

1 Review of machine-vision based methodologies for displacement measurement in civil  
2 structures

3 Yan Xu<sup>1</sup>, James M.W. Brownjohn<sup>1</sup>

4 <sup>1</sup>Vibration Engineering Section, College of Engineering, Mathematics and Physical Sciences,  
5 University of Exeter, UK EX4 4QF

6 Email: yx298@exeter.ac.uk

7  
8 **Abstract**

9 Vision-based systems are promising tools for displacement measurement in civil structures, possessing advantages  
10 over traditional displacement sensors in instrumentation cost, installation efforts and measurement capacity in  
11 terms of frequency range and spatial resolution. Approximately one hundred papers to date have appeared on this  
12 subject, investigating topics like: system development and improvement, the viability on field applications and  
13 the potential for structural condition assessment. The main contribution of this paper is to present a literature  
14 review of vision-based displacement measurement, from the perspectives of methodologies and applications.  
15 Video processing procedures in this paper are summarised as a three-component framework, camera calibration,  
16 target tracking and structural displacement calculation. Methods for each component are presented in principle,  
17 with discussions about the relative advantages and limitations. Applications in the two most active fields: bridge  
18 deformation and cable vibration measurement are examined followed by a summary of field challenges observed  
19 in monitoring tests. Important gaps requiring further investigation are presented e.g. robust tracking methods, non-  
20 contact sensing and measurement accuracy evaluation in field conditions.

21 **Keywords** Vision-based system; Structural displacement; Camera calibration; Target tracking.

23 1 INTRODUCTION

24 Structural health monitoring (SHM) is aimed at providing valuable information for structural assessment and  
25 decision support for maintenance through relevant measures of structural response. Deformation is an important  
26 metric for structural condition and performance assessment for several reasons. In particular serviceability is  
27 reflected through deformation during normal operation, since extreme values and ranges indicate problems that  
28 may limit operational use, while time-varying deformation patterns constructed from discrete displacement  
29 measurements can provide a wealth of information about structure condition.

30 Conventional sensors like linear variable differential transformers (LVDT) require a stationary reference point for  
31 installation and direct access to monitoring structures that could be challenging on site. The global positioning  
32 systems (GPS) have the limitation of measurement accuracy (i.e. sub-centimetre [1] or centimetre level [2]) and  
33 are mostly applied for monitoring campaigns in flexible large-scale structures. Integration schemes from  
34 acceleration measurement are only feasible for short-time signals and might fail to capture the static or quasi-  
35 static components in displacement signals. Such limitations of more traditional displacement sensing technologies  
36 have driven research in non-contact optical sensing. Vision-based monitoring methods have promising features  
37 e.g. simple instrumentation and installation, operation remote from the structure and capacity for multi-point  
38 measurement using a single (camera) sensor.

39 Although there have been earlier optics-based methods used for monitoring civil structure deformation e.g. in the  
40 Tacoma Narrows Bridge [3] and the Tagus Bridge [4], among the earliest applications of opto-electronic vision-  
41 based continuous structural deformation monitoring using CCD (charge-coupled device) arrays was to Humber  
42 Bridge and Severn Bridge in the UK [5], [6]. Since then a number of systems have been developed and evaluated  
43 for structural deformation monitoring in high-rise buildings [7], short-span bridges [8], [9], [10], [11] and long-  
44 span bridges [12], [13], [14].

45 Vision-based systems offer significant potential for structural condition assessment, in particular for system  
46 identification [15–17]. In addition, deformation information has been used for finite element model calibration  
47 [18], damage detection [19] and contribution to bridge weigh-in-motion system with camera assistance for traffic  
48 monitoring [20].

49 Investigations have been made in system improvement in both video acquisition hardware and video processing  
50 software. The feasible video acquisition devices are expanded to include smartphone cameras [15][21], while  
51 artificial targets required in conventional systems were discarded in some recent applications under specific

52 camera configurations [8, 15, 22]. Efficient target tracking techniques in the computer vision field have been  
53 validated in structural deformation monitoring [15], [22], [23] and the measurement results describing structural  
54 displacement have been expanded to three-dimensional [24, 25], [17], [26] and six degree of freedom (DOF)  
55 motions [11, 14].

56 This paper aims to present a summary of key work in the field of vision-based systems for structural displacement  
57 monitoring while highlighting the principles, advantages and shortcomings of these systems. Although previous  
58 reviews of vision-based structural monitoring exist [27–29], the contribution of this work is to provide an overview  
59 of system classifications, methodologies and applications in field monitoring.

60 The paper is organised as follows. The components of a vision-based system for displacement monitoring are  
61 introduced, followed by a comparison of several mature vision-based systems in application scopes in section 2.  
62 In section 3, vision-based systems are categorised based on methods of video processing, with three components  
63 in video processing procedures (i.e. camera calibration, target tracking and structural displacement calculation)  
64 reviewed in terms of principle, applications, advantages and shortcomings, respectively. In section 4, applications  
65 for bridge deformation and cable vibration measurement are reviewed followed by a discussion of measurement  
66 challenges in field applications. Finally, important gaps requiring further investigation are presented e.g. robust  
67 tracking methods, non-contact sensing and measurement accuracy evaluation in field conditions.

## 68 2 VISION-BASED DISPLACEMENT MONITORING SYSTEMS

69 Applying a vision-based system for structural displacement monitoring requires setting up one or more cameras  
70 in a stable location, looking at the ‘target’ contained in a structure and deriving the structural displacement through  
71 target tracking. Here the ‘target’ could be either artificial (e.g. pre-installed marker, LED lamp or planar panel  
72 with special patterns) or an existing structural feature (e.g. bolts or holes). As shown in Fig. 1, the hardware  
73 generally comprises camera, lens, laptop/portable computer with video-processing package and some accessories  
74 e.g. tripod. The video processing software is critical: its role is acquiring the video frames covering the target  
75 region, tracking the target locations in image sequences and finally transforming the target location in image to  
76 time history of structural displacement.

77 Systems for extracting metric information from images or videos exist in several fields as indicated in Table 1 e.g.  
78 digital image correlation (DIC) [9], [31], [32], photogrammetric techniques [33] and motion capture systems  
79 (MCS) [17, 34]. DIC is a measurement tool to extract full-field displacements or strains of a member surface in  
80 experimental solid mechanics [32, 35, 36]. Photogrammetry, originally in the production of topographic maps

81 [37], is expanded to include deflection monitoring of bridge structures [38]. Motion capture systems (MCS) are  
82 usually applied to capture the movements of a high degree-of-freedom skeleton structure with a number of joints  
83 (e.g. human bodies) [39].

84 A vision-based system for structural displacement monitoring owns its unique features, as indicated in the last  
85 row of Table 1. Researchers have performed several investigations into system development targeted at structural  
86 applications and these studies will be reviewed in terms of methodologies in the next section.

### 87 3 REVIEW OF VISION-BASED STRUCTURAL DISPLACEMENT MEASUREMENT

88 In this study, vision-based systems in literature are classified based on video-processing methodologies. A typical  
89 video processing software package could fit into a three-component framework shown in Fig. 2. The derived  
90 displacement data could be interpreted for bridge condition assessment.

91 If the monitoring campaign is only for system identification and exact vibration values [40, 41] are not required,  
92 target tracking may be the only part of the whole video processing procedure needed, but coordinate  
93 transformation might be necessary to align the image motion directions with the structural axes.

94 Next, the methods for camera calibration, target tracking and structural displacement calculation in literature are  
95 reviewed separately.

#### 96 3.1 Camera calibration

97 Camera calibration concerns building the projection relationship between the 3D structural points in the structural  
98 coordinate system and the corresponding 2D points in the image plane. The determined projection transformation  
99 could be used to recover the real locations of targets in structure given the target locations in the image.

100 Three categories of projection transformation are reported in the literature including the full projection matrix,  
101 planar homography and scale factor as indicated in Table 2. In most cases, the projection transformation is  
102 following the full perspective model while it could be simplified to an affine camera model when cameras are  
103 equipped with large focal length lenses [25].

##### 104 3.1.1 Full projection matrix

###### 105 **Principle**

106 The full projection matrix is the general form of projection transformation from the 3D structural system to the  
107 2D image plane under no constraint on camera orientation and structural movement directions and is usually used  
108 to reconstruct the target 3D structural displacement. The projection relationship is demonstrated in Fig. 3 with a

109 point  $P_s(\mathbf{X}_w = [X, Y, Z, 1]^T)$  in the structural coordinate system mapping to a point  $P_1(\mathbf{u} = [u, v, 1]^T)$  in the 2D  
110 image plane,

$$111 \quad \alpha \{\mathbf{u}\} = [\mathbf{H}]_{3 \times 4} \{\mathbf{X}_w\} \quad (1)$$

112 where  $[\mathbf{H}]_{3 \times 4}$  is a full projection matrix and  $\alpha$  is an arbitrary coefficient.

