

33 **Deterioration modelling of small-diameter water pipes under limited**
34 **data availability**

35

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37

38 **Abstract**

39 High volume and low value buried infrastructure assets in the water distribution network are typically
40 less well understood and often sub-optimally managed in comparison to more critical or higher value
41 assets. This is despite attracting an estimated yearly expenditure from water utilities operating in the
42 developed World in excess of £4.42 billion per annum.

43 To address this problem the authors have developed a comprehensive deterioration modelling
44 framework founded on latest geospatial technologies and statistical analysis. The modelling
45 framework is specifically applied to small diameter (25-50mm) water distribution assets, known as
46 communication pipes, which connect individual customers to water distribution mains.

47 Reliability curves are developed from failure data provided by two UK based Water Companies that
48 have captured specific communication pipe failure records since 2001. The deterioration modelling
49 curves and supporting data are compared and contrasted to demonstrate the robustness of this
50 modelling approach, which is shown to be capable of modelling failure rates to a high degree of
51 accuracy. This was validated by comparing the predicted number of failures against three years of
52 failure data not used in the model building process. The yearly failure counts were predicted to within
53 +/-5% accuracy and the overall cumulative modelled failure count at the end of 2014 was predicted
54 within 1%.

55

56 **Key words**

57 Deterioration Modelling, Water distribution, Asset Management

58 **List of Notation**

- 59 $f(T)$ is the probability of failure at time T
- 60 $F(T)$ is cumulative probability of failure at time T
- 61 $R(T)$ is the probability of an asset remaining in service at time T
- 62 T is time in years
- 63 β is the Weibull shape parameter
- 64 η is the Weibull scale parameter in years
- 65 γ is the Weibull location parameter
- 66

67 Introduction

68 Communication pipes are defined as the water carrying assets that lie between the water main and
69 the boundary of the private property being supplied. If a stop-tap or water meter is fitted this usually
70 represents the end of the communication pipe and beyond this point the pipework is referred to as the
71 'supply pipe', which, in the UK, is the responsibility of the property owner (Ofwat, 2014). By their very
72 nature communication pipes are considered high volume and low value assets. With typically one
73 asset for each property, the pipework is of small diameter (25 - 50mm) and the length of the asset lies
74 somewhere between 2-3m or 6-9m depending on the nature of the connection to the distribution
75 main. Shorter connections, which typically occur when the property is located on the same side of the
76 road as the distribution main are known as "short-side" communication pipes. Where-as
77 communication pipes that required a road crossing, due to the location of the distribution main to
78 property, are known as "long-side" connections.

79 In contrast, distribution mains can serve hundreds of customers usually range in size between 50 and
80 300mm in diameter. These assets are typically laid within the road and have significantly higher
81 failure costs, not only due to the more vigorous and challenging repair techniques but as a result of
82 the number of customers impacted. It is, therefore, understandable that past research effort has
83 centred around the proactive management of these larger assets as the economic and social costs of
84 pipe failures continue to rise (Engelhardt et al., 2000). However, an analysis of water company
85 replacement figures between 2002 to 2010 has revealed that on average over 130,000
86 communications pipes are replaced each year across England and Wales (Ofwat, 2010). An assumed
87 replacement cost of £800 per communication pipe would yield a capital investment value of £104M.
88 Water utilities in England and Wales are not obligated to report operational expenditure against
89 individual asset groups, but it is suspected that the Operational expenditure associated with these
90 assets is in the region of an additional 80-120% of the capital value; therefore generating a £200M
91 total expenditure budget in England and Wales for communication pipes alone. Assuming equivalent
92 investment levels for communication pipes in other developed regions of the World, approximately
93 17.8% of the global population, would yield an annualised total expenditure in excess of £4.42bn
94 (\$6.95bn) in these regions alone (United Nations, 2011). Therefore, when considered as a collective
95 asset stock, the global investment in the more developed regions of the World is significant enough to

96 warrant the use of a deterioration model to better understand and manage the performance of these
97 assets in the future. This could be achieved by using the outputs from the deterioration analysis to
98 proactively target the replacement of poorly performing assets, or, via an awareness of upcoming
99 investment requirements and future failure rates.

100 Pipe deterioration modelling can take many forms. At the highest level, models are distinguished by
101 their nature, either physical or statistical. Physical models, generally speaking, are built around the
102 understanding of the underlying physical parameters that govern pipe failure. These require the
103 acquisition of detailed information about the pipe(s) being modelled for accurate predictions to be
104 established (Rajani and Kleiner, 2001). Currently, the collection of this data is costly and it is not
105 widely available across the whole distribution network. Even when data is available, it is commonly
106 limited to water mains of larger diameters which tend to be critical in nature. Therefore, the
107 expenditure associated with the collection of this data is unjustifiable; particularly so for lower value
108 assets like communication pipes.

109 An alternative solution is to use statistical based models which evaluate the relationship between
110 water main condition and key pipe characteristics by the use of historical data, which is mined and
111 statistically evaluated to find patterns that can then be used to formulate a deterioration modelling
112 equation. The most cited and widely recognised publications at the forefront of statistical modelling in
113 the water industry at the time were (Shamir and Howard, 1979), (Clark et al., 1982) and (O'Day et al.,
114 1986). The early developments in these models took a linear form and a few fundamental draw backs
115 have since been identified with linear based models. The main disadvantage is that these models
116 were heavily reliant on the availability of sufficient data for each pipe class for the rate of deterioration
117 to be established without the interference of third party influences that lead to failure. These third
118 party causes are commonly referred to as 'noise' because of their undesired influence on the
119 identification of failure rates. Another important and restricting factor is that these models did not
120 include data from assets where failure had not yet occurred, even though in some instances failure
121 was imminent.

122 In the early 1990's semi-Markovian models were used to describe the deterioration process (Li and
123 Haines, 1992). The semi-Markovian model is a simplification of the deterioration process by
124 modelling the current condition of an asset in one of a number of states. A probability is then applied

125 to each asset to account for the likelihood of it moving into another state over a given time period.
126 These types of model are the more commonly applied where condition information, obtained through
127 inspections conducted over-time, is available. For this reason, semi-Markov deterioration models
128 developed for sewerage assets, where condition inspection information is plentiful, have been found
129 to provide an accurate representation of the assets deteriorating behaviour, (Ward et al., 2014).

130 Although less well published, Artificial Neural Networks (ANN) have also been applied to distribution
131 main networks with the aim of learning the pipe breakage frequency rate through the use of historical
132 incident data and to subsequently predict the future. Sacluti (1999) demonstrated their effectiveness
133 rather early on in development of ANN's for civil engineering applications in a case study in
134 Edmonton, Canada. Jafar et al. (2010) had similar success by coupling an ANN with Multiple-Linear
135 Regression in a distribution network in Wattrelos, France. The authors also both acknowledged
136 potential benefits in the use of ANN's for establishing rehabilitation strategies. Evolutionary
137 Polynomial Regression (EPR) is another machine learning technique used to predict deterioration and
138 failure by discovering patterns in pipe failure data amongst homogenous groups (Giustolisi and Savić,
139 2006). The EPR model produces simple relationship equations between a number of variables and
140 confirmed the importance of; pipe age, diameter and length; when considering pipe burst frequencies
141 and occurrences. The benefit of EPR over more conventional data mining techniques is the simplicity
142 of the relationship equations although it is reliant on the accuracy of the data modelling inputs (L
143 Berardi et al., 2008).

