sc}). Both the current driving force and open probability are coupled to the time-varying membrane potential V(t). Specifically, the driving force decreases as V(t) increases towards the Ca²⁺ reversal potential V_{Ca} whereas the open probability increases with V(t).

179 ENDOGENOUS BUFFERS

In all simulations we assumed the presence of a single immobile endogenous Ca^{2+} buffer, in agreement with Kits et al. (15), and no mobile buffers were considered. Binding of Ca^{2+} to the buffers is described by simple mass action kinetics with one-to-one stoichiometry,

$$B + Ca^{2+} \bigsqcup_{k_{off}}^{k_{on}} CaB,$$
(5)

183 where k_{on} and k_{off} are association and disassociation rates, respectively. The reaction-diffusion 184 equations for the Ca²⁺ concentration and for the free unbound buffers are taken from (20):

$$\frac{\partial [Ca^{2+}]}{\partial t} = D_{Ca} \nabla^2 [Ca^{2+}] - k_{on} [Ca^{2+}] [B] + k_{off} (B_{total} - [B]) + \frac{1}{2F} I_{sc}(t) \delta(r - R, \theta) - k_{uptake} ([Ca^{2+}] - [Ca^{2+}]_0),$$
(6)

$$\frac{\partial [B]}{\partial t} = -k_{on} \Big[Ca^{2+} \Big] \Big[B \Big] + k_{off} \Big(B_{total} - [B] \Big), \tag{7}$$

where D_{Ca} is the diffusion coefficient for unbound Ca²⁺. We chose $D_{Ca}=0.2 \ \mu\text{m}^2 \ \text{ms}^{-1}$ (1) and 185 assumed that the distribution of the immobile buffer is spatially uniform. The second-to-last term 186 in Eq. 6 represents Ca^{2+} influx, where F is Faraday's constant, $I_{sc}(t)$ is the (inward) single-187 channel (or 5-channel-cluster) calcium current, and $\delta(r-R,\theta)$ is the Dirac delta function centered 188 at r=R and $\theta=0$ (i.e., at the center of the base of the cone). The last term defines net Ca²⁺ uptake 189 into internal stores such as the endoplasmic reticulum with constant rate $k_{uptake} = 0.3 \ \mu M/ms^{-1}$. 190 $[Ca^{2+}]_0$ is the Ca²⁺ concentration in case of no Ca²⁺ influx and spatiotemporal equilibrium. In 191 accordance with simulation studies performed by Kits et al. (16) in melanotroph cells, we set the 192 endogenous buffer parameters $k_{on}=0.1 \ \mu \text{M}^{-1} \text{ ms}^{-1}$, $K_{\text{D}}=k_{off}/k_{on}=10 \ \mu \text{M}$, and $B_{\text{total}}=900 \ \mu \text{M}$. No-193 flux boundary conditions hold for Ca²⁺ at all boundaries. The reaction-diffusion equations were 194 solved using the Calcium Calculator (CalC) software developed by Victor Matveev (21). CalC 195 uses an alternating-direction implicit finite difference method, with second order accuracy in 196 197 space and time, and with adaptive time steps.

198 EXOCYTOSIS MODEL

199 We initially used a 6-pool exocytosis model (4), which describes the fraction of granules in various pools of granules described as docked, primed, domain bound, or in one of three pre-200 fusion states distinguished by the number of bound Ca^{2+} ions. However, for the relatively short 201 time courses used here (5 sec), our preliminary simulations showed no significant differences 202 between this 6-pool model and a simpler 4-pool model in which the docked, primed, and domain 203 204 bound pools were combined into a single pool that we call the "primed" pool. We use this simplified model (Fig. 2), which is similar to a model of exocytosis in melanotroph cells (16) in 205 all simulations. Here, the granule can be in one of four different states: a primed state where the 206 granule is adjacent to the plasma membrane (N_0) , or states in which one (N_1) , two (N_2) , or three 207 (N_3) Ca²⁺ ions are bound to the Ca²⁺ sensor, likely synaptotagmin (31). Once in state N_3 the 208 granule fuses with the membrane and releases its hormone content at rate u_1 . Granule release is 209 triggered by local Ca^{2+} levels (C_{loc}), as indicated in Fig. 2, while resupply is dependent on the 210 bulk calcium concentration C_i , which is computed as the submembrane Ca²⁺ concentration 1.5 211 μ m from the channel. The rate of resupply per cell r_1 is 212

$$r_{1} = \frac{C_{i}(t)r_{1}^{0}}{C_{i}(t) + K_{p}},$$
(8)

with $K_p = 2.3 \,\mu\text{M}$ (4, 40), and r_1^0 is the maximal resupply rate per cell.

All secretion model steps are assumed to be reversible, except for fusion. The local Ca^{2+} concentration was determined by solving the Ca^{2+} reaction-diffusion equations and using the Ca^{2+} value at the release site (Eqs. 6,7). The exocytosis model describing release per cell is given by the following differential equations:

$$\frac{dN_{0}}{dt} = -(3k_{1}C_{loc}(t) + r_{-1})N_{0} + r_{1}(C_{i}(t)) + k_{-1}N_{1},$$

$$\frac{dN_{1}}{dt} = -(2k_{1}C_{loc}(t) + k_{-1})N_{1} + 3k_{1}C_{loc}(t)N_{0} + 2k_{-1}N_{2},$$

$$\frac{dN_{2}}{dt} = -(k_{1}C_{loc}(t) + 2k_{-1})N_{2} + 2k_{1}C_{loc}(t)N_{1} + 3k_{-1}N_{3},$$

$$\frac{dN_{3}}{dt} = -(u_{1} + 3k_{-1})N_{3} + k_{1}C_{loc}(t)N_{2},$$
(9)

where N_i is the number of granules in pool *i*. Experimental data (37) indicate a relatively low Ca²⁺ binding affinity; as a consequence, we use the Ca²⁺ affinity value $k_d = k_{-1}/k_1 = 27 \mu M$ in Eqs. 9.

