

1 **COPSE reloaded: An improved model of**

2 **biogeochemical cycling over Phanerozoic time**

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11 **Abstract**

12 The 'COPSE' (Carbon, Oxygen, Phosphorus, Sulphur and Evolution) biogeochemical model predicts
13 the coupled histories and controls on atmospheric O₂, CO₂ and ocean composition over Phanerozoic
14 time. The forwards modelling approach utilized in COPSE makes it a useful tool for testing
15 mechanistic hypotheses against geochemical data and it has been extended and altered a number of
16 times since being published in 2004. Here we undertake a wholesale revision of the model,
17 incorporating: (1) elaboration and updating of the external forcing factors; (2) improved
18 representation of existing processes, including plant effects on weathering and ocean anoxia; (3)
19 inclusion of additional processes and tracers, including seafloor weathering, volcanic rock
20 weathering and ⁸⁷Sr/⁸⁶Sr; (4) updating of the present-day baseline fluxes; and (5) a more efficient
21 and robust numerical scheme. A key aim is to explore how sensitive predictions of atmospheric CO₂,

22 O₂ and ocean composition are to model updates and ongoing uncertainties. The revised model
23 reasonably captures the long-term trends in Phanerozoic geochemical proxies for atmospheric pCO₂,
24 pO₂, ocean [SO₄], carbonate δ¹³C, sulphate δ³⁴S and carbonate ⁸⁷Sr/⁸⁶Sr. It predicts a two-phase
25 drawdown of atmospheric CO₂ with the rise of land plants and associated cooling phases in the Late
26 Ordovician and Devonian-early Carboniferous, followed by broad peaks of atmospheric CO₂ and
27 temperature in the Triassic and mid-Cretaceous – although some of the structure in the CO₂ proxy
28 record is missed. The model robustly predicts a mid-Paleozoic oxygenation event due to the earliest
29 land plants, with O₂ rising from ~5% to >17% of the atmosphere and oxygenating the ocean.
30 Thereafter, atmospheric O₂ is effectively regulated with remaining fluctuations being a
31 Carboniferous-Permian O₂ peak ~26% linked to burial of terrestrial organic matter in coal swamps, a
32 Triassic-Jurassic O₂ minimum ~21% linked to low uplift, a Cretaceous O₂ peak ~26% linked to high
33 degassing and weathering fluxes, and a Cenozoic O₂ decline.

34 **Keywords**

35 Phanerozoic; Biogeochemistry; Carbon; Oxygen; Climate; Modelling

36 **1. Introduction**

37 How the composition of the atmosphere and the global biogeochemical cycling of major elements
38 have changed over geologic time is a subject of broad inter-disciplinary interest. In particular
39 atmospheric CO₂ and O₂ are ‘master variables’ of the Earth system that have been affected by both
40 geological drivers and biological evolution (Lenton and Watson, 2011). Variations in atmospheric CO₂
41 are in turn a key contributor to long-term climate regulation (Walker et al., 1981), and variations in
42 atmospheric O₂ have been linked to the evolution of aerobic life forms (Sperling et al., 2015a). The
43 Phanerozoic is the best studied Eon with the most data. Yet despite numerous proxies to reconstruct
44 past atmospheric CO₂ levels there are still lingering disagreements among those proxies and
45 important gaps in the record especially before ~420 Ma (Royer, 2014). For past atmospheric O₂

46 levels there are only indirect constraints during parts of the Phanerozoic (Bergman et al., 2004). The
47 best established constraint on O₂ is a lower limit of 15-17% from combustion experiments combined
48 with the near continuous presence of fossil charcoal over the past ~420 Myr (Belcher and McElwain,
49 2008; Glasspool et al., 2004; Scott and Glaspool, 2006). A more uncertain upper limit on O₂ of 25-
50 35% has been inferred from the sensitivity of fire frequency to increasing O₂ and the continuous
51 presence of forests over the past ~370 Myr (Glasspool and Scott, 2010; Lenton and Watson, 2000b).

52 The limitations of the proxy record mean that models, combined with data, have a key role to play in
53 trying to reconstruct past variations in atmospheric CO₂ and O₂. However, model predictions should
54 not be confused with reality. In particular, inferences about the supposed effects of predicted
55 variations in atmospheric O₂ on animal evolution (Berner et al., 2007; Falkowski et al., 2005; Graham
56 et al., 1995; Graham et al., 2016) should be treated with caution, given that there are already several
57 quite different model predictions of Phanerozoic O₂ variations (Mills et al., 2016). Before making
58 such inferential leaps, the focus should be on which (if any) of the features in past O₂ (and CO₂)
59 reconstructions are robust to model and data uncertainty.

60 The aim of this paper is therefore to try to better understand, mechanistically and quantitatively, the
61 controls on atmospheric CO₂ and O₂ over Phanerozoic time, and to assess how sensitive predictions
62 of these variables are to factors we are scientifically uncertain about. To undertake such an exercise
63 we need to be clear about our scientific method and specifically the role we want a model to play in
64 gaining knowledge (our epistemology). Hence we start by briefly reviewing existing approaches to
65 modelling Phanerozoic biogeochemical cycling.

66 **1.1. Review of existing modelling approaches**

67 All models of biogeochemical cycling over Phanerozoic timescales typically have some
68 representation of sedimentary reservoirs (e.g. of carbon and sulphur in reduced and oxidised forms)
69 coupled to much smaller ocean-atmosphere reservoirs (e.g. of carbon, oxygen and sulphate).

70 However, there are two very different ways in which the models are used to try and gain knowledge;
71 the inverse (data-driven) and forwards modelling approaches (Fig. 1).

72 Most previous studies following Garrels and Lerman (1981; 1984), and including the GEOCARB family
73 of models (Berner, 1991, 1994, 2006a; Berner and Kothavala, 2001), have taken the inverse (data-
74 driven) modelling approach (Fig. 1a). Whilst some models are driven by rock abundance data (Berner
75 and Canfield, 1989), most are driven by isotopic data, notably the $\delta^{13}\text{C}$ and $\delta^{34}\text{S}$ records and a set of
76 associated assumptions about how they are related to key processes (burial of organic carbon and
77 pyrite sulphur, respectively). This leaves the only remaining data to test the model against as the
78 uncertain proxies for CO_2 (Royer, 2014), and the even sparser and more uncertain constraints on O_2 .
79 Furthermore it is unclear how strongly reconstructing CO_2 constrains past O_2 variations (or *vice*
80 *versa*). Such isotope-driven models are sensitive to the chosen $\delta^{13}\text{C}$ and $\delta^{34}\text{S}$ input data, particularly
81 in their predictions of atmospheric O_2 (Mills et al., 2016), yet these isotope records are imperfectly
82 known with considerable regional variations superimposed on an underlying global signal. Isotope-
83 driven model predictions, particularly of O_2 , are also sensitive to assumptions made about the
84 carbon and sulphur isotope mass balances, to the extent that they are unable to produce plausible
85 reconstructions of atmospheric O_2 without assuming sensitivity of C and S isotope fractionation to
86 O_2 , which provides stabilising negative feedback (Berner et al., 2000; Lasaga, 1989). Isotope-driven
87 models have also typically had to assume 'rapid recycling' of deposited sediments, whereby
88 sedimentary rock reservoirs are divided into 'young' (rapidly recycled) and 'old' components – with
89 the young sedimentary reservoirs assumed to be comparable in size to the ocean-atmosphere
90 reservoirs of C and S, and the old reservoirs typically assumed to be much larger and constant in size.
91 This introduces another form of negative feedback whereby changes in the burial of reduced or
92 oxidised carbon or sulphur are relatively rapidly counteracted by changes in the size and isotopic
93 composition of the young reservoirs (Berner, 1987).

94 In designing the original COPSE model a different, forwards modelling approach was taken (Fig. 1b).
95 A key target was to predict $\delta^{13}\text{C}$ and $\delta^{34}\text{S}$ records for comparison to data – as a means of testing the
96 model's external forcing assumptions and internal mechanistic assumptions (Bergman et al., 2004).
97 This means that COPSE explicitly simulates relevant biogeochemical fluxes such as organic carbon
98 and pyrite sulphur burial (as a function of other variables and forcing parameters) rather than simply
99 driving them with the isotope records. To this end nutrient (P, N) cycling is explicitly represented – a
100 major difference from the GEOCARB family of inverse models – and a range of feedbacks in the
101 coupled C, O, P, S and N cycles are considered. Notably, plausible predictions of atmospheric O_2
102 variation are achieved by assuming some negative feedback(s) within the surface Earth system
103 between O_2 and its sink and/or source fluxes, and several of these candidate feedbacks are mediated
104 by phosphorus cycling (Lenton and Watson, 2000b). The model does not assume rapid recycling of
105 recently deposited sediments (although this may be a geologically reasonable mechanism). Nor does
106 it assume constant sized ancient sedimentary reservoirs (which are hard to justify over Phanerozoic
107 timescales). Instead, for simplicity, single, variable sedimentary reservoirs are assumed for organic
108 carbon, carbonate carbon, pyrite, and gypsum.

109 A more elaborate forwards model is MAGic (Arvidson et al., 2006, 2011, 2013, 2014; Guidry et al.,
110 2007), which shares elements in common with both COPSE and GEOCARB and is particularly focused
111 on the inorganic side of the carbon cycle. MAGic tracks atmospheric CO_2 and O_2 and includes a much
112 more detailed approach to ocean composition and the rock cycle than either GEOCARB or COPSE,
113 with a total of 40 state variables. It tracks seven major ions of seawater (using a Pitzer approach to
114 computing activities), plus phosphate as a limiting nutrient, and marine organic matter. It
115 distinguishes a range of crystalline continental rocks (silicates), shelf/continental sediments and
116 sedimentary rocks, sediments buried in deep cratons, seafloor basalt components, pelagic (deep
117 ocean floor) sediments, and clays. MAGic includes feedback on atmospheric CO_2 from silicate
118 weathering and feedback on atmospheric O_2 from redox-dependent phosphorus burial/recycling
119 (Van Cappellen and Ingall, 1996). The model is driven by a range of geological forcing factors taken

120 from GEOCARB III (Bernier and Kothavala, 2001), BLAG (Bernier et al., 1983), and rock abundance data
121 (including coal). It is not driven by isotope records, nor are these used as a model prediction target.
122 Instead model predictions are compared to CO₂ proxies and to reconstructions of ocean
123 composition. A key difference from COPSE is that the burial flux of terrestrially-derived organic
124 carbon is assumed to be tiny (Arvidson et al., 2006). Hence there is no predicted secular change in
125 atmospheric oxygen levels with the rise of land plants, although greatly enhanced coal deposition in
126 the Carboniferous-Permian is sufficient to drive a predicted O₂ peak at that time (Arvidson et al.,
127 2013).

128 Whilst both forwards and inverse modelling approaches have merits, the scope for testing the
129 predictions of inverse modelling against data is limited by design – because much of the available
130 data has gone into the model as drivers. As so many factors concerning the drivers and feedbacks
131 controlling atmospheric CO₂ and O₂ are uncertain, and given that we only have uncertain proxies for
132 CO₂ and a lower bound on O₂ (neither of which extend to the early Paleozoic), we continue to pursue
133 the forwards modelling approach here – because it gives us several more opportunities to test our
134 understanding and hypotheses (as represented by the model) against independent data (proxy
135 records). One of the key aims here is to see to what degree those proxy records constrain the model
136 mechanisms.

137 Both of the existing modelling approaches have revealed some useful lessons as to how to model
138 the coupled histories of CO₂ and O₂. In particular, there are several good reasons to first understand
139 what controls atmospheric CO₂ and then try to understand what controls O₂. Firstly, ocean-
140 atmosphere carbon has a shorter residence time than oxygen (at least after the early Paleozoic) so
141 CO₂ can be treated as at steady state on a ~1 Myr timescale over which O₂ varies. Secondly, the
142 control exerted by the CO₂ cycle on the O₂ cycle appears to be stronger than *vice versa* (Bergman et
143 al., 2004). Thirdly, our understanding of controls on atmospheric CO₂ is more broadly agreed upon
144 than our understanding of controls on O₂ – notwithstanding some on-running discussion about the

145 cause(s) of Cenozoic CO₂ change (e.g. Caves et al., 2016; Li and Elderfield, 2013; Mills et al., 2014a;
146 Torres et al., 2014; Willenbring and von Blanckenburg, 2010).

147 Existing models suggest that long-term atmospheric CO₂ concentration is governed largely by
148 geologic and biologic forcing factors and by the functional dependencies of terrestrial silicate
149 weathering and seafloor weathering on CO₂ and/or temperature, which provide negative feedback.

150 Whilst organic carbon burial is an important sink of CO₂ and provides coupling to the O₂ cycle (where
151 it is the major source of O₂), in current models it only exerts second-order control on CO₂ (Bergman
152 et al., 2004; Berner, 2006a). However, variations in O₂ may significantly affect vegetation and thus
153 silicate weathering and CO₂ (Bergman et al., 2004).

154 Understanding what controls atmospheric O₂ (and at what resulting levels) remains an outstanding
155 puzzle, with a wider range of feedbacks proposed than for CO₂ (Kump, 1988; Lenton and Watson,
156 2000b; Van Cappellen and Ingall, 1996), together with biologic and geologic forcing. The coupling
157 from the CO₂ cycle to the O₂ cycle may be of first-order importance, with silicate and carbonate
158 weathering potentially providing a large fraction of the phosphorus supply that can ultimately
159 determine organic carbon burial, which is the dominant source of oxygen (Bergman et al., 2004;
160 Lenton et al., 2014). However, selective weathering of phosphorus by plants could act to decouple
161 silicate weathering and organic carbon burial (Lenton et al., 2012, 2016). Changes in the C/P ratio of
162 buried organic matter, especially a large increase in this ratio with the rise of land plants, also exert
163 first-order control on O₂ (Bergman et al., 2004; Berner, 1989; Kump, 1988; Lenton et al., 2016).
164 Furthermore, it has been argued that erosion rates exert a first-order control on organic carbon
165 burial (Berner, 2006a; Blair and Aller, 2012; Hedges and Keil, 1995), providing a further coupling
166 between the CO₂ and O₂ cycles insofar as physical weathering rates control chemical weathering
167 rates and thereby increases in erosion may decrease CO₂ and increase O₂.

168 1.2. Motivation and aims

169 In keeping with the original COPSE study (Bergman et al., 2004), our aim here is to produce a
170 quantitative model that incarnates various mechanistic hypotheses and makes resulting predictions
171 which can be tested against multiple, independent proxy data constraints.

172 We have several reasons to update the COPSE model. Firstly, some of the model assumptions have
173 been critiqued, suggesting alternative hypotheses to test, including the aforementioned argument
174 that organic carbon burial is controlled more by erosion fluxes than by phosphorus supply (Berner,
175 2006a). Secondly, although the original COPSE model sought to make the model forcing independent
176 of isotope inversion, the forcing of uplift was ultimately derived from inversion of the strontium
177 isotope record – an inconsistency which we have subsequently addressed for the Mesozoic and
178 Cenozoic by making $^{87}\text{Sr}/^{86}\text{Sr}$ a predicted variable (Mills et al., 2014a). This modification gives an
179 additional target to test the model against, especially given previously published difficulties in fitting
180 the complete Phanerozoic strontium isotope record (Francois and Walker, 1992). Thirdly, the field of
181 Phanerozoic modelling has advanced. Notably Bob Berner published a combined model of
182 Phanerozoic atmospheric O_2 and CO_2 , GEOCARBSULF (Berner, 2006a), which he subsequently
183 updated to distinguish weathering of volcanic rocks (Berner, 2006b), and revised carbon isotope
184 forcing data and fractionation (Berner, 2009). The importance of volcanic rock weathering in CO_2
185 consumption has been more widely recognised with the emplacement of large igneous provinces
186 (LIPs) linked to both short-term release and long-term drawdown of CO_2 (Schaller et al., 2011), and
187 phosphorus supply from volcanic rock weathering linked to organic carbon burial (Horton, 2015).
188 Partly in response to this we began to extend COPSE to include LIP emplacement and volcanic rock
189 weathering for the Mesozoic-Cenozoic (Mills et al., 2014a). New work on the biogeochemical effects
190 of early plants also motivated other updates to the Paleozoic predictions of COPSE (Lenton et al.,
191 2012, 2016). Finally, in the wider geochemical literature there have also been significant revisions to

192 estimates of key fluxes in the coupled C, O, P and S cycles, for example silicate weathering
193 (Hartmann et al., 2009; Moon et al., 2014).

194 In the following we undertake a thorough review, reconsideration and revision (where warranted),
195 of all aspects of the COPSE model, including bringing together developments of the model since the
196 original paper (Lenton, 2013; Lenton et al., 2012, 2016; Mills et al., 2014a). Our central aim is to
197 illustrate for the reader the effects of the many uncertain aspects of the coupled C, O, P, and S cycles
198 on long-term predictions of atmospheric CO₂, O₂, and ocean composition. In keeping with the
199 philosophy behind the model, we use it as a framework to test mechanistic hypotheses, by making
200 quantitative predictions of $\delta^{13}\text{C}$, $\delta^{34}\text{S}$, $^{87}\text{Sr}/^{86}\text{Sr}$, alongside CO₂ and O₂, which are tested against
201 available data. This evaluation of input assumptions and different mechanistic hypotheses ultimately
202 leads to an assessment of which predicted features of Phanerozoic variation in atmospheric CO₂, O₂
203 and ocean composition are robust to current uncertainties, and which critical uncertainties remain
204 that could be targeted by future work. The remainder of the paper is structured as follows: Section 2
205 describes a comprehensive series of updates to the COPSE model. Section 3 tests their effects by
206 comparing the resulting predictions against multiple proxy records, and arrives at a new baseline
207 model. Section 4 concludes.

208 **2. Model description**

209 A schematic of the revised COPSE model structure is shown in Figure 2. Panel A shows the mass
210 fluxes in the linked C-S-O cycles, which feature in both COPSE and GEOCARBSULF. Panel B shows the
211 feedback-based biosphere component, which is unique to COPSE and is used to calculate the burial
212 fluxes of organic carbon and pyrite sulphur in a forwards manner from other model processes (as
213 opposed to inferring these fluxes through isotope mass balance as in e.g. GEOCARBSULF). All terms
214 in Figure 2 are defined in Tables 1 and 2.

215 Our revision of the model spans changes to its internal structure, changes to its parameters, and
216 changes to the forcing factors driving it. We start by introducing the model reservoirs, i.e. state
217 variables, and the most fundamental structural changes, i.e. addition of new fluxes. Next we
218 describe changes to the model forcing factors. Then we work through the model processes and
219 corresponding equations, including some further structural changes at the level of changing
220 functional dependencies. Finally we consider changes to the baseline fluxes of the model.

221 **2.1. Reservoirs and new fluxes**

222 The revised COPSE model retains at its core the coupled C, O, P and S cycles, and an oceanic cycle of
223 N. Sr is added as an illustrative tracer cycle (which does not affect the overall dynamics) (Mills et al.,
224 2014a). The oceanic N and P cycles are tightly coupled such that versions of the model that remove
225 the N cycle and relate new production directly to P concentration give comparable results (Lenton et
226 al., 2012), but we retain both cycles here.

227 In previous updates to the model, some new fluxes have been introduced (Mills et al., 2014a),
228 notably seafloor weathering is included as a sink of CO₂, and terrestrial silicate weathering is
229 subdivided into contributions from volcanic rocks (termed 'basalt') and from all other non-volcanic
230 igneous silicate rocks (termed 'granite'). Here we also add pyrite and gypsum degassing fluxes of
231 sulphur in line with GEOCARBSULF (Bernier, 2006a). The original COPSE had a partial, interactive Ca
232 cycle, but as gypsum degassing is a source of volatile S but not of Ca, whereas gypsum burial
233 removes both Ca and S from the ocean, this poses a mass balance problem for Ca. Hence we opt to
234 remove the partial, interactive Ca cycle from COPSE. Only the gypsum burial flux was related to
235 modelled calcium, and we now relate this to a prescribed reconstructed change in ocean [Ca] (Horita
236 et al., 2002). Modelling by others has given a more complete treatment of Ca variation over
237 Phanerozoic time (Arvidson et al., 2013).

238 The core model includes surface reservoirs of atmosphere-ocean oxygen (**O**) and carbon (**A**), and
239 oceanic nitrogen (**N**), phosphorus (**P**), and sulphur (**S**), with sedimentary rock reservoirs of organic

240 (reduced) carbon (**G**), carbonate (oxidised) carbon (**C**), pyrite (reduced) sulphur (**PYR**), and gypsum
241 (oxidised) sulphur (**GYP**). These are shown as circles in Figure 2. In our notation, upper case bold
242 italic lettering (e.g. **A**) indicates reservoir size in moles and lower case bold italic lettering (e.g. **a**)
243 indicates reservoir size normalised to the present. Differential equations and present-day reservoir
244 sizes are summarised in Table 1. The meaning of different flux terms and their original baseline
245 values are introduced in Table 2. The additional tracer cycle of strontium includes ocean (**OSr**) and
246 sedimentary carbonate (**CSr**) reservoirs. It is introduced briefly below and described in full in
247 Appendix A.

248 2.2. Forcing factors

249 The original COPSE model was forced by changing solar insolation (*I*), metamorphic and volcanic
250 degassing (*D*), tectonic uplift (*U*), plant evolution and land colonisation (*E*), plant enhancement of
251 weathering (*W*), apportioning of carbonate burial between shallow and deep seas (*B*), and changing
252 C:P burial ratio of terrestrial plant material (CP_{land}) (Table 3). Changing solar insolation is based on
253 established stellar physics and is implicit in the time-dependent calculation of global temperature
254 hence is not discussed further here. Subsequent work using COPSE has suggested several updates to
255 the original geological and biological forcing factors (Fig. 3), and has introduced volcanic, non-
256 volcanic and carbonate rock area, paleogeography effects on runoff (Mills et al., 2014a) and selective
257 biotic weathering of P (Lenton et al., 2012, 2016) as additional forcing factors. Here we first describe
258 further updates to the original set of forcing factors (Fig. 3) and then describe an expanded and
259 updated list of additional forcing factors (Fig. 4). In developing the model we also explored yet
260 further forcing factors (Table 3) which are not included here (in the interests of simplicity), because
261 they had little effect or generated easily falsified results.

262 2.2.1. Degassing (*D*)

263 The controls on metamorphic and volcanic degassing (*D*) – here of sedimentary volatiles – are a
264 subject of ongoing debate. On the longest timescales degassing is expected to be driven by the

265 Earth's decaying internal heat source, but with the supercontinent cycle and associated changes in
266 plate tectonics causing substantial fluctuations about the long-term trend – including recent
267 suggestions that more CO₂ degassing occurs at continental arcs than oceanic arcs (Lee et al., 2013;
268 McKenzie et al., 2016). The original degassing forcing of COPSE followed GEOCARB II (Berner, 1994)
269 in linking subduction rates to seafloor spreading rates estimated based on direct estimates of
270 subduction for the last 180 Myr (Engebretson et al., 1992) and sea-level change prior to that (Gaffin,
271 1987). Recent work has linked degassing for the past 230 Myr to inferred subduction zone length
272 from seismic tomographic imaging of subducted slabs (Van Der Meer et al., 2014), and this forcing
273 has been tried in COPSE (Mills et al., 2014a). Other recent work has sought to quantitatively
274 reconstruct plate tectonics through parts of Phanerozoic time, including changes in subduction zone
275 length (Matthews et al., 2016). However, a complete Phanerozoic reconstruction is currently
276 unavailable. Hence here instead we derive degassing using the original sea-level inversion approach
277 (Gaffin, 1987) applied to a more recent Phanerozoic sea-level dataset (Haq, 2014; Haq and Al-
278 Qahtani, 2005; Haq and Schutter, 2008). The original method (Gaffin, 1987) is simplified, with little
279 effect on the results (Mills et al., 2017). The main change from updating the sea-level data is an
280 increase in inferred degassing from the late Permian to the mid Cretaceous (Fig. 3a).

281 **2.2.2. Uplift (*U*)**

282 Uplift forcing (*U*) is updated (Mills et al., 2014a), following GEOCARBSULF (Berner, 2006b; Royer et
283 al., 2014), such that it is based on a polynomial fit to sediment accumulation rates over Phanerozoic
284 time (Ronov, 1993) rather than inversion of the strontium isotope record. This produces a smoother
285 forcing that follows the same long-term trend as the original forcing (Fig. 3b). It captures the overall
286 modulation of uplift by the supercontinent cycle, but does not resolve specific orogenic events. In
287 recent versions of GEOCARBSULF (Royer et al., 2014), variation in the uplift/erosion forcing is scaled
288 down by a 2/3 power, but here we use the original smooth fit to the Ronov data, reasoning that this
289 represents the supply of new rock available for chemical weathering. For application of the model to
290 specific events within the Phanerozoic, and for capturing some of the fine-scale structure in the

291 strontium isotope record, the uplift forcing could be modulated to capture specific orogenic events,
292 but we do not pursue this here.

293 **2.2.3. Plant evolution (E)**

294 We retain separate forcing factors for plant evolution (E) and plant effects on weathering (W) for
295 consistency with earlier work, although they follow similar trajectories and are multiplied together
296 where they appear in the model weathering equations. For plant evolution (E ; Fig. 3c), we update
297 the rise of the earliest non-vascular plants to capture their higher potential productivity and spatial
298 coverage (Porada et al., 2016) with E increasing from 0 to 0.15 over 465 to 445 Ma (Lenton et al.,
299 2016). We also revise the subsequent rise of rooted vascular plants, including forests, with E
300 increasing more rapidly from $E=0.15$ at 400 Ma to $E=1$ at 350 Ma, in contrast to a slower rise to $E=1$
301 at 300 Ma in the original COPSE model, and a later starting rise from 380 Ma to 350 Ma in
302 GEOCARBSULF.

303 **2.2.4. Plant effects on weathering (W)**

304 We update the effect of the earliest non-vascular plants on weathering (W ; Fig. 3d) to capture
305 stronger effects suggested by recent experimental results and ecophysiological modelling studies
306 (Lenton et al., 2012; Porada et al., 2016) with W increasing from 0 to 0.75 over 465 to 445 Ma
307 (Lenton et al., 2016). Here we also increase weathering amplification W from 0.75 to 1 over 400-350
308 Ma associated with the evolution of rooted vascular plants, including deep rooted trees. We
309 correspondingly remove the original increase in weathering amplification with the Cretaceous rise of
310 angiosperms (W from 0.75 to 1 over 115-100 Ma), which was taken from GEOCARB I and II (Berner,
311 1991; Berner, 1994), noting that GEOCARB III also explores no effect of angiosperms and opts for
312 $W=0.875$ prior to angiosperms (Berner and Kothavala, 2001). Whilst there is some evidence that
313 angiosperms can increase weathering rates relative to gymnosperms (Moulton et al., 2000), there is
314 other evidence that they can suppress weathering rates (Andrews et al., 2008). Hence the
315 assumption of no increase in weathering rates seems a reasonable baseline. In contrast to our

316 chosen forcing, GEOCARBSULF assumes that plants only start to affect weathering at 380 Ma with
317 the rise of trees and that a major increase to $W=0.875$ is complete by 350 Ma, with a further
318 increase to $W=1$ associated with the rise of angiosperms over 130 to 80 Ma (Royer et al., 2014).