144 The application of whole life cost modelling for investment planning is a natural progression from
145 statistical deterioration models which usually form the foundations of the approach (Lei and Sægrov
146 1998). An aggregated statistical model was used in this study alongside a lifetime modelling tool to
147 develop optimised planning regimes. Similar techniques have been used to try to determine the
148 optimal time for pipe replacement by forecasting the service life of a water main under two
149 intervention scenarios; replacement or rehabilitation, (Shamir and Howard, 1979). In advancement
150 towards multi-objective optimisation, researchers have considered how to evaluate the problem of
151 maximising network performance whilst minimising cost. The benefits of presenting the problem in a
152 multi-objective framework are that solutions take the form of a trade-off between cost vs. benefit.
153 Thus, cheaper solutions with lower benefit and lower cost implications are not overlooked; there-by

154 giving the decision maker a broader range of the potential solutions available to them. Halhal et al.,
155 (1997) is one of the first cited examples in this field and work continues, (Berardi et al., 2008),
156 (Engelhardt et al., 2002) and (Nafi and Kleiner, 2010).

157 The aforementioned literature reaffirms that the benefits of these technologies are already being
158 realised for larger and more critical assets, e.g., distribution mains. Water companies are harnessing
159 the power of these techniques to help them select optimal intervention timings and solutions, whilst
160 also targeting maintenance towards poorly performing, high risk assets. In contrast, communication
161 pipes form a typically unmapped and unattributed asset stock, which are often sub-optimally managed
162 as a result of insufficient knowledge and un-optimised investment plans. Although these assets are
163 deemed low value infrastructure in comparison to distribution mains, the high asset volume means
164 that substantial yearly capital investment is needed to maintain serviceability, thus justifying the
165 development and application of a deterioration model to help utility managers better understand the
166 performance of communications pipe. Ward et al. (2015) have progressed the deterioration model
167 further via the development of an asset level decision support tool used to trade-off between whole
168 life costs (totex) and the prevention of future asset failures (serviceability).

169

170 **Methodology**

171 The starting position for the study is to address the lack of data availability and quality for
172 communication pipes, which are often two of the governing factors presenting a barrier to the
173 successful deployment of effective asset management techniques for high volume-low value
174 infrastructure, i.e., where information surrounding the extent, attribution and condition of the asset
175 stock is limited (Vangdal and Reksten, 2011). To overcome this knowledge gap a set of notional
176 assets, which are arbitrary straight line connections formed between customer property address
177 points and the nearest most relevant distribution mains (or trunk main) are generated using a
178 Geospatial Information System (GIS). This approach also allowed for an approximation of asset
179 length. However, with all geospatial processes of this nature some un-realistic asset lengths are
180 created due to the variability of specific individual locations, i.e., where a property actually connects
181 directly to a near-by trunk main but it is digitised as a connection to a distribution main considerable
182 distance away. To account for these anomalies, all notional asset lengths are plotted on a frequency

183 distribution by asset length graph, to help identify a threshold at which individual assets beyond a
184 certain length become highly unlikely or unrealistic. Notional assets lengths exceeding this threshold
185 are subsequently assigned the mean length for the group to avoid unrealistically long lengths biasing
186 the model. For communication pipes, this approach is applied to two groups of asset; short and long
187 side communication pipes. Where-by a long-side communication pipe is defined as a communication
188 pipe connecting to the water main across a road, i.e., the water main is located in the opposite
189 carriage way of the road to the property being supplied. Assets that do not cross a road centre line
190 have been defined as short-side connections for the purpose of this study. The authors deemed this
191 to be a reasonable approach and achieve the main aim of the analysis which is to distinguish between
192 assets with higher associated failure costs, due to asset length and social distribution, e.g., road
193 closures.

194 Determining and attributing pipe dates retrospectively cannot be precise. Therefore, a logical data
195 hierarchical procedure is developed to take advantage of the most appropriate data sources available.
196 Depending on data availability the process uses a mixture of: corporate communication pipe and
197 distribution mains asset age data; property age estimates from the HM Revenue and Customs
198 (HMRC) Valuation Office Agency (VOA); and historic mapping. Each of the data sets were used in the
199 following manner: Distribution mains age was used as an approximation for communication pipe age
200 by identifying which distribution main the communication pipe was connected to and using the
201 installation date for this asset as a surrogate for its own age. This was only applied so long as the
202 distribution main had not been rehabilitated which would have reset the age of the asset. Property
203 age estimates from HMRC Valuation Office Agency were provided at postcode level and despite not
204 being applicable to an individual property, the methodology assumes that the data could be applied
205 with reasonable accuracy where the majority of properties within a postcode were of the same age.
206 Finally, an analysis of historic mapping created development regions, formed by observing the growth
207 of a town over time, Figure 1. For example, housing estates shown on maps produced in 1950 that
208 were previously not visible on a 1940's map were attributed, via selections within polygons, as a
209 1940-1950's development.

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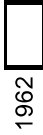
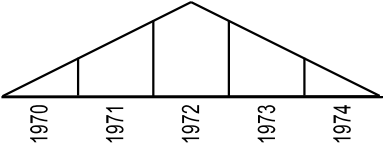
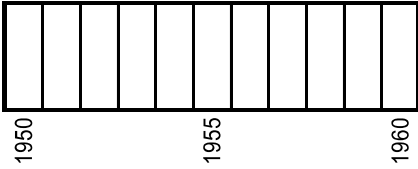
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212 **Figure 1. Development regions**

213 To handle the uncertainty associated with this type of methodology, unique distributions are assigned
214 to each asset depending on the level of confidence surrounding the data source and/or the range of
215 dates it covers. Therefore, the characteristics of a single asset are spread across multiple years
216 according to the distribution, where-by the distribution is selected according to the confidence levels
217 assigned to the different data sources. Whilst it may seem obscure to further segregate individual
218 assets over age ranges, when the asset stock is considered at regional level this approach provides
219 an improved representation of the network by spreading potential uncertainties in the data. Table 1 is
220 prepared to help visualize the different distributions.

221

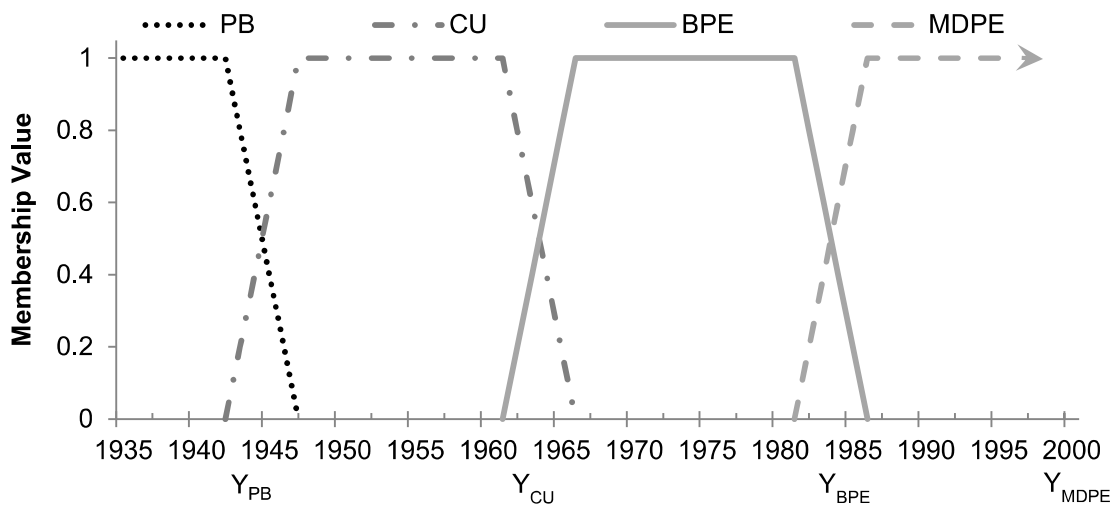
222 **Table 1. Age data uncertainty distributions**

Data Source	Visual representation	Justification
Installed year		Uniform distribution for a single year, where the date is known to be accurate and correct.
Mains Age		The mains installation year is reasonably reliable therefore only a small distribution is applied, centered around the installation year, i.e., 1972.
VOA & Historic mapping		Uniform distribution from the earliest to the latest date spanned by the range for each individual year.