113 The calibration process is shown in Fig. 4 with two main steps. The camera intrinsic matrix is usually estimated  
114 in the laboratory by analysing a set of images of a calibration object taken from different viewpoints [42]. The  
115 calibration object is typically a flat plane or 3D object with a dot or grid pattern of known spacing such as the  
116 chessboard pattern shown in Fig. 4. At least three views of the calibration object with four corner points are  
117 required, but it is suggested to use at least ten images to derive more robust estimates [43]. After laboratory  
118 calibration, any lens functions e.g. autofocus and automated image stabilisation that might lead to changes in  
119 camera internal parameters are disabled.

120 Consumer-grade cameras and smartphone cameras always employ wide angle lenses to increase the field-of-view  
121 [15], leading to distorted images particularly in the corner regions of the frame as shown in Fig. 5(a). The lens  
122 distortion parameters could also be estimated in laboratory calibration and applied to correct the image with the  
123 rectified one in Fig. 5(b). For cameras equipped with lenses producing no apparent lens distortion, the distortion  
124 correction step is not necessary. Naturally for the monitoring measurements, it is preferable to locate the target  
125 region in the central area of the field of view [10] which suffers less lens distortion, as shown in Fig. 5(a).

126 In the second step, the camera extrinsic matrix representing the camera position and orientation is estimated on  
127 site through point correspondences, i.e. 3D structural coordinates of control points and 2D image coordinates of  
128 their projections in an image. Given at least four sets of point correspondences, least-squares optimisation is used  
129 to find the best option of camera extrinsic matrix that minimises the total re-projection error between the detected  
130 image points and the calculated image projection points.

131 The calibration algorithms are available in the Vision System Toolbox of MATLAB and the open-source library  
132 OpenCV.

### 133 **Application review**

134 Camera calibration for full projection matrix estimation is commonly used to measure 3D structural displacement,  
135 with a few examples illustrating the method: The procedures of laboratory and site camera calibration are  
136 described by Kim et al. [44] in an application to structural displacement monitoring in a three-span bridge under  
137 truck-induced vibration. The viability of motion capture systems for the laboratory vibration measurement was

138 verified [34] using a T-shaped calibration wand for the estimation of camera extrinsic parameters. In the case of  
 139 a long span bridge, Martins et al. [14] applied the calibration method to measure the 3D structural displacement  
 140 at mid-span with the assistance of a set of four active targets. The estimated camera parameters can be refined  
 141 when multiple cameras with overlapped views are involved. For example, the methodology described by Chang  
 142 and Ji [24] is based on the epipolar geometry principle of stereoscopic vision where five points including structural  
 143 point  $P_s$ , projection points in two image planes  $P_1^1$  and  $P_1^2$ , and two camera optical centres should all be coplanar,  
 144 as shown in Fig. 6.

#### 145 **Remarks**

146 The full projection matrix is an accurate representation of the projection relationship and is thus applicable to any  
 147 configuration of cameras on site. The lens distortion problems common for consumer-grade cameras do not  
 148 prevent their use for such measurements, since corrections are readily made for distortion using laboratory camera  
 149 calibration.

150 Camera calibration on site requires position information for some structural points. In existing studies this has  
 151 been mainly acquired through the installation of artificial targets. Including artificial targets in laboratory tests is  
 152 easy e.g. attaching a planar chessboard target [24, 44] or placing a planar T-shaped wand in the field of view [17,  
 153 34] while the installation efforts in field tests [14] are much greater. The existing examples of two field  
 154 applications are summarised in Table 3, indicating the feasibility of this method for both short-range and long-  
 155 range monitoring tests.

#### 156 3.1.2 Planar homography

##### 157 **Principle**

158 For the case where the target moves within a plane contained in the 3D structural system (e.g. the XY plane), the  
 159 projection relationship could be simplified to a planar homography between a 2D structural plane  
 160 ( $\mathbf{X}_p = [X, Y, 1]^T$ ) and a 2D image plane ( $\mathbf{u} = [u, v, 1]^T$ )

$$161 \quad \alpha \{\mathbf{u}\} = [\mathbf{P}]_{3 \times 3} \{\mathbf{X}_p\} \quad (2)$$

162 where  $[\mathbf{P}]_{3 \times 3}$  is the planar homography matrix and  $\alpha$  is an arbitrary coefficient.

163 The reconstructed results using planar homography are usually the 2D structural displacement of targets.

164 The calibration process requires at least four sets of 2D-to-2D point correspondences [46], similar to the estimation  
 165 process on site in full projection method.

##### 166 **Application review**

167 The planar homography considers the geometric distortion in the projection process and thus has no constraint on  
 168 camera positioning [47]. The 2D direct linear transform is effective for the planar homography estimation [48],  
 169 for example the method was applied to monitor the oscillation of a laboratory steel frame with a dense array of  
 170 markers glued to the surface [48] and the mid-span deformation of a long-span bridge with an attached planar  
 171 artificial target [49].

## 172 **Remarks**

173 Planar homography applies no constraint on camera positioning and can be used to recover the target 2D structural  
 174 displacements. In its application it is usual that the geometric information needed for calibration is provided by  
 175 attaching artificial planar targets with known dimensions.

176 This calibration method is based on the assumption that the target moves within a structural plane with negligible  
 177 motion along the third axis. Any motion not contained within this plane will lead to measurement error unless the  
 178 motion is purely perpendicular to the camera optical axis.

### 179 3.1.3 Scale factor

#### 180 **Principle**

181 Scale factor is the simplest projection transformation and assumes an equal depth-of-field for all projected points  
 182 or a camera configuration where the optical axis is perpendicular to one structural plane [48]. With this assumption,  
 183 the mapping process converts to a 1D-1D projection indicated in Fig. 7. The scale factor SF from the structural  
 184 displacement to the image motion could be determined by one-dimensional correspondence or the camera-to-  
 185 target distance,

$$186 \quad SF = \frac{|P_1Q_1|}{|P_sQ_s|} \quad (3)$$

$$187 \quad \text{or} \quad SF = \frac{f_{pix}}{D} \quad (4)$$

188 where  $|P_sQ_s|$  and  $|P_1Q_1|$  are the known physical dimension on the structural surface and the corresponding pixel  
 189 length of the projection in image;  $f_{pix}$  is the camera lens focal length in terms of pixel units; and  $D$  denotes the  
 190 distance from the camera optical centre to the structural surface plane.

191 For the system combining a camera with a total station, a projection coefficient called angular resolution [50, 51]  
 192 is used to perform the transformation which represents the angle value ( $\alpha$  in Fig. 7) from the camera optical axis  
 193 to a projection line with the projection length ( $|O_1P_1|$ ) of one pixel. In principle, this projection transformation is

194 similar to the scale factor estimated by camera-to-target distance in Equation (4) where the distance  $D$  is  
195 measured directly by electronic distance measurement (EDM) instrument and the focal length  $f_{pix}$  is related to  
196 the angular resolution  $\theta$  by

$$197 \quad \theta \approx \tan \theta = 1 / f_{pix} \quad (5)$$

### 198 **Application review**

199 Scale factor has been widely used to transform image motion to structural displacement with the features  
200 summarised in Table 4. Mostly the scale factor is determined via a known dimensions in an artificial target  
201 attached to structure [5, 8–10, 12, 13, 15, 52–57] while the method using the camera-to-target distance [22] is less  
202 popular. For 2D structural displacement measurement, the scale factors for two axes within the target plane are  
203 calibrated separately according to dimension correspondences [53–56]. Error analysis indicates that the scale  
204 factor by dimension correspondence is less sensitive to the tilt of camera optical axis [8]. However, the scale factor  
205 using the camera-to-target distance has no dependence on artificial targets and thus is an easier way to realise  
206 completely non-contact monitoring [22].

### 207 **Remarks**

208 Scale factor is the simplest projection transformation, particularly when no artificial target is used [15, 22] and  
209 works when the camera optical axis is perpendicular to the structural surface. Camera positioning is less critical  
210 [8] when known structural dimensions are used for calibration. However, when applying the scale factor derived  
211 from the camera-to-target distance, the tilt angle of the camera optical axis is suggested to be less than  $10^\circ$  through  
212 laboratory validation tests in short distance ( $\leq 3.7$  m) [58]. Care must be taken that different scale factors are  
213 applied to different axes to measure the 2D displacement. This simple method can also be used with cameras  
214 having apparent lens distortion, since the lens distortion correction method previously described can be used [15,  
215 57].

## 216 *3.2 Target tracking*

217 Target tracking is the key part of a video processing software package. In this study, target tracking techniques  
218 are categorised into four types based on target characteristics shown in Table 5, partly referring to [59].