319 **2.2.5. Plant stoichiometry (CP_{land})**

320 We update the forcing of land plant stoichiometry (CP_{land} ; Fig. 3e) to capture a high C/P of earliest
321 non-vascular plants and associated peats. The original model assumed a default C/P = 1000 burial
322 ratio of terrestrially-derived organic matter but increased this to C/P = 2000 over 355-345 Ma then
323 decreased it back to C/P = 1000 over 290-280 Ma in a crude attempt to capture the effect of
324 abundant deposition of coals from swamps in the Carboniferous (and early Permian). Subsequent
325 work noted that non-vascular plant matter has a high C/P ~2000 (Lenton et al., 2016) and that
326 peatland transformation to coaly shales had started by the early Devonian (Kennedy et al., 2013).
327 Hence C/P was increased to 2000 with the rise of the first non-vascular plants, over 465-445 Ma
328 (retaining the decrease to C/P = 1000 over 290-280 Ma). Here we first adopt that forcing, then when
329 we introduce an additional forcing factor of coal basin depositional area (b_{coal}) we change the timing
330 of the decline of C/P to 345-300 Ma, to avoid excessive Carboniferous organic carbon burial as b_{coal}
331 ramps up over this interval.

332 **2.2.6. Pelagic calcification (B)**

333 We update the shape of the shift in the location of carbonate burial from shelves to the deep sea
334 with the rise of pelagic calcifiers (B ; Fig. 3f), which increases carbonate degassing. The approach
335 originally used in COPSE is from GEOCARB I and involves a sharp rise which then saturates. This can
336 be questioned given that the extra carbonate getting subducted should be an integral of what has
337 previously been deposited on slowly moving ocean plates, hence should not increase abruptly even
338 if the deposition flux increases abruptly. In GEOCARB II, Berner (1994) used a linear rise from 150-0
339 Ma and experimented with different initial values of 0.5 to 1 as well as the standard 0.75, showing

340 that this has a substantial effect on CO₂ predictions. Here we adopt the GEOCARBSULF choice of a
341 linear rise from 0.75 to 1 over 150-0 Ma (Royer et al., 2014).

342 **2.2.7. Volcanic silicate rock area (a_{bas})**

343 In recent work (Mills et al., 2014a) we introduced a distinction between volcanic silicate rocks
344 (termed 'basalt') and non-volcanic silicate rocks (termed 'granite'), and a new normalised model
345 forcing representing the exposed area of volcanic rocks (a_{bas}). This forcing captures the combined
346 area of large igneous provinces and volcanic islands (ocean island basalts and island arcs). Here we
347 extend this approach back in time using initial LIP areas from an updated version of the Large
348 Igneous Provinces Commission compilation starting at 720 Ma (Ernst, 2014). The cumulative LIP area
349 forcing was calculated assuming exponential decay with time of each individual LIP from their initial
350 estimated area to their present area. Decay rates for each major LIP were set to retrieve their
351 present day area, and an overall decay rate for other LIPs set to retrieve a cumulative present day
352 area of 4.8×10^6 km² (Mills et al., 2014a). We assume volcanic island area scales with subduction-
353 related degassing (D) as the majority of volcanic islands are linked to island arcs driven by crust
354 subduction (Allegre et al., 2010). The resulting forcing shows a ~2.5 fold increase in volcanic rock
355 area over Phanerozoic time (Fig. 4a).

356 We also estimated an additional contribution to degassing from the emplacement of large igneous
357 provinces (D_{LIP}), but as this is only a small fraction of total degassing, the principal effects of which
358 are on short-term events (Mills et al., 2014a), we do not include it here.

359 **2.2.8. Non-volcanic silicate rock area (a_{gran})**

360 In previous work (Mills et al., 2014a), a normalised forcing of the area of non-volcanic silicate rocks
361 (a_{gran}) was introduced, taken to be the remainder of total continental area (from GEOCARBSULF)
362 minus exposed carbonate area (from GEOCARBSULF) minus volcanic rock area (a_{bas}). Here instead
363 we estimate a kinetically-weighted area forcing of the non-volcanic component of silicate
364 weathering (a_{gran}) based on the Phanerozoic paleogeology reconstructions of Bluth and Kump

365 (1991). We took the midpoint of geologic intervals from the latest geological timescale (Cohen et al.,
 366 2013; updated) and interpolated linearly between them. a_{gran} is assumed to comprise cation
 367 contributions from shield rocks (a_{sil}) and from secondary minerals in sedimentary rocks (a_{sed}), which
 368 make a large contribution to today's non-volcanic silicate weathering flux (Amiotte-Suchet et al.,
 369 2003; Hartmann et al., 2009). 'Shales' have been estimated to contribute ~77% of the non-volcanic
 370 silicate weathering CO_2 consumption flux (Amiotte-Suchet et al., 2003), although a more
 371 sophisticated treatment of current lithology suggests that all non-carbonate sedimentary rocks
 372 contribute ~62% of the non-volcanic silicate weathering flux (or ~52% of total silicate weathering)
 373 (Hartmann et al., 2009). Hence we define $a_{gran} = k_{sed} \cdot a_{sed} + (1 - k_{sed}) \cdot a_{sil}$, as a kinetic and area weighted
 374 forcing factor, and opt for $k_{sed} = 0.6$ as a reasonable estimate. The sedimentary rock types assumed
 375 to contribute significantly to silicate weathering are shales, coals, and evaporites. (Sandstone and
 376 siliceous chert are neglected because they do not contribute greatly to silicate weathering and
 377 COPSE does not keep track of their sedimentary reservoirs.) We sum together the areas of these
 378 three rock types to create a normalised forcing (a_{sed}), making one adjustment from the original
 379 dataset of Bluth and Kump (1991) in that we neglect an inferred sharp increase in exposed shale
 380 area from the Pliocene to the present (taking the Pliocene value as the present value). Exposed
 381 shield silicate area (a_{sil}) from Bluth and Kump (1991) shows a large decline over Phanerozoic time
 382 and replacement largely by sandstones, which (as they discuss) may be partly an artefact. In a_{gran} it is
 383 somewhat counteracted by an increase in the area of shales, coals and evaporites, although a_{gran} still
 384 declines by a factor ~2.5 over Phanerozoic time (Fig. 4b).

385 We also calculated normalised forcing factors for exposed areas of carbonate (a_{carb}), shale (a_{shale}),
 386 organics (shale + coal) (a_{org}), and evaporites (a_{evap}), and experimented with using them to force the
 387 weathering fluxes of carbonate (a_{carb}), pyrite (a_{shale}), organic carbon (a_{org}), and gypsum (a_{evap}), but
 388 leave them out here as they either failed to improve the results or clearly degraded them.

389 **2.2.9. Paleogeography (PG)**

390 Following GEOCARBSULF and Mills et al. (2014a), we consider an additional weathering forcing
 391 representing the combined effects of changes in paleogeography (PG) on global river runoff and on
 392 the fraction of land area undergoing chemical weathering (thus excluding dry regions) (Fig. 4c). For
 393 this we use GCM-based estimates that exclude the effects of changing CO_2 and solar luminosity
 394 (Royer et al., 2014), multiplying together their f_D forcing and a normalised-to-present version of their
 395 f_{Aw}/f_A forcing. We do not further scale the resulting forcing by total land area, as is done in
 396 GEOCARBSULF (Royer et al., 2014), because exposed areas of relevant rock types are dealt with
 397 separately.

398 **2.2.10. Coal deposition (b_{coal})**

399 Coal deposition on land has at times been a significant contributor to global organic carbon burial,
 400 controlled by a combination of the occurrence of subsiding low-relief cratons and a moist climate
 401 (Nelsen et al., 2016). Following other Phanerozoic modelling studies, e.g. Bartdorff et al. (2008), here
 402 we add a coal basin depositional area forcing (b_{coal} , labelled ‘ b ’ for burial to distinguish it from ‘ a ’ for
 403 exposed area forcing), which is ultimately derived from data for coal abundance (Ronov, 1993) (and
 404 hence comparable to what Bluth and Kump, 1991, find for coal depositional area as that too is based
 405 on Ronov’s data). b_{coal} is normalised to 1 at present and has a peak of ~ 12 at the end of the
 406 Carboniferous (~ 300 Ma), but it falls to 0 prior to the Carboniferous, which is at odds with recent
 407 discoveries of early Devonian coaly shales (Kennedy et al., 2013) and with the observation that the
 408 earliest plants were tied to wetland settings by their physiology, so would be expected to have
 409 created peatlands. Hence we set $b_{coal} = 1$ initially until it starts to increase above that at ~ 345 Ma.
 410 The resulting fluctuations in coal depositional area (Fig. 4d) are only assumed to operate on the
 411 small fraction (~ 0.2 ; see below) of today’s terrestrial organic carbon burial flux that is actually buried
 412 in coal basins rather than marine sediments, whereas changes in the C/P ratio of terrestrial organic
 413 matter will operate on the whole burial flux, whether burial occurs in terrestrial or marine settings.
 414 Hence when introducing b_{coal} we combine it with CP_{land} (rather than replacing it).

2.2.11. Selective biotic weathering of phosphorous (F)

415 An additional forcing factor (F) has previously been introduced that represents the selective biotic
416 weathering of P relative to host rock dissolution (Lenton et al., 2012, 2016). This captures the
417 observations that plants and their fungal mycorrhizal symbionts have evolved mechanisms to
418 selectively 'mine' P-rich mineral inclusions in rocks, and experiments show large relative
419 enhancements of P weathering relative to bulk cations (Ca, Mg) by non-vascular plants (Lenton et al.,
420 2012; Quirk et al., 2015). Such selective P weathering represents a mechanism to decouple the
421 inorganic (silicate weathering) and organic (carbon burial) sides of the carbon cycle. It may have
422 been particularly pertinent when early plants were colonising fresh rock surfaces before the
423 establishment of rooting systems, deeper soils and effective P recycling systems. Hence it has been
424 used as a means of forcing mid-Paleozoic increases of organic carbon burial in COPSE (Lenton et al.,
425 2012, 2016). Here we explore an increase from $F=1$ to $F=1.5$ over 465-445 Ma followed by a
426 decrease from $F=1.5$ to $F=1$ over 410-400 Ma (Lenton et al., 2016) (Fig. 4e).

2.2.12. Calcium concentration (c_{cal})

428 In place of the original interactive marine Ca reservoir we explore forcing gypsum burial with a
429 prescribed variation in normalised marine $[Ca^{2+}]$ (c_{cal} , where 'c' is for concentration) following the fit
430 to the data in Figure 8 of Horita et al. (2002) (Fig. 4f). We also considered forcing gypsum burial with
431 a changing evaporite depositional area (b_{evap}) derived from Bluth and Kump (1991), but this yielded
432 readily falsifiable results so we do not include it here.

2.3. Variables

434 Changes to the model functions that are incorporated in the new baseline model are summarised in
435 Table 4, and further alternative functions explored in the hypothesis testing are described in this
436 section. Changes to the model non-flux parameters are summarised in Table 5 (changes to flux
437 parameters are in Table 2). In the following we use a prime to indicate a normalised variable.

439 2.3.1. Atmospheric CO₂

440 Whereas the original model had a constant atmospheric fraction of the total ocean-atmosphere CO₂
 441 reservoir, here atmospheric CO₂ (in PAL, i.e. normalised) is made proportional to the square of the
 442 total amount of carbon in the ocean and atmosphere (normalised variable **a**) following Kump and
 443 Arthur (1999):

$$444 \quad CO_2 = \mathbf{a}^2 \quad (1)$$

445 This makes minimal difference to steady state CO₂ predictions, but variations in the total ocean-
 446 atmosphere carbon reservoir (**A**) are much reduced, allowing greater transient variations in CO₂ in
 447 studies of short-term events, including e.g. the early rise of plants. Present atmospheric CO₂ (1 PAL)
 448 is taken to correspond to a pre-industrial $pCO_2 = 280$ ppm, i.e. $pCO_2 = 280 \cdot CO_2$ (ppm).

449 2.3.2. Global temperature

450 In the interests of simplicity, model comparability, and ability to explore variations in climate
 451 sensitivity, we switch from the original global surface temperature (*T*) function of Caldeira and
 452 Kasting (1992) to the GEOCARB III temperature function (Berner and Kothavala, 2001) (which has a
 453 slightly different implicit variation in solar luminosity with time):

$$454 \quad \Delta T = k_c \cdot \ln CO_2 - k_l \cdot t/570 \quad (2)$$

455 Where $k_c = 4.328^\circ\text{C}$ corresponds to a climate sensitivity of 3°C for a doubling of CO₂ and $k_l = 7.4^\circ\text{C}$
 456 represents the sensitivity to changing solar luminosity, for time, *t*, in Myr ago. Present global
 457 temperature is taken to be 15°C hence $T = 15 + \Delta T$ ($^\circ\text{C}$).

458 2.3.3. Net primary productivity

459 The dependence of global vegetation net primary productivity, V_{npp} , on temperature, *T* ($^\circ\text{C}$), pCO_2
 460 (ppm) and O₂ (PAL) retains the original 'OCT' formulation:

$$461 \quad V_{npp} = k_{npp} \cdot E \cdot (1.5 - 0.5 \cdot \mathbf{o}) \cdot \left(1 - \left(\frac{T-25}{25}\right)^2\right) \cdot \left(\frac{pCO_2 - P_{min}}{P_{1/2} + pCO_2 - P_{min}}\right) \quad (3)$$

462 Where $P_{min} = 10$ ppm, $P_{1/2} = 183.6$ ppm, and $k_{npp} = 2$ is a normalising constant for present $T = 15^\circ\text{C}$
 463 and $p\text{CO}_2 = 280$ ppm. This represents a slightly weaker CO_2 fertilisation effect than the GEOCARB
 464 choices of $k_{\text{CO}_2}=2$, $P_{min} = 0$ ppm, $P_{1/2} = 280$ ppm (but this has little effect on the results).

465 **2.3.4. Fire effects on vegetation**

466 We adjust the fire function following Lenton (2013) to be based on a fit to experimental results for
 467 fuel of 10% moisture content (rather than 20% moisture content in the original model):

$$468 \quad \textit{ignit} = \min(\max(48 \cdot m\text{O}_2 - 9.08, 0), 5) \quad (4)$$

469 where $m\text{O}_2$ (0.21 at present) is the volumetric mixing ratio of O_2 (mol/mol) assuming a constant
 470 remainder of the atmosphere dominated by N_2 :

$$471 \quad m\text{O}_2 = \frac{o}{o+k_{16}} \quad (5)$$

472 with $k_{16} = 3.762$ (as before). The resulting equation for vegetation biomass is as before:

$$473 \quad V = V_{npp} \cdot \frac{k_{fire}}{k_{fire} - 1 + \textit{ignit}} \quad (6)$$

474 but we adopt $k_{fire} = 3$ following Bond et al. (2005) and Lenton (2013), which equates to a 50%
 475 suppression of vegetation biomass by fires at present (relative to the case with no fires; $m\text{O}_2 < 0.19$).
 476 Together this results in a fire feedback that lies intermediate in strength between the original weak
 477 (default) and strong formulations for increases in O_2 , and provides stronger feedback against
 478 decreases in O_2 as fires have a limiting effect on vegetation down to $m\text{O}_2 \sim 0.19$, consistent with
 479 combustion experiments and spatial modelling of fire propagation (Belcher et al., 2010).

480 **2.3.5. Degassing of carbon and sulphur**

481 Carbonate degassing (*ccdeg*) and organic carbon degassing (*ocdeg*) retain their original functional
 482 forms (but the default fluxes are adjusted; see below):

$$483 \quad \textit{ccdeg} = k_{12} \cdot D \cdot B \cdot c \quad (7)$$

$$484 \quad ocdeg = k_{13} \cdot D \cdot g \quad (8)$$

485 The revised model allows for the possibility of degassing fluxes of gypsum and pyrite:

$$486 \quad gypdeg = k_{gypdeg} \cdot D \cdot gyp \quad (9)$$

$$487 \quad pyrdeg = k_{pyrdeg} \cdot D \cdot pyr \quad (10)$$

488 Initially the sulphur degassing fluxes (k_{gypdeg} , k_{pyrdeg}) are set to zero consistent with the original model.

489 **2.3.6. Seafloor weathering**

490 The revised model includes a seafloor weathering sink of CO₂ which is assumed to scale with
 491 degassing (i.e. the rate of oceanic crust production). However, rather than have it depend on CO₂
 492 (Mills et al., 2014a), a direct kinetic temperature dependence is applied:

$$493 \quad sfw = k_{sfw} \cdot D \cdot e^{k_T^{sfw} \cdot \Delta T} \quad (11)$$

494 This assumes deep ocean temperature changes in proportion to global average temperature on long
 495 timescales. $k_T^{sfw} = 0.0608$ corresponds to an activation energy (42 kJ mol⁻¹) appropriate for terrestrial
 496 basalt weathering, which we take as a default. However recent work suggest a much higher
 497 apparent activation energy for seafloor weathering 92 ± 7 kJ mol⁻¹ ($k_T^{sfw} = 0.1332$) implying stronger
 498 negative feedback (Coogan and Dosso, 2015), which we explore as an option below. (Seafloor basalt
 499 oxidation is also a sink of O₂ $\sim 1 \times 10^{12}$ molO₂ yr⁻¹ (Sleep, 2005) but this term in the oxygen balance is
 500 neglected here because it is assumed to scale with D in a similar way to organic carbon degassing.)

501 **2.3.7. Plant effects on terrestrial weathering**

502 The effects of plants on weathering are simplified from the original model, which multiplicatively
 503 applied the effect of plants on weathering term $V \cdot W$ leading to a mixing of abiotic and biotic
 504 responses. This could erroneously exceed (by up to $\sim 56\%$) either end-member for intermediate
 505 values of $V \cdot W$ between 0 (abiotic) and 1 (biotic), making the effects of intermediate plant cover
 506 excessively strong. The original function also multiplied a Michaelis-Menten function of CO₂ for plant

507 productivity within V by another Michaelis-Menten function of CO_2 (f_{plant}) from GEOCARB, which was
 508 also originally intended to capture the CO_2 fertilisation effect on plant productivity. Here we include
 509 just one Michaelis-Menten CO_2 dependence within the variable V , which also encapsulates the plant
 510 evolution forcing factor E . Our simplified effect of biota (or lack of it) on weathering is:

$$511 \quad f_{biota} = [(1 - \min(V \cdot W, 1)) \cdot k_{15} \cdot \text{CO}_2^{0.5} + V \cdot W] \quad (12)$$

512 Where the first term dependent on $\text{CO}_2^{0.5}$ represents abiotic weathering (following GEOCARB) and
 513 the second term represents biotic weathering, which is assumed to scale directly with vegetation
 514 biomass (V). We retain the original model assumption of $k_{15} = 0.15$ (i.e. a roughly 7-fold acceleration
 515 of weathering by plants) as a baseline. As options later we explore the use of $k_{15} = 0.25$ (4-fold
 516 amplification of weathering by plants) as in GEOCARB III, and $k_{15} = 0.1$ (10-fold amplification). We
 517 also consider the possibility that weathering is controlled by vegetation NPP rather than biomass
 518 (using V_{npp} in place of V in the above), which removes any effect of fires on weathering.

519 **2.3.8. Temperature effects on weathering**

520 The effects of temperature on weathering rates (directly and via runoff) are separate from the effect
 521 of plants. The general form for the direct kinetic effect of temperature on weathering is:

$$522 \quad f_T^i = e^{k_T^i \Delta T} \quad (13)$$

523 The original model used an activation energy of 62 kJ mol^{-1} for silicate weathering ($k_T = 0.09$). Here
 524 following Mills et al. (2014a) we use activation energies of 50 kJ mol^{-1} for 'granite' ($k_T^{gran} = 0.0724$)
 525 and 42 kJ mol^{-1} for 'basalt' ($k_T^{bas} = 0.0608$).

526 We retain the original dependencies of silicate (f) and carbonate (g) weathering on runoff:

$$527 \quad f_{runoff} = [1 + 0.038\Delta T]^{0.65} \quad (14)$$

$$528 \quad g_{runoff} = 1 + 0.087\Delta T \quad (15)$$

529 2.3.9. Silicate weathering

530 The total silicate weathering flux at present (k_{silw}) is divided into a volcanic rock ('basalt') fraction
 531 ($k_{basfrac}$) and a non-volcanic rock ('granite') fraction ($1-k_{basfrac}$):

$$532 \quad k_{granw} = (1 - k_{basfrac}) \cdot k_{silw}, \quad k_{basw} = k_{basfrac} \cdot k_{silw} \quad (16)$$

533 The equations for 'granite' (non-volcanic) weathering ($granw$) and 'basalt' (volcanic) weathering
 534 ($basw$) include additional forcing factors capturing changes in exposed areas (a_{gran} , a_{bas}) and
 535 paleogeographic effects on runoff (PG). In the original model all silicate weathering depended on
 536 tectonic uplift, but here whilst weathering of ancient granitic cratons is assumed to depend on uplift
 537 by default, the more rapid weathering of relative young volcanic rocks is assumed independent of
 538 uplift following Mills et al. (2014a):

$$539 \quad granw = k_{granw} \cdot U \cdot PG \cdot a_{gran} \cdot f_{Tgran} \cdot f_{runoff} \cdot f_{biota} \quad (17)$$

$$540 \quad basw = k_{basw} \cdot PG \cdot a_{bas} \cdot f_{Tbas} \cdot f_{runoff} \cdot f_{biota} \quad (18)$$

$$541 \quad silw = granw + basw \quad (19)$$

542 Of course mantle plumes themselves may generate some uplift and volcanic islands are often steep
 543 and rapidly eroding terrains, but these effects are distinct from uplift of continental crust driven by
 544 plate collisions and are assumed to be enfolded in $k_{basfrac}$, which captures the disproportionate
 545 contribution of the relatively small area of volcanic rocks to the total silicate weathering flux. As an
 546 option we consider introducing an uplift dependence of basalt weathering, to help recover the
 547 original model structure. Supply limitation of silicate weathering is not considered here for the
 548 Phanerozoic, although it may have been an important factor in the aftermath of Neoproterozoic
 549 glaciations (Mills et al., 2011).

550 2.3.10. Carbonate weathering

551 Carbonate weathering now includes additional dependencies on crustal carbonate reservoir size and
552 paleogeographic forcing (PG):

$$553 \quad carbw = k_{14} \cdot C \cdot U \cdot PG \cdot g_{runoff} \cdot f_{biota} \quad (20)$$

554 The dependence on the crustal carbonate reservoir size has minimal effect on the results, because it
555 varies very little, but we include it for consistency with the other weathering fluxes.

556 2.3.11. Gypsum weathering

557 Gypsum weathering was originally assumed proportional to carbonate weathering and to the
558 normalised size of the gypsum sedimentary reservoir (gyp). Here we make the functional
559 dependencies explicit:

$$560 \quad gypw = k_{22} \cdot gyp \cdot U \cdot PG \cdot g_{runoff} \cdot f_{biota} \quad (21)$$

561 2.3.12. Oxidative weathering (kerogen)

562 Despite critique (Berner, 2006a), the revised baseline model retains the assumption that oxidative
563 weathering of organic carbon (kerogen) has some sensitivity to variations in atmospheric O_2 at the
564 present high O_2 concentrations. This is defended based on abundant evidence for incomplete
565 oxidation of ancient organic carbon in rapidly uplifting/eroding terrains (Galy et al., 2015).
566 Furthermore, the results of more detailed modelling of oxidative weathering across the observed
567 range of erosion rates (Daines et al., 2017) show a dependence on O_2 that is reasonably
568 approximated by the original square root dependence used in COPSE:

$$569 \quad oxidw = k_{17} \cdot U \cdot g \cdot o^{0.5} \quad (22)$$

570 Later we test the effects of removing the O_2 dependence following Berner (2006a).

571 **2.3.13. Pyrite weathering**

572 Pyrite oxidation has much faster kinetics than kerogen oxidation hence it goes to completion at
 573 present high O₂ concentrations. Indeed detrital pyrite preservation essentially stopped after the
 574 Great Oxidation Event at ~2.4 Ga (Johnson et al., 2014). Hence we agree with the critique of (Berner,
 575 2006a) and remove any dependence on O₂ in the revised model:

$$576 \quad \text{pyr}_w = k_{21} \cdot U \cdot \text{pyr} \quad (23)$$

577 **2.3.14. Phosphorus weathering**

578 The revised model allows the apportioning of the phosphorus weathering flux between different
 579 rock types ($k_{P_{silw}}$, $k_{P_{carbw}}$, $k_{P_{oxidw}}$) to be varied and introduces an additional forcing factor (F)
 580 representing selective P weathering by plants:

$$581 \quad \text{phos}_w = k_{10} \cdot F \cdot (k_{P_{silw}} \cdot \text{silw}/k_{silw} + k_{P_{carbw}} \cdot \text{carbw}/k_{14} + k_{P_{oxidw}} \cdot \text{oxidw}/k_{17}) \quad (24)$$

582 The phosphorus weathering flux from silicates is therefore subdivided into contributions from
 583 ‘granite’ (non-volcanic) and ‘basalt’ (volcanic) rocks, following equations (17)-(19). We considered
 584 making apatite dissolution activation energy distinct from the host rock, but found it did not greatly
 585 alter the results. We also considered whether the P content relative to bulk cations (Ca + Mg,
 586 associated with the alkalinity flux) should differ between volcanic and non-volcanic silicate rocks, but
 587 decided against this as this ratio is highly variable within these rock categories, and because no such
 588 adjustment is broadly consistent with a detailed breakdown of phosphorus weathering (Hartmann et
 589 al., 2014).

590 **2.3.15. Phosphorus distribution and terrestrial organic matter burial**

591 The fraction of the weathered phosphorus flux that is ultimately buried with land plant derived
 592 organic matter (either on land or in the ocean) retains its original linear dependence on terrestrial
 593 vegetation biomass (V). The burial flux of terrestrially-derived organic phosphorus and associated
 594 carbon is taken to encompass both burial on land in peatlands (resulting in e.g. coal deposits) and

595 burial after erosion and transport in aquatic settings, including freshwaters, estuaries, coastal deltas,
 596 and marine sediments (Burdige, 2005; Regnier et al., 2013). Here we distinguish these two burial
 597 pathways and explore as options: (i) forcing the fraction of terrestrially-derived organic matter that
 598 is buried in peatlands by the changing area of coal basin depositional settings (b_{coal}); (ii) a
 599 dependence of aquatic burial of terrestrially-derived material on uplift (U), to capture the
 600 observation that increased erosion transfers more terrestrially-derived organic matter to the ocean,
 601 where in general it is more efficiently preserved than on land (Blair and Aller, 2012). These
 602 alternations are captured by altering the burial flux of P with land plant matter ($pland$) in order to
 603 maintain conservation of phosphorus:

$$604 \quad pland = k_{11} \cdot V \cdot phosw \cdot (k_{aq} \cdot f_P(U) + (1 - k_{aq}) \cdot b_{coal}) \quad (25)$$

605 We set $f_P(U) = 1$ but allow b_{coal} to vary as the default (Table 4). Here k_{aq} is the fraction of terrestrial
 606 organic matter burial occurring in aquatic settings today, which we estimate at $k_{aq} = 0.8$ (and is
 607 potentially higher than this) (Burdige, 2005), consistent with only a small component of burial due to
 608 coals at present. The original function for $pland$ is recovered by setting $k_{aq} = 1$ and $f_P(U) = 1$.

609 The corresponding burial of terrestrially-derived organic carbon also depends on its C/P burial ratio,
 610 which is a normalised forcing factor (CP_{land}) as in the original model:

$$611 \quad locb = \left(\frac{C}{P}\right)_{land} \cdot pland = k_5 \cdot CP_{land} \cdot pland' \quad (26)$$

612 The transfer of the remaining available reactive phosphorus to the ocean where it can fuel marine
 613 productivity is simply given by:

$$614 \quad psea = phosw - pland \quad (27)$$

615 **2.3.16. Marine new production**

616 New production is controlled by the proximate limiting nutrient as before:

$$617 \quad newp = r_{C:P} \cdot \min\left(30.9 \cdot \frac{n}{r_{N:P}}, 2.2 \cdot p\right) = newp_0 \cdot newp' \quad (28)$$

618 Where the values 30.9 and 2.2 are the present average concentrations of nitrate and phosphate in
 619 the ocean (in $\mu\text{mol kg}^{-1}$), $r_{C:P}=117$ and $r_{N:P}=16$ are the Redfield ratios, and therefore N is proximately
 620 limiting at present giving $newp_0 = 225.96$ as a normalising constant.