223

224 After establishing a commissioning distribution for each communication pipe, a further procedure is
 225 developed to determine the likely material for the asset. This assessment was based on industry
 226 research publications and engineering experience from operational management teams who worked
 227 to identify unique operating zones where different materials were installed over-time, (WRc and
 228 UKWIR, 2005). Within these zones unique material age usage profiles were assigned to help account
 229 for the subtle differences surrounding the materials installed over time, often dictated by a local
 230 council's preferences or availability of materials in the region. Rather than using traditional binary
 231 indicators which would assign a single material to an individual asset, the methodology adopts a type
 232 -1 fuzzy inference system (Mendel, 2000). IF-THEN rule sets are used to define the fuzzy
 233 membership of an asset to different pipe materials, depending on its age. The use of this technique
 234 has helped to address the deficiencies that are inherent in the application of binary logic to imprecise
 235 systems by propagating uncertainties through the model (Kleiner et al., 2009). Membership functions
 236 are often applied to linguistic variables that describe a condition or state which is imprecise. However,
 237 in this instance the installation date for the asset is used as the antecedent to which the fuzzy
 238 inference system is applied, in order to derive the consequent which is expressed as a fuzzy
 239 membership of the asset to specific materials .There-by addressing the uncertainty of the material
 240 used at each installation date and also accounting for the phasing in and out of different materials

241 over time. Figure 2 depicts a typical material usage profile showing the phasing in and out of materials
 242 overtime for a single operating zone that installed Lead (PB), Cooper (CU), Black Polyethene (BPE)
 243 and Medium Density Polyethylene (MDPE) pipework overtime. A five year phasing in out period was
 244 identified by both operational teams as the most likely representation of reality due to the fact that
 245 new pipe materials take time to establish themselves as the preferred technology and the stock of the
 246 material being replaced takes time to be depleted. As such, assets installed within a transition period
 247 are attributed with a percentage of both materials, e.g., 20% CU and 80% BPE for assets installed
 248 within this operating zone in 1965.



249

250 **Figure 2. Material usage profile for an individual operating zone**

251 The key assumption underpinning the deterioration modelling process is that all assets in the same
 252 material peer group and of the same age have the same probability of failure. The process fully
 253 accounts for the assets having different commissioning years and different failure years, whilst
 254 applying this age assumption. Hence a PB pipe commissioned in 1930 and reported as failing in
 255 2000 is equivalent in age and hence behaviour to a similar pipe commissioned in 1938 and reported
 256 as failing in 2008. A diagrammatic representation of the full modelling process is presented in Figure 3
 257 which is interpreted as follows. Starting with a random estimation for Weibull parameters, the asset
 258 stock and associated failure counts are modelled on a yearly basis from 1837 to present day, taking
 259 into account new assets that are installed in each year and the predicted failures by material type.
 260 The mathematical form of the 3-parameter Weibull probability density function (pdf) is displayed in
 261 Equation (1), together with the corresponding cumulative Weibull distribution function in Equation (2)

$$262 \quad f(T) = \frac{\beta}{\eta} \left(\frac{T-\gamma}{\eta} \right)^{\beta-1} e^{-\left(\frac{T-\gamma}{\eta} \right)^\beta} \quad (1)$$

$$263 \quad F(T) = 1 - e^{-\left(\frac{T-\gamma}{\eta} \right)^\beta} \quad (2)$$

264 In each year the simulated failures are recorded for each pipe material to allow for a comparison
 265 against the observed failures during the observation window, 2001 and 2011. The individual errors for
 266 each material are then aggregated to provide an overall assessment of error which is used as the
 267 measurement of accuracy during the calibration process. An aggregated error is used to ensure that
 268 the interaction and transition between the different pipe materials are fully accounted for, i.e., as one
 269 asset fails in one of the material groups it can become re-born as a new asset in the same or a more
 270 modern material group depending on the fuzzy rule set applied. This material transition is achieved in
 271 the model by the use of feedback, applied at each time step, to account for the effects of the historic
 272 repair and/or replacement activity. The repair and replacement rates are fixed over time but are
 273 variable by material type – this is necessary to reflect actual business policy whereby certain
 274 materials are replaced more than others. Upon replacement of the pipe, where this is by a different
 275 material, feedback is used to account for the reduction in the former material and the gain in the new
 276 material stock. Future failures of the replacement material(s), known as secondary failures, are
 277 modelled under the same process. Conversely, whilst repairs do not alter the original pipes material,
 278 an adjustment is made in the model to allow for the fact that a pipe failed at particular age and is re-
 279 born in the same material group – effectively a “new” pipe, but with the same probability of failure as
 280 its peers. Two examples are provided to demonstrate this concept for an asset commissioned in 1920
 281 and attributed as 100% PB material.

282 1) *If failure year = 1963 And, intervention type = Replacement*

283 *Then, PB failure count for pipe age 43 years = +1*

284 *And, PB asset stock count for pipe age 43 years = - 1*

285 *And, BPE asset stock count for pipe age 1 years = + 0.8*

286 *And, CU asset stock count for pipe age 1 years = + 0.2*

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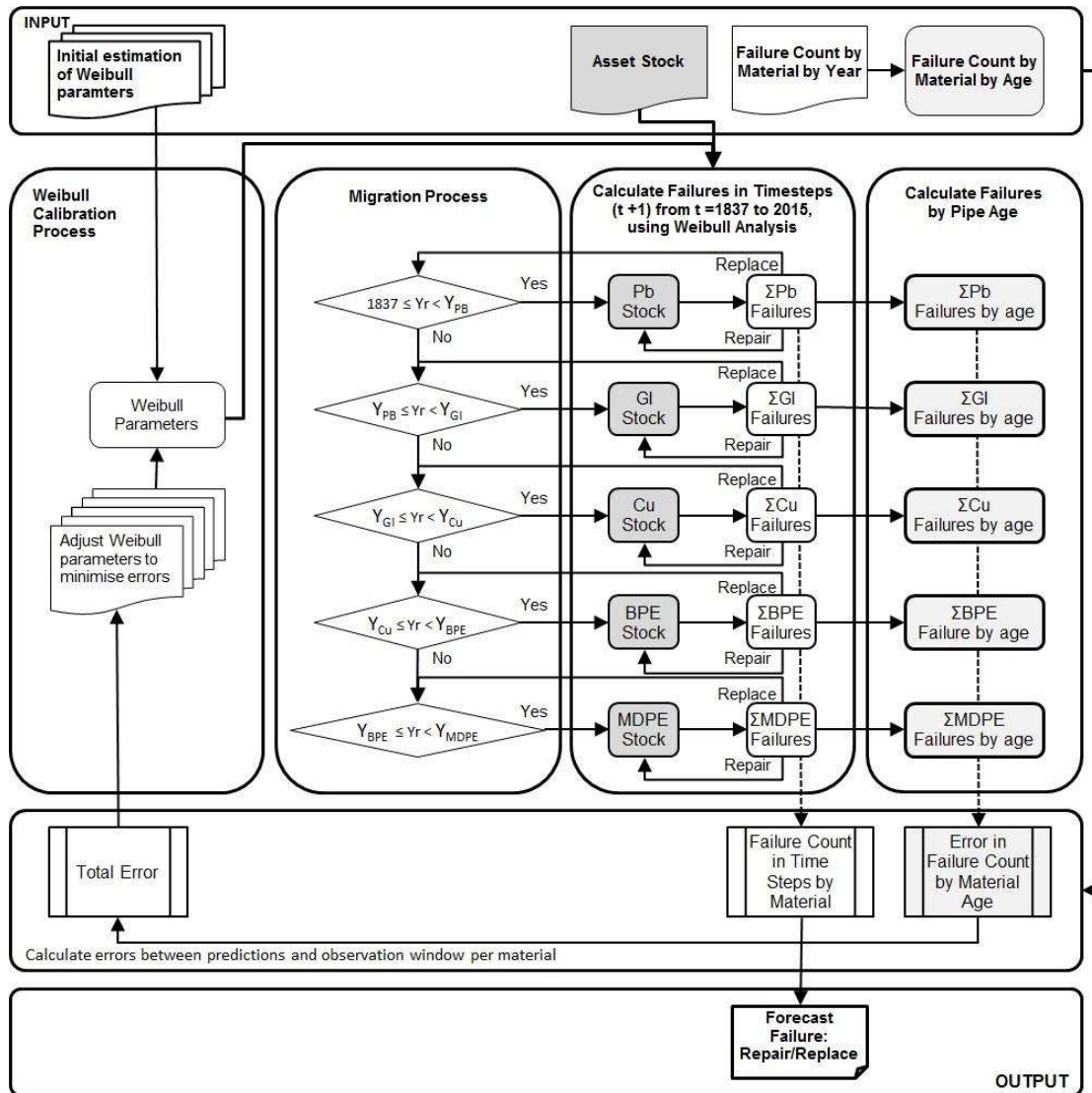
288 2) *If* failure year = 1963 *And*, intervention type = Repair

