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# An Incrementally Scalable and Cost-efficient Interconnection Structure for Data Centers

Junjie Xie, Yuhui Deng, Member, IEEE, Geyong Min, Member, IEEE, Yongtao Zhou

**Abstract**—The explosive growth in the volume of data storing and complexity of data processing drive data center networks (DCNs) to become incrementally scalable and cost-efficient while to maintain high network capacity and fault tolerance. To address these challenges, this paper proposes a new structure, called *Totoro*, which is defined recursively and hierarchically: dual-port servers and commodity switches are used to make Totoro affordable; a bunch of servers are connected to an intra-switch to form a basic partition; to construct a high-level structure, a half of the backup ports of servers in the low-level structures are connected by inter-switches in order to incrementally build a larger partition. Totoro is incrementally scalable since expanding the structure does not require any rewiring or routing alteration. We further design a distributed and fault-tolerant routing protocol to handle multiple types of failures. Experimental results demonstrate that Totoro balances between performance and costs in terms of robustness, structural properties, bandwidth, economic costs and power consumption.

Index Terms—Data center network, Scalability, Network capacity, Cost efficiency, Fault tolerance.

# **1** INTRODUCTION

W ITH the rapid development of information digitization, a huge amount of data is being created every day in various fields. To process these explosively incremental data, large-scale data center networks (DCNs) are built and play a significant role in hosting various applications, such as Instant Messaging (IM), video service, Machine Learning (ML) and so forth. A modern DCN is not just a collection of servers and network devices but needs to be considered as a single computing unit, namely *Warehouse-Scale Computers* (WSC) [1]. Modern DCNs are distinguished from traditional ones by their more rigorous requirements:

1) **Scalability**: DCNs must physically support thousands and even millions of nodes to power the computational tasks and data storage [2]. In practice, DCNs are more likely to be built firstly with a part of integrated components because the investors often prefer to a low startup cost and then enlarge the scale as business expands [3]. Thus DCNs should enable incremental expansion efficiently and such expansion should minimize.

2) **High network capacity**: Cisco has studied the data center traffic and reported that 76.7% of the traffic remains within the data centers [4]. High network capacity is fundamental for a well-designed DCN to support such traffic. Two solutions are widely adopted: a) the "scale up" solution utilizes higher-end devices to upgrade the network capacity; b) the "scale out" solution connects more commodity devices

to satisfy the performance requirements. The later has two advantages of economical efficiency and fault tolerance and thus represents a rising trend in this field.

3) **Fault tolerance**: As the scale of DCNs increases, failures become common in the cloud environment and have a significant impact on the running applications [5]. These damages make fault tolerance a big challenge in the cloud environment.

4) **Cost efficiency**: Costs in today's data center contain four major components: 45% goes to servers (CPU, memory, and storage systems), 25% goes to infrastructure (power distribution and cooling), 15% goes to power draw (electrical utility costs), and 15% goes to network (links, transit, and equipment) [6]. The design of DCNs must balance between performance and costs, especially the economic costs and power consumption.

However, legacy designs of data centers can not fully meet these requirements. In current practice, many data centers follow the legacy ThreeTier [7] structure in which servers are connected in a rack with Top-of-Rack switches at the edge level. Then edge switches are connected with aggregation switches to build the network architecture. On the top of the structure, ThreeTier provides the Internet services by core-routers or core-switches. However, the ThreeTier data centers have three noticeable weaknesses. Firstly, the top-level components often become the bandwidth bottleneck. Secondly, one failure of them can abruptly degrade the crossing traffic. Thirdly, it is expensive to update the top-level switches, leading to the sharp rise of costs. Adding redundant switches and links may lighten these issues without considering the cost. But the ThreeTier structure is still inherently short of adequate scalability and fault tolerance.

To overcome the disadvantages of the traditional Three-Tier structure, this study aims to develop an innovative solution to meet the requirements of well-designed DCNs: high scalability (especially incremental scalability), cost-

J. Xie, Y. Deng and Y. Zhou are with the Department of Computer Science, Jinan University, Guangzhou, China, 510632.

E-mail: xiejunjiejnu@gmail.com, tyhdeng@jnu.edu.cn

<sup>56</sup> Y. Deng is with the State Key Laboratory of Computer Architecture, Institute of Computing Technology, Chinese Academy of Sciences, Beijing, China, 100190.
58 C. Min is with the College of Engineering, Mathematics and Physical

<sup>58</sup> G. Min is with the College of Engineering, Mathematics and Physical Sciences, University of Exeter, Exeter, EX4 4QF, United Kingdom.
60 Email: g.min@exeter.ac.uk

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effectiveness, high network capacity, and fault-tolerance.

1 The servers in the current market commonly own two 2 Network Interface Card (NIC) ports: one for normal connec-3 tion and the other for backup usage [8]. Servers with four 4 or more ports have recently appeared, but such machines 5 are usually high-end and thus are expensive. In terms of 6 network connection, more redundant links make the struc-7 ture more efficient and robust. Adopting high-end machines 8 with more ports or adding more NICs to the existing 9 machines may address the problems of fault-tolerance and 10 bandwidth requirement. However, it is infeasible to build a 11 large-scale DCN with a vast number of high-end machines 12 due to their high cost [9]. Besides, updating hardware (e.g., 13 adding more NICs or replacing 2-port NICs with 4-port 14 ones) may affect the existing business or even destroy the 15 original communication mechanism. Therefore, it is more 16 desirable to construct scalable and fault-tolerant DCNs by 17 utilizing the widely used and low-cost commodity servers 18 with dual ports [1] [8] [10][11]. 19

In this paper, we propose a new interconnection struc-20 ture called Totoro <sup>1</sup>, which adopts commodity servers with 21 two ports. Totoro is recursively defined. When constructing 22 a high-level Totoro, the low-level Totoros use half of their 23 available backup ports for interconnections. Thus, there 24 exist available (un-used) ports for each level structure. This 25 feature makes the expansion of Totoro convenient. If the 26 scale of DCNs needs to be expanded, more servers can 27 be connected and integrated with the existing structures 28 (plugging wires to the available ports) without modifying 29 any existing hardware (e.g., rewiring or updating NICs) 30 or software (e.g., adopting new routing mechanism). As a 31 consequence, Totoro is incrementally scalable. 32

The method of using half of the available ports for 33 expansion was firstly adopted by FiConn [8]. But there exist 34 many significant differences between Totoro and FiConn. 35 Totoro connects servers to switches and thus there are no 36 direct links between any two servers, while FiConn connects 37 servers directly to form a complete graph in each level. Since 38 switches can forward data to several directions, the property 39 of link multiplexing is intrinsical for Totoro, which offers 40 more available ports and is conducive to connecting more 41 redundant links. Compared to FiConn, another advantage 42 is that the data flowing from one partition to another can be 43 distributed to multiple links. This reduces the forwarding 44 loads and makes the data transmission more efficient. We 45 will further discuss and prove that the usage of switches 46 achieves a lower price-performance ratio than FiConn. An 47 existing structure sharing the similar wiring principle of 48 using switches to connect servers is BCube [11]. However, 49 it is extremely hard to expand a completely built BCube 50 since it is mainly designed for modular data centers. The in-51 cremental scalability of BCube is not comparable to Totoro. 52 More details will be discussed in Section 2 and 6. To sum up, 53 the major contributions of this paper are listed as follows. 54

1) We propose a new and cost-effective network structure, Totoro, which is recursively defined and incrementally

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scalable. As only half of the available ports in the lowerlevel structures are used whenever the network is extended to construct a high-level structure, the available ports enable the incremental scalability without any rewiring, hardware replacement or routing alternation. Besides, the use of commodity servers and switches makes the DCNs affordable.

2) We develop a fault-tolerant and effective routing mechanism to handle multiple types of failures in DCNs. The proposed rerouting technology leverages a Base 2 Logarithms Model to bypass the fault domains via neighbor or remote partitions without trapping into the local dilemma. This model does not require any global information, and thus it can efficiently determine the target links to reroute the packets.

3) We investigate the important properties of Totoro, conduct the experiments of evaluating the path failure ratio and network throughput, analyse the structural robustness, bandwidth, cost and power consumption. The results demonstrate that Totoro is a robust and cost-efficient architecture design.

The remainder of this paper is organized as follows. Section 2 introduces the related work. Section 3 details the Totoro structure. Section 4 presents a distributed and fault-tolerant routing protocol for Totoro. Section 5 presents experiments to evaluate the performance and availability of Totoro. Section 6 presents the architecture analysis. Finally, Section 7 concludes this paper.

#### 2 **RELATED WORK**

As cloud computing has developed rapidly in recent years, studies on data center networks (DCNs) have attracted many research efforts from both academic and industrial communities [13] [14] [15].

Considering the weaknesses of the traditional ThreeTier structure, Fares et al. presented an improved ThreeTier structure, namely *FatTree* [16], which scales out with a large number of links and mini-switches. Using more redundant switches, FatTree achieves an oversubscription ratio of 1:1. Based on FatTree, SEATTLE [17] and Portland [18] were proposed to provide "plug-and-play" functionality via flat addressing and hierarchical addressing, respectively. But the scalability of FatTree is still limited by the ports of switches fundamentally. If FatTree needs to be expanded and the existing switches are fully utilized, switches must be replaced to offer more ports. This has negative effects because updating switches will break the existing business and cause steeper costs. In contrast, Totoro is not limited by any hardware (e.g., the number of servers or switch ports) and thus has no bound of scale. To expand the network, we only need add more machines and follow the building principle to connect them to the available backup ports. Besides, Totoro uses fewer switches than FatTree. Based on its connecting philosophy, Totoro needs the switches fewer than 2T/n while FatTree needs 5T/n switches (T indicates the total number of servers and n is the number of switch ports). It is worth noting that using fewer switches leads to the lower cost and energy consumption.