621 **2.3.17. Anoxia**

622 COPSE followed earlier work (Lenton and Watson, 2000a; Van Cappellen and Ingall, 1994; Van
 623 Cappellen and Ingall, 1996) in assigning an anoxic fraction of the ocean (*anox*) that depended on the
 624 ratio of oxygen supply and demand, with a present value of 0.14 (broadly intended to represent the
 625 fractional surface area of ocean below which there is anoxia at some depth). Anoxic fraction
 626 decreased linearly with oxygen from 1 at $O_2 = 0$ to 0 at $O_2 = 1.16$ PAL (for present nutrients), and
 627 increased in a saturating way with new production (for present O_2) from 0 at $newp' = 0.86$ toward 1.
 628 On reflection this is a poor quantitative representation of ocean anoxia, and given growing interest
 629 in past intervals of ocean anoxia and their relationship to O_2 and nutrient levels, we redefine the
 630 anoxia function here. First we note that only 0.2-0.3% of the seafloor is overlain by anoxic bottom
 631 waters (Helly and Levin, 2004). Given the importance of anoxic bottom waters for P cycling (and also
 632 several redox sensitive trace metals) we redefine *anox* as the anoxic fraction of the seafloor, and
 633 assume that this scales with the volume of anoxic waters.

634 Oxygen levels in deeper waters separated from the ocean surface by e.g. thermal stratification are
 635 controlled by the balance of oxygen supply – via transport of surface waters equilibrated with the
 636 atmosphere – and oxygen demand – governed by upwelling transport of deep ocean limiting
 637 nutrient concentration and its uptake efficiency, creating a sinking flux of organic matter. COPSE
 638 does not consider changes in ocean transport hence the oxygenation state of the deeper ocean
 639 depends on the balance of atmospheric oxygen and deep ocean nutrient concentrations. However,
 640 some adjustment is required for the incomplete utilisation of nutrients in the high-latitude upwelling
 641 regions which play a key role in governing the deep ocean oxygenation state today. Based on the

642 results of multi-box models (Canfield, 1998), 1-D box-diffusion models (Ozaki and Tajika, 2013; Ozaki
 643 et al., 2011), and 3-D ocean models (Lenton and Daines, 2017; Monteiro et al., 2012) we define the
 644 control variable for deep ocean anoxia as:

$$645 \quad k_u \cdot newp' - o \quad (29)$$

646 Where $k_u < 1$ captures the (in)efficiency of nutrient uptake in the (high-latitude) surface waters
 647 ventilating the deep ocean, and also (implicitly) the Redfield ratio of remineralisation $-O_2:C \sim 170:117$.
 648 In today's ocean $k_u \sim 0.5$, given the values discussed by Canfield (1998), implying a considerable global
 649 excess of oxygen supply over demand, and further implying that a halving of atmospheric O_2 or a
 650 doubling of ocean nutrients would put the deep ocean on the edge of anoxia. This agrees reasonably
 651 with 3D model results where a ratio of normalised O_2 :limiting nutrient ~ 0.4 (rather than 0.5) makes
 652 half of the ocean volume anoxic (Lenton and Daines, 2017), or under Cretaceous boundary
 653 conditions an approximate doubling of limiting nutrient tips anoxia (Monteiro et al., 2012). Similarly
 654 1-D box-diffusion model results suggest a halving of O_2 tips anoxia (Ozaki and Tajika, 2013) (their
 655 figure 5 with fixed nutrient). Clearly some waters are anoxic today and some will remain oxygenated
 656 even when the deep ocean is tipped anoxic. To account for such spatial redox heterogeneity we use
 657 a logistic functional form:

$$658 \quad anox = \frac{1}{1 + e^{-k_{anox}(k_u \cdot newp' - o)}} \quad (30)$$

659 where k_{anox} controls the sharpness of the transition between oxia and anoxia and (together with k_u)
 660 sets the extent of anoxia at present. For $k_u = 0.5$, $k_{anox} = 12$ gives $anox = 0.0025$ today, consistent with
 661 0.2-0.3% of the seafloor being overlain by anoxic bottom waters (Helly and Levin, 2004) and giving a
 662 fairly sharp transition of $anox$ from 0.23 to 0.77 as o (normalised O_2) drops from 0.6 to 0.4 PAL (for
 663 fixed nutrient), consistent with other models (Lenton and Daines, 2017; Ozaki and Tajika, 2013). The
 664 oxidic fraction of the ocean $k_1 = 0.997527$ is redefined accordingly.

665 2.3.18. Nitrogen cycling

666 The redefining of anoxia and the oxic fraction of the ocean means there is huge potential for water-
 667 column denitrification to increase as anoxia increases. To prevent denitrification completely draining
 668 the ocean of nitrate we introduce a default dependence on nitrate concentration (which was
 669 anyway used as an optional ‘crash preventer’ in the original code at low $n \leq 0.1$):

$$670 \quad \text{denit} = k_4 \left(1 + \frac{\text{anox}}{1-k_1} \right) \cdot n \quad (31)$$

671 Here half of the initial denitrification is assumed to occur under anoxic conditions at depth in
 672 sediments and therefore be insensitive to water column and sediment surface redox state.

673 The function for nitrogen fixation (with $r_{N:P}=16$) is unaltered:

$$674 \quad \text{nfix} = k_3 \left(\frac{P-N/r_{N:P}}{P_0-N_0/r_{N:P}} \right)^2 \text{ for } \frac{N}{r_{N:P}} < P, \text{ else } 0 \quad (32)$$

675 where P_0 and N_0 are the present day reservoir sizes (Table 1).

676 Marine organic nitrogen burial is a small term dependent on marine organic carbon burial and a
 677 fixed C:N burial ratio = 37.5:

$$678 \quad \text{monb} = \text{mocb}/CN_{\text{sea}} \quad (33)$$

679 2.3.19. Marine organic carbon burial

680 To address a previous critique (Berner, 2006a) we include the option to have erosional (uplift)
 681 control of marine organic carbon burial, and we also include an optional dependence on O_2 :

$$682 \quad \text{mocb} = k_2 \cdot f(U) \cdot (\text{newp}')^2 \cdot f(O_2) \quad (34)$$

683 We set $f(U)=1$, $f(O_2)=1$ as the default (as in the original model). For the optional oxygen dependence
 684 we follow Betts and Holland (1991) as explored by Lenton and Watson (2000b):

$$685 \quad f(O_2) = 2.1276 \cdot e^{-0.755 \cdot o} \quad (35)$$

686 although we recognise that seafloor [O₂] can be decoupled from the atmosphere.

687 2.3.20. Phosphorus burial

688 Organic phosphorus burial is calculated from marine organic carbon burial and the (C/P)_{organic} burial
689 ratio (CP_{sea}):

$$690 \quad mopb = mocb/CP_{sea} \quad (36)$$

691 We retain a fixed burial ratio ($CP_{sea} = 250$) as the default (as in the original model). However, we also
692 explore the option to make this burial ratio dependent on anoxia, following Van Cappellen and Ingall
693 (1994, 1996):

$$694 \quad CP_{sea} = \frac{k_{oxic} \cdot k_{anoxic}}{(1-anox) \cdot k_{anoxic} + anox \cdot k_{oxic}} \quad (37)$$

695 Given the update to the *anox* function we adopt $k_{oxic} = 250$ and $k_{anoxic} = 4000$, as originally suggested
696 (Van Cappellen and Ingall, 1994; Van Cappellen and Ingall, 1996), although subsequent work has
697 used as an upper limit $k_{anoxic} \sim 1000$ (Slomp and Van Cappellen, 2007).

698 Iron-sorbed phosphorus (Fe-P) burial retains an inverse dependence on anoxia by default. The
699 redefining of anoxia means there is little scope for Fe-P burial to increase above the present level.

700 We introduce a dependence on phosphate concentration (which was also used as an optional ‘crash
701 preventer’ in the original code at low $p \leq 0.1$):

$$702 \quad fepb = \frac{k_6}{k_1} \cdot (1 - anox) \cdot p \quad (38)$$

703 Predominantly authigenic calcium-bound phosphorus (Ca-P) burial retains a dependence on the
704 supply of organic carbon to the sediments and we also include an optional dependence on anoxia:

$$705 \quad capb = k_7 \cdot newp'^2 \cdot f(anox) \quad (39)$$

706 We set $f(anox)=1$ as the default (Table 4). For the option to have seafloor anoxia suppress the
707 retention of Ca-P in sediments we follow (Slomp and Van Cappellen, 2007):

$$708 \quad f(\text{anox}) = 0.5 + 0.5 \frac{(1-\text{anox})}{k_1} \quad (40)$$

709 **2.3.21. Pyrite burial**

710 Pyrite burial is taken to depend on sulphate concentration and inversely on oxygen concentration.

711 Its dependence on marine organic carbon burial means that it includes an optional dependence on

712 erosion (uplift) as suggested by (Berner, 2006a):

$$713 \quad m_{psb} = k_{m_{psb}} \cdot \frac{s}{o} \cdot m_{ocb'} \quad (41)$$

714 We considered an anoxia rather than O_2 dependence, which would amount to considering anoxic

715 water-column precipitation and preservation of pyrite, but we reason that sedimentary formation of

716 pyrite has been the dominant mechanism over the Phanerozoic.

717 **2.3.22. Gypsum burial**

718 Gypsum burial was originally dependent on ocean sulphate concentration and variable calcium

719 concentration. The calcium variable is replaced here with a forcing factor (c_{cal}):

$$720 \quad m_{gsb} = k_{m_{gsb}} \cdot s \cdot c_{cal} \quad (42)$$

721 **2.3.23. Carbonate burial**

722 Oceanic carbonate is assumed to be in steady state with marine carbonate carbon burial balancing

723 carbonate input from silicate and carbonate weathering (as in the original model):

$$724 \quad m_{ccb} = silw + carbw \quad (43)$$

725 We also experimented with a more complex formulation where marine carbonate burial is assumed

726 to maintain an alkalinity balance of the ocean that is affected by the sulphur cycle (Mills et al.,

727 2014a; Torres et al., 2014), with pyrite burial a source of alkalinity, and pyrite weathering, pyrite

728 degassing and gypsum degassing all sinks of alkalinity (sources of sulphuric acid). To maintain a

729 present day steady state this requires upward adjustment of the silicate weathering flux constant

730 (k_{silw}) such that it balances total volcanic acid input, i.e. both sulphur and carbon degassing. With
731 that adjustment, the effect on the results is small, so for simplicity we leave it out.

732 **2.3.24. Carbon and sulphur isotope systems**

733 COPSE tracks the isotopic composition of all the carbon and sulphur reservoirs. The functional
734 dependencies of carbon and sulphur isotope fractionation are kept the same as in the original model
735 (Bergman et al., 2004). This includes temperature-dependent atmosphere-ocean fractionation of
736 carbon, temperature-dependent fractionation of marine carbonate deposition (assuming calcite
737 throughout), marine organic carbon fractionation (relative to carbonate) dependent on CO_2 and O_2 ,
738 land organic carbon fractionation (relative to atmosphere) dependent on O_2 , and a fixed sulphur
739 fractionation of pyrite burial relative to gypsum burial – as an O_2 -dependence was previously found
740 to considerably degrade the $\delta^{34}S$ predictions (Bergman et al., 2004).

741 **2.3.25. Strontium tracer cycle**

742 A strontium cycle and its isotopes are implemented following Francois and Walker (1992) and
743 Vollstaedt et al. (2014) with some improvements to the formulation described in Mills et al. (2014a).
744 A full description is given in Appendix A. Ocean and sedimentary (carbonate) reservoirs of strontium
745 are considered. Ocean Sr sources are the weathering of old igneous rocks (granites), new igneous
746 rocks (basalts), sedimentary carbonates, and mantle input. Ocean Sr sinks are the incorporation of
747 strontium in (carbonate) sediments and seafloor weathering. The sedimentary Sr pool has input
748 from carbonate burial, and outputs from carbonate weathering and metamorphism. The $^{87}Sr/^{86}Sr$
749 values of mantle input and continental silicates have prescribed present day values (mantle 0.703,
750 'basalts' 0.705, 'granites' 0.715) but are assumed to have increased over time due to Rb decay. The
751 $^{87}Sr/^{86}Sr$ of sedimentary carbonates varies depending on inputs/outputs and is initialised at 0.708 (a
752 reasonable value for the Late Neoproterozoic). The overall approach is not expected to precisely
753 reproduce the ocean $^{87}Sr/^{86}Sr$ record, because of heterogeneity in the ages of rocks being
754 weathered, but it may be possible to capture large-scale features of the record.

755 **2.4. Baseline fluxes**

756 The C, O, P, S and N cycles are assumed to have been in approximate steady-state in pre-industrial
757 time (referred to as the ‘present’) at least for the purpose of assigning a set of balanced baseline
758 fluxes in the model. The slow variables in the model do not necessarily reach this steady state at
759 present. The original model baseline fluxes are listed in Table 2, along with the changes made by
760 Mills et al. (2014a), and some alternative proposals discussed here and tested in the Results section.

761 **2.4.1. Sulphur cycle**

762 The original COPSE and the updated version of Mills et al. (2014a) have no pyrite or gypsum
763 degassing, pyrite weathering/burial of 0.53×10^{12} molS yr⁻¹ and gypsum weathering/burial of 1.0×10^{12}
764 molS yr⁻¹. We retain these fluxes initially and refer to them as ‘low S’ fluxes. Then in exploring a new
765 set of baseline fluxes we introduce pyrite degassing (0.25×10^{12} molS yr⁻¹) and gypsum degassing
766 (0.5×10^{12} molS yr⁻¹) and adjust pyrite weathering to 0.45×10^{12} molS yr⁻¹ and gypsum weathering to
767 2.0×10^{12} molS yr⁻¹, to give the GEOCARBSULF set of fluxes (Royer et al., 2014), which we refer to as
768 ‘high S’ fluxes. Burial of pyrite or gypsum is assumed to match the total of degassing and weathering
769 in this case. Recent constraints on the pyrite burial fraction of total sulphur burial suggest it is 20-
770 35% today (Tostevin et al., 2014), and our low and high sets of S fluxes sit at the upper and lower
771 ends of this range respectively. Other work reconstructing sulphate evaporite burial fluxes on
772 Laurentia has argued for a much larger pyrite burial fraction and associated pyrite oxidative
773 weathering over much of Phanerozoic time (Halevy et al., 2012). However, this is at odds with
774 sulphur isotope constraints, which suggest that pyrite burial only dominated in the early Paleozoic
775 (Canfield, 2013).

776 **2.4.2. Inorganic carbon cycle**

777 Seafloor weathering was previously included at 1.75×10^{12} molC yr⁻¹ (Mills et al., 2014a; Mills et al.,
778 2014b) based on the midpoint of Cenozoic-Cretaceous estimates $\sim 0.5-3 \times 10^{12}$ molC yr⁻¹ from deep
779 sea drilling cores and estimated crust production rates. However, depending on assumptions about

780 the incorporation of sedimentary carbonates, seafloor weathering might range up to $4.1\text{-}5.7 \times 10^{12}$
781 molC yr^{-1} (Alt and Teagle, 1999; Gillis and Coogan, 2011; Staudigel et al., 1989). Seafloor weathering
782 was previously assumed (Mills et al., 2014a) to imply a reduction in terrestrial silicate weathering to
783 4.9×10^{12} molC yr^{-1} (from a baseline carbonate degassing of 6.65×10^{12} molC yr^{-1} from GEOCARB).
784 However, the silicate weathering flux was already low compared to recent estimates, whereas the
785 carbonate weathering flux (13.35×10^{12} molC yr^{-1} from GEOCARB) is high. The estimated total global
786 CO_2 consumption flux by carbonate plus silicate weathering is $\sim 20 \times 10^{12}$ molC yr^{-1} (Amiotte-Suchet et
787 al., 2003; Gaillardet et al., 1999; Hartmann et al., 2009; Munhoven, 2002) in good agreement with
788 COPSE, but the apportioning is very different with $\sim 60\%$ silicate weathering ($\sim 12 \times 10^{12}$ molC yr^{-1}) and
789 $\sim 40\%$ carbonate weathering ($\sim 8 \times 10^{12}$ molC yr^{-1}) (Hartmann et al., 2009). Furthermore, the
790 contribution of volcanic rocks to silicate weathering is estimated to be $\sim 17\text{-}25\%$ (i.e. $2\text{-}3 \times 10^{12}$ molC
791 yr^{-1}) (Hartmann et al., 2009), significantly less than the $\sim 30\text{-}35\%$ or $\sim 4.1 \times 10^{12}$ molC yr^{-1} estimated
792 previously (Dessert et al., 2003), with 35% (of 4.9×10^{12} molC yr^{-1} , i.e. 1.715×10^{12} molC yr^{-1}) having
793 been used in the interim version of COPSE (Mills et al., 2014a). The implication that non-volcanic
794 rocks contribute $\sim 9\text{-}10 \times 10^{12}$ molC yr^{-1} to silicate weathering is at the upper end of another recent
795 estimate carefully accounting for uncertainties ~ 7.85 ($5.78\text{-}9.93$) $\times 10^{12}$ molC yr^{-1} (Moon et al., 2014).
796 Given these considerations we view the inorganic carbon cycle fluxes used by Mills et al. (2014a) as a
797 'low' set of estimates. As a new set of 'high' inorganic C cycle fluxes we take 9×10^{12} molC yr^{-1} for non-
798 volcanic weathering, 3×10^{12} molC yr^{-1} for volcanic weathering (i.e. 25% of silicate weathering; k_{basfrac}
799 $= 0.25$), 8×10^{12} molC yr^{-1} for carbonate weathering, and 3×10^{12} molC yr^{-1} for seafloor weathering,
800 which we add to silicate weathering to give a total carbonate degassing 15×10^{12} molC yr^{-1} (more than
801 a doubling of carbonate degassing relative to the original model).

802 **2.4.3. Organic carbon cycle**

803 The total organic carbon burial flux in the original COPSE of 9×10^{12} molC yr^{-1} , comprising marine-
804 derived 4.5×10^{12} molC yr^{-1} and terrestrially-derived 4.5×10^{12} molC yr^{-1} components, is considerably

805 larger than in GEOCARB ($\sim 5 \times 10^{12}$ molC yr⁻¹) and in an earlier model based on organic carbon content
806 of sediments ($\sim 5 \times 10^{12}$ molC yr⁻¹) (Bernier and Canfield, 1989). However, it is comparable to other
807 models (Slomp and Van Cappellen, 2007) and less than some estimates $\geq 1 \times 10^{13}$ molC yr⁻¹ (Hedges
808 and Keil, 1995; Holland, 1978). Total organic carbon burial is counterbalanced by oxidative
809 weathering of organic carbon (7.75×10^{12} molC yr⁻¹) and organic carbon degassing (1.25×10^{12} molC yr⁻¹).
810 A potential problem with high estimates of organic carbon burial is that the corresponding
811 oxidative weathering flux is right at the upper limit (7.78×10^{12} molC yr⁻¹) of estimates for the supply
812 of organic carbon to weathering environments based on erosional rock flux and 0.4-0.6 wt% content
813 of sediments (Daines et al., 2017), allowing no scope for incomplete oxidative weathering (which is
814 widely recognised to occur and is assumed in COPSE). The discrepancy might be explained by a
815 larger metamorphic flux of organic carbon degassing and/or by relatively rapid recycling of
816 sedimentary organic carbon as thermogenic methane (Daines et al., 2017).

817 Terrestrial organic carbon burial is large in COPSE, but within the range of estimates for the
818 terrestrial contribution to organic carbon burial in marine (mostly deltaic) settings today of
819 $\sim 3.8 \pm 1.1 \times 10^{12}$ molC yr⁻¹, which we base on $\sim 80\%$ (Galy et al., 2015) of $\sim 4.8 \pm 1.4 \times 10^{12}$ molC yr⁻¹
820 (Burdige, 2005) being recent plant matter (the remaining $\sim 20\%$ being recycled ancient organic
821 matter, i.e. kerogen). With the revision to the pyrite burial flux suggested above, the C/S ratio by
822 mass of marine shales would be ~ 2.4 (assuming no terrestrial matter contributing), which is in the
823 range of Cenozoic-Quaternary values (Raiswell and Berner 1986), but this would be higher assuming
824 a (low S) terrestrial contribution to marine shales.

825 Given these considerations we view the original organic carbon burial and oxidative weathering
826 fluxes in COPSE as a 'high' set of estimates. As an alternative 'low' set of fluxes we follow Daines et
827 al. (2017) and consider 5×10^{12} molC yr⁻¹ total organic carbon burial, split 2.5×10^{12} molC yr⁻¹ marine
828 and 2.5×10^{12} molC yr⁻¹ terrestrially-derived, retaining 1.25×10^{12} molC yr⁻¹ organic carbon degassing
829 and therefore 3.75×10^{12} molC yr⁻¹ oxidative weathering.

830 (Note that when the marine and/or terrestrially-derived organic carbon burial fluxes are adjusted
 831 the corresponding baseline marine organic phosphorus burial and/or phosphorus burial with
 832 terrestrial matter, and phosphorus weathering fluxes are adjusted to retain steady state. Also the
 833 baseline nitrogen fixation flux is adjusted to counterbalance any change in organic nitrogen burial.)

834 **2.4.4. Phosphorus cycle**

835 The total phosphorus weathering flux in the original COPSE of 43.5×10^9 molP yr⁻¹ (of which 39×10^9
 836 molP yr⁻¹ went in reactive form to the ocean and 4.5×10^9 molP yr⁻¹ was buried with terrestrial
 837 matter) is in the range of estimates for reactive P flux to the ocean of $23\text{-}155 \times 10^9$ molP yr⁻¹
 838 (Compton et al., 2000) and in good agreement with a recent estimate of P weathering of 37×10^9
 839 molP yr⁻¹ (1144×10^9 gP yr⁻¹) (Hartmann et al., 2014). That estimate may be low given it assumes
 840 stoichiometric release of P with SiO₂ and cations, whereas there is evidence for preferential release
 841 of P by biotic weathering (Lenton et al., 2012; Quirk et al., 2015).

842 The apportioning of the phosphorus weathering flux in the original model of $k_{psilw} = 2/12$, $k_{pcarbw} =$
 843 $5/12$, $k_{poxidw} = 5/12$ was based on an association with the relative size of Fe-P, Ca-P and Org-P burial
 844 fluxes. On reflection, this overestimates the contributions of carbonate and especially oxidative
 845 weathering and underestimates the contribution of silicate weathering, which inputs P from the
 846 mantle (via volcanic rocks) and from the crust (via non-volcanic silicates). Recent detailed estimates
 847 suggest P weathering input comes 29% from volcanic rocks, 16% from plutonic and metamorphic
 848 rocks, 14% from carbonates, and 41% from non-carbonate sediments (which also contribute ~50% to
 849 total silicate weathering) (Hartmann et al., 2014). An upper limit on the contribution of oxidative
 850 weathering to reactive P flux to the ocean based on shale stoichiometry and complete P release is
 851 ~8-13% (Compton et al., 2000), however analysis of weathered shale sequences suggests
 852 sedimentary organic P is more resistant to release than organic C (Kolowitz and Berner, 2002),
 853 meaning this percentage should be lower. Given these considerations we suggest $k_{psilw} = 0.8$, $k_{pcarbw} =$
 854 0.14 , $k_{poxidw} = 0.06$ as an improved apportioning. Applying $k_{basfrac} = 0.35$ or 0.25 then gives a volcanic

855 weathering contribution of 28% or 20% to the P weathering flux, in reasonable agreement with the
856 29% inferred by (Hartmann et al., 2014).

857 The phosphorus burial fluxes in original COPSE of 18×10^9 molP yr⁻¹ as organic P (Org-P), 6×10^9 molP
858 yr⁻¹ as Fe-adsorbed P (Fe-P), and 15×10^9 molP yr⁻¹ as calcium-bound P (Ca-P) (i.e. a 46%:15%:39%
859 split of 39×10^9 molP yr⁻¹), are relatively low compared to more recent estimates and models (Slomp
860 and Van Cappellen, 2007), and the apportioning of P between sinks is questionable. More recent
861 modelling suggests Org-P 20×10^9 molP yr⁻¹, Fe-P 20×10^9 molP yr⁻¹, and Ca-P 40×10^9 molP yr⁻¹, i.e. a
862 25%:25%:50% split of 80×10^9 molP yr⁻¹ (Slomp and Van Cappellen, 2007). However, this represents a
863 considerable increase in P weathering flux relative to current estimates (Hartmann et al., 2014). A
864 smaller fraction of total P burial in organic form can help reconcile a larger total P burial flux with
865 measured (C:P)_{org} burial ratios ~200-250, which for Org-P $\sim 20 \times 10^9$ molP yr⁻¹ imply marine organic C
866 burial $\sim 4\text{-}5 \times 10^{12}$ molC yr⁻¹. However, a marine organic C burial flux of $\sim 2.5 \times 10^{12}$ molC yr⁻¹ (noting the
867 discussion above) is hard to reconcile with an organic P burial flux of $\sim 20 \times 10^9$ molP yr⁻¹ as this implies
868 a burial ratio (C:P)_{org} of ~ 125 close to the Redfield ratio. Given these considerations we view the
869 original P burial fluxes in COPSE as a plausible set of estimates. As an alternative apportioning of P
870 burial fluxes we consider: Org-P 10×10^9 molP yr⁻¹ (for Org-C 2.5×10^{12} molC yr⁻¹), Fe-P 10×10^9 molP yr⁻¹
871 ¹, and Ca-P 20×10^9 molP yr⁻¹, with a corresponding adjustment of the P weathering flux.

872 **2.5. Model implementation, initialisation and integration**

873 The model is now coded in Matlab and the 'stiff' system of coupled ODEs is efficiently computed
874 using a variable order ODE solver (Shampine and Reichelt, 1997). The model is initialised with the
875 reservoir sizes in Table 1 but spun up from 1000 Ma to 550 Ma to give the sedimentary reservoir
876 sizes time to adjust to the initial boundary conditions, in particular the differing Earth surface redox
877 balance prior to plants. In the original study only a 50 Myr spin-up was used, meaning that the
878 sedimentary (and to some degree sulphate) reservoirs were still adjusting during the early Paleozoic.
879 For the original model configuration, by 550 Ma, the longer spin-up leads to a $\sim 0.9 \times 10^{20}$ mol S or

880 $\sim 1.8 \times 10^{20}$ mol O₂ eq. ($\sim 50\%$) increase in the pyrite reservoir (**PYR**), and a $\sim 2 \times 10^{20}$ mol C ($\sim 16\%$)
881 decrease in the organic carbon reservoir (**G**), with a $\sim 0.5 \times 10^{20}$ mol S ($\sim 25\%$) or $\sim 1 \times 10^{20}$ mol O₂ eq.
882 decrease in the gypsum (**GYP**) reservoir and $\sim 1.6 \times 10^{20}$ mol C ($\sim 3\%$) growth in the carbonate carbon
883 reservoir (**C**). Thus the pyrite reservoir is predicted to have been roughly twice the size of the
884 gypsum reservoir at the onset of the Phanerozoic, which seems reasonable given predominantly
885 anoxic Precambrian oceans dominated by pyrite deposition, but some intervals of gypsum
886 deposition in the Paleoproterozoic and Neoproterozoic (Lenton and Daines, 2017).