We used two sets of initial conditions for the granule/exocytosis model. In the model of Chen et al. (4) the number of primed granules (pool N_0) is equal to 40 per cell. Hence, we set as initial condition N_0 =40 primed granules, each a fixed distance from a single channel (so 35 channels are not associated with granules). Assuming that – in any one simulation – all Ca²⁺ channels in the cell behave identically according to the Markov simulation, the granules will be exposed to the same Ca²⁺ profile. To calculate average cellular exocytosis, we performed 10 (single channel) or 5 (cluster) simulations and computed average values of N_i at each time point.

This initial condition (N_0 =40) reflects experiments such as single-cell capacitance measurements of triggered exocytosis, where no exocytosis is occurring before the experiment (36, 37). For interpreting hormone secretion experiments, where secretion is ongoing, the steady state of the model is more relevant. We found that the pools empty within seconds (see Results), and therefore considered initial conditions where all pools are empty to reflect secretion experiments.

The exocytosis rate per cell, with N_3 the average of 10 or 5 trials as explained above, is

$$J_F(t) = u_1 N_3(t), (10)$$

and the cumulative number of fused granules per cell is

$$M_F(t) = \int_0^t u_1 N_3(t') dt'.$$
 (11)

To show how much of the simulated secretion is due to increased Ca^{2+} influx during bursting compared to spiking electrical activity, that is, to investigate whether bursting increases the Ca^{2+} -current sensitivity of exocytosis (26), we related exocytosis to the total charge entering via the Ca^{2+} channel or channel cluster (26):

$$Q(t) = \int_{0}^{t} I_{sc} ds.$$
⁽¹²⁾

The exocytosis model was solved using the MATLAB (R2012b, The MathWorks®)function ode15s.

242 [Figure 2]

244 **RESULTS**

245 Secretion evoked by Ca²⁺ influx through single channels is increased when converting spiking to
246 bursting electrical activity through dynamic clamp

Gonadotrophs release little LH under basal conditions, which has been suggested to be 247 associated to their typical spiking electrical behavior (10). We have previously shown that 248 adding a BK-type K^+ current to a spiking gonadotroph can change its behavior into bursting (35). 249 Figure 3 shows an example of such a cell where the injected BK-type current induces bursting in 250 an otherwise spiking gonadotroph. We also show the average of 10 independent simulations, 251 each with a stochastic Ca^{2+} channel providing Ca^{2+} to the interior of the cell and subsequent Ca^{2+} 252 diffusion. The Ca²⁺ model is driven by either the spiking voltage pattern (left) or the bursting 253 pattern (right) obtained by injecting a BK-type K^+ current via dynamic clamp. Average Ca^{2+} 254 profiles are reported at distances of 30, 200, and 1500 nm from the Ca^{2+} channel. As expected, 255 close to the channel, i.e., 30 nm, Ca^{2+} reaches high concentrations of some tens of micromolar on 256 average with peaks up to $\sim 70 \ \mu M$ during spiking activity and $\sim 110 \ \mu M$ during bursting. The 257 traces are very noisy due to the stochastic openings of the Ca^{2+} channel. The average Ca^{2+} 258 concentration decreases with distance from the channel, reaching less than 1 µM at a distance of 259 1500 nm. In addition, the noise is attenuated due to the effects of diffusion, which acts as a low-260 pass filter. Ca²⁺ measurements using a fluorescent dye such as fura-2 report on the Ca²⁺ 261 concentration averaged over the cell, and have time courses similar to those shown in the bottom 262 row of Fig. 3 (30, 32). 263

264

[Figure 3]

265

We now locate the exocytosis machinery at different distances from the Ca²⁺ channel and use the Ca²⁺ concentration at that location to drive the exocytosis model (Fig. 2 and Eqs. 9). Figure 4 shows the average number of fused granules over time at different distances. If the release site is 30 nm from the channel, it is exposed to very high Ca²⁺ concentrations, whether the cell is spiking or bursting, and exocytosis occurs at its maximum rate that releases all the granules in the primed pool N_0 (40 granules) very soon after the start of the input train. A similar 272 result occurs if the release site is located 100 nm from the channel. Thus, if the release site and channel are within 100 nm of each other it does not matter whether the cell is spiking or bursting. 273 the secretion level will be the same, since the Ca^{2+} concentrations at the exocytotic machinery 274 are in both cases saturating. At a distance of 200 nm there is a difference between exocytosis 275 276 evoked by spiking and that evoked by bursting; the bursting pattern (solid) evokes release at a higher rate than the spiking pattern (dashed), though both release almost all available granules by 277 the end of the 5 second input train. The advantage of bursting over spiking is amplified when the 278 release site is situated further from the channel, at 300 nm or 500 nm. Even though the absolute 279 number of fused granules is lower when the channel and the release site are more distant, the 280 bursting voltage trace releases more granules than the spiking trace at all time points. Thus, our 281 simulations support the notion that adding an outward K⁺ current can, by changing spiking to 282 bursting activity, increase secretion (6, 29). 283