### 219 *3.2.1 Template matching*

#### 220 **Principle**

221 Template matching is a classic technique for target tracking by searching in a new frame for an area most closely  
222 resembling a predefined template, following the procedures demonstrated in Fig. 8. A rectangular region that is a



223 subset in the reference frame is first selected as the template, and could be either an artificial target [5] or a feature  
 224 target on the structural surface [8]. A correlation criterion is required in order to evaluate the similarity level  
 225 between the template and the new image subset. Robust criteria for matching are zero-mean normalised cross  
 226 correlation (ZNCC) and zero-mean normalized sum of squared differences (ZNSSD) which are insensitive to  
 227 offset and linear scale in illumination [35] while another similarity criterion based on orientation code is also  
 228 reported to be effective [60]. The definition of the ZNCC criterion is provided as an example in Equation (6) while  
 229 more details are given in [35].

$$230 \quad C_{ZNCC} = \sum_{i=-M}^M \sum_{j=-N}^N \left[ \frac{(f(x_i, y_j) - f_m)(g(x'_i, y'_j) - g_m)}{\Delta f \Delta g} \right] \quad (6)$$

231 where  $f(x_i, y_j)$  and  $g(x'_i, y'_j)$  denote the image intensity values at the specified pixel locations in the template  
 232 region and the new frame;  $f_m$  and  $g_m$  denote the average intensity values in the template region and the new  
 233 frame; and  $\Delta f$  and  $\Delta g$  denote the standard deviations of intensity values in the template region and the new  
 234 frame.

235 The location in the correlation map reaching the highest similarity is taken as the new image location of the target.  
 236 The default resolution is at pixel level, so interpolation schemes [8] are used to refine the result to the subpixel  
 237 level. The feasible interpolation methods include bi-cubic interpolation [56], second-order polynomial  
 238 interpolation [57] in spatial domain and zero-padding interpolation in frequency domain [8]. If the selected target  
 239 includes robust and identifiable features, Harris corner detection that identifies the edge intersection points  
 240 through a score value related to the eigenvalues of image gradient matrix could be an alternative to refine the  
 241 initial matching location [24].

## 242 **Application review**

243 Template matching is an established method widely applied in structural monitoring from the earliest work on the  
 244 Humber and Severn Bridges in 1990s [5, 6]. Recent applications include displacement monitoring tests on a  
 245 railway bridge [8], a long-span bridge [13] and a high-rise building [7].

246 Digital image correlation (DIC) is an extension of template matching mostly used in experimental mechanics [32,  
 247 35], with the difference that DIC considers the shape distortion under large deformation [61] i.e. Lucas-Kanade  
 248 template matching [62]. As an example, a short-span railway bridge monitoring exercise [63] used normalised  
 249 correlation-based matching and Lucas-Kanade matching and indicated high similarity in both time and frequency  
 250 domain.

251 **Remarks**

252 Template matching is easy to use without user intervention apart from the initial selection of the template region.  
253 It does not have any special requirement for target patterns and has been validated to work well to track artificial  
254 planar targets with specific patterns [5, 6, 24], LED lamp targets [13] and feature targets on structural surfaces [8].  
255 Template matching is not robust to changes in shading, illumination [30, 63] and background conditions [64] in  
256 field, although sensitivity to lighting changes might be reduced using camera auto-exposure settings [30]. The  
257 method is also not appropriate for tracking slender structural components, since the rectangular subset image used  
258 as a template might include background pixels with inconsistent motion.

259

260 3.2.2 Feature point matching

261 **Principle**

262 Instead of analysing all the locations within the target, feature point matching applies to sparse ‘special’ points  
263 within the target region, independently detecting these special points in two images and then finding point  
264 correspondences based on their local appearance. ‘Special’ points in an image, termed ‘interest points’ or  
265 ‘keypoints’ in computer vision, are those which are stable, distinctive and invariant to image transformation and  
266 illumination changes, such as building corners, connection bolts, or other patches with interesting shapes [65].

267 The procedures are indicated in Fig. 9. A popular keypoint detector in step (1) is the Harris corner detector [66]  
268 which is widely used in structural monitoring applications [11, 15, 22, 24, 57]. Instead of using the pixel values  
269 directly for similarity comparison, keypoints are often extracted and described by a more complex representation  
270 (i.e. feature descriptor) according to the shape and appearance of a small window around the keypoint [65]. The  
271 common descriptors and their matching criteria are indicated in Table 6. Float point based descriptors (e.g. scale-  
272 invariant feature transform (SIFT) [67] and speeded up robust features (SURF) [68]) are represented by float  
273 vectors, commonly reflecting various local intensity gradients of a pattern around the keypoint. Binary string  
274 based descriptors (e.g. Binary robust independent elementary features (BRIEF) [69], Oriented FAST and Rotated  
275 BRIEF (ORB) [70] and Fast retina keypoint descriptor (FREAK) [71]) are represented by binary vectors (with  
276 elements of 0 and 1) through pairwise comparisons of image intensities (i.e. whether the former is greater or less  
277 than the latter) over a special pattern around the keypoint. The matching criterion between two binary descriptors  
278 is usually the Hamming distance [69] equal to the number of elements which differ between the two vectors.

279 To verify the matched keypoint correspondences in step (3), geometric alignment is often used based on whether  
280 the keypoints in the first image could fit with the keypoints in the second image after a specific geometric

281 transformation. The widely used approaches for discarding outliers are RANdom SAmple Consensus (RANSAC)  
282 [72] and least median of squares (LMS) [73]. The tracking output is the average motion of keypoints in an image  
283 that inherently has sub-pixel resolution and could be converted to the target location in the image.

#### 284 **Application review**

285 Song et al. [74] proposed a target tracking method based on circular Hough transform for marker detection and  
286 coherent point drift algorithm for marker matching and the method was applied for system identification of a steel  
287 cantilever beam in the laboratory. Field applications include Khuc and Catbas [22, 75] who applied the FREAK  
288 and SIFT methods for deformation measurement in a stadium structure and a railway bridge and Ehrhart and  
289 Lienhart [59, 64] who applied the ORB method for deformation measurement in a short-span footbridge.

#### 290 **Remarks**

291 Feature point matching is an efficient technique since it deals with sparse points instead of the whole region as in  
292 template matching. This technique uses local descriptors to represent keypoints instead of the raw image  
293 intensities and are less sensitive to illumination change, shape change and scale variation.

294 However, feature point matching requires the target region to have rich textures for distinctiveness during the  
295 whole recording period. Also several parameters need to be adjusted manually according to users' experience or  
296 judgement, e.g. contrast threshold for feature detector and distance threshold in matching criteria. These parameter  
297 adjustments might depend on environmental changes, e.g. the threshold for outlier removal might vary with the  
298 illumination condition [22].

299 Currently feature point matching technique has only been validated in several short-range measurement tests [22,  
300 59, 64, 75]. However, the feasibility for long-range monitoring in terms of stability over several hours and how  
301 to choose the best feature descriptors are open questions.

### 302 3.2.3 Optical flow estimation

#### 303 **Principle**

304 Instead of finding matching locations of a complete region or sparse keypoints, optical flow estimation detects  
305 motions or flows of all pixels within the target region. Optical flow is the apparent velocity of movement in an  
306 image resulting from brightness pattern shift [76]. The calculation imposes two constraints, one temporal  
307 constraint on image properties (e.g. image intensity constancy for the same pattern over time) and one spatial  
308 constraint that models the flow properties in an image (e.g. coherent motion in adjacent pixels) [77]. A function  
309 reflecting these two constraints is then defined and optimised to derive a dense estimation of velocity flow for  
310 each pixel. In structural monitoring applications, the output could be converted to image motion instead of velocity

311 by replacing the temporal gradient of image properties in the function with the variation of image properties  
 312 between two discrete frames. Outlier removal is used to retain only sensible image motions, and average image  
 313 motion of the inlier pixels is converted to target location inherently having sub-pixel resolution.

314 Optical flow estimation is an established method with several variant techniques, such as ‘differential’,  
 315 ‘spatiotemporal energy’ and ‘phase-based’. In this section only two methods, the differential technique of Lucas  
 316 and Kanade (LK) [78] and the phase-based technique [79] are discussed.

317 LK optical flow estimation [78] is based on brightness constancy assumption, i.e. projection of the same point has  
 318 the same image intensity in every frame. Since corner points or keypoints are good features mathematically for  
 319 the computation of optical flows, LK method is usually applied for sparse estimation instead of computation at  
 320 every pixel. With keypoints detected in the reference frame usually using the Shi-Tomasi corner detector [80],  
 321 LK algorithm is applied to compute the image motion of each keypoint in the new frame from spatial-temporal  
 322 image brightness variations,

$$323 \quad \begin{bmatrix} \sum_i I_{xi}^2 & \sum_i I_{xi}I_{yi} \\ \sum_i I_{xi}I_{yi} & \sum_i I_{yi}^2 \end{bmatrix} \begin{bmatrix} dx \\ dy \end{bmatrix} = \begin{bmatrix} -\sum_i I_{xi}I_{ti} \\ -\sum_i I_{yi}I_{ti} \end{bmatrix} \quad (7)$$

324 where  $dx$  and  $dy$  denote the optical flows in the horizontal and vertical directions of the image plane;  $I_x$ ,  $I_y$   
 325 and  $I_t$  represent the spatial and temporal gradients of image intensities; and  $i$  denotes the  $i$ th pixel location in a  
 326 square patch (e.g.  $3 \times 3$ ) around a feature point  $(x, y)$ . The image motion is then estimated after discarding false  
 327 motion estimates according to RANSAC or LMS, as with feature point matching.