887 **2.6. Comparison to data**

888 We compare the predictions of the various model versions to six proxy data compilation targets for:
889 CO₂, O₂, SO₄, $\delta^{13}\text{C}$, $\delta^{34}\text{S}$, and $^{87}\text{Sr}/^{86}\text{Sr}$, summarised in Table 6. The CO₂ proxy compilation (Royer,
890 2014) is derived from at least six different sources and although disagreement amongst the different
891 methods has been reduced in recent studies, there are still some notable discrepancies, only
892 partially captured by the ± 1 s.d. uncertainty range used here. There is also a lack of proxy data
893 prior to 420 Ma. The atmospheric O₂ mixing ratio reconstruction is based on the charcoal content of
894 coals (Glasspool and Scott, 2010) scaled by the assumption of a lower limit on O₂ consistent with
895 combustion of 15% and an uncertain upper limit consistent with continuous forests of 25-35%. Here
896 we extend the 15% lower limit back to 420 Ma based on the presence of earlier charcoal reviewed in
897 Lenton et al. (2016). Other studies would put the lower limit for self-sustaining combustion a little
898 higher at 16-17% (Belcher and McElwain, 2008). More fundamentally, the underlying assumption of
899 the method that more oxygen leads to more charcoal can be questioned, because charcoal is the
900 product of pyrolysis, hence more oxygen fuelling combustion could conceivably reduce charcoal
901 production. The other proxy data targets are more established. For SO₄ we consider only fluid
902 inclusion data (avoiding reconstructions based on sulphur isotopes). The carbonate $\delta^{13}\text{C}$ compilation
903 spans different organisms and depths which may generate some shifts in the record that do not
904 reflect a truly global signature (Saltzman and Thomas, 2012). For $\delta^{34}\text{S}$ we only consider carbonate

905 associated sulphate (CAS). The $^{87}\text{Sr}/^{86}\text{Sr}$ record is from conodont apatite, extending LOWESS V5
906 (McArthur et al., 2012) prior to 503 Ma with data from Cox et al. (2016).

907 **3. Results and Discussion**

908 The above considerations represent a potentially bewildering set of multiple changes to the COPSE
909 model. To clarify the effects of different changes we consider a series of cumulative changes to the
910 model. First we revisit the original model predictions in the light of new proxy compilations. Then we
911 look at the effect of updating the original forcing factors with the original model structure. Then we
912 consider the effects of changing the structure and some key functions of the model (that we
913 consider to be clear mechanistic improvements). Next we examine the effects of changing the
914 baseline fluxes. Then we explore the effect of optional additional forcing factors. From this we arrive
915 at an improved model with which we test some further mechanistic hypotheses for changes in the
916 model functions.

917 **3.1. Original model results in the light of new proxy compilations**

918 First we revisit the original model predictions (black dashed line in Fig. 5) in the light of updated
919 proxy records. Proxies for pCO_2 have generally been adjusted downwards since the original COPSE
920 study hence the original model predictions of pCO_2 now appear too high for much of the mid-late
921 Paleozoic (420-300 Ma), they are generally in the range of proxy uncertainty in the Mesozoic-
922 Cenozoic, but miss a Triassic peak around 240-200 Ma. The original model predictions of O_2 are too
923 low in the mid-Paleozoic (420-330 Ma), given the charcoal record at this time, reasonable from then
924 until 60 Ma, but too high for the rest of the Cenozoic (50-0 Ma including at present). The original
925 model predictions of SO_4 are reasonable for the Paleozoic but miss the Mesozoic-Cenozoic dip,
926 because the interactive partial calcium cycle misses a Mesozoic-Cenozoic [Ca] peak. Predicted $\delta^{13}\text{C}$
927 captures the early Paleozoic mean ~ 0 ‰ (although none of its extreme variability), but it misses the
928 persistent rise to $\sim +2$ ‰ that occurs in the Late Ordovician, and the (imposed) peak ~ 350 -280 Ma

929 does not match the observed structure well, although from ~200 Ma onwards the fit to the record is
930 better. Predicted $\delta^{34}\text{S}$ fits the data reasonably well, indicating that this proxy does not constrain SO_4
931 well. We do not expect the original model to capture $^{87}\text{Sr}/^{86}\text{Sr}$ variability, because e.g. it has no
932 distinction in the functional responses of volcanic and non-volcanic silicate rocks. It shows an overall
933 rise in $^{87}\text{Sr}/^{86}\text{Sr}$ driven by Rb decay, and captures some of the structure of variability e.g. at ~350 Ma,
934 because the original uplift forcing is derived from $^{87}\text{Sr}/^{86}\text{Sr}$ (but otherwise surprisingly little of it).
935 Major deficiencies are a failure to capture the high early Paleozoic $^{87}\text{Sr}/^{86}\text{Sr}$ and the Mesozoic low
936 followed by Cenozoic rise of $^{87}\text{Sr}/^{86}\text{Sr}$.

937 **3.2. Updating the original forcing factors**

938 Next we consider how the predictions of the original model are affected by updates to the original
939 forcing factors (Fig. 3) with the results in Figure 5. This mirrors the approach of some of the
940 intervening studies with COPSE (Lenton et al., 2012, 2016).

941 We show the combined effects of updating the degassing (*D*) and carbonate burial (*B*) forcing (blue
942 in Fig. 5), because they both operate on degassing. The updated degassing (*D*) is responsible for
943 increased CO_2 and O_2 250-130 Ma accompanied by slight increases in SO_4 and $\delta^{13}\text{C}$. The fit to CO_2
944 proxies 230-200 Ma and O_2 proxies 220-200 Ma is improved, but CO_2 is too high 160-140 Ma. The
945 updated carbonate burial (*B*) forcing tends to counteract the updated degassing forcing (*D*) during
946 150-0 Ma. Together they slightly lower CO_2 and O_2 during 120-90 Ma and 60-30 Ma somewhat
947 improving the fit to proxies. The updated uplift (*U*) forcing (red in Fig. 5) smooths out some of the
948 variability in model predictions and leads to higher Mesozoic-early Cenozoic CO_2 and O_2 predictions.
949 This generally improves the fit to CO_2 and O_2 proxies until ~130 Ma but degrades it ~120-50 Ma.

950 Combining the updated evolution (*E*), weathering (*W*) and CP_{land} forcing (green in Fig. 5) leads to an
951 earlier drawdown of CO_2 and earlier rise of O_2 , with a corresponding increase in $\delta^{13}\text{C}$ and SO_4 and
952 decrease in $\delta^{34}\text{S}$. The Late Ordovician drawdown of CO_2 to ~8.5 PAL is close to the threshold for
953 triggering Late Ordovician glaciations (Lenton et al., 2012; Pohl et al., 2014) and the fit to CO_2 proxies

954 410-370 Ma is much improved. The fit to O₂ proxies prior to 330 Ma is much improved, although O₂
 955 ~12% in the Silurian is still too low to explain the first charcoal 420-400 Ma. The corresponding
 956 increase in $\delta^{13}\text{C}$ to ~1 ‰ is less than the observed rise to ~2 ‰, which also requires some selective
 957 enhancement of P weathering by early plants (Lenton et al., 2016), explored below. The
 958 corresponding decline in $\delta^{34}\text{S}$ is at the lower end of the data range.

959 Combining all the preceding forcing updates (black in Fig. 5) retains the improvement in mid
 960 Paleozoic CO₂ and O₂ predictions associated with the rise of plants. It increases predicted CO₂ 310-
 961 270 Ma and 250-60 Ma and predicted O₂ prior to 50 Ma. Increased CO₂ 310-270 Ma degrades the
 962 predictions, they are improved 240-200 Ma, but are too high again 180-140 Ma and 100-60 Ma.
 963 Increased O₂ is too high 90-60 Ma and at scattered times beforehand e.g. at 300 Ma.

964 In the following we take forward these updates to the *D*, *U*, *E*, *W*, *B* and *CP_{land}* forcings. Later we
 965 return to reconsider the *CP_{land}* forcing alongside the coal depositional area forcing, as well as adding
 966 a selective P weathering forcing (*F*).

967 **3.3. Changing the baseline model structure**

968 In developing the model we isolated which structural changes to the model have the most significant
 969 effects on CO₂, O₂ and the other predicted variables. Here we summarise the key controls.

970 **3.3.1. Key controls on CO₂**

971 The effect of changes to the controls on weathering, which primarily affect CO₂, are summarised in
 972 Figure 6 (contrast the results to the black dashed line). The inclusion of seafloor weathering (blue)
 973 makes a large contribution to drawing down CO₂, consistent with it varying in line with degassing
 974 (which is generally elevated above present). Making basalt weathering independent of uplift (red)
 975 also tends to significantly lower CO₂ when uplift is below present through most of the Phanerozoic
 976 (except the early Paleozoic). Distinguishing different activation energies for granite and basalt
 977 weathering (cyan) tends to increase CO₂ consistent with a lower overall activation energy and

978 therefore weaker negative feedback on CO₂ especially in the early-mid Paleozoic when both uplift
979 and degassing are relatively high and therefore weathering flux is high. The new vegetation
980 dependence of weathering (green) generates markedly higher CO₂ from the origin of plants
981 onwards, consistent with the original function overestimating plant effects when $EW < 1$. The new
982 temperature function (magenta) noticeably lowers CO₂ in the mid-late Paleozoic and early Mesozoic.
983 Combining all these changes to the weathering response in the model (black) generally leads to
984 markedly lower CO₂ except ~400-350 Ma during the early rise of plants.

985 Changes to the model that alter CO₂ generally tend to alter O₂ in the same direction regardless of
986 whether they have direct effects on the redox balance, because of the link between weathering and
987 P input, and the link between CO₂, productivity and terrestrial organic carbon burial. The exception is
988 the new temperature function (magenta), which has minimal effect on O₂ and other variables
989 because it simply achieves the same weathering flux at a different CO₂ and temperature. Including
990 seafloor weathering (blue) has the largest individual effect on O₂, lowering it throughout because it
991 does not supply P whereas terrestrial weathering does (Mills et al., 2014b), and lowering it indirectly
992 because lower CO₂ suppresses terrestrial productivity. This makes early-mid Paleozoic O₂ too low but
993 fits the O₂ proxy better thereafter. Making basalt weathering independent of uplift (red) markedly
994 lowers O₂ from the late Paleozoic onwards, because lower CO₂ suppresses vegetation productivity,
995 and this improves the fit to the O₂ proxy. Distinguishing different activation energies for basalt and
996 granite weathering and thus lowering overall activation energy (cyan) increases O₂ when it increases
997 CO₂ (in the early Paleozoic and late Mesozoic-Cenozoic), degrading the fit to the O₂ proxy. The new
998 vegetation dependence of weathering (green) has small effects on O₂ despite consistently increasing
999 CO₂, because it has a counteracting direct effect of suppressing P weathering. Combining these
1000 changes (black) leads to markedly lower O₂ throughout, which is too low ~420-380 Ma.

1001 Effects on SO₄, $\delta^{13}\text{C}$ and $\delta^{34}\text{S}$ are modest and do not help to distinguish between mechanisms,
1002 although it is worth noting that including seafloor weathering (blue) lowers SO₄ throughout because

1003 terrestrial weathering fluxes, including gypsum weathering, are reduced, and making basalt
 1004 weathering independent of uplift (red) lowers SO_4 later in the Phanerozoic because CO_2 is reduced
 1005 and with it gypsum weathering. Effects on $^{87}\text{Sr}/^{86}\text{Sr}$ help evaluate these two mechanistic changes.
 1006 Including seafloor weathering (blue) lowers $^{87}\text{Sr}/^{86}\text{Sr}$, improving the Mesozoic-Cenozoic fit to the
 1007 data but degrading the Paleozoic fit. Making basalt weathering independent of uplift (red), leads to
 1008 lower $^{87}\text{Sr}/^{86}\text{Sr}$ in the late Paleozoic, Mesozoic and Cenozoic, improving the overall fit to the data.
 1009 Other changes have minor effects on $^{87}\text{Sr}/^{86}\text{Sr}$. Combining the changes (black) yields a reasonable fit
 1010 to the $^{87}\text{Sr}/^{86}\text{Sr}$ record from ~160 Ma onwards but $^{87}\text{Sr}/^{86}\text{Sr}$ is too low through almost all of the
 1011 Paleozoic and at present, consistent with a high initial choice of 0.35 for the volcanic rock fraction of
 1012 silicate weathering (Table 2), following Mills et al. (2014a).

1013 **3.3.2. Key controls on redox balance, O_2 , SO_4**

1014 Changes that primarily affect the model redox balance, O_2 , SO_4 and only secondarily impact CO_2 are
 1015 included in Figure 7 (again contrast the results to the black dashed line). Replacing the interactive Ca
 1016 cycle with a prescribed ocean [Ca] (blue) (to broadly match sparse fluid inclusion data) yields a
 1017 better fit to SO_4 data (as would be expected) and the Mesozoic-Cenozoic dip in SO_4 generates a
 1018 corresponding small reduction in O_2 . The new fire dependence of vegetation (red) has the greatest
 1019 effect on O_2 increasing it during the early rise of plants and decreasing it once O_2 exceeds PAL,
 1020 consistent with a stronger overall negative feedback on O_2 than in the original model. Removing the
 1021 O_2 dependence of pyrite weathering (cyan) slightly lowers early Paleozoic O_2 and slightly increases
 1022 O_2 after 350 Ma, consistent with the removal of a (weak) negative feedback. The secondary effects
 1023 of these changes on CO_2 are generally very small, with the exception that revising the fire
 1024 dependence of vegetation (red) increases the drawdown of CO_2 associated with the rise of early land
 1025 plants, because the effect of removing fires on vegetation biomass is assumed greater. Effects on
 1026 other predicted variables are modest. The new fire dependence of vegetation amplifies the initial
 1027 rise in $\delta^{13}\text{C}$ with early plants but damps down changes in $\delta^{13}\text{C}$ once O_2 exceeds PAL, consistent with
 1028 stronger negative feedback on organic carbon burial. It also has modest effects on SO_4 and $\delta^{34}\text{S}$.

1029 Removing the O₂ dependence of pyrite weathering (cyan) modestly increases SO₄ and lowers δ³⁴S in
1030 the early Paleozoic.

1031 **3.3.3. Combined effects**

1032 Combining the changes that affect the redox balance leads to similar results (not shown) to just
1033 updating the fire dependence of vegetation (red). Combining the changes affecting the redox
1034 balance with those affecting CO₂ (green in Fig. 7) shows that altering the weathering functions has
1035 the greatest effects. Other changes to the baseline model (Table 4) include the quadratic
1036 dependence of the atmospheric fraction of CO₂, the new anoxia, denitrification and Fe-P burial
1037 functions. These have minimal individual effects on our key data targets (not shown). When these
1038 additional changes are combined with all of those discussed above, we arrive at the new baseline
1039 model structure (black in Fig. 7) which can be compared to the original model structure (black
1040 dashed).

1041 Overall, the changes in model structure lead to lower predictions of CO₂ and O₂ throughout the
1042 Phanerozoic, with a similar pattern of variation (governed largely by the unchanged forcing factors).
1043 With the rise of the earliest plants, CO₂ drops closer to the first proxies at 420 Ma, and is in the range
1044 of the proxies 410-340 Ma, but remains too high 330-300 Ma. CO₂ is in the proxy range 290-240 Ma,
1045 but is at the lower end of the range or below it 230-100 Ma, when before it was generally too high.
1046 From 100-0 Ma the fit to the CO₂ proxies is somewhat improved. Early O₂ is too low, failing to rise to
1047 levels supporting combustion until ~380 Ma and not intersecting the proxy estimates until 330 Ma.
1048 Peak O₂ ~290 Ma is markedly reduced, but 280-240 Ma O₂ is too low. From 230-0 Ma the proxies are
1049 quite variable but predicted O₂ is broadly in the middle of the range with a much less pronounced
1050 Late Cretaceous peak, which previously was above the proxies. The Cenozoic O₂ decline reaches the
1051 present day value whereas previously it ended at 23% (~1.1 PAL). SO₄ predictions are improved by
1052 forcing with reconstructed [Ca] variations, but are a little below proxies 300-250 Ma, consistent with
1053 O₂ being too low at this time. δ¹³C is lowered somewhat throughout, particularly after the rise of

1054 land plants. $\delta^{34}\text{S}$ is relatively insensitive. The fit to the $^{87}\text{Sr}/^{86}\text{Sr}$ record is considerably improved in the
1055 Mesozoic-Cenozoic but degraded in the Paleozoic.

1056 **3.4. Changing the baseline fluxes**

1057 Here we apply alternative sets of model fluxes (Table 2) to the new baseline model (just described,
1058 including the updated D , U , E , W , B and CP_{land} forcing, and shown as the black dashed line), with the
1059 results shown in Figure 8.

1060 Introducing the 'high' set of sulphur fluxes including pyrite and gypsum degassing (blue) decreases
1061 atmospheric CO_2 throughout and decreases atmospheric O_2 from the rise of plants onwards. SO_4 is
1062 increased from the latest Paleozoic onwards, improving the fit to late Paleozoic data but missing low
1063 SO_4 in fluid inclusions at ~ 100 Ma. $\delta^{34}\text{S}$ is not greatly altered consistent with its insensitivity to SO_4 .
1064 $\delta^{13}\text{C}$ is lowered in the early-mid Paleozoic and increased from ~ 380 Ma onwards. $^{87}\text{Sr}/^{86}\text{Sr}$ is lowered
1065 slightly throughout. The effects on O_2 and CO_2 are predominantly due to the introduction of pyrite
1066 degassing, which always tends to decrease O_2 (the introduction of gypsum degassing tends to
1067 increase O_2 in the early Paleozoic but otherwise has little effect on CO_2 or O_2).

1068 Adopting the 'high' set of inorganic carbon fluxes (red) increases atmospheric CO_2 and O_2
1069 throughout the Phanerozoic. Atmospheric CO_2 is increased because seafloor weathering now makes
1070 up a smaller fraction of total terrestrial plus seafloor silicate weathering, and CO_2 has to adjust more
1071 for terrestrial silicate weathering to balance the carbon cycle (recalling that changes in degassing
1072 directly cause counterbalancing changes in seafloor weathering as well as there being a
1073 temperature-mediated negative feedback on seafloor weathering). Atmospheric O_2 is increased
1074 because the shift from seafloor to terrestrial weathering increases P input. Effects on SO_4 , $\delta^{13}\text{C}$ and
1075 $\delta^{34}\text{S}$ are modest. There is a striking overall increase in $^{87}\text{Sr}/^{86}\text{Sr}$ due largely to a decrease in the
1076 volcanic rock fraction of silicate weathering from 0.35 to 0.25 (Table 2), which improves the fit to the
1077 data, particularly in the Paleozoic and at present.

1078 Adopting the 'low' set of organic carbon fluxes (green) produces lower O₂ throughout. δ¹³C is
1079 generally lowered consistent with a smaller organic fraction of total carbon burial, but from ~280 Ma
1080 onwards is notably below the long-term mean of +2 ‰. The lower O₂ allows plants to be more
1081 productive and amplify silicate weathering more, thus lowering CO₂ from ~380 Ma onwards. SO₄ is
1082 lowered in the early-mid Paleozoic and δ³⁴S increased. ⁸⁷Sr/⁸⁶Sr is increased slightly throughout.

1083 Changing the split of P weathering (cyan) leads to higher O₂ almost all the time except ~350-310 Ma.
1084 This reflects the majority of P weathering now being linked to silicate weathering which is generally
1085 above present due to elevated degassing. Hence the biggest increases in O₂ are generally when
1086 degassing is highest in the early Paleozoic and Mesozoic. δ¹³C is correspondingly increased at these
1087 times, improving fit to the Mesozoic data. CO₂ is increased from ~270 Ma onwards, because the
1088 higher O₂ tends to suppress vegetation and its effect on silicate weathering and this arguably
1089 improves fit to the proxy data. Effects on SO₄ and δ³⁴S are small. Changing the apportioning of P
1090 burial fluxes has tiny effects (not shown).

1091 Relative to the new baseline (black dashed), a combined update of the fluxes (black) comprising high
1092 S fluxes, high inorganic carbon fluxes, low organic carbon fluxes, revised split of P weathering and
1093 revised split of P burial fluxes, yields increased atmospheric CO₂ in the early-mid Paleozoic and
1094 particularly the Mesozoic-Cenozoic, the latter improving fit to the proxies 230-110 Ma (but
1095 degrading it 100-60 Ma). It yields an increase in early Paleozoic O₂, improving fit to the constraints,
1096 similar values ~350-300 Ma, and somewhat higher O₂ ~250-0 Ma. SO₄ is somewhat higher
1097 throughout and δ³⁴S variations are reduced. δ¹³C is higher in the early Paleozoic and Mesozoic
1098 improving fit to the long-term mean. ⁸⁷Sr/⁸⁶Sr is increased markedly throughout, considerably
1099 improving the (still poor) fit to data.

1100 3.5. Introducing new forcing factors

1101 We now take forward the new baseline model with this updated set of fluxes and the updated D , U ,
1102 E , W , B and CP_{land} forcing (black dashed line), and consider the effect of additional forcing factors,
1103 with the results shown in Figure 9.

1104 Basalt area forcing (blue), which is relatively low in the early-mid Paleozoic, tends to increase CO_2
1105 until the East European craton event at ~ 380 Ma temporarily lowers it. CO_2 remains somewhat
1106 increased until the ~ 250 Ma Siberian traps emplacement, and then is decreased from the
1107 emplacement of the Central Atlantic Magmatic Province (CAMP) at ~ 200 Ma onwards, which creates
1108 greater than present volcanic rock area. The corresponding effect on $^{87}Sr/^{86}Sr$ is to increase it in the
1109 Paleozoic and decrease it in the Mesozoic-Cenozoic, which improves the overall fit to the data,
1110 including capturing the Phanerozoic minimum of $^{87}Sr/^{86}Sr$ in the Jurassic. Effects on O_2 , SO_4 , $\delta^{13}C$ and
1111 $\delta^{34}S$ are minimal.

1112 Granite forcing (red), which is relatively high throughout the Paleozoic and early Mesozoic, tends to
1113 markedly decrease CO_2 until ~ 150 Ma, generally improving fit to proxy CO_2 except in the Triassic.
1114 $^{87}Sr/^{86}Sr$ is increased until ~ 100 Ma considerably improving the fit to data in the Paleozoic. O_2 is
1115 slightly lowered 400-200 Ma degrading the fit to constraints. SO_4 is somewhat lowered prior to ~ 150
1116 Ma improving the fit to this proxy. Effects on $\delta^{13}C$ and $\delta^{34}S$ are small.

1117 Paleogeography forcing (cyan) has marked effects of increasing CO_2 at two particular times of
1118 reduced runoff and dry continental interiors; in the early Paleozoic when there is a lack of proxy
1119 constraints, and in the Permian-Triassic-Jurassic (~ 300 -150 Ma). The pronounced Triassic CO_2 peak
1120 better fits proxy data. Increased CO_2 represents a readjustment of climate to achieve the same
1121 weathering flux. Hence effects on O_2 , SO_4 , $\delta^{13}C$, $\delta^{34}S$ are minor, with only a slight dip in $^{87}Sr/^{86}Sr$,
1122 meaning these tracers do not provide a further test of the forcing.

1123 Coal depositional area forcing combined with a ramping down of the CP_{land} forcing over 345-300 Ma
1124 (green) generates an increase in O_2 over 320-240 Ma with a Carboniferous-Permian O_2 peak centred
1125 on ~300 Ma that improves the fit to the charcoal-based proxy. $\delta^{13}C$ is increased 330-230 Ma
1126 reflecting increased organic carbon burial. A corresponding peak in CO_2 is generated which is above
1127 proxies. Effects on SO_4 , $\delta^{13}C$ and $\delta^{34}S$ are minimal.

1128 Including an interval of elevated selective weathering of P over 465-400 Ma (together with a
1129 combination of all the other new forcing factors; black), generates a 'hump' in atmospheric O_2 and
1130 $\delta^{13}C$, improving consistency with the earliest charcoal record ~420 Ma onwards, and producing the
1131 observed $\delta^{13}C + 2 \text{‰}$, as well as oxygenating the ocean (Lenton et al., 2016). SO_4 is also somewhat
1132 increased and $\delta^{34}S$ somewhat decreased at this time.

1133 The combination of all the new forcing factors (black), relative to the model without them (black
1134 dashed), yields markedly lower early Paleozoic CO_2 and higher Permian-Triassic CO_2 . The overall fit to
1135 the $^{87}Sr/^{86}Sr$ record is markedly improved although it is still too low in the earliest Paleozoic and
1136 misses a pronounced dip in the Permian. Atmospheric O_2 and $\delta^{13}C$ are noticeably improved in parts
1137 of the Paleozoic.

1138 With all the various updates to the baseline model, the sedimentary reservoirs behave somewhat
1139 differently, with slightly greater growth of the organic carbon reservoir and notably greater
1140 shrinkage of the pyrite sulphur reservoir over Phanerozoic time, leading to normalised reservoir sizes
1141 of $g=1.075$, $c=0.98$, $pyr=0.75$, $gyp=1.25$ at present. Much of the deviation from assumed present day
1142 reservoir sizes is due to the introduction of pyrite and gypsum degassing fluxes, and a Mesozoic
1143 interval of elevated sulphur degassing in which the gypsum reservoir grows at the expense of the
1144 pyrite reservoir. However, as the present day sedimentary reservoirs are not that well known and
1145 the predictions of surface redox reservoirs of oxygen and sulphate are relatively insensitive to
1146 changing the sedimentary reservoir initialisation, we conclude that this mismatch is not a major
1147 concern.

1148 **3.6. Testing hypotheses**

1149 Taking the revised baseline model subject to both the updated original forcing factors and the new
 1150 forcing factors (black dashed line in Figs. 10-12) we now consider some key uncertainties regarding
 1151 controls on CO₂ and alternative hypotheses for controls on O₂.

1152 **3.6.1. Controls on weathering and CO₂**

1153 We start with key controls on terrestrial and seafloor weathering and hence CO₂ (Fig. 10).

1154 In GEOCARB III, Berner switched from the use of $k_{15} = 0.15$ (~7-fold amplification of weathering by
 1155 plants) to $k_{15} = 0.25$ (4-fold amplification by vascular plants relative to moss/lichen cover) based
 1156 mostly on a field study in Iceland (Moulton et al., 2000). He also explored $k_{15} = 0.1$ (10-fold
 1157 amplification). In COPSE, $k_{15} = 0.25$ (blue) predictably leads to lower early Paleozoic CO₂ ~6-7 PAL
 1158 (and lower temperatures ~16 °C, as opposed to ~18 °C with $k_{15} = 0.15$). After the rise of the first
 1159 plants CO₂ drops to ~5 PAL which is just below proxies at 420 Ma. Using $k_{15} = 0.1$ (red) gives higher
 1160 early Paleozoic CO₂ ~14-18 PAL (and higher temperatures ~20 °C). The rise of the first plants draws
 1161 CO₂ down to ~7 PAL, which is consistent with Late Ordovician glaciations (Lenton et al., 2012) and
 1162 whilst high at 420 Ma is within the 410-390 Ma proxy range. The CO₂ predictions for $k_{15} = 0.1$ are
 1163 considerably lower than in GEOCARB III for the same parameter setting presumably because COPSE
 1164 includes a second negative feedback on CO₂ from seafloor weathering, which plays a more
 1165 significant role when abiotic weathering (k_{15}) is lower. This can help explain why decreasing k_{15} and
 1166 increasing CO₂ gives slightly lower Paleozoic O₂, because now seafloor weathering makes up a larger
 1167 fraction of the CO₂ removal flux but is not a source of P. It also explains why early Paleozoic ⁸⁷Sr/⁸⁶Sr
 1168 is somewhat lowered. Conversely increasing k_{15} and lowering CO₂ gives slightly higher Paleozoic O₂,
 1169 because continental weathering is now a larger fraction of the CO₂ removal flux with a
 1170 correspondingly increased source of P, and ⁸⁷Sr/⁸⁶Sr is somewhat increased. Early Paleozoic SO₄
 1171 shows a small change in the same direction as O₂ but there is no significant effect on δ³⁴S or δ¹³C.
 1172 Thus the best chance to evaluate the strength of the biotic weathering effect is from comparison to

1173 CO₂ proxies, which are most consistent with the default ~7-fold amplification of weathering ($k_{15} =$
1174 0.15).

1175 Making weathering dependent on vegetation NPP rather than biomass (green) removes any effect of
1176 fires suppressing weathering by suppressing biomass. This leads to a somewhat slower drawdown of
1177 CO₂ with the early rise of plants (because the beneficial effect of fewer fires on vegetation now does
1178 not affect weathering). There are markedly smaller CO₂ variations after the rise of plants, and
1179 correspondingly a more stable temperature, reflecting a more effective negative feedback on CO₂
1180 and climate when it is not affected by O₂ variations. Effects on O₂ are tiny, whereas there are small
1181 but noticeable effects on $\delta^{13}\text{C}$ because carbon isotope fractionation is assumed to be sensitive to
1182 CO₂ level. There are no significant effects on $^{87}\text{Sr}/^{86}\text{Sr}$, SO₄, or $\delta^{34}\text{S}$. Hence the best evaluation is
1183 against CO₂ proxies, which are better fitted in the latest Paleozoic, but the model predictions appear
1184 rather low in parts of the Jurassic-Cretaceous.