These observations imply that the primed pool of granules can be emptied very quickly, 284 and this fusion process is likely monitored with capacitance measurements of exocytosis that 285 take place over a short period of time (14). In our data, the spiking voltage trace shows 5 spikes 286 287 in 5 seconds, each spike lasting ~40 ms (Fig. 3Ai). On average, each 40 ms depolarization of a pulse train was found to evoke ~10 fF of exocytosis (19). Thus, based on these experiments we 288 expect ~50 fF exocytosis during the 5 seconds in Fig. 3. In our simulations, exocytosis at a 289 distance of 200 nm from the channel is ~30 granules. If we assume that a single granule 290 291 corresponds to ~2fF (39, 42), we get a capacitance measurement of ~60 fF, close to the ~50 fF 292 calculated from (19).

293

[Figure 4]

However, most secretion measurements are made from a cell population over a period of minutes or tens of minutes. In such measurements the resupply of the primed pool by the reserve granule pool is rate limiting. We next look at the effects of resupply by emptying the primed pool N_0 at the beginning of the simulation and from this initial condition evaluate the differential exocytosis evoked by spiking and bursting.

The cumulative number of fused granules as a function of time is shown in Fig. 5 (top panel). Bursting evokes more release regardless of the distance between the channel and the

granule. This is in spite of the fact that at short distances the local Ca^{2+} concentration saturates 301 the release site, and highlights the importance of the dependence of resupply on the global, rather 302 than local, Ca^{2+} concentration. That is, the simulated global Ca^{2+} concentration is higher during 303 bursting than during spiking, as measured by fluorescent dyes (22), and this results in a greater 304 305 rate of resupply in response to bursting. When the channel is close to the release site all granules becoming available due to the resupply are fused almost immediately, so resupply is rate 306 limiting. Farther than 200 nm from the channel, local Ca²⁺ concentrations start to play a 307 predominant role since the exocytosis machinery is no longer saturated, and therefore differences 308 in local Ca²⁺ levels as well as global levels are responsible for differences in the exocytosis rates. 309

310

[Figure 5]

There are two factors that could contribute to the greater effectiveness of bursting at 311 evoking secretion in the model. One is that bursting brings in more Ca^{2+} over the 5 seconds of 312 simulation time, increasing resupply rate relative to spiking, as mentioned above. The other is 313 that the dynamics of Ca^{2+} diffusion and the exocytotic machinery favor the bursting signal over 314 the spiking signal. That is, bursting is more efficient than spiking at evoking release. To test the 315 latter, we plot the number of fused granules versus the total Ca^{2+} entry O (Fig. 5, bottom panels). 316 For release sites closer than 200 nm from the channel the efficiencies of the spiking and bursting 317 patterns are virtually the same. It is only at distances of 200 nm or greater that bursting becomes 318 more efficient than spiking, since at these distances the number of fused granules per total Ca²⁺ 319 entry is larger when the cell is bursting. This is due to the longer duration of the bursting events, 320 which produce longer-duration Ca^{2+} signals that are advantageous for the exocytosis machinery 321 that requires the binding of three Ca^{2+} ions to evoke granule fusion. In fact, in simulations in 322 which only two Ca²⁺ ions are needed to evoke fusion the efficiencies of spiking and bursting are 323 the same at a 200 nm distance, and bursting is only slightly more efficient at 300 and 500 nm 324 distances (not shown). 325

As a final quantification of the effectiveness of bursting vs. spiking at evoking secretion we show the ratio between bursting-evoked secretion and spiking-evoked secretion in Fig. 6 (solid line). This ratio is calculated from the total number of fused granules at the end of the 5sec input voltage train as a function of distance between the channel and the release site. Up until 330 a distance of 100 nm the ratio is ~ 1.5 ; the burst pattern evokes a slightly higher amount of secretion than spiking. Past this distance the ratio increases continuously, reaching a value of 331 ~8.5 at a distance of 700 nm. Thus, there is between 1.5 and 8.5 times more secretion by the end 332 of the 5-sec stimulation with bursting versus spiking. Plotting the ratio of exocytosis during 333 spiking and bursting but normalized to the charge Q (Fig. 6, dashed line) shows that spiking and 334 bursting have almost the same Ca^{2+} current sensitivity close to the channel (i.e., they are equally 335 efficient at evoking release), but farther away bursting becomes more efficient than spiking, 336 reaching a 5.5-fold higher Ca^{2+} current sensitivity at a distance of 700 nm from the channel. 337

In summary, our simulations suggest that LH secretion from a gonadotroph could increase substantially if the electrical pattern switched from spiking to bursting, for example because of the addition of a BK-type current.

341

[Figure 6]

342 Secretion evoked by Ca^{2+} influx through a cluster of channels

The previous simulations assumed that each release site is acted upon by Ca^{2+} from single channels, and indeed there is evidence supporting this, in both endocrine cells and in neuronal synapses (11, 17). However, it is likely that hormone release sites receive Ca^{2+} from several channels, and there is also evidence for this (2, 3). In the next set of simulations we consider such a situation, where a release site is affected by Ca^{2+} from a cluster of 5 stochastic Ca^{2+} channels. For simplicity we assume that these are equidistant from the release site.