DCell [10] is a level-based, recursively defined interconnection structure with typical requirements of multiport (e.g., 3, 4 or 5) servers. DCell scales double exponentially

<sup>57</sup> 1. A preliminary short version of this paper [12] appears in the 58 Proceedings of the 10th IFIP International Conference on Network and Parallel Computing (NPC-2013). We significantly extend the fault-59 tolerant routing algorithm, add the extensive experiments and enrich 60 the architecture analysis in the current paper.

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with the server node degree. It is also fault-tolerant and has high network capacity. As a trade-off, DCell replaces the expensive core switches/routers with multi-port NICs and higher wiring cost. Compared to DCell, Totoro needs fewer ports, but more switches. As being discussed in the section of Introduction, most commodity servers in the current market are equipped with dual-port NICs [8]. Replacing NICs with more-port ones or adding more NICs undoubtedly increases the cost and deployment overhead. Therefore, Totoro adopts dual-port machines as the building foundation 10 and thus significantly reduces the cost. By using switches 11 to connect servers, all data flows from a node to another 12 go through switches only, improving the ports' efficiency. 13 Besides, Totoro adopts a naturally bottom-up resolution to 14 expand incrementally, which is opposite to what DCell uses 15 and makes the incremental deployment more convenient. 16

BCube [11] represents a wonderful attempt to design the 17 network architecture for modular data center. It connect-18 s servers with multiple ports to mini-switches and there 19 are no direct links between servers. BCube places rout-20 ing intelligence on servers. It intrinsically supports vari-21 ous bandwidth-intensive applications and exhibits graceful 22 performance degradation. Nevertheless, large-scale use of 23 multi-port NICs inevitably leads to an expanding overhead, 24 which will be proven in Section 6. Totoro adopts the similar 25 method to connect servers with switches. There are no direct 26 links between servers as well. Partial deployment of Totoro 27 and BCube are also similar since they both use a full top-28 level switches. However, it is more convenient for Totoro 29 to expand a completely deployed structure because there is 30 no need to reserve a port or add NIC on each host. BCube 31 is designed for mega data center and thus the incremental 32 scalability of BCube is not comparable to Totoro.

33 FiConn [8] is also a new server-interconnection structure 34 by adopting servers with two ports and low-end commodity 35 switches to form the network infrastructure. FiConn grows 36 double exponentially. The degree of server nodes in FiConn 37 is always two, leading to a lower wiring cost than DCell. 38 Routing in FiConn also makes a balanced use of links at 39 different levels and is traffic-aware so as to better utilize the 40 link capacities. Totoro shares the similar wiring principle 41 with FiConn by using half of the available backup ports to 42 form a higher-level structure, which provides the feature of 43 incremental scalability. The difference between Totoro and 44 FiConn is that Totoro connects servers with switches instead 45 of direct wires. In FiConn, two partition flows communicate 46 through a unique link. This brings high forwarding loads 47 to the servers at each end of this link. Unlike FiConn, 48 there are multiple links connecting two partitions directly 49 in Totoro. All data flowing from one partition to the other 50 can be distributed to these links, and thus reducing the 51 forwarding load and making data transmission more effi-52 cient. Besides, the intrinsical property of link multiplexing 53 saves the structure more available ports and is conducive 54 to connecting more redundant links. We will further prove 55 that the usage of switches gains a lower price-performance 56 ratio than FiConn in Section 6. 57

Different from the existing work, this paper proposes a new interconnection structure called Totoro for DCN. The key features of Totoro can be summarized as follows:

1) Incremental scalability: Totoro supports not only

TABLE 1: The Denotations Frequently Used in this Paper.

Denotation	Meaning
n	The number of ports on a switch.
k	The top level in a Totoro.
$Totoro_i$	The <i>ith</i> level Totoro.
$Totoro_i[x]$	The <i>x</i> th $Totoro_i$ in a $Totoro_{i+1}$ .
$t_k$	The total number of servers in $Totoro_k$ .
$[a_k, a_{k-1},, a_i,, a_1, a_0]$	A $(k + 1)$ -tuple to denote a server, where $a_i < n \ (0 < i \le k)$ indicates at which $Totoro_{i-1}$ this server is locat- ed and $a_0 < n$ indicates the index of this server in that $Totoro_0$ .
$(u - b_{k-u}, b_{k-u-1},, b_0)$	A combination of an integer and a $(k - u + 1)$ -tuple to denote a switch, where $u \leq k$ indicates that it is a level- $u$ switch, $b_i < n \ (0 < i \leq k - u)$ indicates at which $Totoro_{u+i-1}s$ this switch is located and $b_0$ indicates the index of this switch among level- $u$ switches in that $Totoro_u$ .
$P(src, dst)$ or $src \rightarrow dst$	A path from <i>src</i> to <i>dst</i> .

largely physical interconnection but also flexibly incremental expansion;

2) Cost-effectiveness: Totoro achieves a lower priceperformance ratio;

3) High network capacity: Totoro provides a high bisection width;

4) Fault-tolerance: Totoro offers a fault-tolerant and high-effective routing mechanism to handle multiple types of failures in data centers.

#### **TOTORO INTERCONNECTION NETWORKS** 3

The frequently used denotations in this paper are listed and explained in Table 1.

# 3.1 The Physical Structure of Totoro

Totoro consists of a series of commodity servers with dual ports and low-end *n*-port switches. Dual-port servers are commonly deployed in industry. Low-end switches without uplinks are inexpensive and affordable. These motivate us to build a modern data center at acceptable costs.

Totoro is recursively defined as follows. We connect nservers to an *n*-port switch to form the basic partition of Totoro, denoted by *Totoro*<sub>0</sub>. The switch is called an *intra*switch. Each server in Totoroo is connected to an intraswitch using one port; the rest ports are called *available* ports. If a *Totoro*<sub>0</sub> is considered as a virtual server, the number of available ports in a  $Totoro_0$  is equal to n. Then each  $Totoro_0$  is connected to n/2 switches using half of its available ports (i.e., n/2 ports). As each switch has nports, it is connected to  $n \ Totoro_0 s$ . Now we obtain a larger partition denoted by *Totoro*<sub>1</sub> (as shown in Fig. 1). Then we connect  $n \ Totoro_1 s$  with  $n^2/4$  switches to form a  $Totoro_2$  (see Fig. 2). In each  $Totoro_1$ , half of the available ports, i.e.,  $n^2/4$  ports, are used for connection. Generically, we connect *n*  $Totoro_{k-1}s$  to  $(n/2)^k$  switches to build a  $Totoro_k$ . A switch connecting different partitions is called

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Fig. 1: A  $Totoro_1$  structure with n = 4.

an *inter-switch*. In a  $Totoro_k$ , switches and links connecting different  $Totoro_{k-1}s$  are called *level-k switches* and *level-k links*, respectively. In particular, the level of intra-switch is 0.

It is worth noting that there is no need to connect lowlevel switches to high-level switches in the proposed Totoro structure in order to build the higher-level Totoro. Therefore, no direct link between any two switches is required. This is one typical difference between Totoro and ThreeTier structure.

24 Now a case study is presented to demonstrate how to 25 build a Totoro structure with two given structural param-26 eters: n and k. n determines how many ports of a switch 27 are used while *k* represents how many levels of the target 28 architecture are. Take Fig. 2 as an example where n = 429 and k = 2. Firstly, we connect 4 servers to a 4-port switch 30 to build a bottom partition, *Totoro*<sub>0</sub>. In Fig. 2, a small circle 31 represents a single server and a rectangle filled with 4 circles 32 represents a *Totoro*<sub>0</sub>. For clarity, the intra-switch is omitted 33 in Fig. 2. Repeatedly, we can construct 4  $Totoro_0s$  in the 34 same way. It can be seen that there exist 4 available ports 35 in a  $Totoro_0$  (each server owns one). Then half of them, 36 i.e., 2 ports, are chosen to connect with 2 different switch-37 es, respectively. For example, we connect server [0, 0, 0] to 38 switch (1 - 0, 0) and server [0, 0, 2] to switch (1 - 0, 1). 39 For other  $Totoro_0 s$ , we adopt the same method to get a 40 Totoro1 structure (see Fig. 1), containing 16 servers, 4 intra-41 switches (not shown in Fig. 2) and 2 level-1 switches. To 42 build a  $Totoro_2$ , 4  $Totoro_1s$  are also required. If  $Totoro_1$ 43 is considered as a whole, it can be observed that there are 8 44 available ports in a *Totoro*<sub>1</sub>. We also utilize half of them, i.e., 45 4 ports, to connect with 4 different switches, respectively. In 46 Fig. 2, we connect server [0, 0, 1] to switch (2 - 0), server 47 [0, 1, 1] to switch (2 - 1), server [0, 2, 1] to switch (2 - 2) and 48 server [0, 3, 1] to switch (2-3). Similarly, other *Totoro*<sub>1</sub>s can 49 be connected together and we finally obtain a higher-level 50 Totoro, i.e., *Totoro*<sub>2</sub>. Generically, when *n*-port switches are 51 used to build a  $Totoro_k$ , the numbers of required servers, 52 switches, and links are  $n^{k+1}$  (see Theorem 1 for details), 53  $n^k \times (2 - 1/2^k)$ , and  $n^{k+1} \times (2 - 1/2^k)$ , respectively.