1185 Giving seafloor weathering stronger temperature sensitivity (cyan) generally lowers CO₂, O₂ and
1186 $^{87}\text{Sr}/^{86}\text{Sr}$ except in the late Paleozoic. It is unclear whether overall this improves the fit to data.

1187 Removing the temperature sensitivity of seafloor weathering (magenta) markedly increases CO₂ and
1188 O₂ and somewhat increases $^{87}\text{Sr}/^{86}\text{Sr}$. This creates Permian-Triassic CO₂ levels above the proxies and
1189 increases late Cretaceous-early Cenozoic CO₂ above proxies.

1190 Varying climate sensitivity (Fig. 11) predominantly affects CO₂ predictions. O₂, $\delta^{13}\text{C}$ and SO₄ change in
1191 the same direction as CO₂ but by relatively small amounts. Prior to the rise of plants, temperature
1192 changes in the opposite direction to CO₂, because they are jointly determining the abiotic
1193 weathering flux (e.g., a decrease in climate sensitivity lowers the temperature requiring an increase
1194 in CO₂ and temperature to attain the same weathering flux, but because both CO₂ and temperature
1195 increase the weathering flux, the temperature does not have to increase to its original value). After
1196 the rise of plants, temperature predictions are little altered, because the biotic weathering flux is
1197 controlled by temperature and insensitive to CO₂ (as the Michaelis-Menten response of plants tends

1198 to be saturated) hence variations in climate sensitivity alter CO₂ to achieve roughly the same
1199 temperature. Halving the climate sensitivity to 1.5°C (blue) demands much larger increases in CO₂
1200 throughout to maintain balance in the carbon cycle, putting predicted CO₂ well above proxies most
1201 of the time, and can be ruled out on these grounds. Early Paleozoic temperature is also decreased
1202 from ~18°C to ~15°C (not shown), although early Paleozoic ⁸⁷Sr/⁸⁶Sr is increased, slightly improving
1203 the fit to data. A more modest decrease in climate sensitivity to 2.25°C (green) is more consistent
1204 with the CO₂ proxies, indicating that they help provide a lower bound on climate sensitivity (Royer et
1205 al., 2007). Doubling the climate sensitivity to 6°C (red) lowers CO₂ throughout, putting it below
1206 proxies in the early Devonian and mid Triassic, although the fit is improved at some other times.
1207 Early Paleozoic temperature is increased from ~18°C to ~22°C (not shown), but early Paleozoic
1208 ⁸⁷Sr/⁸⁶Sr is decreased, further degrading the already poor fit to data. A more modest increase in
1209 climate sensitivity to 4.5°C (cyan) is more consistent with the wider literature (IPCC, 2013) and
1210 provides a somewhat better fit to CO₂ proxies than with a 6°C climate sensitivity. Hence we consider
1211 2.25-4.5°C as a reasonable uncertainty range on climate sensitivity.

1212 **3.6.2. Controls on O₂**

1213 Turning to controls on O₂ we first tried removing the dependence of oxidative weathering of organic
1214 carbon on O₂ as suggested by Berner (2006a). However, this causes O₂ levels to drop to zero (not
1215 shown), with the long model spin-up (and this also happens in the original model 'run 3' of Bergman
1216 et al., 2004, when using our longer spin-up). The reason is a simple lack of negative feedback on O₂,
1217 and given evidence for an O₂ sensitivity of oxidative weathering we retain it in the model.

1218 The results of testing other hypotheses for controls on O₂ are summarised in Figure 12.

1219 Next we tested the effects of Berner's (2006a) proposal that organic carbon burial is predominantly
1220 controlled by erosion. Forcing terrestrial-derived organic carbon (and phosphorus) burial with
1221 uplift/erosion (blue) leads to lower predicted O₂ when uplift is below present, especially in the
1222 Triassic-Jurassic, although O₂ is still sufficient to sustain combustion at this time. CO₂ is also lowered

1223 from 330 Ma onwards degrading the fit to proxies in the Mesozoic. $\delta^{13}\text{C}$ is lowered when uplift is
1224 below present because the reduction in terrestrial-derived organic carbon burial causes a
1225 corresponding reduction in total organic carbon burial. Forcing marine organic carbon burial with
1226 uplift/erosion (red) leads to almost identical effects on O_2 . Effects on CO_2 are also comparable.
1227 However, there is little effect on $\delta^{13}\text{C}$ because the reduction in O_2 levels leads to a compensatory
1228 increase in terrestrial productivity and terrestrially-derived organic carbon burial. Forcing both
1229 marine and terrestrial-derived organic carbon burial with uplift/erosion (green) (leaving only burial
1230 of terrestrial material in coal basins independent of uplift) leads to markedly lower O_2 especially in
1231 the later Triassic-Jurassic when it is insufficient to sustain combustion and therefore inconsistent
1232 with the charcoal record. CO_2 is also lowered from 330 Ma onwards, because there is less
1233 suppression of vegetation by fire and therefore faster weathering, and is well below proxies through
1234 much of the Mesozoic. $\delta^{13}\text{C}$ is markedly lowered and clearly below the proxy record in the Triassic.
1235 Given these deficiencies we rule out this model version.

1236 Finally we considered alternative marine-based feedbacks on atmospheric oxygen. Including a direct
1237 feedback of O_2 on marine organic carbon burial (cyan) leads to smaller O_2 variations overall,
1238 including an early Paleozoic increase and slight lowering of later peaks, consistent with an additional
1239 negative feedback (some small CO_2 effects go along with this). However, early Paleozoic $\delta^{13}\text{C}$ is
1240 increased and $\delta^{34}\text{S}$ decreased away from the proxy data. Including Van Cappellen and Ingall's (1996)
1241 feedback of anoxia on $(\text{C}/\text{P})_{\text{organic}}$ burial ratio (magenta) increases early Paleozoic O_2 , but has no
1242 effect after the rise of plants because anoxia never significantly returns to the ocean. It also
1243 increases early Paleozoic $\delta^{13}\text{C}$ and decreases early Paleozoic $\delta^{34}\text{S}$ away from the proxy data. Including
1244 anoxia-sensitive Ca-P burial has almost identical effects on O_2 and the other variables as the Van
1245 Cappellen and Ingall (1996) feedback (hence is not shown).

1246 3.7. Robust features and remaining uncertainties

1247 We present the new baseline model run and a summary of the preceding uncertainty analysis
1248 (Section 3.6) as a grey shaded area around it in Figure 13; adding the variables of global
1249 temperature, anoxic fraction, ocean nitrate and ocean phosphate concentration, to pCO₂ (PAL) and
1250 plotting pO₂ (PAL) rather than mixing ratio (%). The greatest uncertainty for most of these variables
1251 is, appropriately, in the early Paleozoic. This summary figure and the full set of earlier model results
1252 allow us to establish which model predictions withstand testing against proxy data and are robust to
1253 current uncertainties, and which critical uncertainties remain that could be targeted by future work.
1254 We arrange this chronologically into phases in the development of the Phanerozoic Earth system.

1255 Phase 1 is the early Paleozoic, specifically the Cambrian and the early Ordovician prior to the rise of
1256 land plants (~550-465 Ma). Atmospheric CO₂ levels at this time are particularly uncertain due to a
1257 lack of proxies and because COPSE cannot reproduce the unusually high ⁸⁷Sr/⁸⁶Sr. This suggests that
1258 despite the assumed much greater non-volcanic silicate rock area and much smaller volcanic rock
1259 area relative to the present, we are still missing a yet more radical change in lithology (e.g. ongoing
1260 effects of the pan-African orogeny; Godd ris et al., 2017) or a marked reduction in hydrothermal
1261 input of Sr (which might imply lower degassing than assumed). Global temperature predictions from
1262 such a simple model should be viewed as ‘zeroth-order’ given that many climatic factors are not
1263 included. Nevertheless relatively warm predicted temperatures of 16-21 C are broadly consistent
1264 with no ice at the poles in the Cambrian-early Ordovician.

1265 The model robustly predicts low atmospheric O₂ ~0.2 (0.1-0.4) PAL or ~5 (3-10) % mixing ratio and
1266 widespread ocean anoxia in the early Paleozoic, supported by low $\delta^{13}\text{C}$ and high $\delta^{34}\text{S}$ (as well as
1267 several independent redox proxies). In the model, the principal O₂ regulator around ~0.2 PAL is the
1268 oxygen sensitivity of oxidative weathering, as postulated for much of the Proterozoic as well as the
1269 earliest Phanerozoic (Daines et al., 2017). The upper part of the O₂ uncertainty range includes
1270 additional marine-based negative feedbacks on O₂, but we consider these O₂ values and the

1271 corresponding feedbacks less plausible because they tend to increase predicted $\delta^{13}\text{C}$ and decrease
1272 predicted $\delta^{34}\text{S}$ away from the data. Such low $\text{O}_2 \sim 0.2$ PAL is still consistent with the estimated
1273 metabolic needs of the Cambrian fauna (Sperling et al., 2015a). The high predicted anoxic fraction
1274 should be viewed semi-quantitatively given the schematic nature of the function. Nevertheless
1275 complex models show that the deeper ocean would be mostly anoxic for $\text{O}_2 \sim 0.2$ PAL and limiting
1276 nutrient concentration near present levels, assuming a biological carbon pump (Lenton and Daines,
1277 2017). The large increase in anoxia relative to today qualitatively alters the predicted nutrient
1278 balance of the early Paleozoic ocean, supporting a much larger increase in water-column
1279 denitrification and a corresponding increase in phosphate relative to the Redfield ratio, such that
1280 nitrogen fixation can balance denitrification. The prediction of high ocean $[\text{PO}_4]$ is consistent with
1281 evidence from iron formations combined with the inference of high ocean $[\text{Si}]$ (Planavsky et al.,
1282 2010). It does not, however, equate to higher new production or organic carbon burial in COPSE,
1283 because available nitrogen (the limiting nutrient) is at comparable levels to today. The early
1284 Paleozoic ocean is predicted to be 'non-Redfieldian' with $\text{N/P} \sim 5-6$ (rather than today's $\text{N/P} \sim 14$),
1285 consistent with the response of nitrogen cycling to anoxic oceans in the GENIE model (Lenton and
1286 Daines, 2017).

1287 Phase 2 is the mid Paleozoic rise of land plants, spanning the Late Ordovician-Silurian-Devonian-early
1288 Carboniferous ($\sim 465-350$ Ma). Assuming early Paleozoic CO_2 and temperature were relatively high, a
1289 two-phase drawdown of atmospheric CO_2 and temperature – in the Late Ordovician and Devonian-
1290 early Carboniferous – best fits available proxy data. The model associates the first drawdown phase
1291 with the rise of the earliest non-vascular plants and the second with the rise of rooted vascular
1292 plants (including trees). It also supports a large amplification of weathering rates by vegetation,
1293 likely greater than the factor of 4 used in GEOCARBSULF and potentially up to a factor of 10.
1294 Predicted Late Ordovician CO_2 levels are sufficiently low to explain glaciation at this time, which
1295 thanks to the unusual paleogeography could have been abruptly triggered at relatively high global
1296 temperature (Pohl et al., 2014; Pohl et al., 2016). COPSE predicts the second phase of CO_2 drawdown

1297 associated with the rise of vascular plants 400-350 Ma caused greater global cooling (partly a simple
1298 consequence of the natural logarithmic dependence of temperature on CO₂). This produces the
1299 lowest predicted global temperatures of the Phanerozoic, consistent with the longest-lived interval
1300 of glaciations stretching to the lowest latitudes being during the Carboniferous-Permian.

1301 A 'mid-Paleozoic oxygenation event' is robustly predicted, i.e. a major rise in atmospheric O₂ and
1302 associated oxygenation of the ocean due to the rise of land plants. This represents a change in the
1303 oxygen regulation regime, from the predominant negative feedback being on the sink of oxygen
1304 (oxidative weathering) to being on the source (organic carbon burial). This requires a substantial
1305 secular increase in organic carbon burial, which is here associated with the earliest, non-vascular
1306 land plants (Lenton et al., 2016) (unlike in the original COPSE model where it is associated with the
1307 later evolution of trees). Others argue that earliest plant productivity and/or effects on weathering
1308 could not have been large enough to affect such a change (Edwards et al., 2015; Quirk et al., 2015),
1309 but we have yet to find any other way of reproducing the secular changes observed in the multi-
1310 proxy record, including the appearance of fossil charcoal by ~420 Ma. The predicted rise of oxygen
1311 and oxygenation of the oceans continues with the rise of rooted, vascular plants, but as the oxygen
1312 regulation regime has already shifted it proves harder for them to cause changes in atmospheric O₂.
1313 The predicted dip in O₂ and reassertion of ocean anoxia at ~395 Ma is a consequence of the imposed
1314 phosphorus weathering forcing designed to reproduce a transient drop in $\delta^{13}\text{C}$ at this time, but O₂
1315 goes too low given that there is charcoal through this interval (Lenton et al., 2016). It serves to
1316 illustrate that the Earth surface redox state could have been particularly sensitive during this
1317 oxygenation transition, although the real Earth system had anoxic events later in the Devonian
1318 (Algeo and Scheckler, 1998).

1319 With plants established, the model Earth system thereafter is in a regime where atmospheric CO₂
1320 tends to be regulated most strongly against decreases (i.e. regulation against a lower limit) and O₂
1321 against increases (i.e. regulation against an upper limit). There are subsequent variations in both CO₂

1322 and O₂ but they are smaller than the mid-Paleozoic transition, and tend to be reversible rather than
1323 one-way changes (albeit very long-lived). Consequently, we treat the rest of the Phanerozoic as
1324 'Phase 3', but we divide it into two parts based on two modelled CO₂ and O₂ positive excursions.

1325 Phase 3a is the late Paleozoic-early Mesozoic, spanning the Carboniferous-Permian-Triassic (~350-
1326 200 Ma) and including the finale of supercontinent (Pangea) formation. There is a broad predicted
1327 peak of CO₂ in this interval, rising through the later Carboniferous and Permian to a Triassic peak.
1328 However, predicted atmospheric CO₂ is particularly uncertain because the model cannot reproduce
1329 the marked Permian drop in ⁸⁷Sr/⁸⁶Sr, which may indicate uncaptured changes in degassing or
1330 lithology. Paleogeography forcing (a particularly dry supercontinent interior) can help explain the
1331 Triassic peak seen in CO₂ proxies, as would a decoupling of seafloor weathering from surface
1332 temperature changes, or a reduction in climate sensitivity. Subsequently the model predicts a CO₂
1333 minimum at ~200 Ma around the Triassic-Jurassic boundary which is not seen in proxies. The CO₂
1334 drop is due to a mix of LIP emplacement (CAMP), a dip in reconstructed degassing, and a rapid
1335 recovery of wetter continental weathering conditions. Part of the problem with the model here is
1336 that the CAMP is assumed to weather too rapidly as there is an excessively rapid negative shift in
1337 ⁸⁷Sr/⁸⁶Sr.

1338 The model predicts a peak in O₂ ~1.35 (1.3-1.4) PAL or ~26.5 (25.5-27) % mixing ratio, centred on
1339 ~290 Ma and associated with the Carboniferous-Permian interval of coal deposition. This is
1340 comparable to the O₂ peak predicted in the original COPSE (Bergman et al., 2004), but below the
1341 ~35% (Berner and Canfield, 1989) or ~30% (Berner, 2006a) peak levels predicted with other models.
1342 O₂ drops to a predicted minimum ~1 (0.85-1.05) PAL or ~21 (18-22) % mixing ratio centred on ~200-
1343 190 Ma, which is associated with low organic carbon burial rates including a hiatus in coal deposition
1344 during the Triassic. This is consistent with the charcoal record which shows that O₂ was sufficient to
1345 sustain combustion at this time, and in the model this requires that no more than about half of total
1346 organic carbon burial can be controlled by erosion. The maximum and minimum in O₂ are linked to a

1347 corresponding predicted maximum and broad minimum in $\delta^{13}\text{C}$. The predicted $\delta^{13}\text{C}$ fluctuations are
1348 comparable in size to those seen in the data compilation, but COPSE does not reproduce the timing
1349 and higher frequency of those $\delta^{13}\text{C}$ fluctuations well, hence the real O_2 record may have exhibited
1350 more fluctuations of different timing, albeit within similar bounds. A rise in SO_4 to a Permian peak is
1351 also predicted, which is due partly to rising O_2 but mostly to an assumed decline in ocean $[\text{Ca}]$, which
1352 then reverses in the Late Permian.

1353 Phase 3b is the mid-late Mesozoic and Cenozoic, spanning the Jurassic-Cretaceous-Paleogene-
1354 Neogene (~ 200 -0 Ma), and including the rise of calcareous phytoplankton and the break-up of the
1355 supercontinent (Pangea) – with increasing uplift and a peak then decline in degassing. The model
1356 captures an overall peak then decline of CO_2 driven by the peak in degassing (and to some degree
1357 the rise of uplift), but it does not capture the finer scale structure suggested by the proxy
1358 compilation. The Phanerozoic minimum and then major rise in $^{87}\text{Sr}/^{86}\text{Sr}$ is reasonably well captured
1359 and attributable to both a decline in degassing causing a decline in hydrothermal Sr input (and shift
1360 from seafloor to terrestrial weathering) and a decoupling of volcanic weathering from uplift such
1361 that as uplift increases there is a marked shift from weathering of volcanic rocks to ancient cratons
1362 (Mills et al., 2014a). The broad global temperature peak in the Late Cretaceous is consistent with
1363 paleoclimate reconstructions. The subsequent Paleocene-Eocene peak in temperature is missing,
1364 because the model fails to predict a peak in CO_2 at this time, and it also fails to capture
1365 corresponding stable values of $^{87}\text{Sr}/^{86}\text{Sr}$ (followed by an accelerated rise). Together these
1366 deficiencies may indicate an unresolved Paleocene-Eocene peak in degassing and hydrothermal Sr
1367 input. The model does predict a cooling at ~ 35 Ma (near the Eocene-Oligocene boundary) due to LIP
1368 emplacement (the 'Afar' event) driving a CO_2 decline.

1369 A broad Late Cretaceous (~ 90 -70 Ma) peak of $\text{O}_2 \sim 1.3$ (1.15-1.5) PAL or ~ 26 (23.5-28.5) % mixing
1370 ratio is robustly predicted, albeit at lower O_2 levels than in the original model. It is driven by a peak
1371 in degassing and consistent with abundant Cretaceous charcoal. The predicted Cenozoic decline in

1372 O₂ is robust. A corresponding predicted decline in $\delta^{13}\text{C}$ is consistent with proxies but due more to
1373 changing isotope fractionation than to a decline in organic carbon burial.

1374 **4. Conclusion: forward look**

1375 The process of revising the COPSE model and comparing its predictions to proxy data reveals a mixed
1376 picture with regard to constraining the forcing factors and mechanisms at play in controlling
1377 Phanerozoic CO₂ and O₂ variations. Trying to reproduce the long timescale structure of ⁸⁷Sr/⁸⁶Sr does
1378 help constrain key processes of seafloor weathering and the decoupling of volcanic weathering from
1379 uplift that control both CO₂ and O₂ levels. Trying to reproduce the $\delta^{13}\text{C}$ record helps constrain past
1380 O₂ variations. However, predicting $\delta^{34}\text{S}$ offers little constraint on O₂ or even SO₄, and whilst
1381 predicting SO₄ offers some weak constraint on O₂ it is more sensitive to (prescribed) ocean [Ca].
1382 Hence in future there is a need to explore a wider range of proxy data targets to see if they can help
1383 constrain model mechanisms and forcing factors. This in turn may invite a more spatially-resolved
1384 modelling approach for those proxies (e.g. of ocean redox state) that are clearly influenced by both
1385 local and global processes and which hence it is difficult to treat in a globally-averaged way.

1386 Clearly a simplified box model such as COPSE is not expected to capture all features of the proxy
1387 record. More spatially elaborate models are already being used to examine past changes in
1388 weathering (Donnadieu et al., 2006; Godd ris et al., 2014) and in ocean composition (Lenton and
1389 Daines, 2017). In principle a simple model can be calibrated on the results of more realistic complex
1390 models, as is done e.g. for the global temperature function from GEOCARBSULF used here. Equally
1391 new forcing factors can be introduced to represent things not resolved by a simple model, for
1392 example the paleogeography forcing developed for GEOCARBSULF and applied here. However
1393 adding such forcing factors detracts from the transparency of a simplified approach and it runs the
1394 risk of over-fitting it to available data. If one can almost as easily run a more realistic, spatially-

1395 resolved model then that may be a better way to go. Indeed we are developing a framework
1396 whereby more elaborate box models can be coupled together and applied to deep time questions.

1397 We have also begun to extend the application of COPSE further back in time to simulate changes in
1398 the Proterozoic Earth system (Daines et al., 2017; Mills et al., 2014b). Further work is needed to
1399 capture Precambrian forcing, including a more generic approach to the effects of the super-
1400 continent cycle on degassing, uplift and LIPs, and the effects of the Earth's decaying internal heat
1401 source on degassing. Equally the nature of redox and nutrient cycling in a more anoxic ocean needs
1402 elaboration. In principle the model could be extended even further back in time through the Great
1403 Oxidation, but this would require some representation of the contribution of methane (and
1404 potentially other greenhouse gases) to global temperature.

1405 The results of the present study suggest that there was a major, potentially two-phase, drawdown of
1406 atmospheric CO₂ with the rise of land plants and associated cooling in the Late Ordovician and
1407 Devonian-early Carboniferous. Thereafter atmospheric CO₂ was well regulated, particularly against
1408 decreases, but there were peaks in the Triassic and mid-Cretaceous. Not all of the structure in the
1409 CO₂ proxy record is captured, which given its strong dependence on forcing factors suggests that
1410 reconstructions of degassing, uplift and changing lithology could be significantly improved.

1411 A mid-Paleozoic oxygenation event is robustly predicted, i.e. a major rise in atmospheric O₂ and
1412 associated oxygenation of the ocean due to the rise of land plants. Atmospheric O₂ is effectively
1413 regulated thereafter with remaining fluctuations being a Carboniferous-Permian O₂ peak (~26%)
1414 linked to burial of terrestrial organic matter in coal swamps, a Triassic-Jurassic O₂ minimum (~21%)
1415 linked to low uplift, a Cretaceous O₂ peak (~26%) linked to high overall degassing and weathering
1416 fluxes, and a Cenozoic O₂ decline. Two of these robust features are qualitatively at odds with other
1417 models. First, COPSE predicts much lower O₂ in the early Paleozoic than GEOCARBSULF or MAGic,
1418 consistent with marine redox proxies (Lenton et al., 2016; Sperling et al., 2015b), whilst still being
1419 consistent with the metabolic O₂ requirements of early animals (Sperling et al., 2015a). Second,

1420 COPSE predicts a Mesozoic peak then Cenozoic decline of O₂ rather than a monotonic Mesozoic-
1421 Cenozoic rise of O₂ as seen in some versions of GEOCARBSULF (Berner et al., 2007; Falkowski et al.,
1422 2005). The latter prediction is made by inverting the $\delta^{13}\text{C}$ record, but it has been shown that this
1423 technique can also produce high Mesozoic O₂ followed by a Cenozoic O₂ decline (Mills et al., 2016),
1424 consistent with COPSE.

1425 **Acknowledgements**

1426 We thank Josh Williams for assistance with the basalt area forcing, Noam Bergman for developing
1427 the original COPSE model, Andy Watson for input to COPSE over the years, the late Bob Berner for
1428 pioneering the field of Phanerozoic biogeochemical modelling, and Dana Royer and an anonymous
1429 referee for constructive reviews.

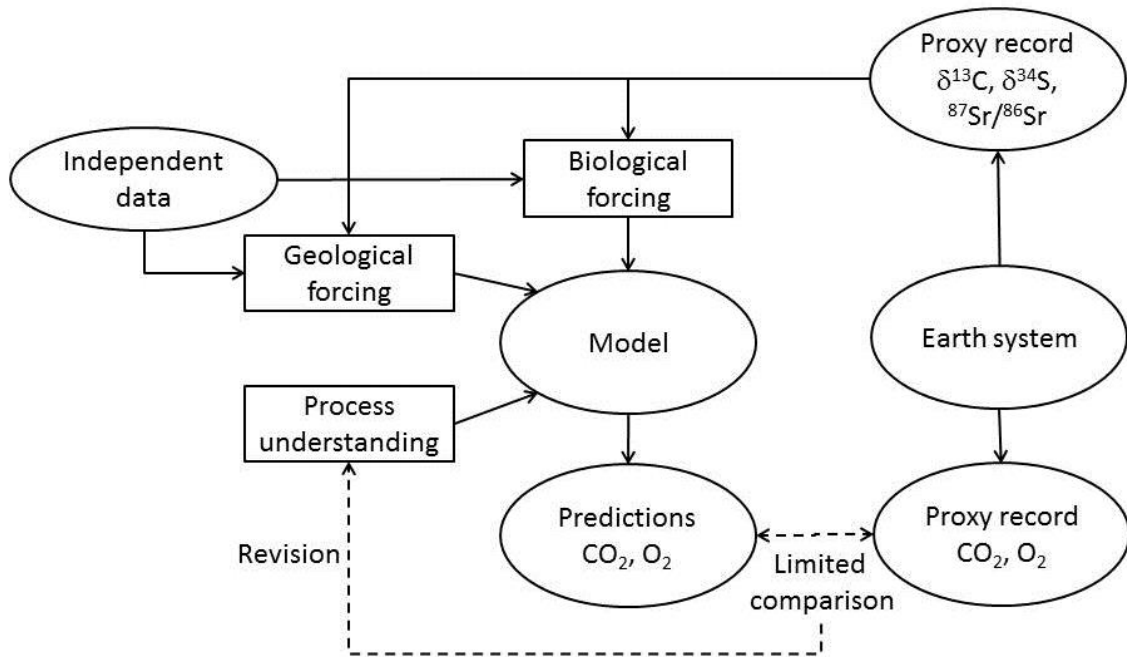
1430 The revised COPSE model code, written in Matlab and under Github version control, is available at
1431 <https://github.com/sjdaines/COPSE/releases>. The code is also available from the lead author on
1432 request.

1433 Funding: This work was supported by the Natural Environment Research Council [grant numbers
1434 NE/P013651/1, NE/N018508/1] (to T.M.L. and S.J.D.); a Royal Society Wolfson Research Merit Award
1435 (to T.M.L.); and a University of Leeds academic fellowship (to B.J.W.M.).