328 Phase-based optical flow estimation is based on local phase constancy assumption. The method first proposed by  
 329 Fleet and Jepson in 1990 [79], is receiving new attention together with the motion magnification technique [81]  
 330 which visualises motions in image sequences that are not visible to the naked eye. The mathematical details of  
 331 phase-based optical flow estimation are explained in [23] and the algorithm is briefly summarised here.

332 The Fourier shift theorem indicates that a delay of a signal in the time domain corresponds to a linear phase  
 333 variation in the frequency domain. Similarly, the image motion in spatial domain is also reflected in phase changes  
 334 in spatial frequency domain. The phase here is the local phase [82] corresponding to a specific spatial location  
 335 instead of the whole image, usually derived by employing a quadrature pair of filters consisting of an even real  
 336 part and an odd imaginary part [83] i.e. Gabor filters [84] and Gaussian derivative filters [23] (demonstrated in  
 337 Fig. 10). The image motion at each pixel is then estimated from the spatial-temporal variations of the local phase  
 338 for the filtered image.

339 **Application review**

340 LK optical flow estimation was applied in a laboratory test of a multi-storey metal tower [15] for system  
341 identification, and for field application in deformation measurement in a footbridge [59] and bridge stay-cable  
342 vibration measurement [85, 86].

343 Implementations of phase-based optical flow estimation were mostly focused on system identification, i.e.  
344 extracting modal frequencies and mode shapes in laboratory tests [23, 87] and identifying modal frequencies of  
345 high-rise tower buildings [88].

346 **Remarks**

347 Optical flow estimation enables tracking of features on a structural surface without the requirement for artificial  
348 targets. It provides fast and accurate results in controlled environmental conditions.

349 Like feature point matching, optical flow estimation prefers target patterns with distinct and robust features over  
350 the whole test period. Edges are not suitable for tracking due to the ‘aperture problem’ i.e. only the motion  
351 component perpendicular to the local edge direction could be detected instead of the true motion of the edge. If  
352 the structural motion along edges is one dimensional translation with known direction e.g. bridge stay cable  
353 vibration [85], optical flow estimation is viable.

354 Phase-based optical flow estimation is mostly applied for system identification in the laboratory but is harder to  
355 use in field conditions due to high signal noise [88]. Measurement of image motion is sensitive to the choice of  
356 pixel location [89], while a selection strategy to ensure satisfactory measurement has not yet been clearly reported.  
357 Changes of lighting and background conditions might lead to apparent measurement error [88].

358 3.2.4 Shape-based tracking

359 Other than general techniques, there are also some target tracking methods that depend on the special shapes of  
360 target patterns which could appear in custom-made artificial targets or structural components (e.g. line-like cables).  
361 Table 7 provides a summary of target patterns commonly used. With lack of generality, these methods have  
362 limitations for application.

363 3.2.5 Summary of target tracking performance

364 In terms of target tracking, the nominal algorithm resolution can be better than 0.01 pixel while the reported  
365 accuracy in practice varies from 0.5 to 0.01 pixel [95]. The real-time processing was realised in [8] [49] [63] using  
366 the template matching method, in [16] [86] using the optical flow estimation method and in [13] [51] [52] [53]  
367 using the shape-based tracking approaches. Although not reported in the existing applications, the feature point  
368 matching approach is capable of being used for real-time application [70]. Among the four tracking methods,

369 template matching requires the least user intervention apart from the initial selection of template region while in  
370 the other three methods, some threshold values that might be environmentally dependent are required as user  
371 inputs.

372 Ehrhart and Lienhart [64] evaluated the performance of three techniques (optical flow, template matching and  
373 feature point matching) by tracking structural features of a footbridge and reported that feature point matching is  
374 robust to the changes of background condition (i.e. snowfall) whereas drift over time was observed in the  
375 measurement by the two other methods. Busca et al. [96] evaluated three techniques (template matching, edge  
376 detection and digital image correlation) on a steel truss railway bridge, concluding that the three techniques  
377 provide similar tracking performance while tracking accuracy is slightly poorer for natural targets. Khaloo and  
378 Lattanzi [97] investigated four optical flow estimation methods for dense displacement measurement. The study  
379 indicated that classic+NL method (i.e. introducing a weighted non-local term into the classical optical flow  
380 formulations [77]) provided the most consistent and accurate measurement. However, the coarse-to-fine schemes  
381 (i.e. building image pyramids for each frame and computing optical flows on each layer of pyramids to get rid of  
382 the small motion constraint) are necessary for Lucas–Kanade and Horn–Schunck methods to deal with large  
383 displacement.

### 384 3.3 *Structural displacement calculation*

385 Structural displacement could be easily derived from the change of structural coordinates given the image location  
386 of a target (output of target tracking) and the projection transformation relationship (output of camera calibration).  
387 In this case, the projection transformation is a fixed value or matrix without any update during the test.

388 Another less common method to derive structural displacement is based on the variation of real-time camera  
389 extrinsic matrix. The camera extrinsic matrix represents the camera pose i.e. position and orientation relative to  
390 the structural system. Since the camera is physically fixed during the recording, variation of camera extrinsic  
391 matrix is related to the change of target pose (position and orientation) and could be used to estimate the target  
392 motions in six degrees of freedom (6DOF).

#### 393 3.3.1 Offline projection transformation

##### 394 **Principle**

395 For single camera applications using scale factor or planar homography, the 2D structural coordinate/displacement  
396 is derived uniquely through transforming the target location/motion in an image to that in the structure via a  
397 projection transformation value or matrix.

398 When two or more cameras with overlapped views are used to monitor the same target, 3D structural displacement  
399 can be extracted based on triangulation method [46].

#### 400 **Application review**

401 Applications of scale factor and planar homography for 2D structural displacement measurement have been  
402 reviewed in Section 3.1.

403 For stereoscopic view or multiple cameras, the triangulation method was used in [24], [33], [98] for 3D structural  
404 displacement measurement. A multi-camera arrangement provides more reliable results than a single view but the  
405 measurement quality has high dependency on the time-synchronisation of camera recordings.

#### 406 3.3.2 Online pose estimation

##### 407 **Principle**

408 For single camera applications, using a fixed projection transformation relationship only supports recovery of 2D  
409 structural displacement. Some researchers tried to extract more information about target motion (up to 6DOF)  
410 using a single camera by updating the real-time target pose in the structural system.

411 Estimation of camera extrinsic matrix is performed for every frame and the 3D translational and rotational target  
412 motions are extracted from the changes of camera extrinsic matrix compared to the initial frame. The calibration  
413 process requires at least four non-collinear points with known dimensions or spacing in structure that should have  
414 consistent motion.

##### 415 **Application review**

416 Greenbaum et al. [99] applied the online pose estimation method for the laboratory 3D motion measurement of  
417 an oscillating rigid object with a few targets of known positions distributed on its surface. In field applications,  
418 Chang and Xiao [11] used a planar target with square grid patterns attached to a bridge surface for the  
419 measurement of 6DOF structural displacement while Martins et al. [14] tracked four non-coplanar LED targets  
420 together to reconstruct the 3D structural motion in a long span bridge.

##### 421 **Remarks**

422 The greatest advantage of the method is the capacity to extract 6DOF structural motions from single camera, but  
423 it has a high requirement on the nature of tracked targets which should consist of at least four non-collinear points  
424 with precisely known geometry. The target or a set of target points should have rigid motions and be visible during  
425 the whole recording period e.g. artificial planar targets with salient corner points [11], distributed target points on  
426 structural surface [99] or a set of LED targets [14].

427 This technique cannot measure translation along the camera optical axis [11], thus the camera should be  
428 configured to avoid facing any motion direction of interest.

429 The measurement accuracy of this method might be poorer than offline projection transformation method. In a  
430 footbridge monitoring test by Chang and Xiao [11], using a 36.4 mm focal length camera placed about 5.2 m from  
431 mid-span generated measurement noise with standard deviations of 0.76 mm and 1.09 mm in two horizontal  
432 directions. This was much larger than would be achieved by offline projection transformation method in a similar  
433 test [100] (tracking 0.2 mm bridge vertical displacement with the 85 mm focal length and 27 m camera-to-target  
434 distance). Therefore this method is not recommended for field applications unless the target size is not negligible  
435 compared to the camera-to-target distance [96].

#### 436 4 FIELD APPLICATIONS AND CHALLENGES

437 This section summarises the existing field applications of vision-based systems in two active fields, bridge  
438 deformation measurement and cable vibration measurement. A discussion about measurement challenges in field  
439 applications is also presented.

##### 440 4.1 Application examples

441 Video acquisition devices are now expanded to include smartphone cameras, with numerous  
442 applications including vibration measurement of a laboratory multi-floor tower structure [15] and cable  
443 vibration measurement of a cable-stayed footbridge [21]. In these two applications, smartphones are  
444 only used as the data acquisition system with the recorded video files post-processing for data  
445 extraction. Smartphone applications for real-time video acquisition and processing are also viable [101]  
446 through experimental validations.