Figure 7 shows the Ca²⁺ concentration at different distances from the channel cluster in response 349 to the spiking or bursting voltage trace. Close to the cluster (30 nm), Ca^{2+} rises to a level of 350 several hundreds of micromolar, about five times larger than in the single-channel case. At 351 greater distances, the increase over the single-channel level is less, since now the different 352 clusters are 6600 nm apart so that a release site located 1500 nm from a cluster is >5000 nm from 353 the next nearest cluster. In contrast, with uniform distribution of the same number of channels 354 (the single channel case), a release site located 1500 nm from one channel was located the same 355 distance from a second channel, so it received an equal amount of Ca^{2+} from both. Hence, 356 whereas a cluster of 5 channels provides \sim 5 times higher Ca²⁺ levels to granules located close to 357

the channels, a granule located 1500 nm from channels will be exposed to just $\sim 5/2=2.5$ times higher Ca²⁺ concentrations in the case of channel clusters compared to the single-channel configuration.

361

[Figure 7]

Figure 8 (upper panels) shows that bursting is always superior to spiking in evoking exocytosis 362 363 when channels are in clusters and the primed pool is initially empty. In contrast, the difference in Ca^{2+} current sensitivity is hardly observable when the release site is less than 300 nm from the 364 channel cluster (Fig. 8, lower panels). It is therefore mostly the larger amount of Ca^{2+} entering 365 during bursting that determines the difference in secretion. Figure 9 summarizes the results for 366 367 channel clusters. Even at the closest release site/cluster distances the bursting-to-spiking ratio of the total number of fused granules is ~1.5, and increases to ~4.5 at 700 nm (solid line). The 368 relative efficiency, i.e., the bursting-to-spiking ratio of the total number of granules normalized 369 to Ca^{2+} entry, is ~1 up to 300 nm, and increases then to ~2.5 at 700 nm. Thus, just as with single-370 channel-evoked release, bursting provides more secretion than does spiking when exocytosis is 371 372 triggered by channel clusters. However, the advantage of bursting over spiking becomes manifest at greater distances for clusters than for single channels, 100 nm in Fig. 6 vs. 300 nm in Fig. 9. 373 374 Because the trends are qualitatively similar with single-channel and cluster-evoked secretion, we focus on only one type (single-channel secretion) in the remaining simulations. 375

376

[Figure 8]

377

[Figure 9]

378 Bursting superiority depends on the frequency of spiking

As a second example, we now use recordings from a GH4 cell line. It has previously been shown that pseudo-plateau bursting in some pituitary cells converts to spiking when BK-type K⁺ channels are pharmacologically blocked, reducing the bulk Ca^{2+} concentration (8). Does this manipulation also result in a decrease of the domain Ca^{2+} and therefore in decreased secretion? We have shown that bursting can be rescued by adding BK current back to the cell using the dynamic clamp technique (here and in (34)). In Fig. 10 we use both procedures. We begin with a bursting lacto-somatroph GH4C1 cell (left column), then convert it to a spiking cell by the addition of the BK channel blocker iberiotoxin (middle column), and finally convert the spiking cell back to a bursting cell using dynamic clamp to inject a model BK current (right column). For each case we calculate the Ca^{2+} concentration at varying distances from the single stochastic channel, as in prior simulations. Close to the channel, the Ca^{2+} concentration is about the same for all three voltage traces. However, at the greater distances, 1500 nm, the Ca^{2+} levels corresponding to the bursting voltage traces are higher than those corresponding to the spiking voltage trace, as has been observed in experiments (18).

We next use these Ca^{2+} time courses to simulate exocytosis for release sites located at 393 different distances from the Ca^{2+} channel (Fig. 11). The results are summarized in Fig. 12, where 394 we show the number of fused granules evoked by the dynamic clamp-induced bursting vs. that 395 evoked by the spiking trace (solid black curve). In both cases, the ratio is near 1 up until a 396 397 separation distance of ~150-200 nm. At greater separations the ratio increases, indicating that at these greater distances the bursting trace is more effective at evoking exocytosis than the spiking 398 trace. Normalizing to Ca^{2+} influx reveals that the ratio of Ca^{2+} current sensitivity is higher for 399 spiking close to the channel (ratio < 1) whereas bursting is more efficient farther from the 400 channel (Fig. 12). The fact that bursting is less superior to spiking after normalizing to Ca^{2+} 401 influx compared to the previous simulations of exocytosis using the traces from a gonadotroph 402 (Figs. 5 and 6) can be explained by noticing that, for this example, iberiotoxin-induced spiking 403 (Fig. 10B) occurs at a much higher rate (~1.8 Hz) than bursting (~0.8 Hz) (Fig 10A, C). Thus, 404 the dynamics of Ca^{2+} entry is important for the control of exocytosis in addition to the number of 405 Ca^{2+} ions entering the cell. 406

407	[Figure 10]
408	[Figure 11]

409 [Figure 12]

411 **DISCUSSION**

In the absence of hypothalamic stimulation or inhibition, pituitary lactotrophs and 412 somatotrophs release prolactin and growth hormone, while gonadotrophs comparatively secrete a 413 negligible amount of luteinizing hormone. This difference in basal hormone release was matched 414 by differences in spontaneous electrical activity between these cell types: lactotrophs and 415 somatotrophs often exhibit "pseudo-plateau" bursts of activity, causing periodic Ca²⁺ influx, 416 while gonadotrophs usually produce spikes that are too brief to perturb the bulk Ca^{2+} level 417 substantially (9). Such differences in the bulk Ca^{2+} profiles lead to the hypothesis that different 418 patterns of spontaneous electrical activity result in different rates of hormone release. Bursting 419 causes hormone release from lactotrophs and somatotrophs, while spiking causes no hormone 420 421 release from gonadotrophs.