The linking principle of Totoro is:  $1/2^k$  of the links in a certain partition are connected to several *k*-level partitions (i.e., *Totoro<sub>k</sub>s*). As *k* grows, the percentage of *k*-level links declines, which means that most of the links are provided to access the data stored nearby. This closely matches the fact that most of the relevant data is put together, also known as spatial locality [19].



Fig. 2: Given 4-port switches, a  $Totoro_2$  structure can be constructed from  $4 Totoro_1 s$ . Each  $Totoro_1$  contains  $4 Totoro_0 s$ and 4 servers are connected in each  $Totoro_0$ .

In some other structures, like DCell or FiConn, there is only one direct link between two adjacent partitions. If this link is busy or disabled, the routing mechanism has to bypass this link with the help of other neighbor partitions. Distinctly, this creates more forwarding workloads for other servers in those partitions. Through comparison, the structure of Totoro reduces the accessing distance between servers in the fault situation because there are several interswitches between two partitions. The servers in a  $Totoro_i$  $(0 \le i \le k)$  can access servers in another  $Totoro_i$  directly by  $(n/2)^{i+1}$  paths without going through any other *Totoro*<sub>i</sub>. For instance, server [0,1] in Fig. 1, needs to access server [1,1]. Under the normal circumstances, we can choose the path  $[0,1] \rightarrow (0-0,0) \rightarrow [0,0] \rightarrow (1-0) \rightarrow [1,0] \rightarrow$  $(0-1,0) \rightarrow [1,1]$ . Assume that one link between servers and the inter-switch fails (e.g.,  $[0,0] \rightarrow (1-0)$ ), this path is unavailable now. In this case, another path  $[0,1] \rightarrow (0-0,0) \rightarrow$  $[0,2] \to (1-1) \to [1,2] \to (0-1,0) \to [1,1]$  can be chosen. As a result, the communication is still between two  $Totoro_0s$ without going through any other. For instance, the path from server [0, 1] to server [1, 1] will not across  $Totoro_0[2]$ . This feature also naturally supports multi-path routing if we simultaneously activate all existing routing selections. For example, if the paths of  $[0,1] \rightarrow (0-0,0) \rightarrow [0,2] \rightarrow$  $(1-1) \to [1,2] \to (0-1,0) \to [1,1]$  and  $[0,1] \to (0-0,0) \to (0-1,0) \to (0-1,0)$  $[0,0] \rightarrow (1-0) \rightarrow [1,0] \rightarrow (0-1,0) \rightarrow [1,1]$  are both utilized, the throughput between server [0, 1] and server [1, 1] will double.

Observing the Totoro structure, it is clear that not all servers are connected to inter-switches. In our design philosophy, unused ports are left for extension. For a *k*-level Totoro using *n*-port, the number of available ports for expansion is  $n^{k+1}/2^k$ . Thus, the proposed Totoro is open and easy for extension. FiConn [8] makes use of all available backup server ports for interconnection, i.e., adding shortcut links to improve the bisection bandwidth. As a trade-off, Totoro does not adopt this method since the percentage of available backup ports is not high  $(1/2^{k+1})$  and keeping the routing simple and consistent is quite important. Especially

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1	Alg	Algorithm 1: Totoro Building Algorithm				
2	1 F	1 Function TotoroBuild (n, k)				
3	2	$t_k = n^{k+1}$				
4	3	for $tid = 0$ to $(t_k - 1)$ do				
5	4	$s(s_k,, s_i,, s_0) = $ TotoroIDToTuple ( <i>tid</i> )				
6	5	$intraSw = (0 - b_k,, b_i,, b_0)$				
7	6	for $i = 1$ to k do				
8	7	$b_i = s_i$				
9	8	$b_0 = 0$				
10	9	Connect(s, intraSw)				
10	10	for $u = 1$ to $k$ do				
11	11	<b>if</b> $(tid - 2^{u-1} + 1) \mod 2^u == 0$ then				
12	12	$interSw = (u - b_{k-u}, b_{k-u-1},, b_1, b_0)$				
13		for $i = u$ to $(k - 1)$ do				
14	13	$b_i = s_{i+1}$				
15	14	$b_0 = (tid/2^u) \mod (n/2)^u$				
16	15	Connect(s, interSw)				
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when upgrading the scale of data centers, removing and replugging shortcut links bring significant deployment complexity. We also advocate using low-end switches without uplinks and expanding Totoro by increasing the structural levels rather than updating the switches. This helps to reduce the device cost and the management cost in data centers.

#### 3.2 Totoro Building Algorithm

29 A server in Totoro can be indicated in two ways: To-30 toro tuple and Totoro ID. Totoro tuple is a (k + 1)-tuple 31  $[a_k, a_{k-1}, ..., a_i, ..., a_1, a_0]$ , which indicates where this server 32 is located and can help calculate the common partition of 33 two servers. In routing algorithm, it is a vital step to find 34 out the common partition of the source server and the 35 destination server. For example, servers [0,0] and [0,1] in 36 Fig. 1 are in the same  $Totoro_0[0]$  in terms of their common 37 prefix (i.e., [0]). Totoro ID is an unsigned integer, taking a 38 value from  $[0, t_k)$ . Totoro ID will be used in the header of 39 packets to identify a server uniquely, performing like IP 40 Address. Note that, the mapping between Totoro tuple and 41 Totoro ID is a bijection.

42 In addition, a switch is denoted as a combination of an 43 integer and a (k - u + 1)-tuple  $(u - b_{k-u}, b_{k-u-1}, ..., b_1, b_0)$ . 44 Note that,  $b_0$  is identically equal to 0 when u = 0. Because 45 there is only one intra-switch in a  $Totoro_0$ . Algorithm 1 46 presents how Totoro can be built. The key step in this 47 algorithm is to determine the level of the outgoing link of 48 this server (Line 11). The function **Connect** represents the 49 operation that a server is connected to a switch manually. 50 The time complexity of Algorithm 1 is  $O(k \times t_k)$  where  $t_k$ 51 denotes the total number of nodes in a  $Totoro_k$ .

52 Considering the fact that the linking philosophy and ad-53 dress configuration of Totoro are slightly more complex than 54 ThreeTier structures, some automatic address configuration 55 mechanisms, e.g., [20] would be introduced to make the 56 deployment faster and easier.

#### 58 3.3 Incremental Deployment

59 Incremental deployment of interconnection networks be-60 comes a common requirement due to the scalability requirement. To incrementally deploy an interconnection network, three important aspects should be considered: 1) no rewiring, 2) no hardware replacement, and 3) no software modification. These requirements ensure that the existing applications will not be affected and can be achieved in the proposed Totoro structure.

When *n*-port switches are used, a *k*-level Totoro remains  $n^{k+1}/2^k$  ports for expansion and thus there is no need to change the existing structure. A straightforward way to gradually construct Totoro is the "bottom-up" approach. Totoro firstly builds the complete low-level structures and connects them to the top-level switches. We also make sure that all k-level links are connected in each  $Totoro_{k-1}$ and deploy full top-level switches. This approach provides the full network capacity at the top level but the ports of top-level switches will not be fully utilized. Since low-cost switches are adopted, this approach is affordable.

#### 3.4 Properties of Totoro

To investigate the scalability of Totoro, Theorem 1 reveals that the number of servers,  $t_k$ , in Totoro scales exponentially as the level increases.

**Theorem 1.** In  $Totoro_k$ , the total number of servers is

$$t_k = n^{k+1}. (1)$$

*Proof:* A  $Totoro_0$  has  $t_0 = n$  servers.  $n Totoro_0 s$  are connected to n-port inter-switches to form a Totoro1. Hence, there are  $t_1 = n \times t_0$  servers in a  $Totoro_1$ . In general, a  $Totoro_i$   $(1 \leq i \leq k)$  consists of n  $Totoro_{i-1}s$  and has  $t_i = n \times t_{i-1}$  servers. Finally, the total number of servers in  $Totoro_k$  is  $t_k = n^{k+1}$ .

The proposed Totoro is suitable for different sizes, from thousands to millions of nodes. In accordance with the wiring philosophy, a  $Totoro_k$  always remains  $t_k/2^k$  ports for extension. Henceforth, the total number of Totoro,  $t_k$ , can be infinite in theory as the structural level k increases.

Theorem 2 shows that the average node degree of Totoro, denoted by  $degree_{avg}$ , approaches to 2 when k grows, but will never reach 2.

**Theorem 2.** In  $Totoro_k$ , the average node degree is

$$degree_{avg} = 2 - \left(\frac{1}{2}\right)^k.$$
 (2)

*Proof:* Let  $c_i$   $(1 \leq i \leq k)$  denote the number of available ports in  $Totoro_i$ . A  $Totoro_0$  has  $c_0 = n$  available ports. By using half of the available ports in each *Totoro*<sub>0</sub>,  $n Totoro_0 s$  are connected to *n*-port inter-switches to form a Totoro<sub>1</sub> which has  $c_1 = n \times c_0/2 = n^2/2$  available ports. In general, a *Totoro<sub>i</sub>* has  $c_i = n \times c_{i-1}/2$  available ports. Finally, a  $Totoro_k$  has  $c_k = n \times c_{k-1}/2 = n \times (n/2)^k$ available ports. In other words, there are  $c_k$  one-degree servers while the others are two-degree. Therefore, the total node degree in  $Totoro_k$  is  $degree_{total} = 2 \times t_k - n \times (n/2)^k$ . In combination with Theorem 1, the average node degree is  $degree_{avg} = degree_{total}/t_k = 2 - (1/2)^k.$ 

Theorem 2 demonstrates that Totoro is always incomplete and highly scalable by using available backup ports. In addition, a low node degree means that fewer links are required, leading to the lower deployment cost.