447 The existing applications of vision-based systems in field tests involve the deformation measurement  
448 of a wide range of structural types including: high-rise buildings [7, 88], bridges [5, 6, 8, 10–14, 18, 20,  
449 22, 30, 44, 45, 49, 51–55, 59, 63, 64, 75, 98, 102–104] and stadium structures [22, 105]. Work in the  
450 two most active fields, i.e. bridge deformation measurement and cable vibration measurement are  
451 summarised in Table 8 and Table 9, respectively.

452 The viability of vision-based systems for bridge displacement measurement has been verified through comparison  
453 with traditional displacement sensors, e.g. LVDT [10, 55, 103], laser sensors [55] and potentiometers [44] for  
454 short-span bridge and GPS [13, 30, 49] for long-span bridges. The displacement data could be interpreted for



455 system identification [8, 11, 12, 49, 54, 55, 63, 75], evaluation of load carrying capacity [53], model calibration  
456 [18] and estimation of vehicle weights [20]. Artificial targets are commonly used in existing applications to assist  
457 camera calibration, whereas recent investigations [51, 63, 75, 103, 104] overcome the dependence on artificial  
458 targets and realise completely non-contact sensing based on a simplified projection transformation i.e. scale factor.  
459 Another promising application of vision-based systems is to estimate cable tension forces based on vibration  
460 measurement. Measurement accuracy was verified through comparison work with traditional sensors e.g.  
461 accelerometers [40, 85, 106], velocimeters [41] and load cells [105]. Vision-based systems require no access to  
462 cables [16, 30, 40, 85, 86, 90, 105, 106] and are capable of measuring the vibrations of multiple cables using a  
463 single camera [16, 86, 105, 106] that is comparable to an array of accelerometers.

#### 464 4.2 *Measurement accuracy and challenges*

465 Measurement accuracy of vision-based systems depends on several parameters, e.g. camera-to-target distance,  
466 target pattern features, lighting conditions, camera mounting stability and video processing methods. Khuc et al.  
467 [22] investigated the measurement accuracy of a vision-based system in a laboratory and suggested an accuracy  
468 of 0.04 mm in a short-range distance (< 14 m). Martins et al. [14] demonstrated the uncertainty evaluation of  
469 displacement measurement by a vision-based system on a long-span bridge monitoring test and illustrated a  
470 standard measurement accuracy of 1.7 mm in the vertical direction. The high noise range might limit the field  
471 application of vision-based systems for system identification on civil structures although high frame rate is taken  
472 for vision-based systems.

473 The achievable accuracy in field tests might be much poorer than that of controlled conditions. The authors  
474 investigated the field challenges through a series of monitoring tests in two short-span and two long-span bridges  
475 which have been reported in [30]. A summary of the main findings from the tests and the literature is presented  
476 here.

- 477 • Camera and support motion induced by wind [10] might lead to apparent measurement error. Except for  
478 improving camera mounting configurations [30], a common correction method is to additionally track the  
479 ‘nominal’ motion of a fixed target e.g. bridge towers or adjacent buildings. Recent work [97] indicates another  
480 promising approach for camera motion compensation through removing the averaged motion of background  
481 pixels based on dense optical flow estimation.
- 482 • Variation in lighting and background conditions is one of the critical challenges during field tests. The  
483 influence of lighting variations might be reduced by enabling camera auto-exposure settings [30].

484 Correlation-based template matching is not robust to this effect apart from testing during overcast weather,  
485 whilst the feature point matching method was reported to be less sensitive [64].

486 • Atmospheric refraction and turbulence of optical light propagating through the air are common error sources  
487 for any optical-based instrument, especially for long-range measurements. Refraction deviation could be  
488 minimal for short-term displacement measurement while the air turbulence movement has a larger influence  
489 [52]. Quantification of the induced error based on mathematical models is demonstrated in a vision-based  
490 measurement test of a long-span bridge [107].

491 • Observations from short-term tests (with duration less than twelve hours) do not find an apparent influence  
492 of temperature variations on measurement accuracy, while this effect is necessary to consider for long-term  
493 tests e.g. with duration a few months or more. A time-frequency approach indicates the potential for error  
494 compensation based on investigation of the correlation models linking measurement errors and temperatures  
495 [108].

## 496 5 SUMMARY AND PROSPECTS

497 As evidenced from the review, vision-based systems are promising tools for structural displacement measurement  
498 having advantages in cost, installation efforts and measurement capacities of frequency range and spatial  
499 resolution. Although the potential in field applications has been validated in many articles, there are a few aspects  
500 still to mature.

501 • Robust target tracking methods. Template matching and optical flow estimation are established methods  
502 widely used in short-range and long-range measurement tests, but they are not robust to lighting and  
503 background changes. Feature point matching is a relatively new and promising tracking method, but  
504 investigations regarding several aspects e.g. selection strategy of proper threshold parameters, sensitivity on  
505 environmental effects and field viability for long-range measurement are rare, and need to be expanded. It is  
506 still an open question about the most robust tracking method for vision-based systems to deal with changes  
507 in lighting conditions during field tests.

508 • Completely non-contact measurement. Artificial targets are commonly included to assist the camera  
509 calibration process, but dependence on artificial targets is eliminated in a few field applications [15, 22, 75,  
510 104]. These studies were based on a simplified projection transformation i.e. scale factor that is not a general  
511 approach and imposes constraints on camera positioning. To develop a non-contact vision-based system for

512 the general case, requiring control points with known locations is the main obstacle which could possibly be  
513 resolved via the assistance of surveying instruments, such as total station.

- 514 • Distributed sensing of structural displacement. Vision-based systems have the capacity for simultaneous  
515 multi-point displacement measurement that is comparable or superior to an array of accelerometers for system  
516 identification. Currently, bridge applications primarily focus on the mid-span displacement measurement,  
517 while the potential of distributed sensing and system identification is not well investigated.
- 518 • Measurement uncertainty evaluation. Measurement accuracy and uncertainty are of great importance for a  
519 mature measurement system. Quantified descriptions about measurement accuracy haven been made in some  
520 references (e.g. [8, 22, 54, 64]) through comparisons with reference measurements. However, the quality of  
521 vision-based measurements could be time-varying, environmentally dependent and differ significantly with  
522 various test configurations. The influential factors include the test configurations (e.g. the camera-to-target  
523 distance and the target features), the video processing methods used and the environmental conditions (e.g.  
524 the lighting conditions, the atmospheric refraction and turbulence). A systematic evaluation of vision-based  
525 measurement methodologies will require extensive experimental effort by the research community with  
526 publication of case studies contributing to evolving guidance for field applications.

527 LIST OF ABBREVIATIONS

528 The following table describes the abbreviations and acronyms used throughout this article.

<b>Abbreviation</b>	<b>Meaning</b>
<b>BRIEF</b>	Binary robust independent elementary features
<b>DIC</b>	digital image correlation
<b>DOF</b>	degree of freedom
<b>FREAK</b>	Fast retina keypoint descriptor
<b>LK</b>	Lucas and Kanade optical flow
<b>LMS</b>	least median of squares
<b>MCS</b>	motion capture systems
<b>ORB</b>	Oriented FAST and Rotated BRIEF
<b>RANSAC</b>	RANdom SAmples Consensus
<b>SF</b>	scale factor
<b>SIFT</b>	scale-invariant feature transform
<b>SURF</b>	speeded up robust features
<b>ZNCC</b>	zero-mean normalised cross correlation
<b>ZNSSD</b>	zero-mean normalised sum of squared differences

529

530 **Compliance with Ethical Standards:**

531 Conflict of Interest:

532 The authors declare that they have no conflict of interest.

533

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776 continuous monitoring of displacement. *Renew Energy*. doi: 10.1016/j.renene.2017.07.104

777

779 Table 1 Summary of vision-based systems

<b>Vision-based systems</b>	<b>Main study objects</b>	<b>Measurement information</b>	<b>Features</b>
<b>Digital image correlation (DIC)</b>	Small-scale experimental members under large distortional deformation	Full-field displacements or strains on member surface	<ul style="list-style-type: none"> <li>• Laboratory application in controlled environment;</li> <li>• Fixed camera locations;</li> <li>• Dense measurement with high resolution;</li> <li>• Usually large deformation with shape distortion.</li> </ul>
<b>Motion capture systems (MCS)</b>	Objects or human bodies with a high degree-of-freedom skeleton structure	3D locations of each joints in structure	<ul style="list-style-type: none"> <li>• Laboratory application in controlled environment;</li> <li>• Fixed camera locations;</li> <li>• At least two cameras with overlapped views;</li> <li>• Markers and calibration object for calibration assistance.</li> </ul>
<b>Photogrammetry</b>	Initially aerial and terrestrial applications; now bridges under live loads	3D geometry of objects and deflection measurement	<ul style="list-style-type: none"> <li>• Field applications on structures mainly in stationary status;</li> <li>• Movable locations of camera;</li> <li>• Distributed control points for calibration assistance.</li> </ul>
<b>System for structural monitoring</b>	Structures with small deformation compared with structure scale.	2D or 3D displacement with proper sample rate.	<ul style="list-style-type: none"> <li>• Field applications and easy installation preferred;</li> <li>• High accuracy and also high calculation efficiency (for real-time dynamic measurement);</li> <li>• Small deformation compared with structure scale and camera-to-structure distance.</li> </ul>

781 Table 2 Projection transformation from structure to image plane

<b>Projection transformation</b>		<b>Assumptions</b>	<b>Recovered localisation information of target</b>
<b>(1)</b>	Full projection matrix	--	3D structural coordinates
<b>(2)</b>	Planar homography	The motion along one axis in structural coordinate system is negligible	2D structural coordinates
<b>(3)</b>	Scale factor	The camera optical axis is perpendicular to one plane in the structural coordinate system (e.g. the target plane XY).	2D motions within the target plane

782

783 Table 3 Summary of two field applications in literature using the full projection matrix as projection  
 784 transformation

<b>References</b>	<b>[11]</b>	<b>[14, 45]</b>
Focal length	36.4 mm	600 mm (composed by a 300 mm telephoto lens and a 2x tele-converter)
Camera-to-target distance	5.2 m	500 m
Artificial targets installed	A planar 3x3 chessboard	A 3D target set combined by distributed four LED targets with the whole dimensions of 250 mm, 350 mm and 250 mm along the three axes
Observed maximum displacement	6 mm	1.82 m
Measurement evaluation	Not commented about vertical measurement; Measurement noise along the two other directions with the standard deviations at 0.76 mm and 1.09 mm, respectively.	Uncertainty at 15 mm to 20 mm in the vertical and transverse directions.