We tested this hypothesis in this paper. While Ca^{2+} triggers hormone release and bursting 422 creates larger amplitude oscillations of average intracellular Ca²⁺ than spiking, this does not 423 necessarily mean that bursting is more effective at triggering hormone release. The Ca2+ 424 concentration that matters is that seen by the hormone-containing granules at their release sites, 425 and if the release sites are close to Ca^{2+} channels, the high Ca^{2+} concentration in the 426 microdomains around the channels created by a single spike may be just as effective as that due 427 428 to a burst in triggering fusion of granules. Indeed, we found that spiking is as effective as bursting in releasing a full pool of primed granules, as long as the release site is within 100 nm 429 430 from the channel (Fig. 4). However, if the primed pool of granules is initially empty, or if the release site is located more than 100 nm from the channel, we found that bursting was always 431 432 more effective than spiking in triggering granule fusion.

There are two mechanisms for this difference between bursting and spiking. The first 433 results from the larger entry of Ca²⁺ caused by bursting over spiking. Because the fraction of 434 open Ca^{2+} channels is increased for a longer period of time during a burst than during a spike, a 435 burst causes a larger increase in bulk Ca²⁺. Since the replenishment of the primed pool of 436 granules depends on bulk Ca^{2+} , bursting causes a higher rate of granules priming, which in turn 437 results in a higher rate of granule fusion. This effect is independent of the microdomain Ca²⁺ 438 concentration, so bursting causes a higher rate of granule fusions even if the release site is 100 439 nm or less from the channel (Fig. 5 top panels). However, this mechanism relies on the fact that, 440

441 at similar event frequency, bursting means that the electric potential across the cell membrane 442 stays high (i.e., at levels where the cell Ca^{2+} current is high) for a larger fraction of time than 443 spiking. If spiking frequency is increased relative to bursting frequency so that the total amount 444 of active time is the same, then bulk Ca^{2+} will be similar and so will the priming rate. In that 445 sense, the bursting pattern is not more effective than the spiking pattern if the amount of activity 446 (and therefore Ca^{2+} entry) is normalized.

Nevertheless, there is a second mechanism that makes bursting more effective than 447 spiking at triggering granule fusion, even if we normalize by the total amount of Ca^{2+} entry. 448 Because three free Ca^{2+} ions must bind to the release machinery to trigger fusion, fusion is 449 facilitated by a stable high local Ca^{2+} level. This is more likely to happen during bursting than 450 spiking, since Ca^{2+} influx can be maintained longer during a burst than during a spike. This 451 advantage of bursting can be observed when the release site is more than 100 nm away from the 452 channel (Fig. 5 bottom panels). Cells must quickly restore intracellular Ca^{2+} to low levels using 453 ATP-driven pumps, so there is an energetic cost associated with the entry of each Ca²⁺ ion. For 454 release sites far from the Ca²⁺ channels, the bursting pattern of activity results in a more efficient 455 use of Ca^{2+} ions than the spiking pattern. 456

This may not be true at higher spike frequencies. If we increase spike frequency the 457 interval between each increase in local Ca^{2+} goes down, so the higher effectiveness of bursting 458 might only be observed for release sites further away from the channels. We see that for the BK 459 (endogenous or injected by dynamic clamp) vs. no BK (i.e., in the presense of iberiotoxin) case. 460 where the maximum Ca^{2+} concentration reached at 200 nm (Fig. 10) is similar to what we saw in 461 Fig. 3, but the interspike interval is lower so Ca^{2+} does not go back down for long – in that case 462 spiking is at least as efficient as bursting in evoking release, for release sites up to 500 nm away 463 from the channels (Fig. 11). Nevertheless, the bursting pattern caused by the presence of a BK 464 current evoked more granule fusion because of the high average bulk Ca²⁺ during bursting, 465 466 which results in higher rate of replenishment of the primed granules.

There are many examples in endocrinology where the pattern of a signal plays an important role. A well-known example is that the frequency of hypothalamic gonadotropinreleasing hormone pulses determines the differential release of luteinizing and follicle470 stimulating hormone by gonadotrophs (41). Here we used a hybrid experimental/modeling approach to show that the actual pattern of electrical activity can trigger different rates of 471 472 hormone release. Since the discovery that pituitary cells are electrically active 40 years ago, researchers have wondered how pituitary cells tune electrical activity to regulate hormone release 473 (24). It has been argued that since hypothalamic factors act on a number of ion channels on 474 pituitary cell membranes, electrical activity provides numerous ways for the hypothalamus to 475 modulate pituitary hormone release. Some of these factors may even modulate the time constant 476 of BK channels to switch the electrical activity pattern from spiking to bursting (6). The present 477 work shows that this switch to bursting may improve the effect of hypothalamic stimulating 478 neurohormones in increasing pituitary hormone secretion. 479

In summary, our modeling results show that bursting is superior to spiking in evoking 480 pituitary hormone release, since it brings more Ca^{2+} into the cell, thus augmenting both local and 481 global Ca²⁺ levels, which in turn increases resupply of secretory granules and exocytosis. We 482 found further that channel clustering is advantageous to isolated channels in controlling 483 secretion. Our results have implications beyond pituitary secretion. For example, human 484 pancreatic beta-cells show rapid bursting resembling pituitary plateau bursting (23, 27), which 485 has been suggested to be advantageous for insulin secretion (25). Further, Ca^{2+} channel 486 clustering in beta-cells has been suggested to be important for insulin exocytosis (2). 487

488

489 **GRANTS**

JT and RB were partially supported by grant DMS1220063 from the National ScienceFoundation.