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Algorithm 2: Totoro Routing Algorithm						
1 F	<b>unction</b> <i>TRoute</i> ( <i>src, dst</i> )					
2	if $src == dst$ then					
3	_ return NULL					
4	lcl = getLCL(src, dst)					
5	if $lcl == 0$ then	// in the same $Totoro_0$				
6	return P(src, dst)					
7	else					
8	P(m, n) = getNearest	Path(src, dst, lcl)				
9 <b>return</b> <i>TRoute</i> ( <i>src</i> , <i>m</i> )+ <i>P</i> ( <i>m</i> , <i>n</i> )+ <i>TRoute</i> ( <i>n</i> , <i>dst</i> )						

**Theorem 3.** The bisection width (BiW) of  $Totoro_k$  is

$$BiW = \frac{t_k}{2^{k+1}}.$$
(3)

*Proof:* Bisection width denotes the minimal number of links to be removed so as to partition a network into two parts of equal size. Considering the linking philosophy, there exist  $(n/2)^k$  top-level (i.e., k-level) switches in a  $Totoro_k$ . We divide these top-level switches into two equivalent sets, indicated by  $S_A$  and  $S_B$ . We also divide all nodes into two equal sets, indicated by  $N_A$  and  $N_B$ . Then we unlink all switches in  $S_A$  from nodes in  $N_B$  and keep the connection between  $S_A$  and  $N_A$ . Similarly, we unlink all switches in  $S_B$  from nodes in  $N_A$  and keep the connection between  $S_B$  and  $N_B$ . Now the network is divided into two equal parts. In the above process, half of the links on each switch have been unplugged, i.e.,  $(n/2)^k \times n/2 = (n/2)^{k+1} = t_k/2^{k+1}$  links are removed (Note that each switch has n links). Hence, Theorem 3 has been proved.

A larger bisection width implies a higher network capacity and a more resilient structure against failure. A low-level Totoro can hold a large number of servers. Thus, Totoro has a relative large bisection width. We will further compare Totoro and other structures in Section 6.

## 4 TOTORO ROUTING

40 In DCNs, how to reroute the packets to bypass the failures 41 becomes a vital problem [5] [21]. The fashionable approach 42 that shares global link states is impracticable due to the 43 huge volume of traffic caused by sending link states. As 44 the servers deployed in DCNs are all commodity servers, it is extremely difficult to finish this computational task with 45 46 an  $O(n^3)$  time complexity of thousands or even millions of 47 nodes at short notice.

Since Totoro is layered and the connection is regular (see 48 Algorithm 2), we design Totoro Routing Algorithm based on 49 Divide and Conquer Algorithm [10] instead of the shortest path 50 algorithm. Then the whole network is partitioned into some 51 domains, Totoro Broadcast Domains. Link states are limited in 52 such a domain rather than spread globally. In combination 53 of these two strategies, a fault-tolerant routing mechanism, 54 namely Totoro Fault-tolerant Routing, is proposed to deal with 55 several common failure scenarios. 56

#### 58 4.1 Totoro Routing Algorithm (TRA)

59 *TRA* is based on Divide and Conquer Algorithm and is more60 simple and efficient. Suppose the source server (denoted

TABLE 2: The Mean Value and Standard Deviation of the Path Length in TRA and SPA.

n	Ŀ	$t_k$	$M_k$	TRA		SPA	
	ĸ			Mean	StdDev	Mean	StdDev
24	1	576	6	4.36	1.03	4.36	1.03
32	1	1024	6	4.40	1.00	4.39	1.00
48	1	2304	6	4.43	0.96	4.43	0.96
24	2	13824	10	7.61	1.56	7.39	1.32
32	2	32768	10	7.68	1.50	7.45	1.26

by src) is in a  $Totoro_{i-1}$  ( $0 < i \leq k$ ) partition and the destination server (denoted by dst) is in another  $Totoro_{i-1}$  $(0 < i \leq k)$  partition. These two  $Totoro_{i-1}s$  belong to the same  $Totoro_i$   $(0 < i \leq k)$ . Thus, there must be at least one level-*i* path between these two  $Totoro_{i-1}s$  to connect each other. To find out the path from src to dst in Totoro: firstly, we need to find out one such level-*i* path (denoted by P(m, n)); we suppose servers m and src are in the same  $Totoro_{i-1}$  while servers n and dst are in the another  $Totoro_{i-1}$ ; then, the problem is divided into two sub-problems, i.e., to work out the path from src to m and the path from n to dst; we use the same method to gain P(src, m) and P(n, dst) recursively; in this process, if the beginning and the ending of a path are found in the same *Totoro*<sub>0</sub>, the directed path between them is returned; finally, we join P(src, m), P(m, n) and P(n, dst) for a full path.

The function **TRoute** in Algorithm 2 follows the whole process mentioned above. The function **getLCL** returns the *Lowest Common Level* (LCL) of two nodes. The function **getNearestPath** picks a level-*lcl* path nearest to the given source host. For example, in Fig. 1, **getNearestPath**([0,0], [1,1], 1) returns P([0,0], [1,0]) rather than P([0,2], [1,2]). The time complexity of Algorithm 2 is  $O(2^k)$  where *k* denotes the top level of *Totoro*. Considering *k* is always smaller than 4 because a low-level Totoro can hold a large number of servers and the larger *k* is not required, the actual time complexity is acceptable.

Denoting the distance between the server and its direct neighbor switch as 1, the maximum distance between two servers,  $M_k$ , can be given by the following theorem.

**Theorem 4.** The maximum distance between two servers in  $Totoro_k$  is

$$M_k = 2^{k+2} - 2. (4)$$

*Proof:* Algorithm 2 reveals that the routing algorithm divides the path into two sub-paths, which are connected by an intermediate link. The length of intermediate link is 2. Thus, we can easily get  $M_k = 2 \times M_{k-1} + 2$ , which is further transformed into  $M_k + 2 = 2 \times (M_{k-1} + 2)$ . Through using the induction, this theorem can be proved.

In fact, Theorem 4 reveals the upper bound of network diameter. The shorter the network diameter is, the more effective the routing mechanism will be. The performance of routing algorithm can be directly evaluated according to the path length. Table 2 lists the mean values and the standard deviations of the path length by using TRA and

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SPA (Shortest Path Algorithm<sup>2</sup>) for Totoro with different nand k. In terms of the mean value and standard deviation, we observe that the differences are both small, indicating that the performance of TRA is close to SPA under the conditions of different sizes. Although SPA is globally optimal, its computation complexity is as high as  $O(n^3)$  and thus it is not suitable for routing in data center. However, SPA gives the upper bound of routing performance (e.g., path length, and path failure ratio) [10]. Such comparison suggests that the proposed TRA is efficient enough. Thus, we build the fault-tolerant routing algorithm in Totoro based on TRA since it is much simpler than SPA.

12 Considering the following case:, suppose [0,0] in Fig. 13 1 needs to access [1,1], but link  $[0,0] \rightarrow (1-0)$  and link 14  $[1,2] \rightarrow (1-1)$  both fail (e.g., the corresponding ports are 15 unavailable or there is something wrong with the wires). 16 In this case, no matter which intermediate path is chosen 17 (i.e.,  $[0,0] \to [1,0]$  or  $[0,2] \to [1,2]$ ), TRA will fail to find 18 a path from [0,0] to [1,1]. In fact, however, there still exist 19 available paths, such as  $[0,0] \rightarrow [0,2] \rightarrow [2,2] \rightarrow [2,0] \rightarrow$ 20  $[1,0] \rightarrow [1,1]$ . Therefore, TRA is not fault-tolerant and we 21 need a more powerful and robust mechanism to solve this 22 problem. Since the network state, e.g., link state is crucial 23 for a routing mechanism, we naturally decide to utilize it to 24 make a fault-tolerant routing mechanism. Instead of sharing 25 link states in the whole network, the structure is divided 26 into several partitions for efficiency. Each partition is called 27 a TBD, which is detailed below. 28

# 4.2 Totoro Broadcast Domain (TBD)

30 In this subsection, the definition of Totoro Broadcast Domain 31 (TBD) is introduced to break up the network. Firstly, we 32 define a variable called bcl (Broadcast Level) for broadcast 33 domain, which means that a *Totoro*<sub>bcl</sub> is a TBD. The server 34 in a TBD is called *inner-server* while the server connected to 35 TBD with an outgoing link whose level is larger than *bcl* is 36 called outer-server. Take Fig. 1 as an example, and assume 37 bcl = 0. Then [0,0], [0,1], [0,2] [0,3] and (0-0,0) can be 38 regarded as a TBD. [1,0], [2,0], [3,0], [1,2], [2,2] and [3,2]39 are outer-servers of this TBD.

40 Servers detect the state of links connecting them and 41 broadcast the link state information to its intra-switch and 42 inter-switch (if it has) periodically. If a server receives a 43 packet of link states, it handles the packet based on the 44 following steps: If this packet has ever been received, then 45 just drop it. Otherwise, save the link states and determine 46 whether the packet comes from inter-switch. If this is the 47 case, broadcast it to the intra-switch. If not, broadcast it 48 to inter-switch if this server is connected to an inter-switch 49 with a link whose level is less than or equal to *bcl*.