1436

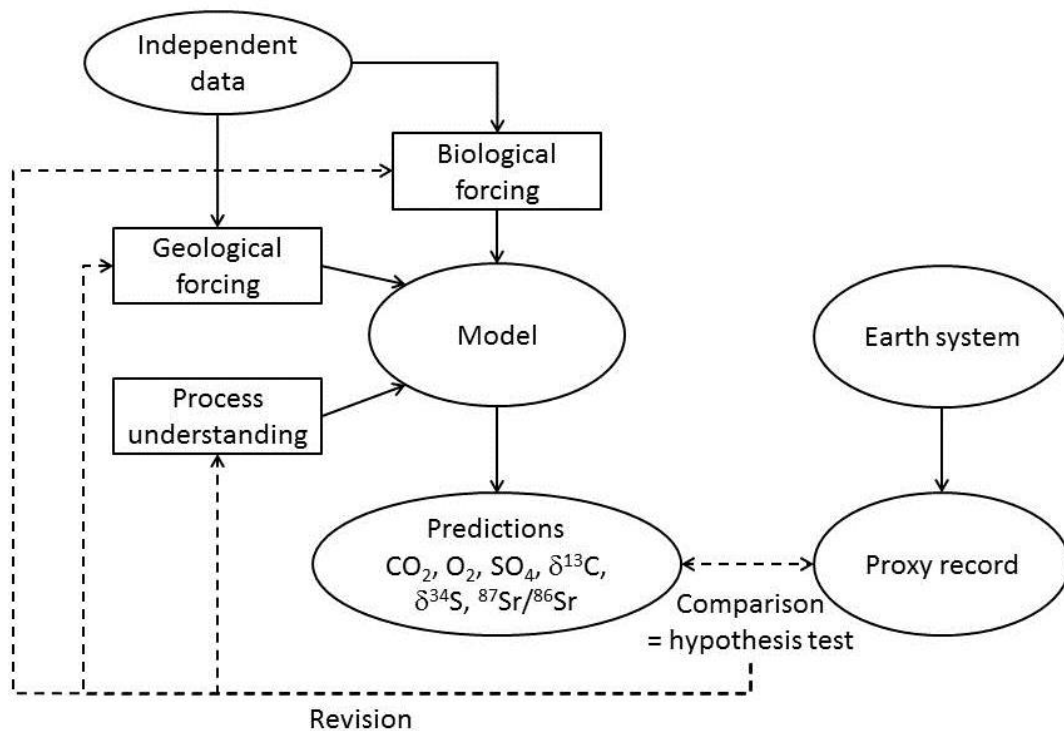
1437 **Figures and captions**

1438 (a)



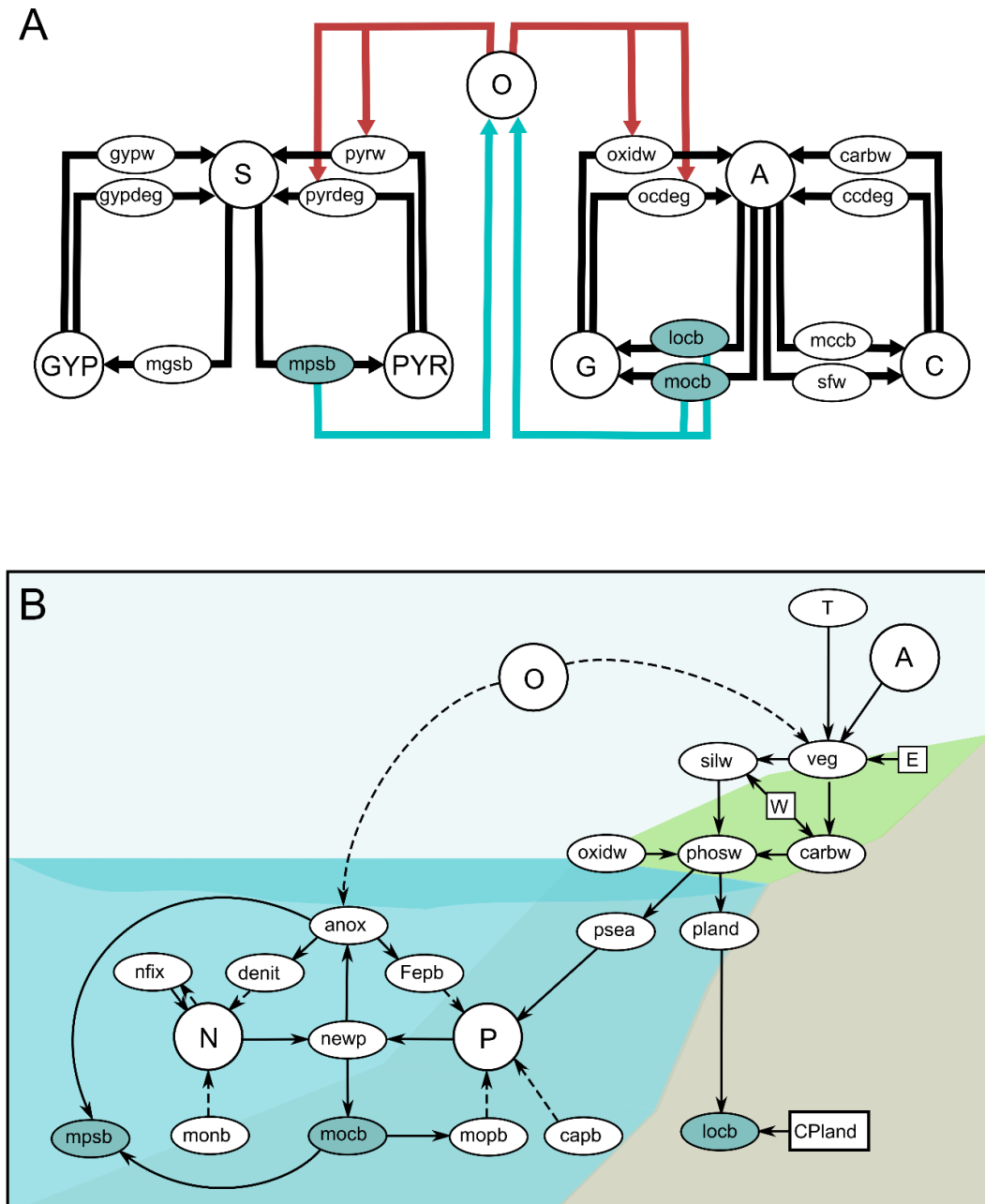
1439

1440 (b)



1441

1442 **Figure 1. Different approaches to modelling Phanerozoic biogeochemical cycling: (a) inverse**1443 **modelling approach (b) forwards modelling approach (pursued herein).**



1444

1445 **Figure 2. COPSE model schematic:** (A) Carbon, Sulphur and Oxygen cycle fluxes. Here arrows show

1446 mass fluxes, blue arrows show oxygen sources and red arrows show oxygen sinks. (B) Dynamic

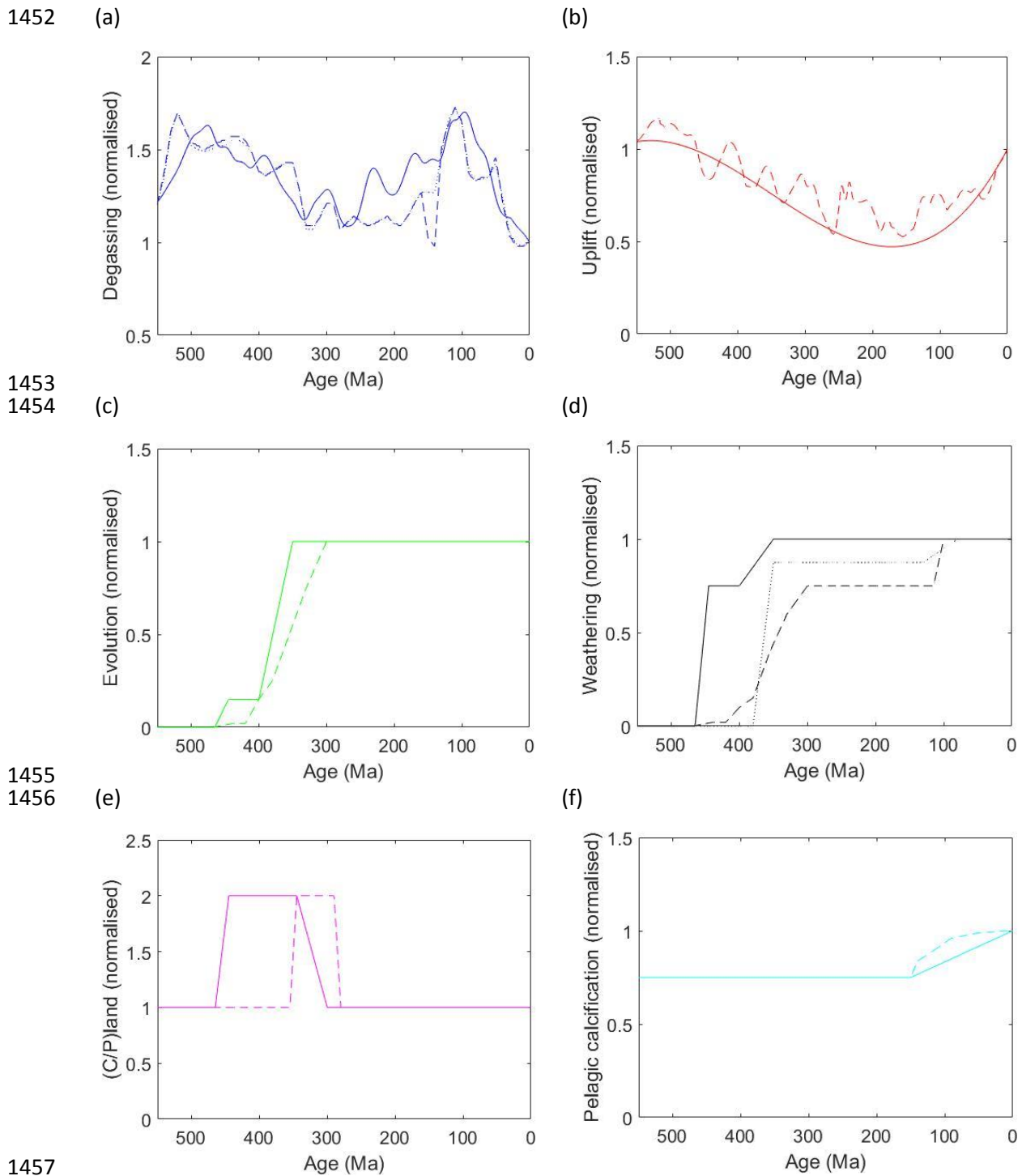
1447 nutrient and biosphere system. Here arrows show positive/direct (solid) or negative/inverse

1448 (dashed) relationships between model parameters. All terms are defined in Tables 1 and 2 and

1449 described in the text. In both diagrams blue ovals show burial fluxes of organic carbon and pyrite

1450 sulphur, which are the long term sources of free oxygen.

1451 *[Print version should be in colour.]*

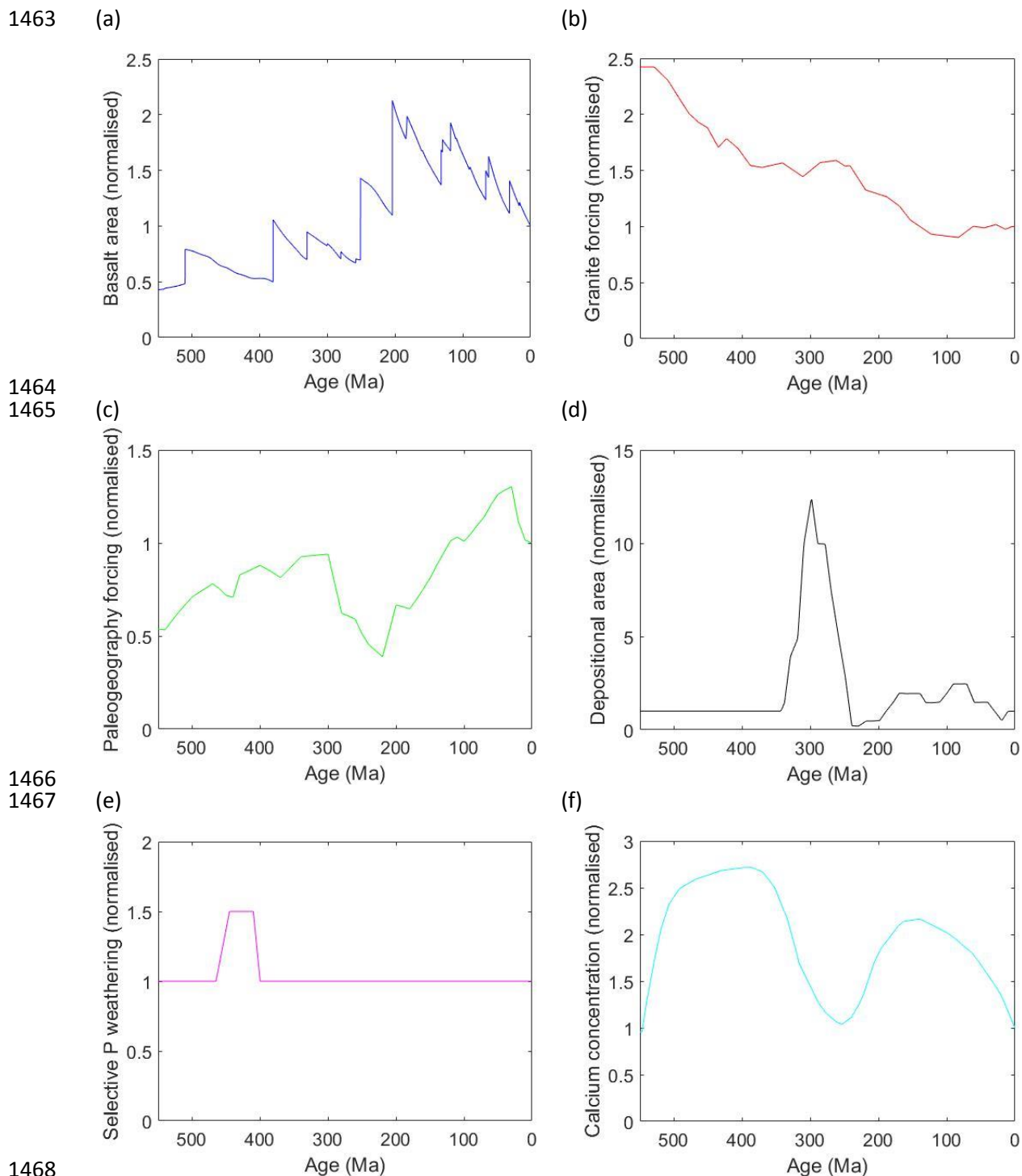


1457

1458 **Figure 3. Updating the original forcing factors:** (a) degassing, D (blue), (b) uplift, U (red), (c) plant1459 evolution, E (green), (d) plant effects on weathering, W (black), (e) plant stoichiometry, CP_{land} 1460 (magenta), (f) pelagic calcification, B (cyan). Original COPSE (dashed), revised COPSE (solid),

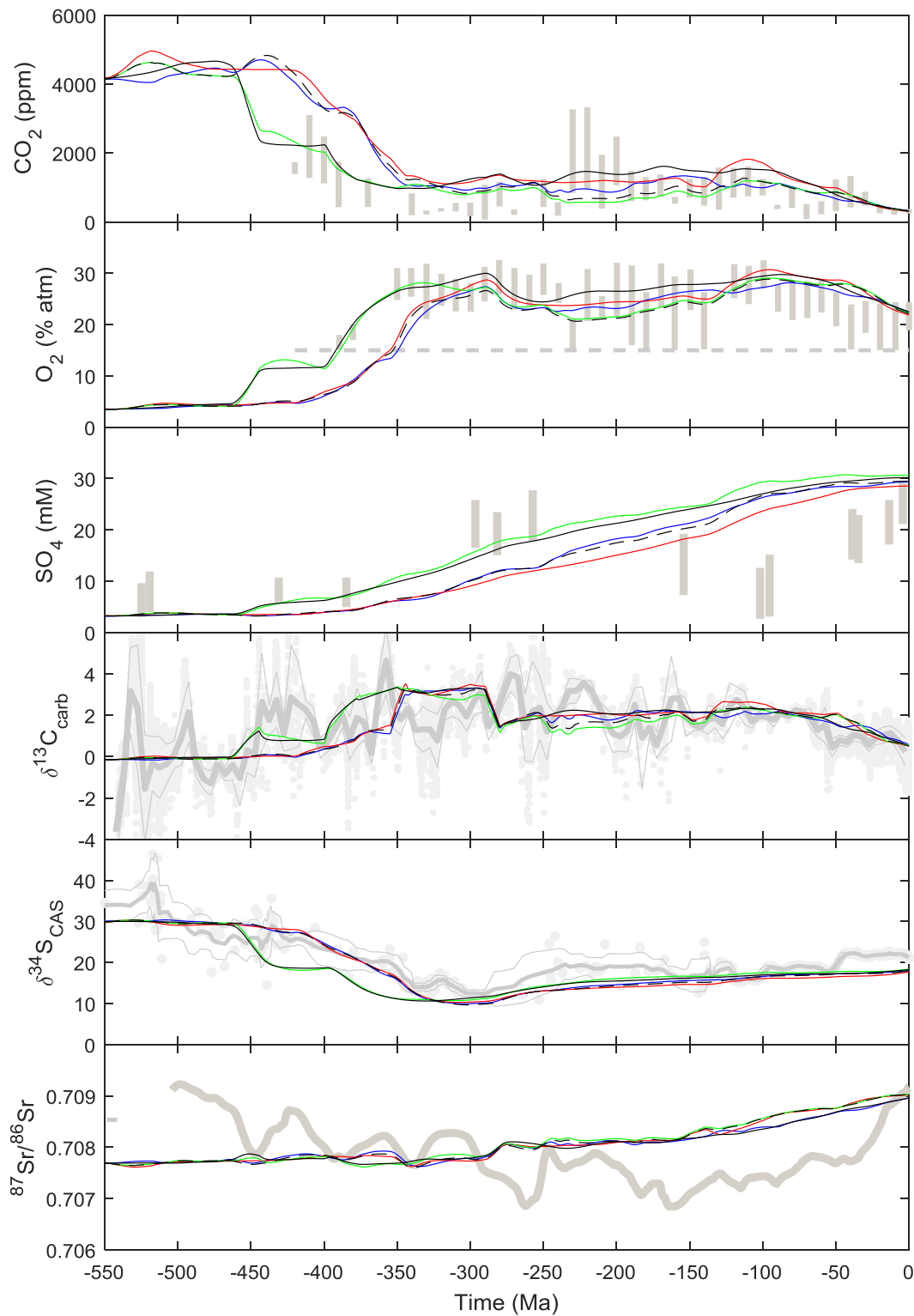
1461 GEOCARBSULF (dotted).

1462 [Print version should be in colour.]



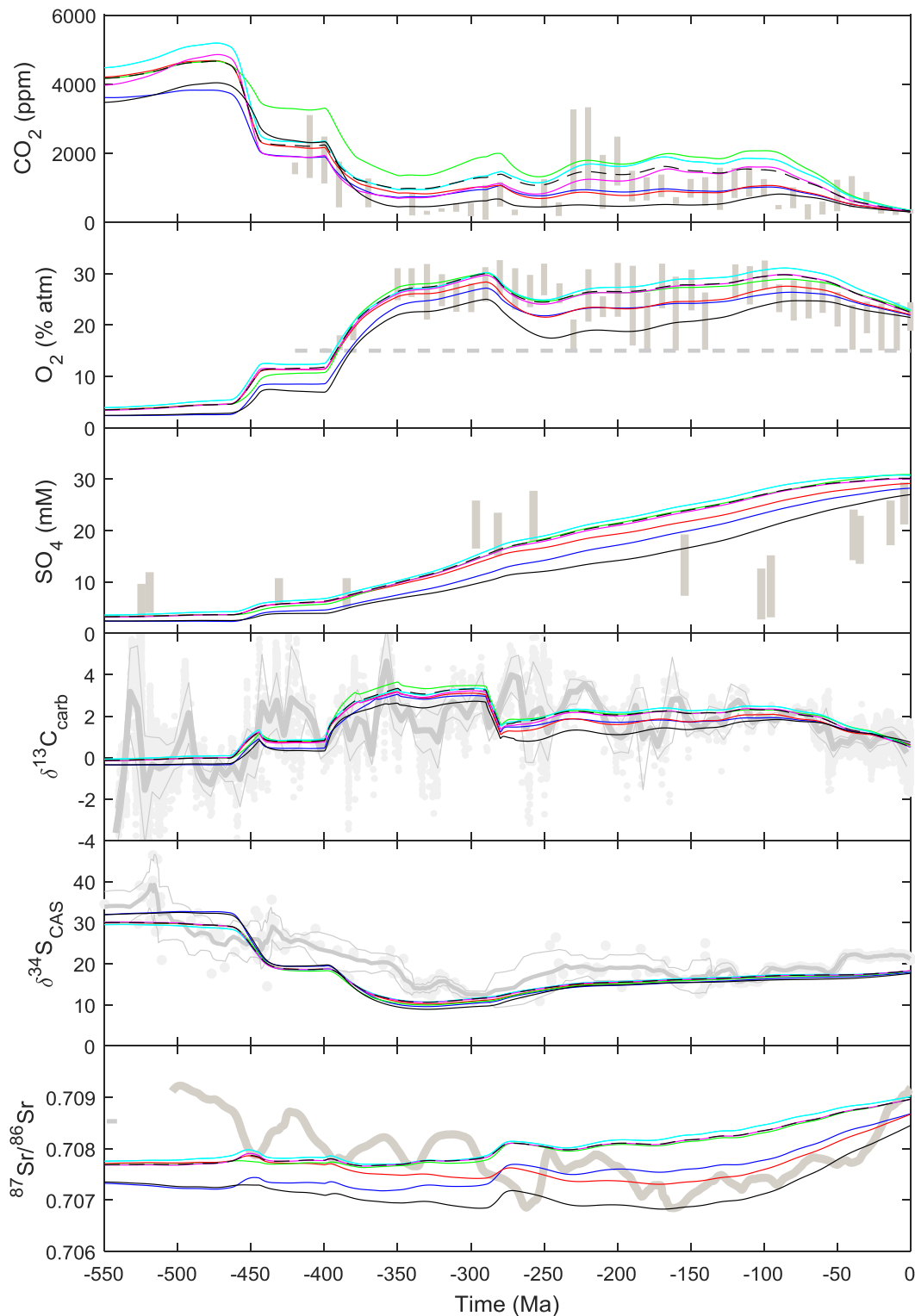
1469 **Figure 4. Additional forcing factors:** (a) ‘basalt’ (volcanic silicate rock) area, a_{bas} (blue), (b) ‘granite’
 1470 (non-volcanic silicate rock) kinetically-weighted area, a_{gran} (red), (c) paleogeography forcing of
 1471 runoff, PG (green), (d) coal basins depositional area, b_{coal} (black), (e) selective weathering of
 1472 phosphorus, F (magenta), (f) calcium concentration, c_{cal} (cyan).

1473 [Print version should be in colour.]



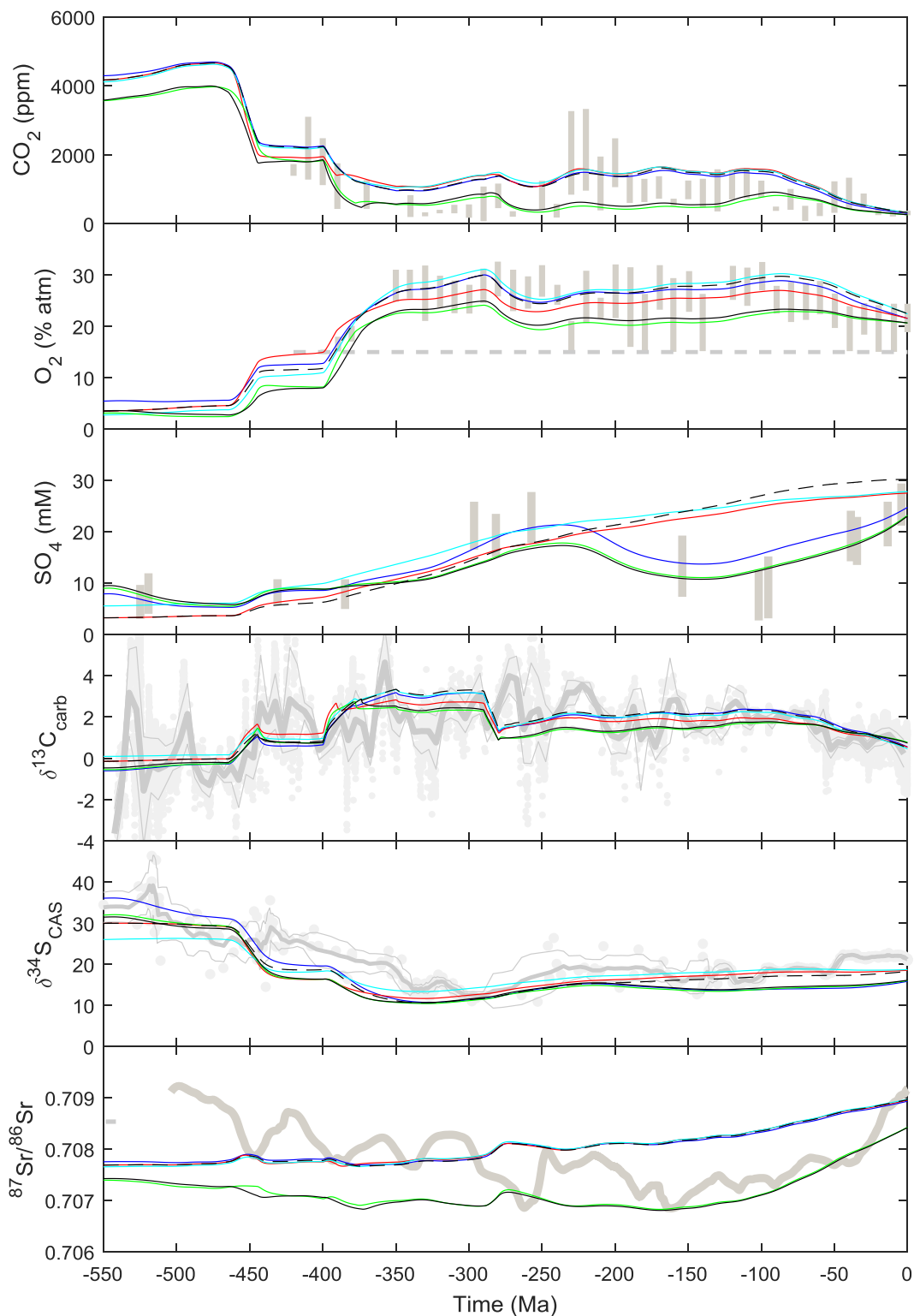
1474

1475 **Figure 5: Effect of updating the original forcing factors on predictions of CO_2 , O_2 , SO_4 , $\delta^{13}\text{C}$, $\delta^{34}\text{S}$,**
 1476 **$^{87}\text{Sr}/^{86}\text{Sr}$.** Original model (black dashed) with updates to forcing factors: *D* and *B* (blue), *U* (red), *E*, *W*
 1477 and *CP_{land}* (green), and all combined (black). Predictions are compared to proxy data in grey (detailed
 1478 in Table 6); vertical bars for CO_2 , O_2 , SO_4 are binned data with uncertainty ranges, grey dashed line
 1479 for O_2 is lower limit consistent with charcoal evidence of combustion, dots for $\delta^{13}\text{C}_{\text{carb}}$ and $\delta^{34}\text{S}_{\text{CAS}}$ are
 1480 original data, with running mean (bold line) \pm 1 s.d. (thin lines). [Print version should be in colour.]