289 *Then*, PB failure count for pipe age 43 years = +1

290 *And*, PB asset stock count for pipe age 43 years = +/- 0

291

292 The calibration process itself is an iterative procedure which seeks to minimise the aggregated error
293 by solving for the Weibull parameters for each pipe material to give the most representative failure
294 output. The calibration process solves for all three Weibull parameters using either: 1. The method of
295 least squares, solved by using the non-linear generalized reduced gradient method (Lasdon et al.,
296 1974); or, 2. Through the application of a multi-objective genetic algorithm considering the residual
297 error in two dimensions, using the NSGAI algorithm in GANetXL (Bicik et al. 2008; Savić et al. 2011).
298 Whilst the genetic algorithm offered a minor improvement in the overall calibration of the parameters,
299 the computational requirement did not warrant its use. Therefore, for the purposes of expediency, the
300 Weibull parameters are calibrated using the method of least squares.



301 **Figure 3. Material migration in a deterioration modelling framework**

302

303 The output from the process is a calibrated set of Weibull parameters which describe probability of
 304 failure for each pipe material over its lifecycle. The probabilities of failure over time have been
 305 transformed into a more commonly used metric, reliability, for the comparison of asset performance in
 306 the case studies. Reliability values at yearly asset age time steps are calculated by subtracting the
 307 cumulative probability of failure from 1, to obtain a probability value between 0 and 1 which describes
 308 the percentage of asset stock likely to be in service at any asset age (T), Equation 3.

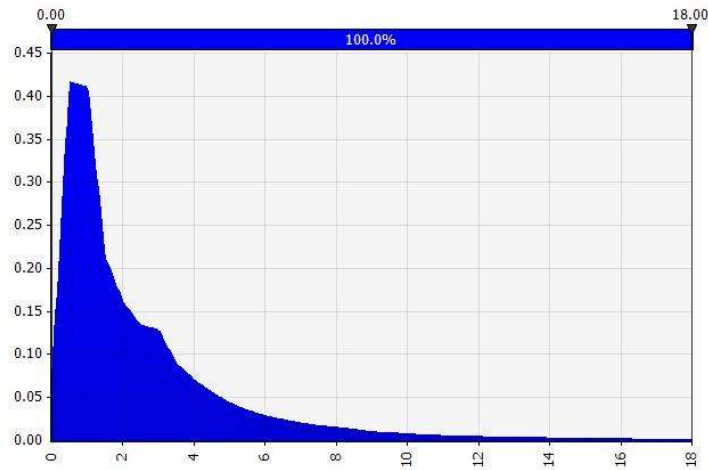
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$$R(T) = (1 - F(T)) = 1 - \left(1 - e^{-\left(\frac{T-\gamma}{\eta}\right)^\beta}\right) \quad (3)$$

310

311 **Case Study**

312 The modelling approach has been developed to model the deterioration and failure of communication
313 pipes assets which have previously presented a challenge to utility managers due to the typically
314 unmapped and unattributed nature of the asset stock. The methodology has been applied
315 independently to two English water utility providers, allowing testing of the accuracy and robustness of
316 the approach. Both companies in this study own and operate a similar sized asset portfolio of
317 approximately 800,000 communication pipe per Water Company, of which c.85% are unmapped in
318 both organisations.

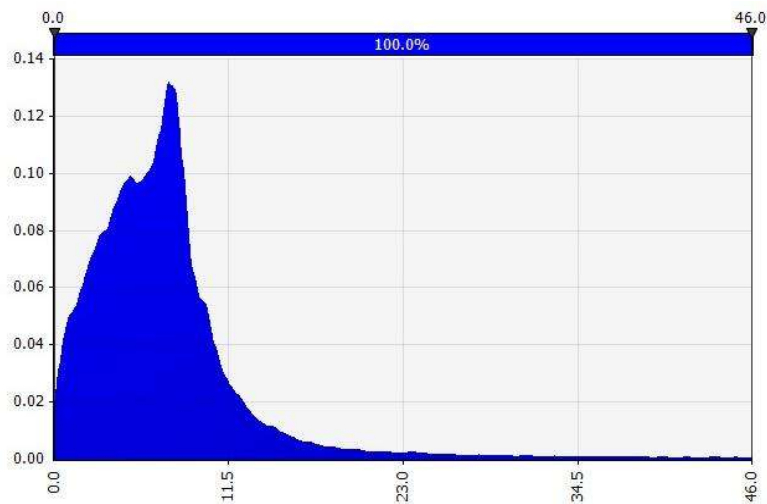
319 The previously described notional communication pipe asset digitisation and attribution process,
320 developed in GIS, was run for all unmapped and/or unattributed assets across both regions. A
321 frequency distribution by asset length graph was then used to identify a threshold at which individual
322 assets beyond a certain length become highly unlikely or unrealistic in each region to account for local
323 geographic conditions and typical arrangements. The outputs for Water Company 1 provided a
324 threshold of 18m and 46m for short-side and long-side communication pipes lengths respectively. A
325 mean length value of 2.5m and 7.3m for short and long-side connections was observed and these
326 mean values were applied as corrections to all notional assets in excess of the threshold lengths. As
327 expected, a greater standard deviation from the mean was witnessed for long side connections of
328 5.4m versus 2.7m for short-side connections. This is to be expected and reflects the non-standard
329 property layouts for dwellings set back from the road, as opposed to those that follow more traditional
330 construction arrangements that run parallel to the road alignment. The short and long side
331 communication pipe length distributions, post correction, are shown in Figure 4 and Figure 5 for Water
332 Company 1.