50 As a result, all inner-servers get the link states of every 51 inner-server and every outer-server while outer-servers only 52 own the states of the links that connect inner-servers and 53 themselves. The reason is that we will regard an outer-54 server as a proxy in the failure scenarios and data will 55 only flow from inner-servers to outer-servers. Hence, outer-56 servers do not need to get the link states among inner-57 servers. Note that, inner-servers and outer-servers are not





Fig. 3: Totoro Fault-tolerant Routing.

fixed in different TBDs. That is to say, as an outer-server in one TBD (e.g.,  $Tototro_0[1]$ ), a server (e.g., [0,0]) will never share the link states to inner-servers (e.g., [1,0]). But as an inner-server in another TBD (e.g.,  $Tototro_0[0]$ ), this server (e.g., [0,0]) will share link states with outer-servers (e.g., [1,0]).

# 4.3 Totoro Fault-tolerant Routing (TFR)

To combine TRA and TBD, we propose a distributed, faulttolerant routing protocol for Totoro. In a real-world situation, there are four common types of failures: link, server, switch and rack. By *Using Redundant Links* and *Rerouting Through Neighborhoods*, TFR displays the excellent faulttolerance capacity to handle these four types of failures. The evaluation will be detailed in Section 5.

# 4.3.1 Using Redundant Links

Although TRA is efficient, it cannot deal with failures efficiently as discussed above. Assume that source server *src* needs to access the destination server *dst*, the current server is *cur* and the selected path, P(m,n), fails. In this case, the failure cannot be detected until the packet arrives at server *m*. This may cause a lot of useless forwarding. So, what if there is enough intelligence to find out an available P(m, n)?

Note that the key of TRA is to figure out the *Lowest Common Level* (Algorithm 2, Line 4), denoted by *lcl*, and a nearest level-*lcl* link (Algorithm 2, Line 8), denoted by P(m, n), between two  $Totoro_{lcl-1}s$  where *src* and *dst* are located respectively. Before determining the routing path, we must make sure that P(m, n) can be found out in its TBD so as to know its state. Here, the following constraint is given to *bcl* to provide this feature.

*Theorem 5.* The constraint to *bcl* is

i.e.,

$$n^{bcl+1} \ge 2^k,\tag{5}$$

$$bcl \ge \log_n 2^k - 1. \tag{6}$$

Theorem 5 implies that there is at least one outgoing link with *level*  $\leq k$  in a TBD. In other words, a TBD contains

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links of all levels, from 0 to k. Thus, we can always find out P(m, n) and its state which is shared within this TBD. Note that, the value of *bcl* should be as small as possible because sharing link states in a large TBD will cause huge traffic loads.

In order to further improve the routing efficiency, we replace TRA with Dijkstra algorithm within TBD. This will not create heavy burden on the server since the number of servers in a TBD is not large. Among TBDs, we still use TRA for routing.

As shown in Fig. 3, by virtue of TRA, server *cur* finds 11 that the whole path consists of P(cur, m), P(m, n), and 12 P(n, dst). Nevertheless, there is no need to work out the 13 whole path in the routing calculation. Instead, we can work 14 out the next hop only. Hence, the above process can be 15 simplified to identify the path from server cur to server n, 16 which is an outer-server of  $TBD_0$ . Thus, Dijkstra algorithm 17 is adopted to find out the next hop with link states shared 18 in  $TBD_0$ . Furthermore, we add a *proxy* field to the packet 19 header, representing a temporary destination. After working 20 out P(m,n), server n is set as the proxy. If this field is 21 not empty, intermediate servers just need to find out the 22 next hop to the proxy through the use of Dijkstra algorithm 23 rather than TRA. After the packet arrives at the proxy, TRA 24 will be used again to find out the next proxy. This strategy 25 can help reduce the overhead of routing calculation. If the 26 chosen proxy is unreachable (e.g., P(m, n) fails), we just 27 pick out another link P(m', n') whose level is the same as 28 P(m, n) and set server n' as the proxy. Through redundant 29 links, the packet is rerouted to a reachable proxy to bypass 30 the failure. 31

In conclusion, TRA is used to find out the proxy through
the nearest path firstly. In case of failure, the packet is
rerouted to another reachable proxy through redundant
links. Moreover, if there exist several available links, TRA
can choose one of them according to a random algorithm
or the link load. After that, Dijkstra algorithm is adopted to
determine the next hop to the proxy server.

# 4.3.2 Rerouting Through Neighborhoods

41 We use redundant links to bypass a failed link. However, if 42 all required level-*i* links in the current TBD are unavailable, 43 we cannot find out a path from the current server to dst 44 because some servers or inter-switches may fail simultane-45 ously. Server failure and switch failure are also common in a 46 long-running cloud platform. As failures are associated and 47 occur closely, we need a strategy to "escape from" the local 48 area.

49 Observing the structure of Totoro, we find that TBDs 50 are associated by inter-links, whose levels vary from bcl to 51 k. Naturally, we can utilize the adjacent TBDs to bypass 52 the failures. Take Fig. 3 as an example,  $TBD_0$  has three 53 neighborhoods:  $TBD_1$ ,  $TBD_2$  and  $TBD_3$ .  $TBD_1$  is the 54 destination of TBD.  $TBD_2$  is connected to  $TBD_0$  by a link 55 whose level is smaller than *i* and thus  $TBD_2$  and  $TBD_0$ 56 belong to the same  $Totoro_i[src]$ , leading to a benefit that 57 there still exist links connecting to the destination TBD with 58 the required *i*-level (i.e., *LCL*) after the packets are rerouted 59 to  $TBD_2$ . So the packets can be delivered to the destination 60 TBD directly.

Since the outage of data center is inevitable [21], a worse scenario may happen that a row of racks are all down if their power is cut off. In this case, intermediate TBDs may be unreachable and rerouting the packets to neighbor TBDs in the same low-level substructure is useless. Therefore, we adopt a more aggressive method to reroute packets to a neighbor TBD which is far from the trouble spot. Take  $TBD_3$  as an example, it is connected with  $TBD_0$  by a link whose level is greater than or equal to *i* and thus  $TBD_3$  and  $TBD_0$ belong to different  $Totoro_i$ s. If Path(m, n), Path(m', n')and Path(p, pp) all fail, the higher-level Path(q, qq) can be chosen to bypass failures.

In addition, there exist two more unavoidable problems: 1) how to quantitatively determine the level of rerouting links? 2) how to limit the rerouting times due to their huge cost? Here we define a variable RTR (Remaining Times to Retry) and a calculation model to solve these two problems. RTR indicates how many times the rerouting technique can be retried. Whenever the packet is rerouted, RTR needs to be decreased. If it reduces to 0, the packet will be dropped. We naturally believe that the more times the packets are rerouted, the worse the situation must be. Hence, a smaller value of RTR indicates that a higher-level rerouting link should be used. However, rerouting through a higher-level link will cause a longer path and heavier forwarding workload and thus we should reduce the use of higher-level links. To meet the above requirements, we leverage a Base 2 Logarithms Model to calculate the required rerouting level, rl, as follows:

# Theorem 6.

 $rl = min(lcl + |\log_2 RTR\_MAX| - |\log_2 RTR|, k),$ (7)

where *RTR\_MAX* is the maximum value of the initial RTR and *lcl* is the required level (i.e., the current *LCL*).

If we assume lcl = 2 and RTR MAX = 8, the rerouting levels will be 2, 3, 3, 3, 3, 4, 4, 5 with the decrement of RTR. As observed, this model will select lower rl (e.g., level-2) and level-3) many times and skip to higher level (e.g., level-4 and level-5) faster (i.e., after a few retrying times) if it still fails. This implies that the lower-level rerouting links will be tried more while the higher-level ones will be adopted less. Even though this model is simple, the experimental results will prove that it is efficient enough. Note that, if there are more than one link with the required level, one of them is chosen in accordance with a random algorithm or the link load. Furthermore, TFR is not loop free. Frequent rerouting may form a ring. Besides RTR, the field of TTL (Time To Live, hop count of the packet) in IP header will be also used to prevent packets from persisting. If either TTL or RTR reduces to 0, TFR just drops this packet and sends an unreachable message to the source server, if necessary.

#### 4.3.3 Algorithm

Algorithm 3 shows the detailed procedure of TFR. Let *pkt* and *pkt.dst* denote the packet and its destination. If this host is the packet destination, deliver it to the upper layer (Line 3). Otherwise, check whether this host is the proxy. If yes, clear the *proxy* field (Line 5). The empty *proxy* field means that a new proxy will be set in the following steps if

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1	Al	gorithm 3: Totoro Fault-tolerant Routing Algorithm
2	1 F	<b>Sunction</b> TotoroFaultTolerantRoute (this, pkt)
3	2	if $pkt.dst == this$ then
4	3	deliver( <i>this</i> , <i>pkt</i> ) and return $TRUE$
5	4	if $pkt.proxy == this$ then
6	5	$\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $
7	6	if $pkt.ttl \le 0$ then
8	7	drop( <i>pkt</i> ) and <b>return</b> <i>FALSE</i>
9	8	next = getNextByDijkstra(pkt.dst)
10	9	if $next == NULL$ then
11	10	if $pkt.proxy == NULL$ then
12	11	lcl = getLCL(this, pkt.dst)
13	12	pList = getPathsByLevel(this, pkt.dst, lcl)
1/1	13	next = selectAProxy(pkt, pList)
45	14	if $next == NULL$ then
15	15	pList = getReroutingPaths(this, pkt, lcl)
16	16	next = selectAProxy(pkt, pList)
17	17	else
18	18	<pre>next = getNextByDijkstra(pkt.proxy)</pre>
19		
20	19	if $next ! = NULL$ then
21	20	send( $next$ , $pkt$ ) and return $TRUE$
22	21	drop(pkt) and return FALSE