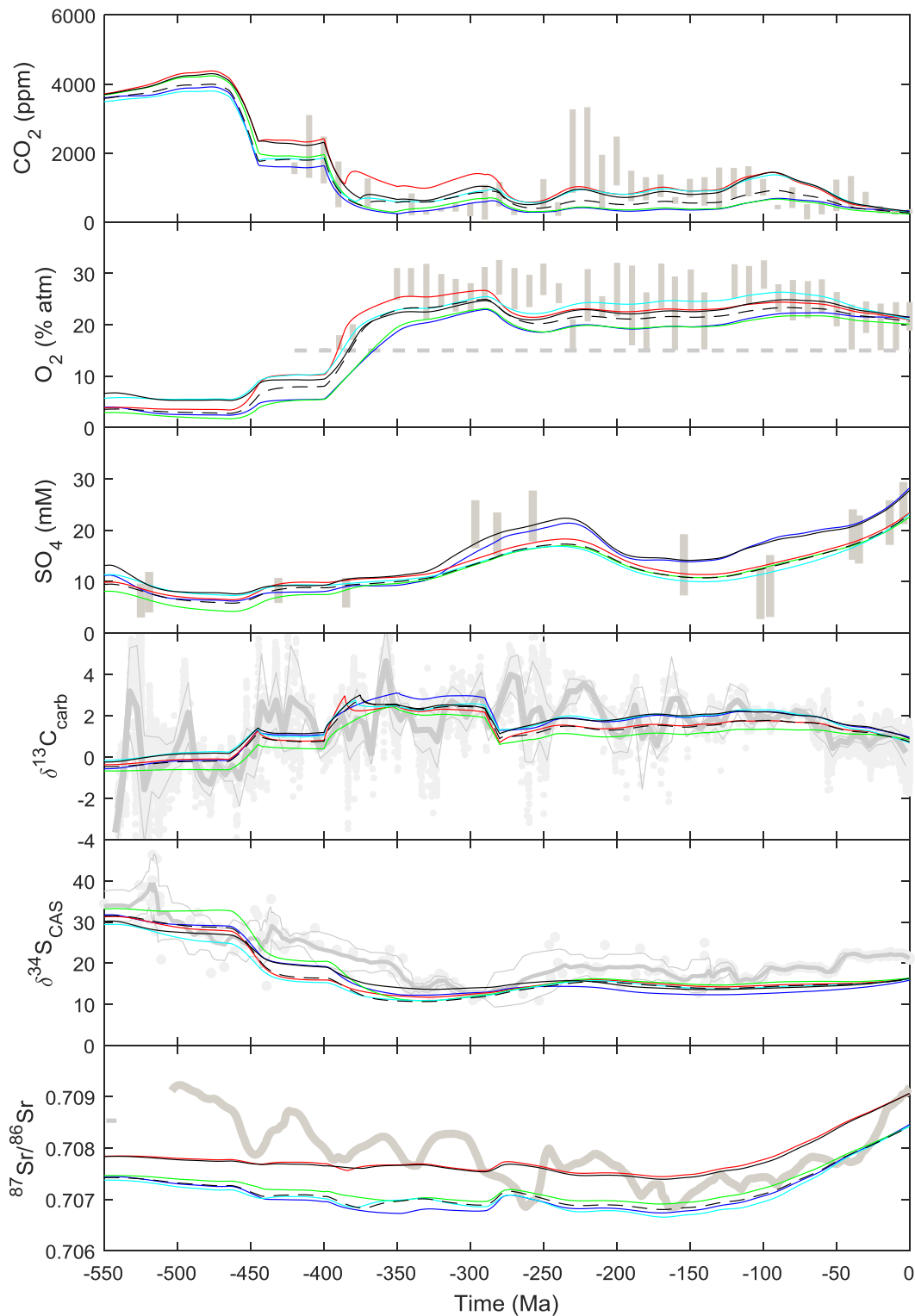
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1482 **Figure 6: Effects of updating weathering controls on predictions of CO_2 , O_2 , SO_4 , $\delta^{13}\text{C}_{\text{carb}}$, $\delta^{34}\text{S}_{\text{CAS}}$, $^{87}\text{Sr}/^{86}\text{Sr}$.**
 1483 Starting from the original model with updated forcing of D , U , E , W , B , CP_{land} (black dashed), with
 1484 individual additions of: seafloor weathering (blue), making basalt weathering independent of uplift
 1485 (red), distinguishing different activation energies for basalt and granite weathering (cyan), new
 1486 vegetation dependence of weathering (green), new temperature function (magenta), and combining
 1487 all these changes (black). [Print version should be in colour.]



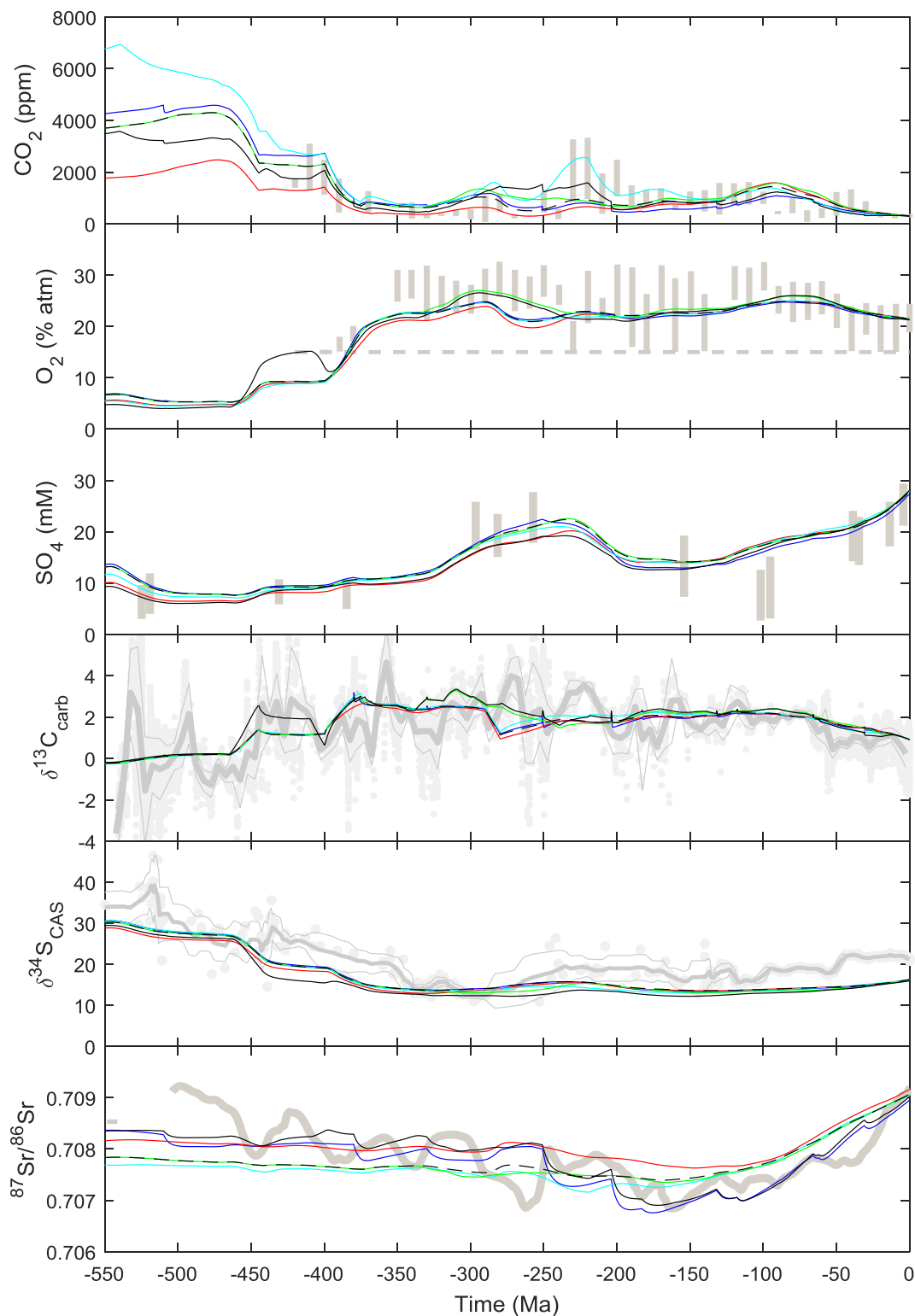
1488

1489 **Figure 7: Effects of updating redox controls and combining changes to the baseline model on**
 1490 **predictions of CO_2 , O_2 , SO_4 , $\delta^{13}\text{C}$, $\delta^{34}\text{S}$, $^{87}\text{Sr}/^{86}\text{Sr}$.** Starting from the original model with updated
 1491 forcing of D , U , E , W , B , CP_{land} (black dashed), with individual additions of: replacing the interactive
 1492 Ca cycle with prescribed $[\text{Ca}]$, c_{cal} (blue), new fire feedback on vegetation (red), removing the O_2
 1493 dependence of pyrite weathering (cyan), combining all these changes with weathering function
 1494 updates (green), additionally including all other changes to the baseline model (black). [Print version
 1495 should be in colour.]



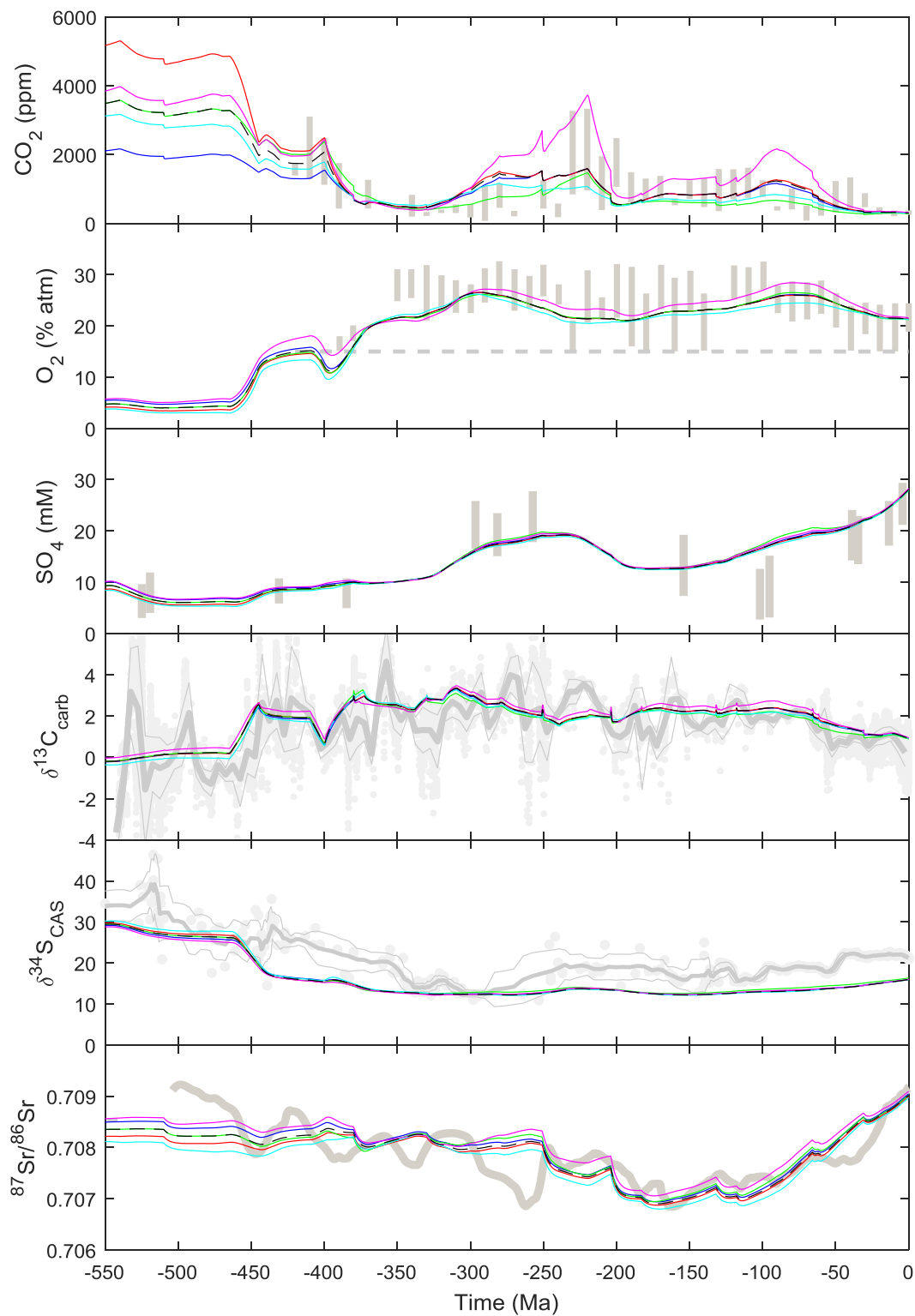
1496

1497 **Figure 8: Effects of updating the baseline fluxes on predictions of CO_2 , O_2 , SO_4 , $\delta^{13}\text{C}_{\text{carb}}$, $\delta^{34}\text{S}_{\text{CAS}}$, $^{87}\text{Sr}/^{86}\text{Sr}$.**
 1498 Starting from the new baseline model with updated forcing of D , U , E , W , B , CP_{land} (black dashed),
 1499 with individual variants from it: high S fluxes (blue), high C inorganic fluxes (red), low C organic fluxes
 1500 (green), revised split of P weathering (cyan), and combination of all these flux updates with revised
 1501 split of P burial fluxes (black). [Print version should be in colour.]



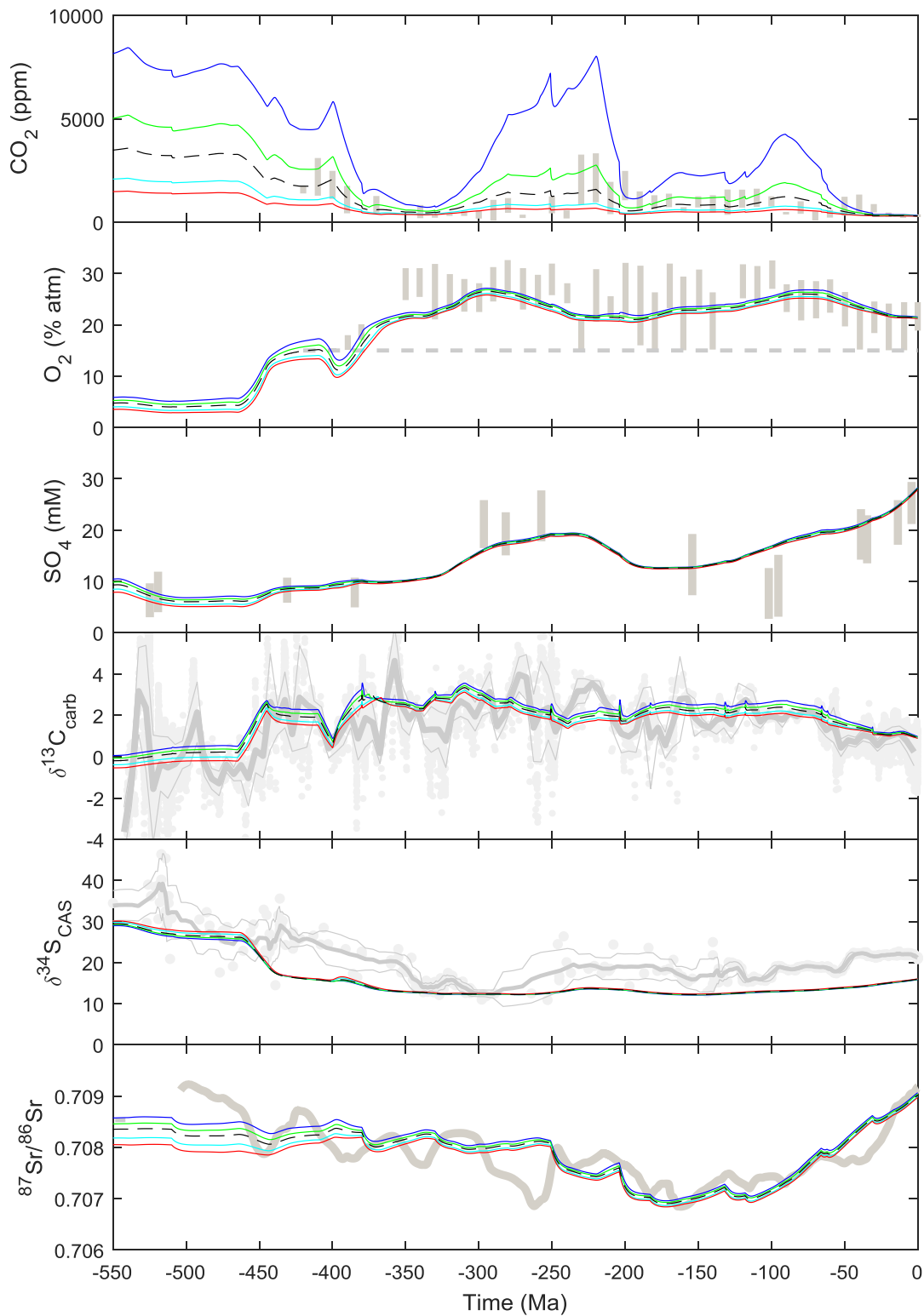
1502

1503 **Figure 9: Effects of new forcing factors on predictions of CO_2 , O_2 , SO_4 , $\delta^{13}\text{C}$, $\delta^{34}\text{S}$, $^{87}\text{Sr}/^{86}\text{Sr}$.** Starting
 1504 from the new baseline model with updated forcing of D , U , E , W , B , CP_{land} and updated fluxes (black
 1505 dashed), with individual forcing factors: basalt area, a_{bas} (blue), granite area, a_{gran} (red),
 1506 paleogeography, PG (cyan), coal basin depositional area, b_{coal} , with adjustment of CP_{land} (green), all of
 1507 the preceding combined with selective weathering of phosphorus, F (black). [Print version should be
 1508 in colour.]



1509

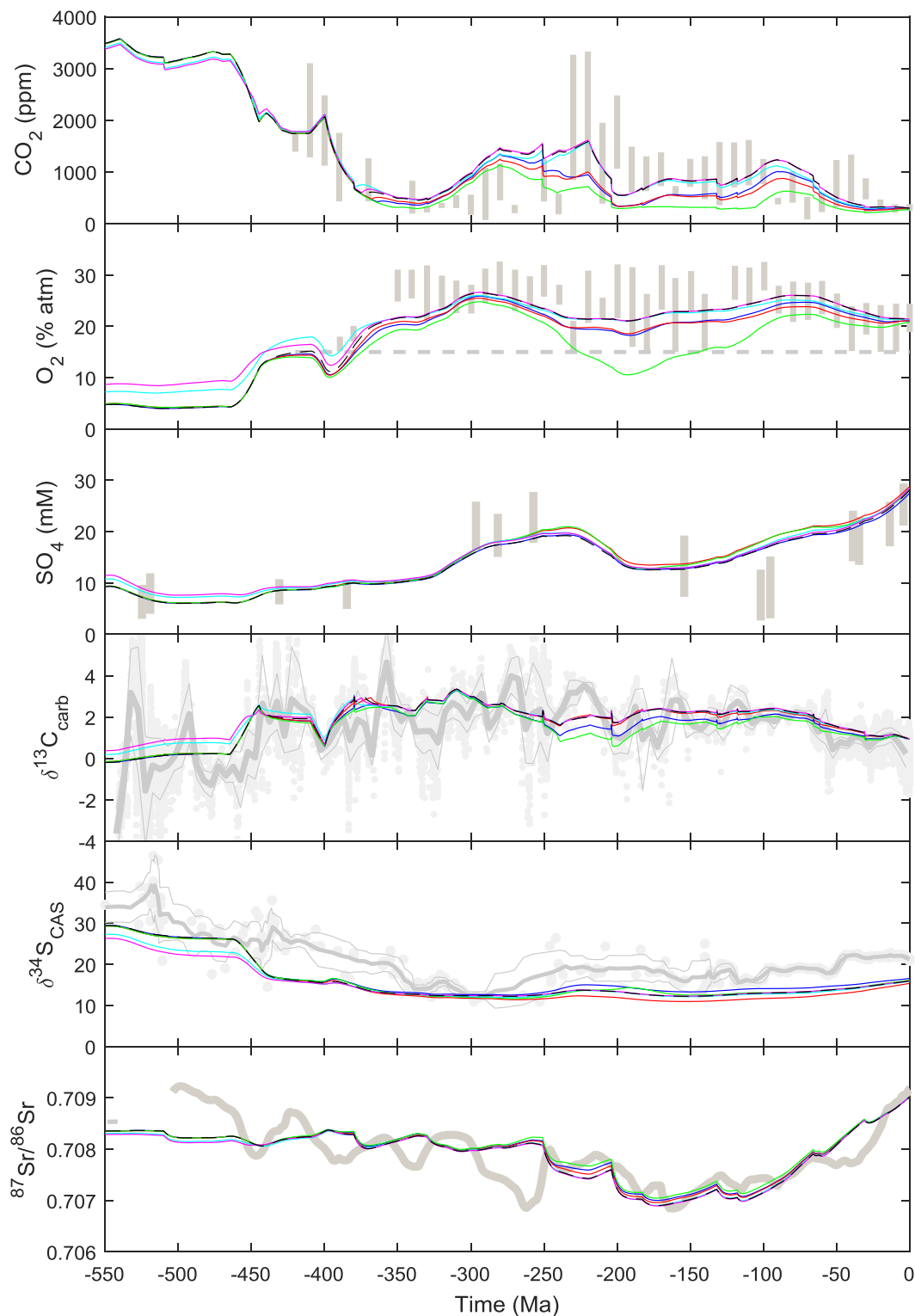
1510 **Figure 10: Testing hypotheses for controls on weathering.** Starting from the new baseline model
 1511 with updated original forcing factors, updated fluxes, and new forcing factors (black dashed), with:
 1512 4-fold amplification of weathering by plants ($k_{15} = 0.25$) (blue), 10-fold amplification of weathering
 1513 by plants ($k_{15} = 0.1$) (red), weathering dependent on vegetation NPP (rather than biomass) (green),
 1514 stronger temperature sensitivity of seafloor weathering (cyan), no temperature sensitivity of
 1515 seafloor weathering (magenta). [Print version should be in colour.]



1516

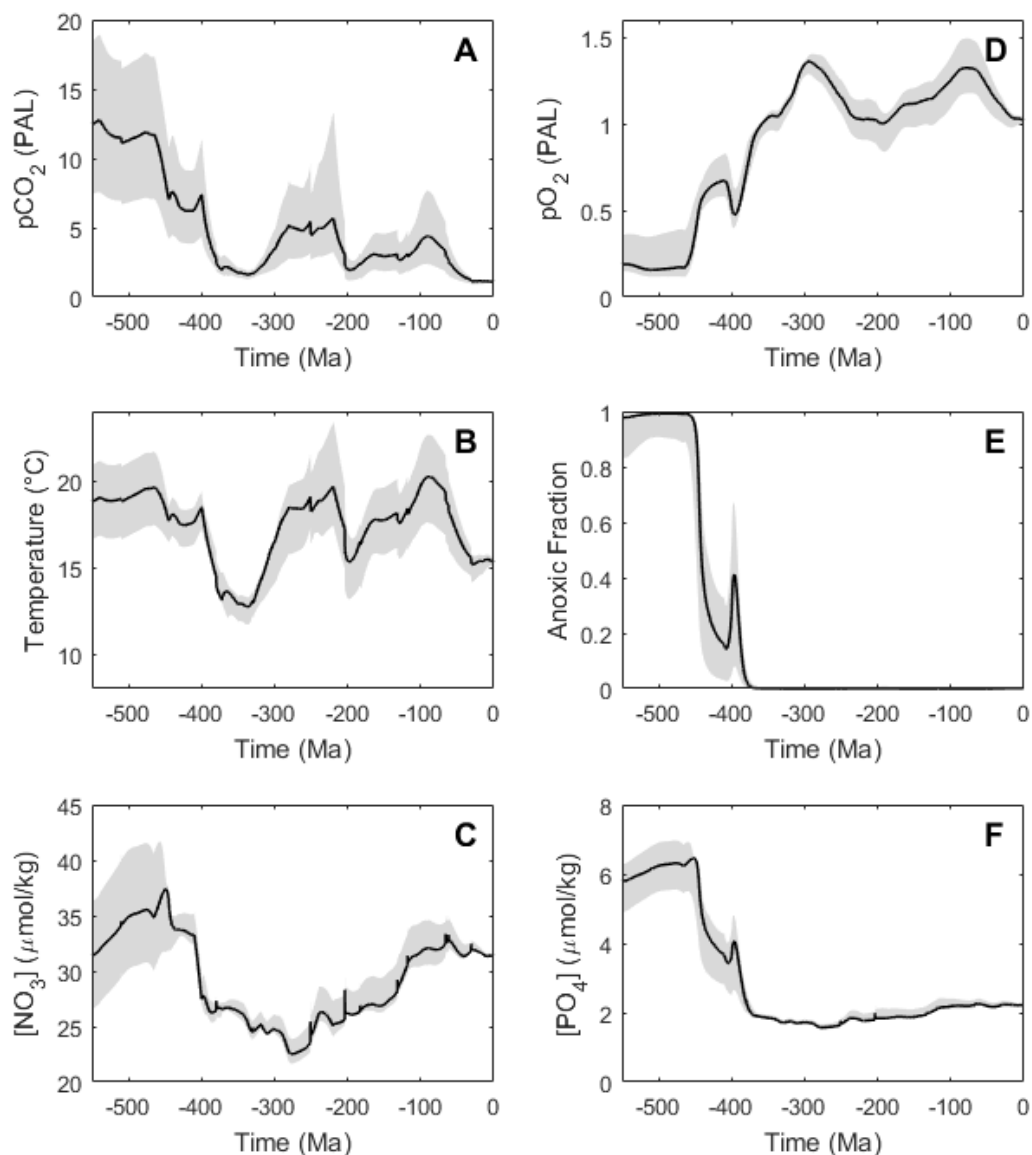
1517 **Figure 11. The effect of varying climate sensitivity.** Starting from the new baseline model with
 1518 updated original forcing factors, updated fluxes, and new forcing factors, and varying the climate
 1519 sensitivity from the default 3°C (black dashed) to: 1.5°C (blue), 2.25°C (green), 4.5°C (cyan), 6°C (red).
 1520 *[Print version should be in colour.]*

1521



1522

1523 **Figure 12: Testing hypotheses for controls on O₂.** Starting from the new baseline model with
 1524 updated original forcing factors, updated fluxes, and new forcing factors (black dashed), with: land-
 1525 derived organic carbon burial dependent on uplift (blue), marine organic carbon burial dependent
 1526 on uplift (red), land-derived and marine organic carbon burial dependent on uplift (green), marine
 1527 organic carbon burial dependent on O₂ (cyan), marine (C/P)_{organic} increasing with anoxia (magenta).
 1528 *[Print version should be in colour.]*



1529

1530 **Figure 13. New best guess model and uncertainty range from testing alternative hypotheses.** The
 1531 uncertainty range (in grey) spans all of the hypothesis tests in Section 3.6 and Figures 10-12, with the
 1532 exception of climate sensitivities of 1.5°C and 6°C, and the combined uplift forcing of marine and
 1533 terrestrial organic carbon burial – because we consider these cases falsified by that analysis: (A)
 1534 atmospheric $p\text{CO}_2$, (B) global temperature, (C) ocean nitrate concentration, (D) atmospheric $p\text{O}_2$, (E)
 1535 anoxic fraction of the ocean, (F) ocean phosphate concentration.