492

493 **DISCLOSURES**

494 No conflicts of interest, financial or otherwise, are declared by the authors.

495

497 **REFERENCES**

- Allbritton NL, Meyer T, Stryer L. Range of messenger action of calcium ion and inositol 1,4,5-trisphosphate. *Science* 258: 1812–5, 1992.
- Barg S, Ma X, Eliasson L, Galvanovskis J, Göpel SO, Obermüller S, Platzer J,
 Renström E, Trus M, Atlas D, Striessnig J, Rorsman P. Fast exocytosis with few
 Ca(2+) channels in insulin-secreting mouse pancreatic B cells. *Biophys. J.* 81: 3308–23,
 2001.
- Bertram R, Smith GD, Sherman A. Modeling study of the effects of overlapping Ca2+ microdomains on neurotransmitter release. *Biophys. J.* 76: 735–50, 1999.
- Chen Y, Wang S, Sherman A. Identifying the targets of the amplifying pathway for insulin secretion in pancreatic beta-cells by kinetic modeling of granule exocytosis. *Biophys. J.* 95: 2226–2241, 2008.
- 5. Dubinsky JM, Oxford GS. Ionic currents in two strains of rat anterior pituitary tumor
 510 cells. J. Gen. Physiol. 83: 309–339, 1984.
- 511 6. Duncan PJ, Sengul S, Tabak J, Ruth P, Bertram R, Shipston MJ. Large conductance
 512 Ca(2+) -activated K(+) channels (BK) promote secretagogue-induced transition from
 513 spiking to bursting in murine anterior pituitary corticotrophs. *J. Physiol.* 593: 1197–1211,
 514 2015.
- Freeman ME, Kanyicska B, Lerant A, Gyorgy N. Prolactin: Structure, Function, and
 Regulation of Secretion. *Physiol. Rev.* 80: 1523–1631, 2000.
- Van Goor F, Li Y-X, Stojilkovic SS. Paradoxical Role of Large-Conductance Calcium Activated K+ (BK) Channels in Controlling Action Potential-Driven Ca2+ Entry in
 Anterior Pituitary Cells. J. Neurosci. 21: 5902–5915, 2001.
- 520 9. Van Goor F, Zivadinovic D, Martinez-Fuentes AJ, Stojilkovic SS. Dependence of
 521 pituitary hormone secretion on the pattern of spontaneus voltage-gated calcium influx.
 522 Cell type-specific action potential secretion coupling. *J. Biol. Chem.* 276: 33840–33846,
 523 2001.
- 10. Van Goor F, Zivadinovic D, Stojilkovic SS. Differential expression of ionic channels in rat anterior pituitary cells. *Mol. Endocrinol.* 15: 1222–1236, 2001.
- Hagiwara S, Ohmori H. Studies of single calcium channel currents in rat clonal pituitary
 cells. J. Physiol. 336: 649–61, 1983.
- Hodgking AL, Huxley AF. A quantitative description of membrane current and its application to conduction and excitation in nerve. *J. Physiol.* 117: 500–44, 1952.

- Keja JA, Kits KS. Single-channel properties of high- and low-voltage-activated calcium channels in rat pituitary melanotropic cells. *J. Neurophysiol.* 71: 840–55, 1994.
- Kits KS, Mansvelder HD. Regulation of exocytosis in neuroendocrine cells: Spatial
 organization of channels and vesicles, stimulus-secretion coupling, calcium buffers and
 modulation. *Brain Res. Rev.* 33: 78–94, 2000.
- 535 15. Kits KS, de Vlieger T a, Kooi BW, Mansvelder HD. Diffusion barriers limit the effect
 536 of mobile calcium buffers on exocytosis of large dense cored vesicles. *Biophys. J.* 76:
 537 1693–1705, 1999.
- Kits KS, de Vlieger T a, Kooi BW, Mansvelder HD. Diffusion barriers limit the effect of mobile calcium buffers on exocytosis of large dense cored vesicles. *Biophys. J.* 76: 1693–1705, 1999.
- 541 17. Klingauf J, Neher E. Modeling buffered Ca2+ diffusion near the membrane: implications
 542 for secretion in neuroendocrine cells. *Biophys. J.* 72: 674–90, 1997.
- Li YX, Rinzel J, Vergara L, Stojilković SS. Spontaneous electrical and calcium oscillations in unstimulated pituitary gonadotrophs. *Biophys. J.* 69: 785–95, 1995.
- Mansvelder HD, Kits KS. The relation of exocytosis and rapid endocytosis to calcium
 entry evoked by short repetitive depolarizing pulses in rat melanotropic cells. *J. Neurosci.* 18: 81–92, 1998.
- 548 20. Matveev V, Zucker RS, Sherman A. Facilitation through buffer saturation: constraints on endogenous buffering properties. *Biophys. J.* 86: 2691–2709, 2004.
- 550 21. Matveev V. CalC The Calcium Calculator Victor Matveev, NJIT.
 551 https://web.njit.edu/~matveev/.
- Milescu LS, Yamanishi T, Ptak K, Mogri MZ, Smith JC. Real-time kinetic modeling
 of voltage-gated ion channels using dynamic clamp. *Biophys. J.* 95: 66–87, 2008.
- Misler S, Barnett DW, Gillis KD, Pressel DM. Electrophysiology of stimulus-secretion coupling in human beta-cells. *Diabetes* 41: 1221–8, 1992.
- 556 24. Mollard P, Schlegel W. Why are endocrine pituitary cells excitable? *Trends Endocrinol.* 557 *Metab.* 7: 361–365, 1996.
- Pedersen MG, Cortese G, Eliasson L. Mathematical modeling and statistical analysis of calcium-regulated insulin granule exocytosis in beta-cells from mice and humans. *Prog. Biophys. Mol. Biol.* 107: 257–264, 2011.
- Pedersen MG. On depolarization-evoked exocytosis as a function of calcium entry:
 Possibilities and pitfalls. *Biophys. J.* 101: 793–802, 2011.