333

334

Figure 4. Short side communication pipe length distribution



335

336

Figure 5. Long side communication pipe length distribution

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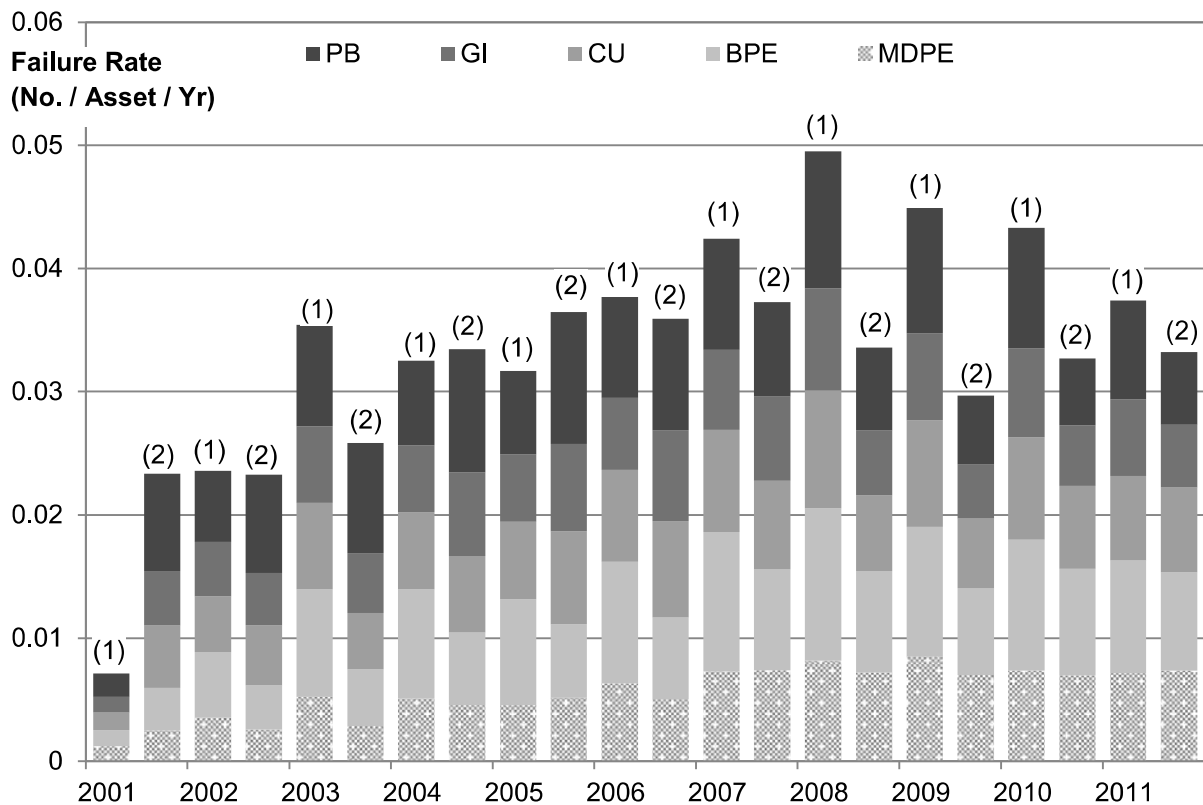
338 Asset age and material were later inferred for the notional asset stock using the most appropriate
 339 available age data source for each asset and the associated fuzzy material rule sets according to the
 340 operating zone encompassing that asset. Eight and twelve distinctly different operating zones and
 341 accompanying fuzzy rules sets were identified by the two utilities companies, leading to the
 342 assignment of the assets within these zones to materials according to the fuzzy rule set for the zone,
 343 e.g., Figure 2. . For the purposes of deterioration model calibration a combined 122,649
 344 communication pipe failure observations were supplied over an eleven year period between 2001 to
 345 2012 by Water Company 1 (60,827 records) and Water Company 2 (61,822 records). A normalised

346 failure rate calculation for each material and each observation year is plotted using Equation 4, Figure
 347 6, to provide a comparison of the failure data supplied by each Water Company.

$$348 \text{ Failure Rate (No. per year)} = \frac{\sum \text{Failures Count}}{\sum \text{Assets}} \quad (4)$$

349 It is observed in Figure 6 that the failure rates witnessed by both companies are broadly in agreement
 350 and identify higher failure rates for PB and BPE pipe materials and lower rates for Galvanised Iron
 351 (GI). Whilst the observed failure rates for PB assets during this window are higher than other
 352 materials, it does not indicate that PB is a poorly performing material. In fact, given the estimated
 353 average age for PB pipes, which were no longer installed past the 1960's, the failure rate is
 354 surprisingly comparable to the more modern pipe material, BPE.

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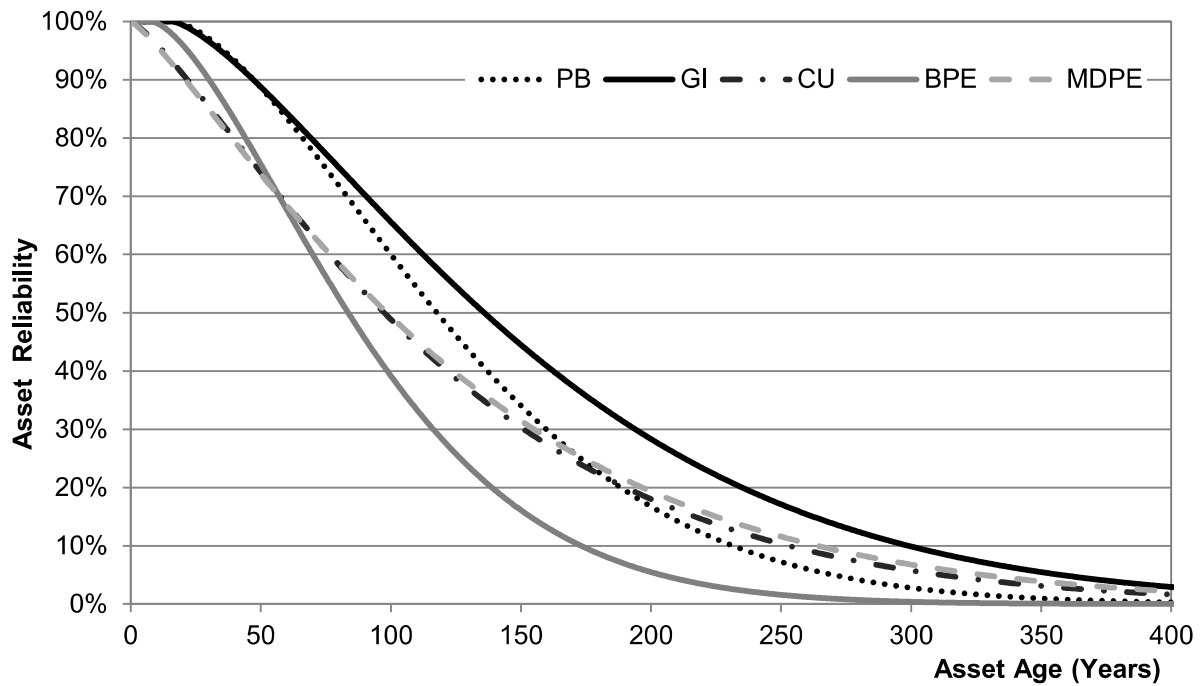
357 **Figure 6. Comparison of failure rates by material type over-time between Water Company (1)**
 358 **and (2).**

359

360 The failure observation records used for the calibration of deterioration curves for each pipe material
361 are applied independently for each Water Company to account for any subtle differences in pipe
362 material performance in each region, which could arise from differing ground conditions, climate
363 variations and/or the quality of workmanship during installation. The observations used in the
364 calibration of the deterioration curves were recorded over an eleven year period, 2001 to 2011
365 inclusive. The failure observations for Water Company 1 in 2001 were not used in the calibration
366 process to prevent from biasing the model based on smaller than normal failure counts. The notably
367 reduced failure counts in this year are thought to be due to missing records, captured on a previous
368 work order management database as the company transitioned to a new system. Whilst a failure
369 observation window of ten years is deemed to be relatively low for assets installed as far back as the
370 1800's, statistical modelling techniques have been shown to be successful when applied to buried
371 water distribution network assets with similar failure histories (Røstum, 2000), (Le Gat and Eisenbeis,
372 2000), (Mailhot et al., 2000) and (Pelletier et al., 2003). Given that communications pipes are smaller
373 and less critical assets than those modelled in the aforementioned literature, the availability of failure
374 data is surprising.

375 A Weibull based statistical modelling approach was selected due to the relatively low failure records in
376 respect to the overall asset stock (8%) and for the usefulness of the graphical Weibull survival curve
377 outputs in an engineering and decision making context (Weibull, 1951), Figure 7. It is observed that
378 each pipe material tends to follow a typical S-Curve reliability distribution which can generally be
379 described as follows: Failure at commissioning due to deterioration is generally low, with asset
380 reliability values in excess of 90% for assets under 40 years of age. However, after the initial onset of
381 failure the asset reliability decreases at its fastest rate for a period of time and until it reaches a more
382 steady state of reducing reliability between approximately 75 to 125 years. After the steady state of
383 reducing reliability, incremental change in probability of failure lowers as the asset progresses
384 towards "old age", when the majority of assets in the same class have failed leaving a small residual
385 remaining in a serviceable state for a notable time period.