785



786 Table 4 Features of two calibration methods for scale factor

<b>Scale factor</b>	<b>By camera-to-target distance</b>	<b>By dimension correspondences</b>
Target dependence	Target free	Artificial targets always required
Camera positioning constraint	Very sensitive to the tilt of camera optical axis	Less sensitive to the tilt of camera optical axis
Applications	Mostly used in the short-range measurement; The long-range measurement feasible for the vision-based systems assisted the total station.	Widely used in both the short-range and the long-range measurement

787

788 Table 5 Categories of target tracking methods

<b>Tracking methods</b>		<b>Regions or points tracked for matching</b>
(1)	Template matching	Rectangular subset of the frame as the target region
(2)	Feature point matching	Sparse ‘special’ points with salient features within the target region
(3)	Optical flow estimation	Every pixel location within the target region
(4)	Shape-based tracking	Line-type, circular-shaped or custom-made targets

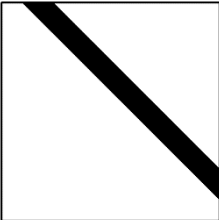
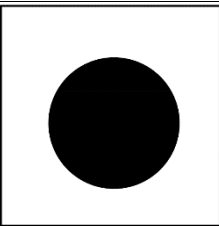
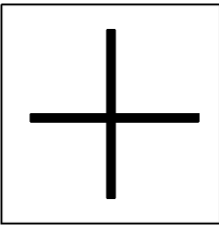
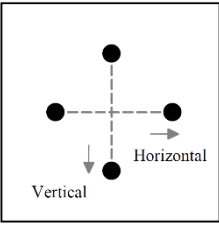
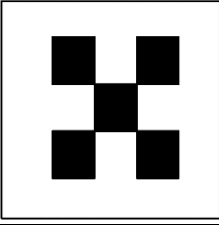
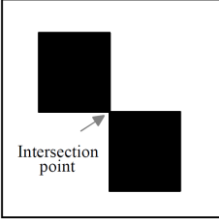
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790 Table 6 Categories of feature descriptors and corresponding matching criteria

<b>Descriptor categories</b>	<b>Descriptor names</b>	<b>Matching criteria</b>
<b>Float point based</b>	Scale-invariant feature transform (SIFT) [67] Speeded up robust features (SURF) [68]	Euclidean distances in feature space [65]
<b>Binary string based</b>	Binary robust independent elementary features (BRIEF) [69] Oriented FAST and Rotated BRIEF (ORB) [70] Fast retina keypoint descriptor (FREAK) [71]	Hamming distance [69]

791

792 Table 7 Examples of shape-based tracking

Ref.	Target patterns	Determination of target location
[30, 90]		<p>Detecting the edges of line-shaped patterns and building image point correspondences among image sequences [90] or computing the cable motion from the distance between two identified edges [30]</p>
[12, 41][91][92]		<p>Detecting the edges of circular-shaped patterns through brightness thresholding or edge detection and computing the centroid coordinates for the circle</p>
[52]		<p>Detecting the edges of cross-shaped patterns through image gradient and computing the arithmetic mean of edge coordinates as the target location</p>
[53–55][93][94]		<p>Detecting four spots through brightness thresholding and computing the motions along the specified horizontal and vertical directions</p>
[11]		<p>Detecting grid dots by Harris corner detector and applying the image coordinates of grid dots for the estimation of camera extrinsic matrix</p>
[10]		<p>Detecting the edges of squares through brightness thresholding and computing the coordinates of the intersection point</p>

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794 Table 8 Review of studies about bridge displacement measurement using vision-based systems

Ref.	Application structures	Camera calibration	Target tracking method	Target type	Measured displacement	Data interpretation
[5, 6]	Humber Bridge & Second Severn Crossing, UK	Scale factor	Correlation-based template matching	Planar target	2D displacement at mid-span	
[52]	A highway bridge & a railway viaduct	Scale factor	Shape-based tracking	Planar target	Vertical displacement at mid-span	
[12]	Vincent Thomas Bridge, USA	Scale factor	Shape-based tracking	LED targets	Vertical displacement at mid-span	<ul style="list-style-type: none"> <li>• Extracting modal frequencies</li> </ul>
[53–55]	Highway bridges	Scale factor	Shape-based tracking	Planar target	2D displacement at mid-span	<ul style="list-style-type: none"> <li>• Estimating load carrying capacity for load test</li> <li>• Evaluating measurement by comparison with the reference sensors (LVDT &amp; Laser)</li> </ul>
[44]	A roadway bridge	Full projection matrix	Shape-based tracking	Planar target	2D displacement at mid-span	<ul style="list-style-type: none"> <li>• Evaluating measurement by comparison with the reference sensor (potentiometer)</li> </ul>
[11]	A cable-stayed footbridge	Online pose estimation	Shape-based tracking	Planar target	3D displacement at mid-span	<ul style="list-style-type: none"> <li>• Extracting modal frequencies</li> </ul>
[13]	Tsing Ma Bridge, Hong Kong	Scale factor	Correlation-based template matching	LED targets	Vertical displacement at mid-span	<ul style="list-style-type: none"> <li>• Evaluating measurement by comparison with the reference sensor (GPS)</li> </ul>
[63]	A railway viaduct	Scale factor	Lucas-Kanade template matching	Natural features	Vertical displacement of sound barrier	<ul style="list-style-type: none"> <li>• Extracting modal frequencies</li> </ul>
[10]	A railway bridge	Scale factor	Shape-based tracking	Planar target	Vertical displacement at mid-span	<ul style="list-style-type: none"> <li>• Evaluating measurement by comparison with reference sensor (LVDT)</li> </ul>
[8, 18, 103, 104]	A footbridge, a highway bridge & a railway bridge	Scale factor	Correlation-based template matching	Both planar target and natural features	Vertical displacement at mid-span	<ul style="list-style-type: none"> <li>• Extracting modal frequencies</li> <li>• FE model calibration</li> </ul>
[14, 45]	P25A bridge, Portugal	Online pose estimation	Shape-based tracking	LED targets	3D displacement at mid-span	<ul style="list-style-type: none"> <li>• Evaluating measurement uncertainty</li> </ul>
[51, 59, 64]	A footbridge	Scale factor	Correlation-based template matching	Both planar target and natural features	Vertical displacement at mid-span	<ul style="list-style-type: none"> <li>• Extracting modal frequencies</li> </ul>

<b>Ref.</b>	<b>Application structures</b>	<b>Camera calibration</b>	<b>Target tracking method</b>	<b>Target type</b>	<b>Measured displacement</b>	<b>Data interpretation</b>
			Feature point matching Optical flow estimation			<ul style="list-style-type: none"> <li>Evaluating measurement accuracy and stability of three tracking methods</li> </ul>
[30, 49]	Humber Bridge, UK	Planar homography	Correlation-based template matching	Planar target	2D displacement at mid-span	<ul style="list-style-type: none"> <li>Extracting modal frequencies</li> <li>Evaluating measurement by comparison with the reference sensor (GPS)</li> </ul>
[20]	A roadway bridge	Scale factor	Lukas–Kanade method	Natural features	Vertical displacement at mid-span	<ul style="list-style-type: none"> <li>Estimating vehicle weights</li> </ul>
[75]	A railway bridge	Scale factor	Feature point matching	Natural features	Vertical displacement at mid-span	<ul style="list-style-type: none"> <li>Extracting modal frequencies</li> </ul>