27. 563 Riz M, Braun M, Pedersen MG. Mathematical modeling of heterogeneous electrophysiological responses in human β-cells. *PLoS Comput. Biol.* 10: e1003389, 2014. 564 28. Sherman A, Keizer J, Rinzel J. Domain model for Ca2(+)-inactivation of Ca2+ channels 565 at low channel density. Biophys. J. 58: 985-95, 1990. 566 29. Stojilkovic SS, Tabak J, Bertram R. Ion channels and signaling in the pituitary gland. 567 Endocr. Rev. 31: 845-915, 2010. 568 30. Stojilkovic SS, Zemkova H, Van Goor F. Biophysical basis of pituitary cell type-569 570 specific Ca2+ signaling-secretion coupling. Trends Endocrinol. Metab. 16: 152-9, 2005. 31. Stojilkovic SS. Ca2+-regulated exocytosis and SNARE function. Trends Endocrinol. 571 Metab. 16: 81-83, 2005. 572 Stojilkovic SS. Pituitary cell type-specific electrical activity, calcium signaling and 32. 573 secretion. Biol. Res. 39: 403-423, 2006. 574 575 33. Tabak J, Gonzalez-Iglesias AE, Toporikova N, Bertram R, Freeman ME. Variations in the response of pituitary lactotrophs to oxytocin during the rat estrous cycle. 576 577 Endocrinology 151: 1806–13, 2010. Tabak J, Tomaiuolo M, Gonzalez-Iglesias a. E, Milescu LS, Bertram R. Fast-578 34. 579 Activating Voltage- and Calcium-Dependent Potassium (BK) Conductance Promotes Bursting in Pituitary Cells: A Dynamic Clamp Study. J. Neurosci. 31: 16855–16863, 580 2011. 581 35. Tashjian AH, Yasumura Y, Levine L, Sato GH, Parker ML. Establishment of clonal 582 strains of rat pituitary tumor cells that secrete growth hormone. Endocrinology 82: 342-583 52, 1968. 584 Thomas P, Surprenant a, Almers W. Cytosolic Ca2+, exocytosis, and endocytosis in 585 36. single melanotrophs of the rat pituitary. Neuron 5: 723-733, 1990. 586 Thomas P, Wong JG, Lee a K, Almers W. A low affinity Ca2+ receptor controls the 587 37. final steps in peptide secretion from pituitary melanotrophs. Neuron 11: 93–104, 1993. 588 Tse A, Hille B. GnRH-induced Ca2+ oscillations and rhythmic hyperpolarizations of 589 38. pituitary gonadotropes. Science. 255: 462-464, 1992. 590 Vardjan N, Jorgačevski J, Stenovec M, Kreft M, Zorec R. Compound exocytosis in 591 39. pituitary cells. Ann. N. Y. Acad. Sci. 1152: 63-75, 2009. 592 593 40. **Voets T**. Dissection of Three Ca2+-Dependent Steps Leading to Secretion in Chromaffin Cells from Mouse Adrenal Slices. Neuron 28: 537-545, 2000. 594

- Wildt L, Häusler A, Marshall G, Hutchison JS, Plant TM, Belchetz PE, Knobil E. Frequency and amplitude of gonadotropin-releasing hormone stimulation and gonadotropin secretion in the rhesus monkey. *Endocrinology* 109: 376–85, 1981.
 Zorec R, Sikdar SK, Mason WT. Increased cytosolic calcium stimulates exocytosis in
- bovine lactotrophs. Direct evidence from changes in membrane capacitance. J. Gen. *Physiol.* 97: 473–497, 1991.
- 601

603 FIGURE CAPTIONS

Figure 1. Calcium diffusion characteristics in the model. a) Spherical cell model used in 604 simulations. The cell diameter is 13 μ m. Ca²⁺ diffusion and buffering are simulated in a conical 605 region of the sphere. The channel or channel cluster is located at the center of the cone base on 606 the surface of the sphere. The base radius in the single channel case is 1.5 µm and in the cluster 607 case 3.3 μ m. b) Upper panel: submembrane Ca²⁺ concentrations (color coded, in μ M) as a 608 function of time and the distance to the channel (d, measured along the cone base as indicated in 609 panel a) during spiking electrical activity. Lower panel: Ca^{2+} concentration at 500 nm from the 610 channel as function of time. 611

Figure 2. Kinetic scheme of the exocytosis model. The pool N_0 consists of granules primed for fusion and its resupply depends on the bulk cytosolic Ca²⁺ concentration C_i . Fusion occurs upon Ca²⁺ binding controlled by the local concentration of Ca²⁺, C_{loc} . The pools N_1 , N_2 , N_3 correspond to the three Ca²⁺ bound states, and u_1 is the fusion rate.