25 necessary (Lines 13 and 16). Then check the field of Time-26 To-Live *ttl* and reduce it. If *ttl* is less than or equal to 0, 27 drop the packet (Line 7). After that, try to get the next 28 hop on the path from the current host to the destination 29 by using Dijkstra algorithm (Line 8). If this host and the 30 destination node are in the same TBD, getNextByDijkstra 31  $(O((V + E) \log V))$  where V and E represent the nodes and 32 edges of a TBD will return the next hop. Otherwise, further 33 calculation is required. Firstly, check whether the proxy field 34 is empty (Line 10). If not, we just work out the next hop to 35 the proxy node (Line 18). Otherwise, get the LCL between 36 the current host and destination node (Line 11). Then find 37 out all available paths that connect TBDs in which this host 38 and the destination are located, respectively, with the given 39 level *lcl* (Line 12). The function **getPathsByLevel** ( $O(2^k)$ ) is 40 based on Algorithm 2 but it returns multiple paths between 41 the given source and destination. *pList* is sorted according 42 to the distance (or link states). Then invoke the function 43 selectAProxy (Line 13), which searches the given *pList*, sets 44 the *proxy* filed, and returns the next hop. If it fails (Line 14), 45 rerouting should be adopted. The function getRerouting-46 **Paths**  $(O(2^k))$  firstly checks the value of RTR, then calculates 47 the required rerouting level based on Theorem 6 and gets 48 those eligible paths. Following the above steps, the packet 49 is sent if the next hop is identified (Line 20). Otherwise, the 50 algorithm drops the packet (Line 21). The time complexity of 51 Algorithm 3 is  $O(2^k + (V+E) \log V)$ , which mainly depends 52 on the scale of a TBD and the rerouting time. 53

#### 4.4 Addressing and Forwarding

56 Totoro uses a 32-bit address to identify a unique server. The 57 *i*-th ( $0 \le i \le 3$ ) byte in the address indicates the *i*-th value 58  $a_i$  of Totoro tuple (see Table 1), which is also the index in 59 *i*-level structure. Note that a 4-level Totoro (k = 3, n = 48) 60 can support as many as five millions servers.

TABLE 3: Network Parameters in the Experiments.

$T_{n,k} / S_{n,k}$	Network	n	k	$t_k$
$T_{12,2} / S_{12,2}$	$Totoro_{12,2}$	12	2	1728
$T_{16,1} / S_{16,1}$	$Totoro_{16,1}$	16	1	256
$T_{16,2} / S_{16,2}$	$Totoro_{16,2}$	16	2	4096

Since most applications are based on TCP/IP, the function of routing and forwarding in Totoro can be implemented as a 2.5-Layer driver between IP layer and the link layer without affecting end-host applications. We need to add a header between IP header and Ethernet header, including fields used in TFR like source address, destination address, proxy address, RTR (Remaining Times to Retry) and so forth. Totoro address is mapped one-to-one to IP address. When a packet is sent from IP layer, the Totoro 2.5-Layer driver translates the IP address into Totoro address, utilizes TFR to calculate the proxy, attaches the Totoro header and delivers the packet to the Ethernet. When a packet arrives, Totoro driver will use TFR to determine whether delivering the packet to the IP layer (the current host is the destination) or rerouting the packet to the next hop by the *proxy* field. Before delivering the packet to the upper layer, Totoro header should be detached.

The software-based solution which is introduced above has been proven to be available in DCell [10] and BCube [11]. Considering the CPU overhead, hardware-based solutions like CAFE [22] and ServerSwitch [23] are also desirable candidates for implementing Totoro's routing and forwarding in real data center environments. They can handle self-defined packets through simple APIs and easy configurations. In addition, commodity switches used in Totoro are not required to be programmable. There is no any modification about them.

#### 5 **EXPERIMENTS AND RESULTS**

## 5.1 Fault Tolerance

In the experiments, we compare TFR and SPA which offers a performance upper bound under the structure of Totoro. The network parameters are shown in Table 3. Two arguments are considered: the switch ports (n) and the structural level (k). The design of the simulation experiments aim at studying how these two structural arguments affect the routing performance. The network scales vary from hundreds to thousands of servers.  $T_{n,k}$  corresponds to the experiment which runs TFR on the Totoro structure with given n and k while  $S_{n,k}$  corresponds to the experiment which runs SPA. Besides, each Totoro<sub>0</sub> is considered as a rack. Failures are generated randomly and the failure ratios vary from 2% to 20%. To achieve reliable experimental results, nodes route packets to all the other nodes 20 times in each simulation experiment and the final result is given by the average of the 20 running results. In each scenario, the numbers of packets to be sent in  $Totoro_{12,2}$ ,  $Totoro_{16,1}$ and  $Totoro_{16,2}$  are about 3M, 65K and 18M, respectively.

Fig. 4(a) depicts the results of the path failure ratio under server failures. It shows that the performance of TFR is almost identical to that of SPA, regardless of the structural

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Fig. 4: Evaluation of Path Failure Ratios

arguments of n and k. SPA is globally optimal and is always able to find out a path from the source to the destination if it exists. The remarkable performance of TFR benefits from the rerouting technique, through which, TFR can maximize the usage of redundant links when server failures occur.

19 Fig. 4(b) plots the path failure ratio versus link failure 20 ratio. It can be observed that the path failure ratio of TFR 21 increases as the link failure ratio rises. The proposed TFR 22 is almost identical to that of SPA in the 1-level structure 23 (i.e.,  $Totoro_{16,1}$ ). However, in the 2-level structure (i.e., 24  $Totoro_{12,2}$  and  $Totoro_{16,2}$ ), it cannot perform as well as SPA 25 when the link failure ratio increases and the performance 26 gap between them becomes larger and larger. For instance, 27 in  $Totoro_{16,2}$ , the gap is 1% (0.03 - 0.02) when the link 28 failure ratio is 4%. It rises to 4% (0.15 - 0.11) when the 29 link failure ratio increases to 16%. This is because the link 30 failure results in only very few nodes to be disconnected. 31 SPA can achieve a good performance even when the link 32 failure ratio is high. But TFR is not globally optimal and 33 not guaranteed to find out an existing path. In fact, TFR is 34 good enough when the link failure ratio is not large (i.e., 35 lower than 10%). Furthermore, we also observe that TFR 36 with a higher structural level has a lower path failure ratio. 37 For example, when the link failure ratio is 12% with given 38 n = 16, the path failure ratio is 13% when k = 1 (i.e., 1-level 39 structure) while it is 10% when k = 2 (i.e., 2-level structure). 40 This fact indicates that the fault tolerance of TFR is more 41 apparent in a Totoro with more levels.

42 Fig. 4(c) depicts the result of the path failure ratio versus 43 switch failure ratio. It shows that TFR achieves the per-44 formance equivalent to SPA in the 1-level structure (i.e., 45  $Totoro_{16,1}$ ). But the performance gap between TFR and 46 SPA becomes larger and larger with the increase of switch 47 failure ratio in the 2-level structures (i.e.,  $Totoro_{12,2}$  and 48  $Totoro_{16,2}$ ). It can also be observed that the path failure 49 ratio of SPA becomes lower in a higher-level Totoro. It 50 means that more redundant high-level switches help bypass 51 the failure rather than become the single point of failure. 52 For this reason, our next work is devoted to improving 53 the performance of TFR under switch failure. Note that, 54 the ladder-shaped polygonal line of  $Totoro_{16,1}$  does not 55 imply that the path failure ratio is strongly associated with 56 a certain range of failure ratios. This is caused by the small 57 number of switches in  $Totoro_{16,1}$  and Totoro has the same 58 number of failed switches in a range of ratios. 59

The results under rack failures are very similar to those of the server failures shown in Fig. 4(a). To evaluate the

effects of our rerouting technology, we further compare TFR with TRA (i.e., the original routing in Algorithm 2 for Totoro without any rerouting technology) and SPA under link failures. The experimental results in Fig. 4(d) reveal that TFR greatly benefits from the proposed rerouting strategy.

It must be emphasized that the legacy SPA is impracticable in the real data centers due to its large traffic loads of sharing link states and its high computation complexity. But SPA offers the upper bound of routing performance and is used to compare the performance of our proposed TFR.

#### 5.2 Throughput

We develop a flow-level simulator based on the approach [24] to evaluate the throughput of Totoro <sup>3</sup>. The Maximum Segment Size (MSS) is set to be 1500*B*. In the current DCNs, the intra-rack RTT is approximately  $100\mu s$  [25]. Hence, the flow's RTT is set as the result of  $100\mu s$  multiplied by the number of switches along the path from the source to the destination. We use a synthetic flow workload from [26], which contains 80000 flows with the total size of 4TB. The flow sizes vary from 1KB to 1GB. The source and destination of each flow are randomly chosen from 0 to 4096. Besides, all flows are launched within 135 seconds.

Furthermore, we build Totoro and five state-of-the-art DCN structures, namely ThreeTier, FatTree, DCell, BCube and FiConn. Specifically, 16-port switches are adopted to construct a 2-level Totoro. ThreeTier structure uses 16-port switches in each level. Each ToR switch in ThreeTier has sixteen 1Gbps downlinks and five 1Gbps uplinks (i.e., 3.2 : 1 oversubscription). Each Aggregate connects sixteen ToR switches and has one 10Gbps uplink to the core (i.e., 8 : 1 oversubscription). Each switch used in FatTree has 26 ports. DCell is built as a 2-level structure with 8-port switches. BCube and FiConn utilize 16-port switches and both have 2-level structures. The number of nodes in Totoro, ThreeTier, FatTree, DCell, BCube and FiConn are 4096, 4096, 4394, 5256, 4096, and 5328, respectively. Except the uplinks of Aggregation switches in ThreeTier, data rates of other links in the experiment are all 1*Gbps*.