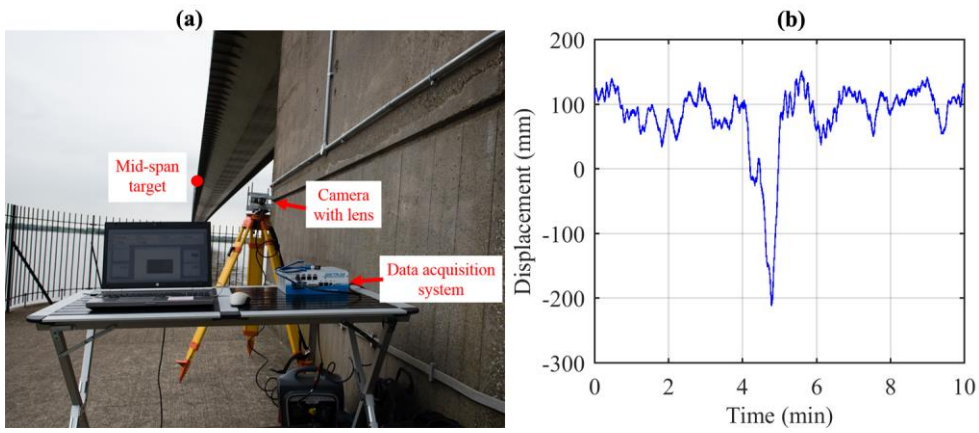
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796 Table 9 Review of studies about cable vibration measurement using vision-based systems

<b>Ref.</b>	<b>Application structures</b>	<b>Target tracking methods</b>	<b>Data interpretation</b>
[85]	A footbridge	Optical flow estimation	<ul style="list-style-type: none"> <li>• Extracting modal frequencies</li> </ul>
[90]	A footbridge	Shape-based tracking	<ul style="list-style-type: none"> <li>• Extracting modal frequencies</li> <li>• Identifying mode shapes.</li> </ul>
[86]	Guadiana Bridge, Portugal	Optical flow estimation	<ul style="list-style-type: none"> <li>• Extracting modal frequencies</li> </ul>
[40, 106]	Gwangan Bridge and a two-pylon cable-stayed bridge in Busan-Geoje Fixed Link, Korea	Correlation-based template matching	<ul style="list-style-type: none"> <li>• Extracting modal frequencies</li> <li>• Estimating cable tension</li> </ul>
[41]	Chi-Lu Bridge, Taiwan China	Shape-based tracking	<ul style="list-style-type: none"> <li>• Extracting modal frequencies</li> <li>• Identifying the mode shape ratio of cables</li> </ul>
[105]	Hard Rock Stadium, USA	Correlation-based template matching	<ul style="list-style-type: none"> <li>• Extracting modal frequencies</li> <li>• Estimating cable tension</li> </ul>
[30]	A footbridge	Shape-based tracking	<ul style="list-style-type: none"> <li>• Extracting modal frequencies</li> </ul>
[21]	A footbridge	Edge detection	<ul style="list-style-type: none"> <li>• Extracting modal frequencies</li> <li>• Estimating cable tension</li> </ul>

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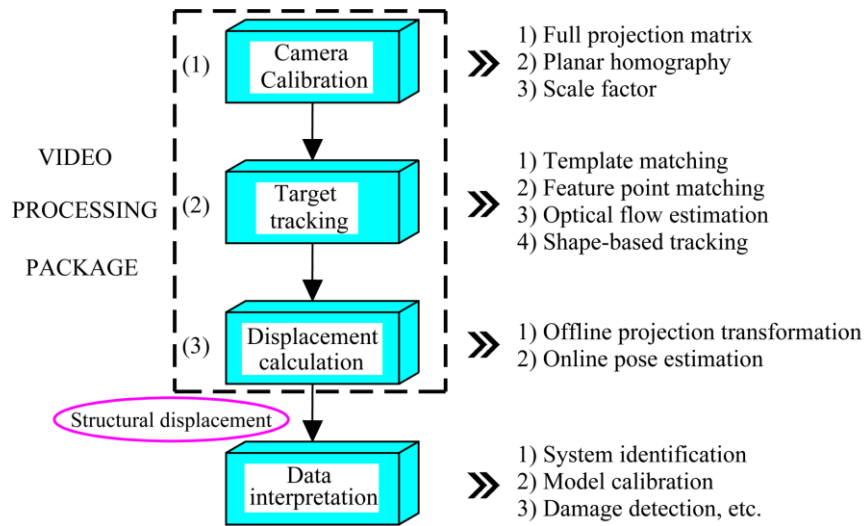
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800 Fig. 1 Vision-based system for structural displacement monitoring of the Humber Bridge [30]: (a) site  
801 configuration of the vision-based monitoring system; and (b) 10-min time history signal of vertical displacement  
802 at the bridge mid-span measured by the vision-based monitoring system.

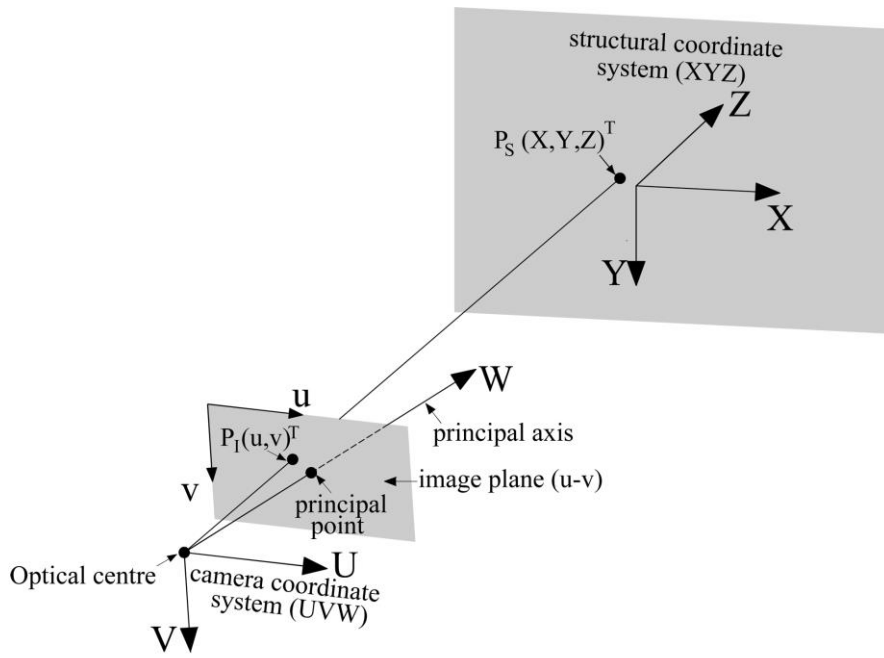


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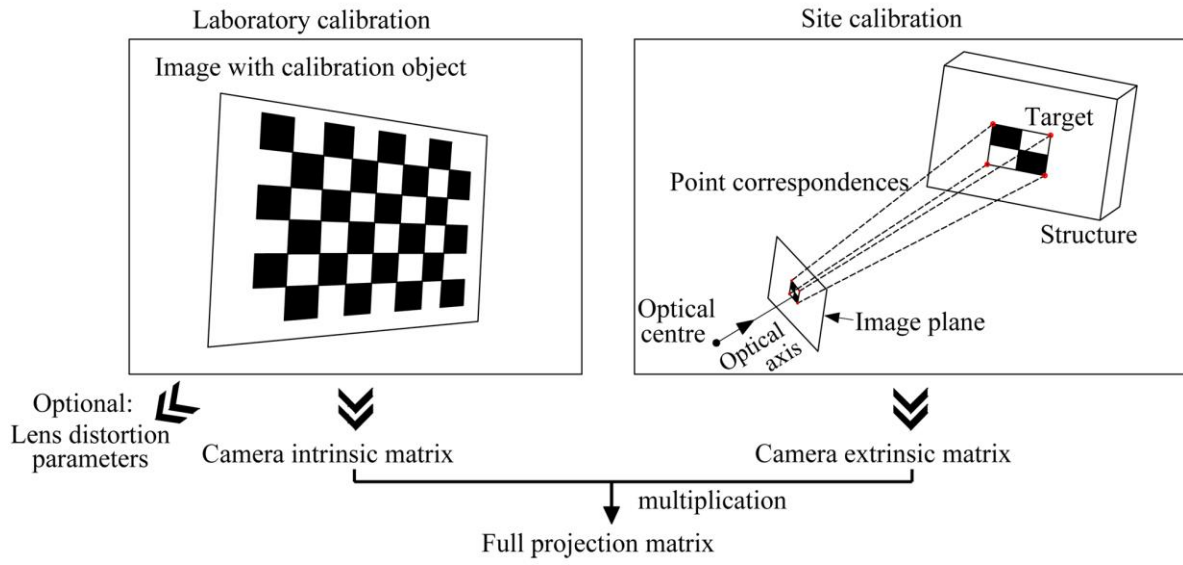
804 Fig. 2 Video processing procedures for structural displacement measurement and common methods in each step.