Figure 3. Ca^{2+} concentration at different distances from a single stochastic Ca^{2+} channel on the surface of a conical region (average of 10 independent trials). The Ca^{2+} channel is placed at the center of the cone base with radius 1.5 µm. The Ca^{2+} concentration is determined using a mathematical model, in response to actual spiking (A) and bursting (B) voltage traces from a gonadotroph. The switch to bursting was obtained by injecting a model BK-current into a spiking cell using the dynamic clamp technique.

Figure 4. Single channel exocytosis simulation results with N_0 =40 primed granules as initial condition. Number of fused granules (average of 10 simulations) during spiking (dashed curve) and bursting (solid curve) electrical activity for different distances between the single Ca²⁺ channel and a release site as a function of time.

Figure 5. Single channel exocytosis simulation results with all the pools initially empty. Top panels (i) show the number of fused granules as a function of time, as in Fig. 4. Bottom panels (ii) show the cumulative number of fused granules during 5 seconds of simulation as function of the cumulative calcium entry Q. (A) granules located at 30 nm, (B) 100 nm, (C) 200 nm, (D) 300 nm, or (E) 500 nm from the channel. Figure 6. Summary of single channel exocytosis results with all the pools initially empty. The bursting-to-spiking ratio of the total number of fused granules during 5 seconds of electrical activity (solid line) shows that bursting evokes more secretion at all distances. In contrast, the bursting-to-spiking ratio of the total number of granules normalized to change entry Q (dashed line) shows that the efficiency of spiking and bursting are comparable for release sites located close to the channel, but that bursting has superior efficiency farther from the channel.

Figure 7. Ca^{2+} concentrations for a cluster of 5 channels (average of 5 independent trials). The Ca²⁺ channel is placed at the center of the cone base with radius 3.3 µm. The Ca²⁺ concentration is determined using the mathematical model, in response to actual spiking (A) and dynamicclamp induced bursting (B) voltage traces from a gonadotroph (same traces as in Fig. 3).

Figure 8. Channel cluster exocytosis simulation results with all the pools initially empty. Top panels (i) show the number of fused granules as a function of time, evoked by spiking (dashed curve) or bursting (solid curve). Bottom panels (ii) show the cumulative number of fused granules during 5 seconds of simulation as a function of the cumulative Ca^{2+} entry *Q*. (A) granules located at 30 nm, (B) 100 nm, (C) 200 nm, (D) 300 nm, or (E) 500 nm from the channel.

Figure 9. Summary of channel cluster exocytosis results with all the pools initially empty. The bursting-to-spiking ratio of the total number of fused granules during 5 seconds of electrical activity (solid line) shows that bursting evokes more secretion at all distances. In contrast, the bursting-to-spiking ratio of the total number of granules normalized to change entry Q (dashed line) shows that the efficiency of spiking and bursting are comparable for release sites located close to the channel cluster, but that bursting has superior efficiency farther away.

Figure 10. Ca^{2+} concentration at different distances from a stochastic Ca^{2+} channel on the surface of a conical region (average of 10 independent trials). The Ca^{2+} channel is placed at the center of the cone base with radius 1.5 µm. (A) Bursting profile in control condition. (B) Spiking profile in the presence of the BK channel blocker iberiotoxin. (C) Bursting profile in the presence of iberiotoxin and when BK current is injected back using the dynamic clamp. Sub panels show the experimentally recorded voltage profile (i), and simulated Ca^{2+} concentrations at 30 nm (ii), 200 nm (iii), or 1500 nm (iv) from the channel. Figure 11. Single channel exocytosis simulation results with all the pools initially empty for dynamic clamp-induced bursting. Top panels (i) show the number of fused granules as a function of time, evoked by a spiking voltage trace (gray dashed curves) and bursting induced by dynamic clamp in the presence of iberiotoxin (black solid curves). Bottom panels (ii) show the cumulative number of fused granules during 5 seconds of simulation as a function of the cumulative Ca²⁺ entry Q. (A) granules located at 30 nm, (B) 100 nm, (C) 200 nm, (D) 300 nm, or (E) 500 nm from the channel.

Figure 12. Summary of exocytosis simulation results with all the pools initially empty during BK-current block and dynamic clamp. The ratios of the total number of fused granules between bursting that results from dynamic clamp application with iberiotoxin vs. spiking that results from iberiotoxin alone (solid black curve). The ratios of the total number of fused granules normalized to the charge entry Q are given by the dashed curves.

Parameter	Value	Unit		
Current Simulation				
S _m	7	mV		
v _m	-4	mV		
k_+	0.0234	ms ⁻¹		
<i>k</i> .	0.018	ms ⁻¹		
g Ca	20	pS		
Diffusion Simulation				
D_{Ca}	0.22	$\mu m^2 s^{-1}$		
B _{total}	900	μΜ		
K_D	10	μΜ		
k _{on}	0.1	$\mu M^{-1}ms^{-1}$		
k_{off}	1	ms ⁻¹		
$[Ca^{2+}]_0$	0.22	μΜ		
Secretion Model				
k_{I}	3.7	$\mu M^{-1}s^{-1}$		
<i>k</i> - ₁	100	s ⁻¹		
r_1^0	3.6	s ⁻¹		
K_p	2.3	μΜ		
r ₋₁	0.001	s ⁻¹		
<i>u</i> ₁	1000	s ⁻¹		

Table 1. Default parameters of the Ca^{2+} channel model, Ca^{2+} diffusion simulations and exocytosis model.









200 nm

1500 nm

30 nm

