386



387 **Figure 7. Deterioration profiles by material for Water Company 1**

388

389 It can also be seen that whilst the reliability of GI assets is consistently higher than other materials
 390 over-time and conversely BPE is consistently lower, the reliability of the other materials is
 391 interchangeable over time. For instance, it is observed that PB assets outperform CU and MDPE
 392 pipework up until an asset age of approximately 115 years at which time PB continues to have a
 393 lower reliability. However, when considering an even more useful comparator for material
 394 performance, asset half-life, it shows little difference in performance: PB (101 years), MDPE (98
 395 years), CU (97 years). Where-as it can be seen that 50% of GI assets are expected to be in service
 396 past 120 years of age in comparison to only 75 years for BPE. The accuracy of all the deterioration
 397 modelling curves against the failure observations for Water Company 1 and Water Company 2 are
 398 shown by the coefficient of determination, R-Squared, in Table 2 and Table 3. In support of this
 399 analysis, Figure 8 is produced to demonstrate the accuracy of predicted total failure counts for PB
 400 pipes by asset age versus the actual failure observations.

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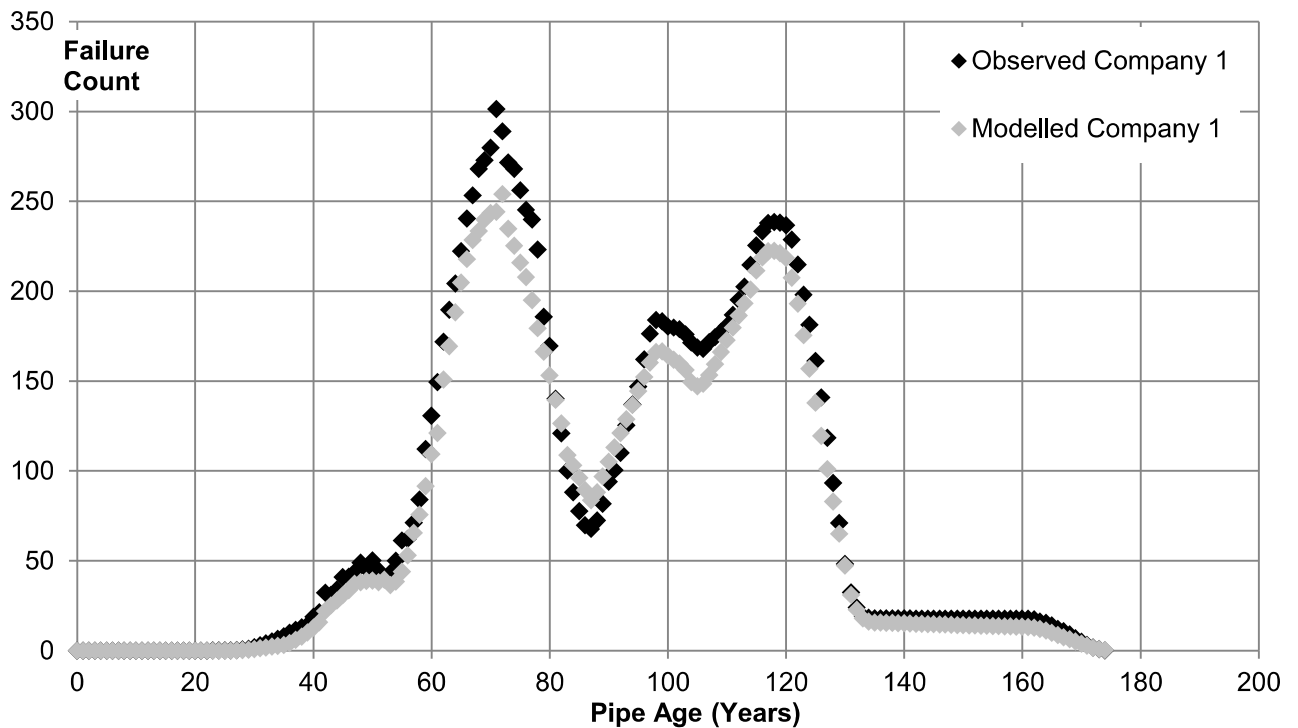


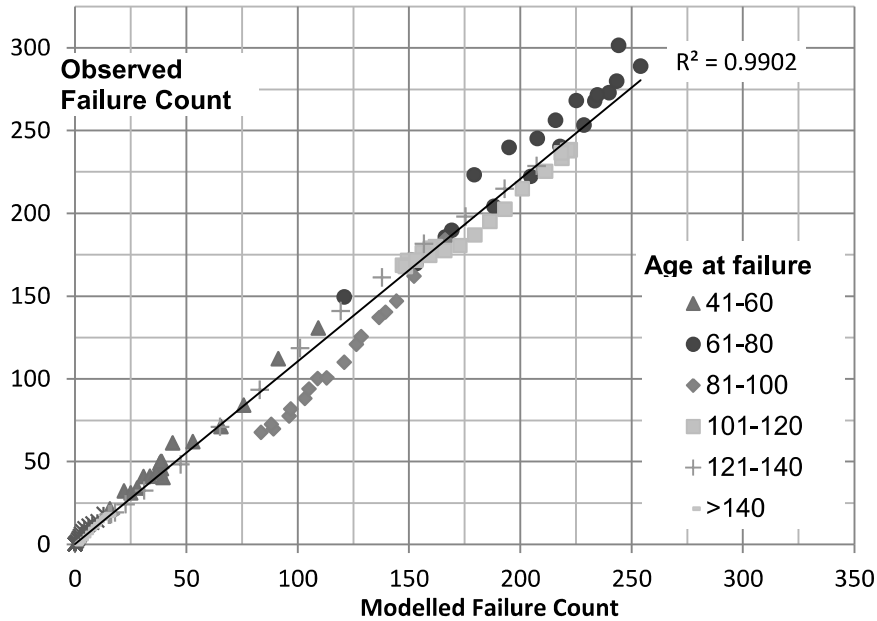
Figure 8. Modelled vs. Observed Failure Counts for Lead (PB) Pipes by Age

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403

404 Figure 8 clearly demonstrates two distinct pipe ages where the failure count is highest; pipe age 70
 405 years and 120 years. The 70 year peak coincides with steepest rate of failure for PB, Figure 7, and
 406 the highest asset stock attributed to post World War II construction. The accuracy of the data fit
 407 between the modelling outputs and the observed failure data is evaluated using a commonly accepted
 408 coefficient of determination, R-Squared (Gupta and Guttman, 2014) . The R-Squared is calculated by
 409 looking at the individual errors between predicted and observed failure counts for specific pipe ages
 410 and materials, e.g, 42 year old PB pipe. Therefore, each point on the graph represents a single pipe
 411 age and the associated predicted failure counts for this pipe is plotted against the observed failures,
 412 Figure 9. Whilst this is a fairly onerous assessment of model accuracy it helps to identify the individual
 413 age bands at which the deterioration model either over predicts, 81 – 100 years, or under-predicts, 61
 414 – 80 years. For PB pipes it is observed that the model fairly consistently under predicts, albeit only
 415 marginally but more notably around the peak failures. Reassuringly, this is not a common
 416 characteristic of the model. In fact, BPE is the only other material with a slight under prediction.
 417 Whereas the other pipe materials experience marginal over predictions at the peak failure rates.