805

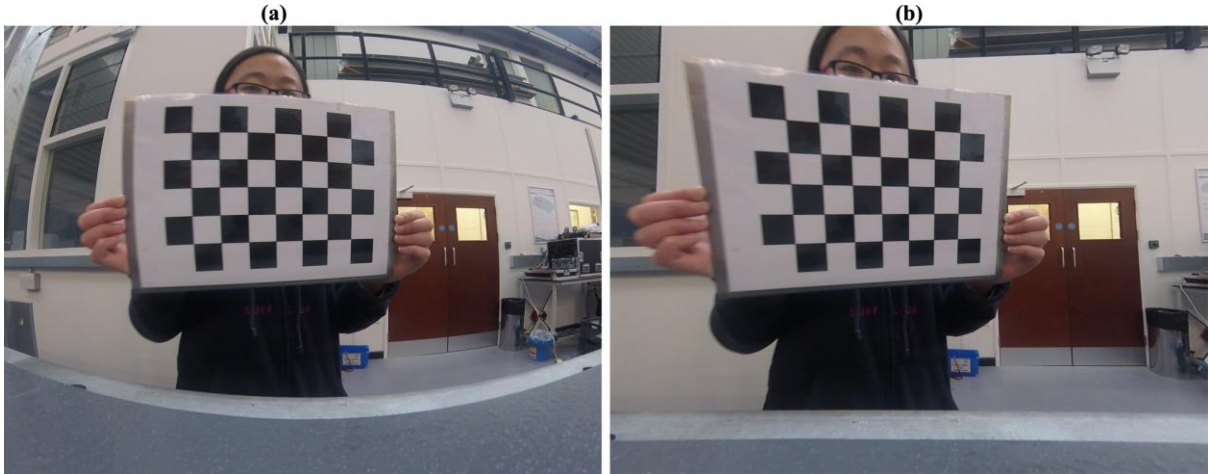


806 Fig. 3 Camera projection model: central perspective projection.

807



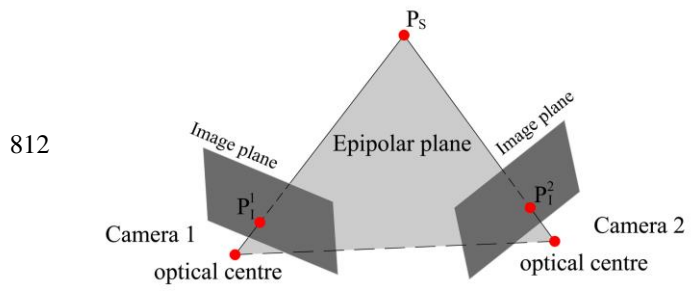
808 Fig. 4 Calibration steps for estimation of full projection matrix.



809

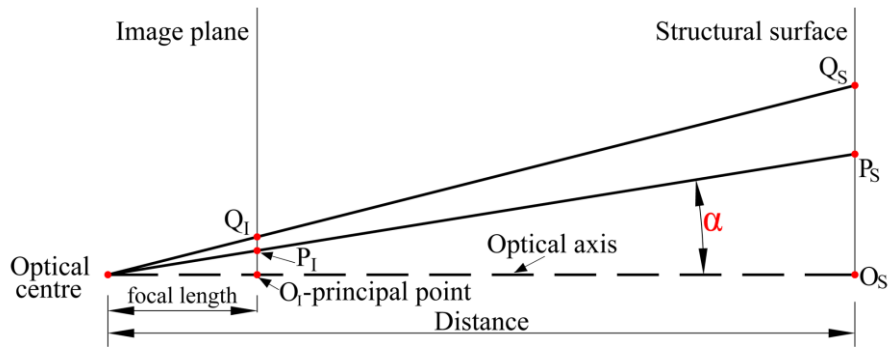
810 Fig. 5 Images of chessboard taken by GoPro Hero 4 Session camera: (a) raw image; and (b) image after distortion

811 correction.

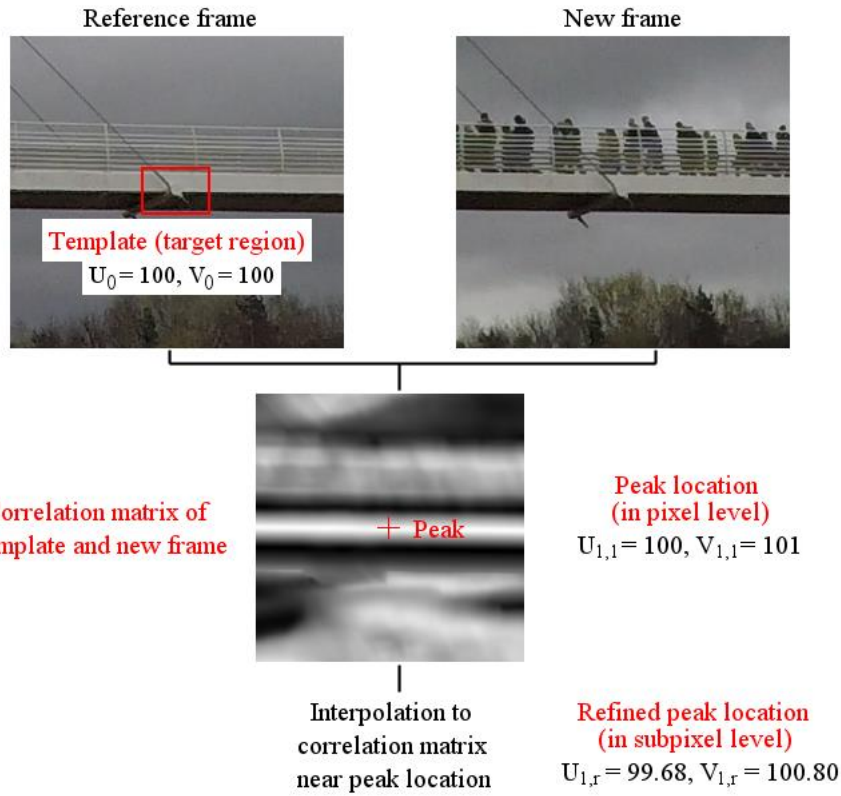


813 Fig. 6 Epipolar geometry principle of stereoscopic vision

814



815 Fig. 7 Camera projection model when the optical axis of camera is perpendicular to the structural surface.



816

817 Fig. 8 Procedures of template matching method for target tracking: The horizontal and vertical coordinates of the  
 818 target centre in the image plane are denoted as  $U$  and  $V$ , respectively; and the subscripts 0 and 1 represents the  
 819 image coordinates in the reference and new frames, respectively.

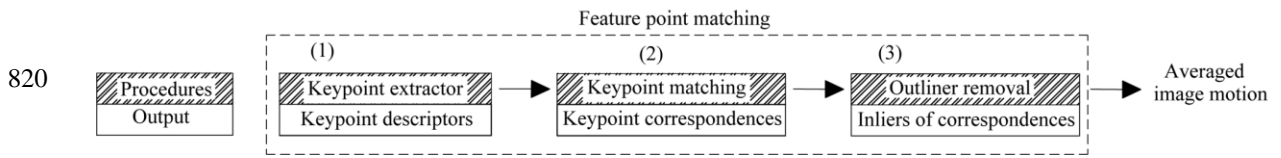
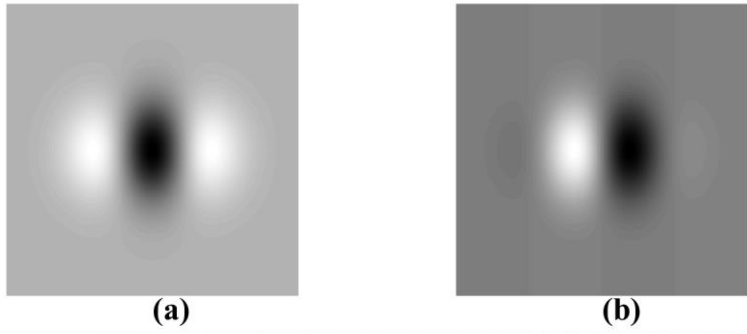
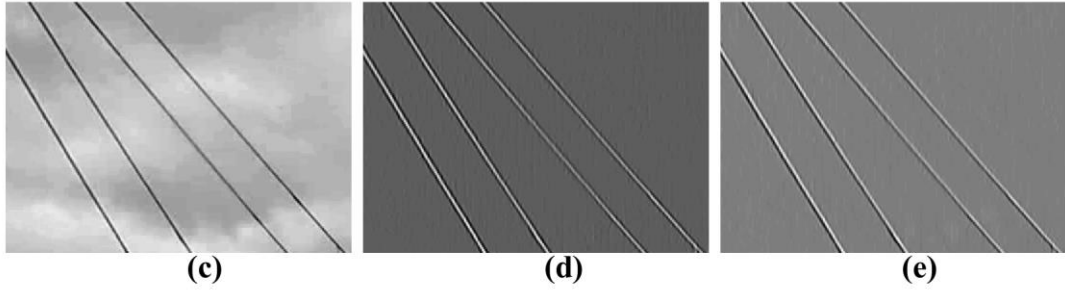


Fig. 9 Procedures of feature point matching for target tracking





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Fig. 10 Image after filtering by a quadrature pair of Gaussian derivative filters in the image width direction: (a) the real part of Gaussian derivative filters; (b) the imaginary part of Gaussian derivative filters; (c) the raw image of footbridge stay cables; (d) the real part of filtered image data; and (e) the imaginary part of filtered image data.