1536 **Tables**1537 **Table 1. Core COPSE model reservoirs and differential equations.**

Reservoir	Label	Differential equation	Initial size (mol)
Ocean (reactive) nitrogen	N	$\frac{dN}{dt} = nfix - denit - monb$	4.35×10^{16}
Ocean (phosphate) phosphorus	P	$\frac{dP}{dt} = psea - mopb - fepb - capb$	3.1×10^{15}
Atmosphere-ocean O ₂	O	$\frac{dO}{dt} = locb + mocb - oxidw - ocdeg + 2 \cdot mpsb$ $- 2 \cdot pyr w - 2 \cdot pyrdeg$	3.7×10^{19}
Atmosphere-ocean CO ₂	A	$\frac{dA}{dt} = oxidw + ocdeg + carbw + ccdeg - locb$ $- mocb - mccb - sfw$	3.193×10^{18}
Sedimentary organic (reduced) carbon	G	$\frac{dG}{dt} = locb + mocb - oxidw - ocdeg$	1.25×10^{21}
Sedimentary carbonate (oxidised) carbon	C	$\frac{dC}{dt} = mccb + sfw - carbw - ccdeg$	5.0×10^{21}
Ocean (sulphate) sulphur	S	$\frac{dS}{dt} = gypw + pyr w + gypdeg + pyrdeg$ $- mgsb - mpsb$	4.0×10^{19}
Sedimentary pyrite (reduced) sulphur	PYR	$\frac{dPYR}{dt} = mpsb - pyr w - pyrdeg$	1.8×10^{20}
Sedimentary gypsum (oxidised) sulphur	GYP	$\frac{dGYP}{dt} = mgsb - gypw - gypdeg$	2.0×10^{20}

1538

1539 **Table 2. Core COPSE model fluxes and baseline values.** ('Original' = Bergman et al., 2004, 'G³' = Mills et al., 2014a, 'New' = new baseline arrived at here.)

Process	Label	Constant	Original	G ³	lowS	highS	lowC _{in}	highC _{in}	lowC _{org}	highC _{org}	New	Notes
Nitrogen cycle			10¹² molN yr⁻¹									
Nitrogen fixation	<i>nfix</i>	k_3	8.72						(8.67)		8.67	
Denitrification	<i>denit</i>	$2k_4$	8.6								8.6	
Marine organic N burial	<i>monb</i>	k_2/CN_{sea}	0.12						(0.07)		0.07	CN _{sea} =37.5
Phosphorus cycle			10⁹ molP yr⁻¹									
Reactive P weathering	<i>phosw</i>	k_{10}	43.5						(33.5)		42.5	
Terrestrial organic P burial	<i>pland</i>	$k_{11}k_{10}$	4.5						(2.5)		2.5	CP _{land} =1000
Reactive P to ocean	<i>psea</i>	$(1-k_{11})k_{10}$	39						(31)		40	
Marine organic P burial	<i>mopb</i>	k_2/CP_{sea}	18						(10)		10	CP _{sea} =250
Iron-sorbed (Fe-P) burial	<i>fepb</i>	k_6	6								10	
Ca-bound (Ca-P) burial	<i>capb</i>	k_7	15								20	
Carbon cycle (inorganic)			10¹² molC yr⁻¹									
Carbonate C degassing	<i>ccdeg</i>	k_{12}	6.65	6.65			6.65	15			15	
Carbonate weathering	<i>carbw</i>	k_{14}	13.35	13.35			13.35	8			8	
Silicate weathering	<i>silw</i>	k_{silw}	6.65	4.9			4.9	12			12	
Granite weathering	<i>granw</i>	k_{granw}		3.185			3.185	9			9	
Basalt weathering	<i>basw</i>	k_{basw}		1.715			1.715	3			3	
Seafloor weathering	<i>sfw</i>	k_{sfw}	0	1.75			1.75	3			3	
Carbonate burial	<i>mccb</i>	$k_{14}+k_{silw}$	20	18.25			18.25	20			20	
Carbon cycle (organic)			10¹² molC yr⁻¹									
Organic C degassing	<i>ocdeg</i>	k_{13}	1.25						1.25	1.25	1.25	
Oxidative C weathering	<i>oxidw</i>	k_{17}	7.75						3.75	7.75	3.75	
Marine organic C burial	<i>mocb</i>	k_2	4.5						2.5	4.5	2.5	
Terrestrial organic C burial	<i>locb</i>	k_5	4.5						2.5	4.5	2.5	
Sulphur cycle			10¹² molS yr⁻¹									
Gypsum degassing	<i>gypdeg</i>	k_{gypdeg}	0		0	0.5					0.5	
Pyrite degassing	<i>pyrdeg</i>	k_{pyrdeg}	0		0	0.25					0.25	
Gypsum weathering	<i>gypw</i>	k_{22}	1.0		1.0	2.0					2.0	
Pyrite weathering	<i>pyrw</i>	k_{21}	0.53		0.53	0.45					0.45	
Gypsum burial	<i>mgsb</i>	k_{mgsb}	1.0		1.0	2.5					2.5	
Pyrite burial	<i>mpsb</i>	k_{mpsb}	0.53		0.53	0.7					0.7	

1540 **Table 3. Model forcing factors.** (All normalised to 1 at present with the exception of insolation.)

Forcing	Description	Basis	Source(s)
<i>Original model forcing factors</i>			
<i>I</i>	Insolation (solar luminosity)	Stellar physics	(Caldeira and Kasting, 1992)
<i>D</i>	Metamorphic and volcanic degassing	Inversion of sea-level curve	(Mills et al., 2017)
<i>U</i>	Tectonic uplift	Sediment accumulation rates	(Bernier, 2006b; Ronov, 1993)
<i>E</i>	Plant evolution and land colonisation	Fossil record and model estimates of global net primary productivity	(Lenton et al., 2016), updated here
<i>W</i>	Plant enhancement of weathering	Experimental and field study results	(Lenton et al., 2012), updated here
<i>CP_{land}</i>	C/P burial ratio of terrestrial plant material	Attempt to capture Paleozoic coal deposition	(Lenton et al., 2016), updated here
<i>B</i>	Apportioning of carbonate burial between shallow and deep seas	Fossil record of evolution of planktonic calcifiers	(Bernier, 1994)
<i>Additional forcing factors included herein</i>			
<i>a_{bas}</i>	Exposed area of volcanic silicate rocks	Reconstructed area of large igneous provinces (LIPs) and volcanic islands	(Ernst, 2014; Mills et al., 2014a)
<i>a_{gran}</i>	Kinetically-weighted area of non-volcanic silicate rocks	Reconstructed lithology of shield, shale, coal, evaporite	(Bluth and Kump, 1991)
<i>PG</i>	Paleogeography effect on runoff/weathering	Climate model simulations	(Royer et al., 2014)
<i>b_{coal}</i>	Depositional area of coal basins	Coal abundance data	(Bartdorff et al., 2008)
<i>F</i>	Selective biotic weathering of P relative to host rocks	Experimental results	(Lenton et al., 2012, 2016)
<i>c_{cal}</i>	Ocean calcium concentration	Best fit to fluid inclusion data	(Horita et al., 2002)
<i>Further forcing factors experimented with but not included here</i>			
<i>D_{LIP}</i>	Degassing associated with LIP emplacement	Volume of emplaced LIPs	(Ernst, 2014; Mills et al., 2014a)
<i>a_{carb}</i>	Exposed carbonate area	Reconstructed lithology	(Bluth and Kump, 1991)
<i>a_{shale}</i>	Exposed shale area	Reconstructed lithology	(Bluth and Kump, 1991)
<i>a_{org}</i>	Exposed organic (shale + coal) area	Reconstructed lithology	(Bluth and Kump, 1991)
<i>a_{evap}</i>	Exposed evaporite area	Reconstructed lithology	(Bluth and Kump, 1991)
<i>b_{evap}</i>	Depositional area of evaporites	Reconstructed lithology	(Bluth and Kump, 1991)

1542 **Table 4. Changes to the baseline COPSE model functional forms**

Functional form used in the new baseline model	Original functional form
$CO_2 = a^2$	$CO_2 = a$
$\Delta T = k_c \cdot \ln CO_2 - k_l \cdot t/570$	Complex function from Caldeira and Kasting (1992)
$ignit = \min(\max(48 \cdot mO_2 - 9.08, 0), 5)$	$ignit = \max(586.2 \cdot mO_2 - 122.102, 0)$
$gypdeg = k_{gypdeg} \cdot D \cdot gyp$	-
$pyrdeg = k_{pyrdeg} \cdot D \cdot pyr$	-
$sfw = k_{sfw} \cdot D \cdot e^{k_T^{sfw} \Delta T}$	-
$f_{biota} = [(1 - \min(V \cdot W, 1)) \cdot k_{15} \cdot CO_2^{0.5} + V \cdot W]$	$f_{biota} = \left[CO_2^{0.5} \cdot (1 - \min(V \cdot W, 1)) + \min(V \cdot W, 1) \cdot \left(\frac{2a}{1+a} \right)^{0.4} \right] \cdot [k_{15} + (1 - k_{15}) \cdot V \cdot W]$
$granw = k_{granw} \cdot U \cdot PG \cdot a_{gran} \cdot f_{Tgran} \cdot f_{runoff} \cdot f_{biota}$	-
$basw = k_{basw} \cdot PG \cdot a_{bas} \cdot f_{Tbas} \cdot f_{runoff} \cdot f_{biota}$	-
$silw = granw + basw$	$silw = k_{12} \cdot U \cdot f_T \cdot f_{runoff} \cdot f_{biota}$
$carbw = k_{14} \cdot C \cdot U \cdot PG \cdot g_{runoff} \cdot f_{biota}$	$carbw = k_{14} \cdot U \cdot g_{runoff} \cdot f_{biota}$
$gypw = k_{22} \cdot gyp \cdot U \cdot PG \cdot g_{runoff} \cdot f_{biota}$	$gypw = k_{22} \cdot gyp \cdot U \cdot g_{runoff} \cdot f_{biota}$
$pyrw = k_{21} \cdot U \cdot pyr$	$pyrw = k_{21} \cdot U \cdot pyr \cdot o^{0.5}$
$phosw = k_{10} \cdot F \cdot \left(k_{P_{silw}} \cdot \frac{silw}{k_{silw}} + k_{P_{carbw}} \cdot \frac{carbw}{k_{14}} + k_{P_{oxidw}} \cdot \frac{oxidw}{k_{17}} \right)$	$phosw = k_{10} \cdot \left(k_{P_{silw}} \cdot \frac{silw}{k_{12}} + k_{P_{carbw}} \cdot \frac{carbw}{k_{14}} + k_{P_{oxidw}} \cdot \frac{oxidw}{k_{17}} \right)$
$pland = k_{11} \cdot V \cdot phosw \cdot (k_{aq} + (1 - k_{aq}) \cdot b_{coal})$	$pland = k_{11} \cdot V \cdot phosw$
$anox = \frac{1}{1 + e^{-k_{anox}(k_u \cdot newp' - o)}}$	$anox = \max\left(1 - k_1 \cdot \frac{o}{newp'}, 0\right)$
$denit = k_4 \left(1 + \frac{anox}{1 - k_1}\right) \cdot n$	$denit = k_4 \left(1 + \frac{anox}{1 - k_1}\right)$
$fepb = \frac{k_6}{k_1} \cdot (1 - anox) \cdot p$	$fepb = \frac{k_6}{k_1} \cdot (1 - anox)$
$mgsb = k_{mgsb} \cdot s \cdot cal$	$mgsb = k_{mgsb} \cdot s \cdot cal$

1543

1544 **Table 5. Changes to the COPSE model non-flux parameters explored herein.** (Flux parameters are in

1545 Table 2. References and justification for chosen values are given in the text.)

Label	Meaning	Original model	New default value	Options explored
k_1	Present oxic fraction	0.86	0.997527	-
k_{15}	Pre-plant weathering	0.15	0.15	0.1, 0.25
k_{fire}	Fire frequency control	100	3	-
k_c	Climate sensitivity control	N/A	4.328°C	2.164°C, 3.246°C, 6.492°C, 8.656°C
k_l	Luminosity sensitivity control	N/A	7.4°C	-
k_T^{sfw}	Temperature sensitivity of seafloor weathering	N/A	0.0608	0.1332
k_T^{gran}	Temperature sensitivity of granite weathering	0.09	0.0724	-
k_T^{bas}	Temperature sensitivity of basalt weathering	0.09	0.0608	-
k_{psilw}	Silicates fraction of P weathering	2/12	0.8	-
k_{pcarb}	Carbonates fraction of P weathering	5/12	0.14	-
k_{poxid}	Oxidative fraction of P weathering	5/12	0.06	-
k_{aq}	Terrestrial organic matter burial fraction in aquatic settings	N/A	0.8	-
k_u	Nutrient utilisation efficiency	N/A	0.5	-
k_{anox}	Sharpness of oxic-anoxic transition	N/A	12	-

1546

1547

1548 **Table 6. Proxy data targets to which the model predictions are compared.**

Variable	Proxy source(s)	Data aggregation	Data sources
CO ₂	Stomatal index, phytoplankton alkenones, liverwort $\delta^{13}\text{C}$, paleosol $\delta^{13}\text{C}$, boron $\delta^{11}\text{B}$, nahcolite	10 Myr bins, +/-1 s.d.	(Royer, 2014)
O ₂	Charcoal content of coals, scaled between assumed limits of 15% and 25-35%	10 Myr bins, uncertainty range from uncertain upper limit	(Glasspool and Scott, 2010) lower limit extended to 420 Ma based on (Lenton et al., 2016)
SO ₄	Fluid inclusion data only	-	(Algeo et al., 2015; Brennan et al., 2004; Horita et al., 2002; Lowenstein et al., 2005)
$\delta^{13}\text{C}$	Carbonates from a range of organisms and depths	5 Myr bins, mean +/- 1 s.d.	(Saltzman and Thomas, 2012)
$\delta^{34}\text{S}$	Carbonate associated sulphate (CAS)	9 point moving mean +/-1 s.d.	(Algeo et al., 2015; Kampschulte and Strauss, 2004; Paytan et al., 1998)
$^{87}\text{Sr}/^{86}\text{Sr}$	Conodont apatite	LOWESS V5, plus one bin for data 543-548 Ma	(McArthur et al., 2012), plus 543-548 Ma data from (Cox et al., 2016)

1550 **Appendix A: Strontium cycle and its isotopes**

1551 A strontium cycle and its isotopes are implemented following Francois and Walker (1992) and
 1552 Vollstaedt et al. (2014) with some improvements to the formulation described in Mills et al. (2014a).
 1553 Ocean (OSr) and sedimentary carbonate (SSr) reservoirs of strontium are considered. The strontium
 1554 reservoir calculations are summarised in Table A.1, with the fluxes defined and present day baseline
 1555 values given in Table A.2, and other constants defined in Table A.3. Fluxes of strontium are tied,
 1556 where possible, to existing model variables via first-order scaling relationships.

1557 The ocean reservoir of strontium (OSr) has inputs from the mantle, weathering of old igneous rocks
 1558 (granites), new igneous rocks (basalts), and sedimentary carbonates, and outputs from incorporation
 1559 of strontium in (carbonate) sediments and seafloor weathering. Input of strontium to the ocean
 1560 from the mantle (Sr_{mantle}) is assumed to be proportional to degassing (D):

$$1561 \quad Sr_{mantle} = k_{Srmantle} \cdot D \quad (A.1)$$

1562 Inputs of strontium to the ocean from weathering of basalts (Sr_{basw}) and granites (Sr_{granw}) follows the
 1563 same apportioning as the corresponding carbon fluxes:

$$1564 \quad Sr_{basw} = k_{Srbasw} \cdot \frac{basw}{k_{basw}} \quad (A.2)$$

$$1565 \quad Sr_{granw} = k_{Srgranw} \cdot \frac{granw}{k_{granw}} \quad (A.3)$$

1566 Input of strontium from carbonate sediments (Sr_{sedw}) is assumed to scale with carbonate weathering
 1567 and with the concentration of strontium in the sedimentary carbonate reservoir (the latter differs
 1568 from Mills et al., 2014a):

$$1569 \quad Sr_{sedw} = k_{Sr sedw} \cdot \frac{carbw}{k_{carbw}} \cdot \frac{SSr}{SSr_0} \quad (A.4)$$

1570 Removal of strontium through burial in (carbonate) sediments is assumed proportional to the rate of
 1571 carbonate sediment deposition and the concentration of strontium in the ocean:

1572
$$Sr_{sedb} = k_{Sr_{sedb}} \cdot \frac{m_{ccb}}{k_{m_{ccb}}} \cdot \frac{OSr}{OSr_0} \quad (A.5)$$

1573 The rate of strontium removal in seafloor weathering is assumed to depend on the seafloor
 1574 weathering rate and the strontium concentration in the ocean (the latter differs from Mills et al.,
 1575 2014a):

1576
$$Sr_{sfw} = k_{Sr_{sfw}} \cdot \frac{sfw}{k_{sfw}} \cdot \frac{OSr}{OSr_0} \quad (A.6)$$

1577 The relative proportions of the burial and seafloor weathering removal fluxes of strontium are
 1578 assumed to follow the same proportions as the corresponding fluxes in the carbon system, with the
 1579 total flux dictated by assuming present day steady state for oceanic Sr concentration.

1580 The sedimentary reservoir of strontium (SSr) has an input from carbonate burial (Sr_{sedb}), and outputs
 1581 from carbonate weathering (Sr_{sedw}) and metamorphic conversion to crustal rocks (Sr_{metam}). The
 1582 output from sediment metamorphism is assumed to be proportional to degassing (D) and the
 1583 concentration of strontium in the sedimentary carbonate reservoir (the latter differs from Mills et
 1584 al., 2014a):

1585
$$Sr_{metam} = k_{Sr_{metam}} \cdot D \cdot \frac{SSr}{SSr_0} \quad (A.7)$$

1586 Although there is no fractionation of Sr isotopes associated with the input and output fluxes to the
 1587 ocean, decay of ^{87}Rb to ^{87}Sr influences the $^{87}\text{Sr}/^{86}\text{Sr}$ ratio over long timescales (and is responsible for
 1588 the differing $^{87}\text{Sr}/^{86}\text{Sr}$ values between different rock types). The decay process is represented
 1589 explicitly in the model:

1590
$$^{87}\text{Sr}/^{86}\text{Sr}_{granite} = ^{87}\text{Sr}/^{86}\text{Sr}_0 + ^{87}\text{Rb}/^{86}\text{Sr}_{granite}(1 - e^{-\lambda t}) \quad (A.8)$$

1591
$$^{87}\text{Sr}/^{86}\text{Sr}_{basalt} = ^{87}\text{Sr}/^{86}\text{Sr}_0 + ^{87}\text{Rb}/^{86}\text{Sr}_{basalt}(1 - e^{-\lambda t}) \quad (A.9)$$

1592
$$^{87}\text{Sr}/^{86}\text{Sr}_{mantle} = ^{87}\text{Sr}/^{86}\text{Sr}_0 + ^{87}\text{Rb}/^{86}\text{Sr}_{mantle}(1 - e^{-\lambda t}) \quad (A.10)$$

1593 Where time (t) is in years from Earth formation (taken to be 4.5 billion years ago). For each rock
 1594 type, the present day rubidium-strontium ratio is then calculated (Table A.3) such that the observed
 1595 present day $^{87}\text{Sr}/^{86}\text{Sr}$ ratio is achieved for each rock type after 4.5 billion years:

$$1596 \quad ^{87}\text{Rb}/^{86}\text{Sr} = \frac{(^{87}\text{Sr}/^{86}\text{Sr}_{\text{present}} - ^{87}\text{Sr}/^{86}\text{Sr}_0)}{(1 - e^{-\lambda \cdot 4.5 \times 10^9})} \quad (\text{A.11})$$

1597 The isotopic composition of the ocean and the sediments are calculated by first creating reservoirs
 1598 consisting of Sr concentrations multiplied by their isotopic ratios, where $\delta S r_X$ denotes the $^{87}\text{Sr}/^{86}\text{Sr}$
 1599 ratio of reservoir X :

$$1600 \quad \frac{d(OSr \cdot \delta S r_{\text{ocean}})}{dt} = S r_{\text{granw}} \cdot \delta S r_{\text{granite}} + S r_{\text{basw}} \cdot \delta S r_{\text{basalt}} + S r_{\text{sedw}} \cdot \delta S r_{\text{sediment}} + S r_{\text{mantle}} \cdot$$

$$1601 \quad \delta S r_{\text{mantle}} - S r_{\text{sedb}} \cdot \delta S r_{\text{ocean}} - S r_{\text{sfw}} \cdot \delta S r_{\text{ocean}} \quad (\text{A.12})$$

$$1602 \quad \frac{d(SSr \cdot \delta S r_{\text{sediment}})}{dt} = S r_{\text{sedb}} \cdot \delta S r_{\text{ocean}} - S r_{\text{sedw}} \cdot \delta S r_{\text{sediment}} - S r_{\text{metam}} \cdot \delta S r_{\text{sediment}} +$$

$$1603 \quad SSr \cdot \lambda \cdot (^{87}\text{Rb}/^{86}\text{Sr}_{\text{carbonate}}) \cdot e^{\lambda(4.5 \times 10^9 - t)} \quad (\text{A.13})$$

1604 The carbonate sediment isotopic reservoir evolution includes a term to account for rubidium decay
 1605 within the sedimentary reservoir. The present-day rubidium-strontium ratio of sediments
 1606 $^{87}\text{Rb}/^{86}\text{Sr}_{\text{carbonate}}$, (Table A.3), is calculated to achieve the average crustal $^{87}\text{Sr}/^{86}\text{Sr}$ of 0.73 (Veizer
 1607 and Mackenzie, 2003) .

1608 The ocean and sediment $^{87}\text{Sr}/^{86}\text{Sr}$ ratios are calculated by dividing the new reservoirs by the known
 1609 concentration or total:

$$1610 \quad \delta S r_{\text{ocean}} = \frac{OSr \cdot \delta S r_{\text{ocean}}}{OSr} \quad (\text{A.14})$$

$$1611 \quad \delta S r_{\text{sediment}} = \frac{SSr \cdot \delta S r_{\text{sediment}}}{SSr} \quad (\text{A.15})$$

1612 Present day fluxes are taken from Francois and Walker (1992) with differences being the split of
 1613 basalt and granite weathering and the split of seafloor weathering and sediment burial. The present

1614 day fluxes are such that although the ocean reservoir is in steady state, the sedimentary pool of
 1615 strontium is out of steady state and growing. However, over Phanerozoic time the generally greater
 1616 than present degassing tends to generate shrinkage of the sedimentary reservoir. This shrinkage is
 1617 buffered considerably by the assumed dependence of metamorphic conversion on the sedimentary
 1618 strontium reservoir size. Nevertheless the sedimentary reservoir needs to be initialised larger than
 1619 present (typically 6×10^{18} mol) at 600 Ma to approach the present day value.

1620 The choice of present day values for $^{87}\text{Sr}/^{86}\text{Sr}$ of mantle, basalt and granite together with the
 1621 corresponding input fluxes determine the present day 'attractor' value (a) for the composition of the
 1622 ocean and sediments, following:

$$1623 \quad a = \left(\frac{k_{Sr_{silw}}}{k_{Sr_{mantle}} + k_{Sr_{silw}}} \right) \cdot (k_{basfrac} \cdot \delta Sr_{basalt} + (1 - k_{basfrac}) \cdot \delta Sr_{granite}) + \left(\frac{k_{Sr_{mantle}}}{k_{Sr_{mantle}} + k_{Sr_{silw}}} \right) \cdot \delta Sr_{mantle} \quad (A.16)$$

1625 Using $k_{basfrac}=0.25$ and the other values from (Francois and Walker, 1992), including
 1626 $\delta Sr_{granite}=0.718$, gives $a=0.7105$, whereas the ocean is at ~ 0.709 and sedimentary carbonates at
 1627 ~ 0.708 , suggesting some internal inconsistency in that set up. Previously we used $\delta Sr_{granite}=0.715$
 1628 (Mills et al., 2014a), which gives $a=0.7091$, consistent with the present ocean state, and we adopt
 1629 that value here.

1630 In our previous work (Mills et al., 2014a) sedimentary carbonate was initialised at $\delta Sr_{sediment} =$
 1631 0.714 in order to recover present day values, but this is hard to justify given that Phanerozoic
 1632 carbonates have ranged over $0.7065-0.709$ and the Neoproterozoic saw a major rise from ~ 0.706 to
 1633 ~ 0.709 (Halverson et al., 2007). The use of a high initial sedimentary $^{87}\text{Sr}/^{86}\text{Sr}$ tends to drag up the
 1634 initial ocean $^{87}\text{Sr}/^{86}\text{Sr}$, but without evidence for such high values here instead we initialise with
 1635 $\delta Sr_{sediment} = 0.708$, which is roughly the Phanerozoic average and a reasonable value for the late
 1636 Neoproterozoic.

1637 **Table A.1. Strontium reservoirs and differential equations.**

Reservoir	Label	Differential equation	Present size (mol)
Ocean Sr	OSr	$\frac{dOSr}{dt} = Sr_{granw} + Sr_{basw} + Sr_{sedw} + Sr_{mantle} - Sr_{sedb} - Sr_{sfw}$	1.2×10^{17}
Sed. Sr	SSr	$\frac{dSSr}{dt} = Sr_{sedb} - Sr_{sedw} - Sr_{metam}$	5×10^{18}

1638

1639 **Table A.2. Strontium fluxes and baseline (present day) values.**

Process	Label	Constant	Baseline flux (molSr yr ⁻¹)	Source/Notes
(Silicate weathering)		$k_{Sr_{silw}}$	13×10^9	(Francois and Walker, 1992)
Basalt weathering	Sr_{basw}	$k_{basfrac} \cdot k_{Sr_{silw}}$		split follows carbon cycle
Granite weathering	Sr_{granw}	$(1 - k_{basfrac}) \cdot k_{Sr_{silw}}$		split follows carbon cycle
Sediment weathering	Sr_{sedw}	$k_{Sr_{sedw}}$	17×10^9	(Francois and Walker, 1992)
Mantle input	Sr_{mantle}	$k_{Sr_{mantle}}$	7.3×10^9	(Francois and Walker, 1992)
Seafloor weathering	Sr_{sfw}	$k_{Sr_{sfw}}$		split follows carbon cycle
Sediment burial	Sr_{sedb}	$k_{Sr_{sedb}}$		split follows carbon cycle
Sediment metamorphism	Sr_{metam}	$k_{Sr_{metam}}$	13×10^9	(Francois and Walker, 1992)

1640

1641 **Table A.3. Other constants in the strontium cycle.**

Constant	Label	Value	Source/Notes
⁸⁷ Rb decay rate	λ	$1.4 \times 10^{-11} \text{ yr}^{-1}$	(Francois and Walker, 1992)
Original value	$^{87}\text{Sr}/^{86}\text{Sr}_0$	0.69898	at formation of the Earth
⁸⁷ Sr/ ⁸⁶ Sr basalt	δSr_{basalt}	0.705	(Francois and Walker, 1992)
⁸⁷ Sr/ ⁸⁶ Sr granite	$\delta Sr_{granite}$	0.715	reproduces present ocean composition
⁸⁷ Sr/ ⁸⁶ Sr mantle	δSr_{mantle}	0.703	(Francois and Walker, 1992)
⁸⁷ Rb/ ⁸⁶ Sr mantle	$^{87}\text{Rb}/^{86}\text{Sr}_{mantle}$	0.066	for correct present day ⁸⁷ Sr/ ⁸⁶ Sr
⁸⁷ Rb/ ⁸⁶ Sr basalt	$^{87}\text{Rb}/^{86}\text{Sr}_{basalt}$	0.1	for correct present day ⁸⁷ Sr/ ⁸⁶ Sr
⁸⁷ Rb/ ⁸⁶ Sr granite	$^{87}\text{Rb}/^{86}\text{Sr}_{granite}$	0.26	for correct present day ⁸⁷ Sr/ ⁸⁶ Sr
⁸⁷ Rb/ ⁸⁶ Sr sediments	$^{87}\text{Rb}/^{86}\text{Sr}_{carbonate}$	0.5	for correct present day ⁸⁷ Sr/ ⁸⁶ Sr assuming crustal average ⁸⁷ Sr/ ⁸⁶ Sr of 0.73

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