418



419

420

Figure 9. Data Fit for Lead (PB) Failures by Pipe Age

421

A full analysis of the accuracy of all pipe material deterioration models for Water Companies 1 and 2

422

is presented in Table 2 and Table 3, showing R-Squared values greater than 0.959 for all material

423

types across both organisations. The failure observation counts used in the calibration of the Weibull

424

parameters are also shown. It is observed that the Weibull parameters and associated deterioration

425

curves are similar in nature between Water Company 1 and Water Company 2, despite the modelling

426

framework being customised for each company to account for the different historic material usage

427

profiles and failure observations. This is reassuring as it is expected that communication pipes of the

428

same material and those installed in the same year, would deteriorate in a similar manner regardless

429

of where they were installed. The reason for the location parameter (γ) only being used for older pipe

430

materials is because failure observations in the dataset were not observed in these materials for ages

431

less than 16 and 29 years. This is due to the phasing out of the PB and GI pipework between the

432

1950's to 70's and our failure observation window starting in 2001. As a result, all failures occurring in

433

the early ages of asset life, which is often referred to as infant mortality, are missed by this model.

434

However, this will not hinder the accuracy of the model for future predictions because PB and GI

435

assets are no longer installed and infant mortality failures counts are typically very low.

436

437

438 **Table 2. Water Company 1 Modelling Data**

Material	Failure	β	η	γ	R^2	439
	Observations					440
PB	13,972	1.599	127.968	16	0.990	
GI	3,090	1.398	155.875	16	0.990	441
CU	14,074	1.259	130.434	0	0.988	442
BPE	15,609	1.536	90.005	0	0.988	
MDPE	13,454	1.218	133.136	0	0.996	443
						444

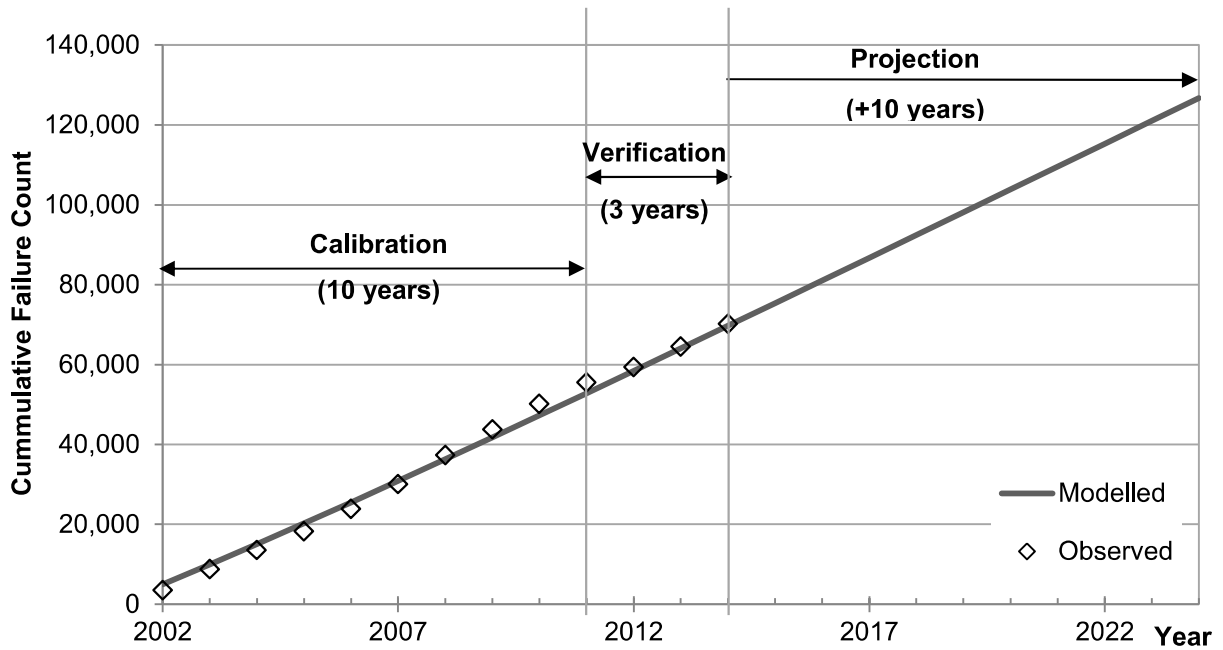
445 **Table 3. Water Company 2 Modelling Data**

Material	Failure	β	η	γ	R^2	446
	Observations					447
PB	26,094	1.458	103.479	29	0.973	
GI	15,247	1.158	152.056	29	0.960	448
CU	5,161	1.149	130.707	29	0.996	449
BPE	8,210	1.804	110.162	0	0.988	
MDPE	7,110	0.922	343.824	0	0.974	450
						451

452 Weibull deterioration curves are particularly useful for predicting future failure rates over a given time
 453 horizon, whereby the time horizon for failure projections can be extended for more accurate models
 454 (Røstum, 2000). To test the accuracy of the calibrated model in this study the predicted future failures
 455 are tested against the observed failures for the three years immediately following calibration, 2012 to
 456 2014. A cumulative yearly failure count is produced to show the accuracy of the modelled output
 457 versus the observed failures during the calibration window (2002 to 2011) and the three year model
 458 verification period (2012 to 2014). A ten year failure rate projection is also plotted, Figure 10. The
 459 cumulative failure count is a useful comparator for model accuracy because it is not influenced by
 460 yearly extremes which can be caused by unpredictable external conditions such as the weather. The
 461 final cumulative failure count from 2002 to 2014 produced by the model is within 1% of the observed
 462 failures. It is also reassuring that on average the absolute error for the modelling predictions during

463 the verification window are within 5% for each individual year. This is compared to 8% for the
464 calibrated data when yearly outliers are removed. Where-by outliers are defined as those with values
465 +/- 1 standard deviation from the mean. Without this exclusion the models performance against the
466 validation and calibration data is 18% and 14% respectively.

467



468

469

Figure 10. Model calibration, verification and projection

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472

473 **Conclusions**

474 This paper demonstrates the effectiveness of a bottom up deterioration modelling framework for small
475 diameter water distribution assets which connect individual customers to water distribution mains. The
476 low asset value and low consequence of failure, for individual assets of this nature, is thought to be
477 the main reason why previous literature has been focused on larger and more critical assets.
478 However, when considered as a collective asset group, investment across the developed World is
479 estimated to be in excess of £4.4bn per year, demonstrating the potential benefits of adopting more
480 comprehensive asset management techniques founded on deterioration models of this nature.

481 The modelling approach developed by the authors uses a series of geospatial algorithms and fuzzy
482 rule sets to infer the asset stock and assign basic attribution, prior to calibrating Weibull reliability
483 curves for the five most commonly installed pipe materials; PB, GI, CU, BPE and MDPE. A three
484 parameter Weibull function is used to simulate failures for each time step so that they can be
485 compared against actual failure records within a ten year observation window for each material.
486 Feedback processes that incorporate fuzzy rules sets have been introduced within the modelling
487 framework to account for the fact that these assets are either repaired or replaced upon failure and
488 that different materials were used when replacing these assets over time. The output is a calibrated
489 set of Weibull parameters for each pipe material which can be used to calculate yearly reliability
490 values that describe the probability of an asset remaining in service at any given age.

491 All five pipe materials were observed to behave differently over time and the modelled failure rates
492 showed good correlation to the observed failures with R-Squared values exceeding 0.97. Similar
493 reliability curves were observed for each of the materials between two UK based Water Companies
494 that this modelling framework was applied to independently. Finally, the accuracy of the modelling
495 approach was validated by comparing the predicted number of failures against three years of failure
496 data not used in the calibration process. The yearly failure counts were predicted to within +/-5%
497 accuracy and the overall cumulative modelled failure count at the end of 2014 was predicted within
498 1%.