The throughput results for DCNs are depicted in Fig. 5. FatTree and BCube complete the data transmission firstly while the ThreeTier structure takes about 65 seconds longer. As FatTree and BCube both use vast switches and abundant links to connect servers, they can achieve

<sup>3.</sup> The simulator is available in http://dsc.jnu.edu.cn/projects/totoro/totoro-exp.tar.gz now.

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Fig. 5: Throughput Comparison of DCNs.

the highest bandwidth. Although their wirings are much sparser than FatTree and BCube, Totoro, DCell and FiConn also achieve comparable throughput, which only takes 10 seconds longer. During the transmission, the highest throughput of Totoro, FatTree, DCell, BCube and FiConn all exceed 250*Gbps*. However, the highest throughput of ThreeTier hovers around 160*Gbps*, equal to the total link capacity of the core switch. This is mainly because the corelevel switch of ThreeTier becomes the bottleneck. It is also notable that ThreeTier will degrade more seriously since the congestion in the core may cause queues to build up the buffer of each lower-level sender.

### 6 ARCHITECTURE ANALYSIS

## 6.1 Robustness

Bilal et. al. [27] proposed a *Deterioration* metric  $\sigma_M$ , which can be calculated as the difference between the average metric value at various failure percentages and the initial metric without failure  $M_0$ , divided by  $M_0$ .  $\sigma_M$  can be represented as

$$\sigma_M = \left| \frac{1}{M_0} \left( \frac{\sum_{i=1}^n M_i}{n} - M_0 \right) \right|,\tag{8}$$

where  $M_i$  is the value of metric M when i percent of the nodes fail. A lower  $\sigma_M$  represents the higher robustness.

Here we calculate  $\sigma_M$  of a  $Totoro_2$  (n = 14) with 2744 servers in total for six graph metrics namely:

**Cluster size** max(v): the size of the largest connected component. A larger max(v) means a more robust structure;

Average shortest-path length  $\langle l \rangle$ : the average length of all the shortest paths among all node-pairs. The smaller  $\langle l \rangle$  represents the higher robustness;

Average nodal degree  $\langle d \rangle$ : the average degree of all nodes. A larger  $\langle d \rangle$  exhibits the better robustness (see the performance analysis for more details);

**54 Algebraic connectivity**  $\mu_{|v|-1}$ : the second smallest **55** Laplacian eigenvalue. The larger value translates to the higher robustness;

57 Symmetry ratio  $\frac{\varepsilon}{D+1}$ : the quotient between the number 58 of distinct eigenvalues of the network adjacency matrix and 59 the network diameter. The lower the value, the better the 60 robustness (see the performance analysis for more details);

TABLE 4: Comparison of Robustness in terms of  $\sigma_M$ .

Metric	FatTree	ThreeTier	DCell	Totoro ( $\sigma_M$ )
max(v)	Middle	Low	High	Middle (0.8034)
$\langle l  angle$	Middle	Low	High	High (0.6121)
$\langle d  angle$	Middle	Low	High	High (0.3163)
$\mu_{ v -1}$	High	Low	Middle	Middle (0.0176)
$\frac{\varepsilon}{D+1}$	Middle	Low	High	High (0.7770)
$\lambda_1$	Middle	Low	High	High (0.1142)

**Spectral radius**  $\lambda_1$ : the largest eigenvalue of the network adjacency matrix. The structure with a larger spectral radius is considered more robust.

We only consider the *targeted attack*, in which the most vital nodes <sup>4</sup> are removed to disconnect the network, taking into account 1% to 6% of the nodes failure. Note that  $\langle l \rangle$ ,  $\mu_{|v|-1}$ ,  $\frac{\varepsilon}{D+1}$  and  $\lambda_1$  are merely calculated for the largest connected component. Thus we can observe that the robustness increases during the higher nodes failure for  $\langle l \rangle$ ,  $\mu_{|v|-1}$  and  $\frac{\varepsilon}{D+1}$ . This also proves that the classic metrics are not appropriate for quantifying the DCN robustness.

We also collect approximate  $\sigma_M s$  of other three stateof-the-art DCN structures from [27], namely DCell, FatTree and ThreeTier. Since such data is received from the similar scale of DCNs, i.e., about 2K nodes, we compare Totoro with them and present the qualitative results in Table 4. Like DCell, Totoro shows higher robustness than FatTree and ThreeTier for almost all metrics. For max(v), DCell outperforms Totoro because the wiring number in DCell is much denser than Totoro. However, the comparison results still confirm that Totoro is inherently fault-tolerant.

## 6.2 **Topological Properties**

To evaluate the topology, we compare Totoro with the traditional ThreeTier structure and several recent structures, such as FatTree, DCell, BCube and FiConn. Let T, n and k denote the total number of servers, the number of ports on a switch and the structural level, respectively. Specially, ThreeTier structure adopts Cisco data center ThreeTier model topology [7], which consists of core, aggregation and access layers.  $n_{acc}$  servers are connected to an access switch (no redundancy for access layer) which uses their uplinks to connect all aggregation switches. Each aggregation switch also has  $n_{agg}$  downlinks to all access switches. Three Tier structure contains  $N_{agg}$  aggregation modules and each module consists of two aggregation switches (one for redundancy). In the core layer, two core switches (one for redundancy) can access each aggregation switches respectively. For simplicity, We do not consider any inter-switch link. Table 5 summarizes the topological comparison results.

**Number of servers:** DCell and FiConn grow doubleexponentially with the level *k*. Totoro and BCube are exponentially incremental. The scale of ThreeTier and FatTree is limited by switches' ports and thus they lack scalability.

Number of switches: In practice, ThreeTier uses less switches than other structures. But such switches are highdensity and more expensive. FatTree needs most switches

4. For Totoro, we found that the most effective method to disparate the network is to remove some high-level inter-switches.

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TABLE 5:	Comparison	of Topol	logical	Property.
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Structure	# of Servers (T)	# of Switches	# of Wires	Degree	Diameter
ThreeTier	$n_{acc}n_{agg}$	$n_{agg} + 2N_{agg} + 2$	$T + 2N_{agg}n_{agg} + 2N_{agg}$	1	6
FatTree	$\frac{n^3}{4}$	$5 \cdot \frac{T}{n}$	$3 \cdot T$	1	6
DCell	$> (n + \frac{1}{2})^{2^k} - \frac{1}{2}$	$\frac{T}{n}$	$(1+\frac{k}{2})\cdot T$	k+1	$2^{k+1} - 1$
BCube	$n^{k+1}$	$(1+k) \cdot \frac{T}{n}$	$(1+k) \cdot T$	k+1	k+1
FiConn	$> 2^{k+2} \times \left(\frac{n}{4}\right)^{2^k}$	$\frac{T}{n}$	$\left(\frac{3}{2} - \frac{1}{2^{k+1}}\right) \cdot T$	$2 - \frac{1}{2^k}$	$2^{k+1} - 1$
Totoro	$n^{k+1}$	$\left(2 - \frac{1}{2^k}\right) \cdot \frac{T}{n}$	$\left(2 - \frac{1}{2^k}\right) \cdot T$	$2 - \frac{1}{2^k}$	$2^k$

#### TABLE 6: Comparison of Bandwidth

Metric	BiW	$AR_{o2o}$	$AR_{o2m/m2o}$	BoD
ThreeTier	$\frac{n_{core}N_{core}}{2}$	1	1	$\frac{T^2}{N_{core}}$
FatTree	$\frac{T}{2}$	1	1	T
DCell	$\frac{T}{4 \log_n T}$	k+1	k+1	$T \cdot 2^k$
BCube	$\frac{T}{2}$	k+1	k+1	$T \cdot 2^k$
FiConn	$\frac{T}{4 \times 2^k}$	2	2	$T \cdot 2^{k+1}$
Totoro	$\frac{T}{2^{k+1}}$	2	2	$T \cdot 2^k$

to be non-oversubscribed. Compared to DCell, BCube and FiConn, Totoro uses considerable amount of switches.

26 Number of wires: The number of wires reflects the
27 density of available paths among nodes as well as the
28 overhead of deployment and maintenance. As the structure
29 level k increases, FiConn has the sparsest wiring density.
30 The number of wires in Totoro will be almost twice as large
31 as server nodes and this is a moderate situation to balance
32 the performance and the deployment overhead.

33 Degree: The server degree of Totoro and FiConn approaches to 2 as k grows, but will never reach 2. They all achieve a smaller node degree than DCell and BCube, which
36 means a lower overhead for deployment and maintenance.
37 Furthermore, Totoro and FiConn are always incomplete and highly scalable by using available backup ports.

Diameter: It is known that the smaller the diameter 39 is, the more efficient the routing mechanism will be. Both 40 ThreeTier and FatTree have a fix diameter of 6. BCube 41 achieves the smallest diameter among all structures. The 42 diameters of Totoro, DCell and FiConn increase exponen-43 tially as the structural level grows. Due to the fact that a 44 low-level Totoro can hold a large number of servers (e.g., 45 a  $Totoro_2$  with n = 32 has 32,768 servers and a  $Totoro_3$ 46 with n = 16 has 65, 536 servers), the diameters of  $Totoro_2$ 47 and Totoro3 are only 10 and 18, respectively. In addition, 48 even though the diameters of ThreeTier and FatTree are 49 both small, they cannot be comparable to Totoro since their 50 scalability is limited by the number of switch ports. 51

#### 6.3 Bandwidth

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54 We evaluate four metrics about bandwidth to compare55 Totoro with state-of-the-art structures:

56Bisection Width (BiW): The bisection width of Three-57Tier is related to its core layer design.  $n_{core}$  denotes the58ports of a core switch.  $N_{core}$  represents the number of59core switches. To separate a ThreeTier structure, we only60need to unplug half of its core links. This implies that the

bandwidth of ThreeTier is totally limited by the core layer. FatTree uses more redundant switches in each layer. It has a large bisection width of T/2. DCell has a large bisection width of  $T/(4 \log_n T)$  since there are more ports on a server. The BCube structure is considered closely related to the generalized Hypercube [11]. It also achieves a large bisection width of T/2, which inherits the good characteristics of Hypercube. The bisection width of FiConn and Totoro are similar. As aforementioned, a low-level Totoro can hold a large number of servers. When we take a small number of k, the bisection width is large, e.g., BiW = T/4, T/8, T/16 when k = 1, 2, 3, respectively. A large bisection width means a fault-tolerant and resilient structure. In addition, a relative large bisection width also leads to the higher network capacity.

Acceleration Ratio under One-to-One communication models ( $AR_{o2o}$ ): Parallel paths between two nodes help accelerating the communication in One-to-One model. If these paths are node-disjoint, the acceleration will be more significant. There exist more than one links from a certain server leaf to the access layer in ThreeTier. But only one is usually active and others are blocked for backup. Thus no acceleration is supported under One-to-One communication. FatTree suffers the same problem. For DCell, BCube, Fi-Conn and Totoro, it can be proved that the acceleration ratio under One-to-One communication model, i.e., the number of parallel paths which are node-disjoint, is the port number of NIC. Note that in Totoro and FiConn, no parallel paths exist if the source or destination node is one-degree. This is a worthwhile trade-off to provide incremental scalability.

Acceleration Ratio under One-to-Many and Many-to-**One communication models (** $AR_{o2m}$  **and**  $AR_{m2o}$ **):** In some distributed file systems like GFS and HDFS, One-to-Many and Many-to-One communication models are common and can be accelerated by using multiple paths. Take One-to-Many model for example, the source node distributes several unique data blocks through different paths. Then the destination nodes share their own blocks with each other to finish the whole process. Thus the One-to-Many communication is accelerated. It is required that these parallel paths are edge-disjoint, i.e., no edges appear on two paths simultaneously. Edge-disjoint complete graphs can be built to determine whether a structure can speed up One-to-Many communication [11]. For DCell, BCube, FiConn and Totoro, the acceleration ratio under O2M or M2O model equals the port number of NIC.

**Bottleneck Degree (BoD):** All-to-All communication model is widely used in parallel data processing framework, e.g., MapReduce. BoD is a metric that denotes the maximum

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Fig. 6: Comparison of Cost and Power

number of flows traveling through a single link under the All-to-All communication model. The bigger BoD means the heavier traffic workloads. For ThreeTier,  $N_{core}$  represents the number of core switches. ThreeTier has a large BoD since a large number of flows burden the core layer much. FatTree has the smallest BoD owing to the non-oversubscribed design. The BoD of Totoro is related to the structural level k. It is much smaller than ThreeTier, which means that the All-to-All flows are spread out over all links.

#### 6.4 Cost and Power

27 Cost and power consumption are two significant issues 28 for DCNs. Costs in DCN contain four major components: 29 servers, infrastructure, power draw and network [6]. The ex-30 isting studies have shown that datacenter computers rarely 31 operate at full utilization [28] [29]. Some studies aimed to 32 reduce the rapidly growing energy (or power) consumption 33 [30] [31]. In this paper, we only discuss cost and energy 34 consumption about static deployment <sup>5</sup>, leaving energy-35 saving routing as our future work.

36 We build a container with 2048 servers as our compari-37 son model. The price and power consumptions of switches 38 and NICs are from Cisco, eBay and [11]. We build the same 39 ThreeTier as that in Section 6.2 according to [7], including 43 40 access (WS-C4948-10G-E,  $48 \times 1GE + 2 \times 10GE$ ), 2 aggrega-41 tion (WS-C6506-E,  $48 \times 10GE + 4 \times 40GE$ ) and 2 core (WS-42 C6504-E,  $4 \times 40GE$ ) switches. The oversubscription ratios 43 are 4.8 : 1 for access layer and 6 : 1 for aggregation layer. 44 For FatTree, DCell, BCube, FiConn and Totoro, commodity 45 8-port switches (D-Link DGS-1008D) are used. ThreeTier<sup>6</sup> 46 and FatTree require 1-port NICs (Intel EXPI9400PT). Servers 47 in DCell and BCube are equipped with 4-port NICs (Intel 48 EXPI9404PT). FiConn and Totoro need 2-port NICs (Intel 49 EXPI9402PT). Fig. 6 depicts the comparison of cost, power 50 and the numbers of switches and wires.

For ThreeTier, switches are much more expensive than
those of other structures and consume the most power, even
thought they are few in number. FatTree has the largest
number of switches while they are commodity ones and
thus the cost and power consumption are moderate. DCell

57 5. We only consider the NICs, switches and wires since CPU, main memory and disk are not directly relevant to the topology structure.

6. For common ThreeTier structures, a server may be equipped with a
2-port NIC, one for active traffic and another for backup. For simplicity, we assume a 1-port NIC is required.

and BCube have a higher cost and power consumption on NIC due to their usage of 4-port NICs. Totoro and FiConn control the switch cost successfully and achieve a graceful power saving. The numbers of switches and wires of Totoro also imply that their deployment overhead are acceptable and uncomplicated, which is consistent with the analysis of Degree property in Section 6.2.

In addition, ThreeTier and FatTree are usually oversubscripted in real data center environments. Their cost, power and wiring complexity can come down significantly as the over-subscription increases. However, the performance will degrade if the over-subscription is too large, as we discuss in the introduction. Moreover, the scaling of ThreeTier and FatTree are still limited to the number of switch ports and they are also not incrementally scalable.

In conclusion, Totoro is comparable with other structure in costs, power and deployment complexity. The superiority of Totoro is that it is incrementally scalable.

# 6.5 Price-performance Ratio

From the above analysis, Totoro and FiConn both achieve a relatively higher cost-efficiency. Totoro has a higher bisection width double that of FiConn while FiConn shows some advantages over Totoro in less cost, power and wires. Generally speaking, there always are some trade-offs in system design. Structures with a lower price/performance ratio are more desirable. Here we exploit **Price/BisectionWidth** ratio to evaluate the trade-off.

Suppose that *T* is the total number of hosts, *n* is the number of ports on a switch, *k* is the structural level,  $P_h$  and  $P_s$  are the prices of host and switch, respectively. The cost to build a *Totoro*<sub>k</sub> structure is:

$$C_t = T \times P_h + \frac{T}{n} \times (2 - \frac{1}{2^k}) \times P_s.$$
(9)

Similarly, the cost of  $FiConn_k$  structure is:

$$C_f = T \times P_h + \frac{T}{n} \times P_s. \tag{10}$$

In combination with the bisection widths, the difference between their Price/BisectionWidth ratio is:

$$D = \frac{C_t}{T/2^{k+1}} - \frac{C_f}{T/(4 \times 2^k)}.$$
(11)

According to Eqs. (9) and (10), Eq. (11) can be transformed to:

$$D = 2^{k+1} \times (\frac{P_s}{n \times 2^k} - P_h).$$
 (12)

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Since  $n \ge 4$ ,  $k \ge 2$  and the price of commodity switch is much less than that of host, we can draw a conclusion that D is smaller than 0, i.e., Totoro achieves a lower priceperformance ratio than FiConn.

# 7 CONCLUSION AND FUTURE WORK

The existing structures of interconnection networks are hardly to meet the requirements of both incremental scalability and cost-efficiency. This drives us to develop a new structure called Totoro. The theoretical analysis and extensive experiments all demonstrate that Totoro satisfies the design goals of scalability, cost-effectiveness, high network capacity and robustness. The proposed structure can significantly help the DCN builders rethink the present design and provides an alternative solution to the existing DCNs, especially in the scenario that incremental scalability and cost-effectiveness are vitally required.

18 Even though Totoro achieves relatively high bandwidth and has a low network diameter, there exist trade-offs 20 between such network goodness and economy. Similar to 21 DCell, BCube and FiConn, packet-forwarding in Totoro may 22 experience delays. This is mainly because we regard servers as "routers" in the forwarding and the packet-handling ability of current NIC is still weaker than the professional chips on switches or routers. But this weakness will be 26 overcome as the NIC becomes more and more powerful.

In the future work, we will focus on the problem of energy saving and be devoted to the design of elastic routing, which is self-adaptive to the traffic mode to lower the overall energy consumption. As a consequence, that Totoro structure is elastic enough to balance the performance and energy conservation due to the vast redundant paths.

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Junjie Xie is a research student at the Computer Science Department of Jinan University. His current research interests cover network interconnection, data center architecture and cloud computing.

Yuhui Deng is a Professor in the Department of Computer Science at Jinan University. His research interests cover green computing, cloud computing, information storage, computer architecture, performance evaluation, etc.

Geyong Min is a Professor of High Performance Computing and Net-working in the Department of Mathematics and Computer Science within the College of Engineering, Mathematics and Physical Sciences at the University of Exeter, United Kingdom. His research interests include Next Generation Internet, Wireless Communications, Multimedia Systems, Information Security, Ubiquitous Computing, Modelling and Performance Engineering.

Yongtao Zhou is a research student at the Computer Science Department of Jinan University. His current research interests cover data deduplication and distrtributed system.