499 The benefit of developing an accurate modelling framework to simulate future deterioration and failure
500 of Communication pipe assets is that future maintenance expenditure can be modelled, which in turn
501 provides Water Companies with a better understanding of their future capital and operational

502 budgetary requirements. Additional benefits could be realised through the application of a whole life
503 cycle cost optimisation model to identify the most cost effective maintenance strategy with respect to
504 total expenditure. Similarly, maintenance strategies could also been developed with the objective of
505 improving serviceability if a relationship between asset degradation and performance can be
506 established. For example, by understanding the impact of GI pipework degradation on discolouration
507 events and/or low pressure, a targeted proactive replacement programme could be implemented with
508 the aim of improving customer satisfaction. However, this is a complex phenomena to model due to
509 the number of additional contributing factors that lead to reduced serviceability, some of which are
510 associated with the water distribution network itself and not necessarily the communication pipe
511 assets. Therefore, the delivery of an effective proactive communication pipe replacement programme
512 should give consideration to the combined structural and serviceability performance of all components
513 in the distribution network.

514

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518

519 **References**

- 520 Berardi, L., Giustolisi, O., Kapelan, Z., and Savic, D. A. (2008) Development of pipe deterioration
521 models for water distribution systems using EPR. *Journal of Hydroinformatics*, 10(2), 113.
522 [online] <http://www.iwaponline.com/jh/010/jh0100113.htm>.
- 523 Bicik, J., Morley, M. S., and Savić, D. A. (2008) “A Rapid Optimization Prototyping Tool for
524 Spreadsheet-based Models”. *Proceedings of the Water Distribution Systems Analysis*
525 *conference*. South Africa, 472–482.
- 526 Clark, R., Stafford, C., and Goodrich, J. (1982) *Water Distribution Systems: A Spatial and Cost*
527 *Evaluation*. *Journal of the Water Resources Planning and Management Division*, 108(3), 243–
528 256.
- 529 Engelhardt, M. ., Skipworth, P. ., Savić, D. ., Saul, A. J., and Walters, G. (2000) *Rehabilitation*
530 *strategies for water distribution networks : a literature review with a UK perspective*. *Urban*
531 *Water*, 2.
- 532 Engelhardt, M., Skipworth, P., Savic, D. a., Cashman, a., Walters, G. a., and Saul, a. J. (2002)
533 *Determining maintenance requirements of a water distribution network using whole life costing*.
534 *Journal of Quality in Maintenance Engineering*, 8(2), 152–164. [online]
535 <http://www.emeraldinsight.com/10.1108/13552510210430026>.
- 536 Le Gat, Y. and Eisenbeis, P. (2000) *Using maintenance records to forecast failures in water networks*.
537 *Urban Water*, 2(3), 153–181.
- 538 Giustolisi, O. and Savić, D. A. (2006) *A symbolic data-driven technique based on evolutionary*
539 *polynomial regression. , 207–222*.
- 540 Gupta, B. and Guttman, I. (2014) *Statistics and Probability with Applications for Engineers and*
541 *Scientists*, John Wiley & Sons.
- 542 Halhal, D., Walters, G. A., Ouazar, D., and Savić, D. A. (1997) *Water Network Rehabilitation with*
543 *Structured Messy Genetic Algorithm*. *Journal of Water Resources Planning and Management*,
544 123(3), 137 – 146. [online] <http://link.aip.org/link/JWRMD5/v123/i3/p137/s1&Agg=doi>.
- 545 Jafar, R., Shahrour, I., and Juran, I. (2010) *Application of Artificial Neural Networks (ANN) to model*
546 *the failure of urban water mains*. *Mathematical and Computer Modelling*, 51(9-10), 1170–1180.
547 [online] <http://linkinghub.elsevier.com/retrieve/pii/S0895717710000051>

548 Kleiner, Y., Rajani, B., and Sadiq, R. (2009) "Drinking Water Infrastructure Assessment: The National
549 Research Council of Canada Perspective". World Environmental and Water Resources
550 Congress 2009. Kansas City, Missouri, American Society of Civil Engineers, 1–10. [online]
551 [http://ascelibrary.org/doi/abs/10.1061/41036\(342\)67](http://ascelibrary.org/doi/abs/10.1061/41036(342)67).

552 Lasdon, L. S., Fox, R. L., and Ratner, M. W. (1974) Nonlinear optimization using the generalized
553 reduced gradient method. *RAIRO-Operations Research-Recherche Opérationnelle*, 3(8), 73–
554 103.

555 Lei, J. and Sægrov, S. (1998) Statistical approach for describing failures and lifetimes of water mains.
556 *Water science and technology*, 38(6), 209–217.

557 Li, D. and Haimes, Y. (1992) Optimal maintenance-related decision making for deteriorating water
558 distribution systems: 1. Semi-Markovian Model for a water main. *Water Resources Research*,
559 28(4), 1053–1061.

560 Mailhot, A., Pelletier, G., Noël, J.-F., and Villeneuve, J.-P. (2000) Modeling the evolution of the
561 structural state of water pipe networks with brief recorded pipe break histories: Methodology and
562 application. *Water Resources Research*, 36(10), 3053–3062. [online]
563 <http://doi.wiley.com/10.1029/2000WR900185>.

564 Mendel, J. . . (2000) *Uncertain Rule-based Fuzzy Logic Systems: Introduction and New Directions*,
565 Prentice Hall.

566 Nafi, A. and Kleiner, Y. (2010) Scheduling Renewal of Water Pipes While Considering Adjacency of
567 Infrastructure Works and Economies of Scale. *Journal of Water Resources Planning and*
568 *Management*, 136(5), 519–530.

569 O'Day, K., Weiss, R., Chiavari, S., and Blair, D. (1986) *Water main evaluation for*
570 *rehabilitation/replacement*. American Water Work Association.

571 Ofwat (2010) June Return. Past information on company performance (June returns). [online]
572 <http://www.ofwat.gov.uk/regulating/junereturn/jrhistoricdata/>.

573 Ofwat (2014) Responsibility for water and sewerage pipes. [online]
574 <http://www.ofwat.gov.uk/consumerissues/rightsresponsibilities/supplypipes/>

575 Pelletier, G., Mailhot, A., and Villeneuve, J. (2003) Modeling Water Pipe Breaks — Three Case
576 Studies. *Journal of Water Re*, 129(1), 115–123.

577 Rajani, B. and Kleiner, Y. (2001) Comprehensive Review of Structural Deterioration of Water Mains :
578 Physically Based Models. *Urban Water*, 3(3), 151–164.

579 Røstum, J. (2000) Statistical Modelling of Pipe Failures in Water Networks.

580 Sacluti, F. R. (1999) Modeling Water Distribution Pipe Failures Using Artificial Neural Networks.

581 Savić, D. a., Bicik, J., and Morley, M. S. (2011) A DSS generator for multiobjective optimisation of
582 spreadsheet-based models. *Environmental Modelling & Software*, 26(5), 551–561. [online]
583 <http://linkinghub.elsevier.com/retrieve/pii/S1364815210003087>.

584 Shamir, U. and Howard, C. (1979) An Analytic Approach Pipe Replacement. *American Water Work*
585 *Association*, 71(5), 248 – 258.

586 United Nations (2011) Population Division. Department of Economic and Social Affairs, World
587 *Popu*(ST/ESA/SER.A/313).

588 Vangdal, A. C. and Reksten, K. (2011) “Experience from inspection of water pipes – hard fact based
589 AM - opportunities and consequences”. *Proceeding of the 4th Leading Edge Conference on*
590 *Strategic Asset Management*. Mülheim an der Ruhr, Germany.

591 Ward, B., Selby, A., Gee, S., Rosser, S., and Savić, D. (2014) Assessing impacts of the private sewer
592 transfer on UK utilities. *Infrastructure Asset Management*, 1(2), 23–33. [online]
593 <http://www.icevirtuallibrary.com/content/article/10.1680/iasma.13.00003>.

594 Ward, B., Smith, D., Roebuck, J., Savic, D.,and Collingbourne, J., (2015) Optimised investment
595 planning for high volume- low value buried infrastructure assets. In Review.

596 Weibull, W. (1951) A Statistical Distribution Function of Wide Applicability. *Journal of Applied*
597 *Mechanics*, 293–297.

598 WRc and UKWIR (2005) A Guide to Water Service Pipes. 3rd Edition. WRc.

599