

1 **Flume experiments on the impact of a cross-flow turbine on an erodible** 2 **bed**

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7 8 **ABSTRACT**

9 Understanding the effect of tidal turbines on local erosion of the estuarine bed is crucial for design
10 and maintenance of turbines with stable foundations and assessment of their environmental impacts.
11 This report describes the results of flume experiments on clear-water scour caused by a single cross-
12 flow turbine in steady flow conditions. The turbine investigated is a Momentum Reversal Lift (MRL)
13 turbine originally designed in collaboration with the University of Exeter. Results show that the
14 turbine can cause significant bed scour, particularly when it was not spinning and in a particular
15 orientation of blades. This is opposite to the previous findings for axial flow turbines. The bottom
16 plate of the turbine, although increasing scour depth, was found to increase the turbine performance
17 and reduce adverse effects on the downstream flow. The findings highlight the importance of regular
18 monitoring and taking immediate repair actions for a tidal installation.

19
20 *Keywords:* Flume experiments, scour, tidal turbine, cross-flow turbine

21 22 **1. Introduction and background**

23
24 Tidal energy has the potential to be a significant contribution to energy generation in the UK. In
25 particular, significant amounts of energy can potentially be extracted from shallow-water estuarine
26 zones which are abundant around the UK. This energy resource is predicted to represent nearly 50%
27 of the tidal energy potential of the whole of Europe (Elghali et al. 2007; Magagna and Uihlein 2015)
28 and, if realized, could save million tonnes of carbon annually and power millions homes. This energy
29 can be extracted through barrages or through freestanding underwater hydrokinetic turbines, and there
30 are significant reasons for preferring the latter. However the use of hydrokinetic turbines in practice
31 is currently limited with an important factor being the challenge in evaluating their effects on seabed
32 erosion, foundation stability and marine life. The importance of studying these effects therefore
33 cannot be overestimated.

34 The Momentum Reversal Lift (MRL) turbine is a novel design of hydrokinetic turbine,
35 originally designed by Aquascientific Ltd in collaboration with University of Exeter, UK. The flow
36 hydrodynamics and power output of the MRL turbine have been studied both computationally and
37 experimentally (Gebreslassie 2012; Gebreslassie et al. 2013a; b; Ordonez-Sanchez et al. 2017;
38 Sutherland et al. 2018). Its cross-flow design is also particularly suitable to the shallow water
39 environment in an estuary. These factors make it a good choice for investigating the scour induced
40 by a tidal turbine. Moreover, unlike axial flow devices (e.g. Hill et al. 2014, Hill et al. 2016a, Hill et
41 al. 2016b, and Musa et al. 2018a) for which scour and hydrodynamics have been studied in literature,
42 no previous study has investigated the scour effects of cross-flow turbines.

43 The findings of this work are expected to inform expertise and guidelines (e.g. Musa et al.
44 2018b) for optimal design and maintenance of hydrokinetic tidal turbines, more efficient extraction
45 of marine renewable energy in the UK, and improved management of environmental effects.
46

47 2. Experimental setup and methodology

48
49 Experiments were carried out in a horizontal 605mm wide ($= B =$ width of approach flow), 10m long
50 sediment recirculating flume at the University of Exeter. The flume is equipped with a traverse system
51 (with a movement precision of $1 \mu\text{m}$) for positioning instruments at specified x , y and z coordinates,
52 where x , y and z refer to streamwise, spanwise and vertical directions. A side view of a typical
53 experiment is shown in Fig. 1 where $x = 0$ is at the left edge of the vertical plate; $y = 0$ is at the
54 centreline of the flume (positive toward left when looking downstream); and $z = 0$ is at the surface of
55 the initial flat bed level at time $t = 0$.

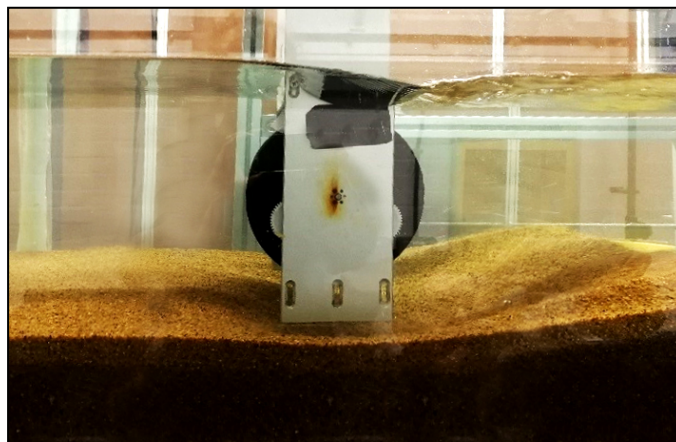


Fig. 1. Side view of the turbine in a preliminary experiment at $t = 6$ minutes. Flow is from left to right. Turbine is rotating clockwise.

56

57 2.1. Sediment

58 A difficult choice is the selection of particle size. The most common estuarine bed materials are
59 alluvial muds. Unfortunately, their binding forces and bed flow processes depend on the absolute
60 level of velocities and do not scale in any informative manner. Consequently, a uniform silica sand
61 was chosen with a median particle size $d_{50} = 1.37$ mm which corresponds, at operation scale, to coarse
62 gravel and thus has practical significance. This choice also accelerated scour process in the
63 experiments. The chosen particle size resulted in clear-water scour conditions with $U/U_{cr} = 0.93$
64 where U is mean velocity of approach flow ($= Q/(Bh)$ where Q and h are flow discharge and depth of
65 approach flow, respectively) and $U_{cr} (= U/\eta_*^{1/2}$, where η_* is relative flow intensity calculated
66 according to Yalin and da Silva 2001) is critical velocity for initiation of sediment movement.
67

68 2.2. Turbine

69 The turbine used in the present work was a Momentum Reversal-Lift (MRL) turbine. A review of the
70 turbine specifications is presented by Janssen and Belmont (2009), Ordonez-Sanchez et al. (2017)
71 and Sutherland et al. (2018). The novelty of the MRL turbine is that it extracts energy by deploying
72 both lift and momentum reversal (drag) of the flow on the turbine, thereby increasing power output.
73 MRL turbine has three symmetrical blades rotating 180° for one full rotation of the primary shaft of
74 the turbine. The high flow blockage ratio of the turbine makes it ideal for estuarine zones with shallow

75 water. In practice, MRL turbines would be operated in extended horizontal arrays; so the use of a
 76 relatively narrow flume, with narrow wall layers (i.e. small gradient of streamwise velocity near the
 77 walls), does not constitute an unacceptable artefact. To minimize adverse effects, the original model
 78 was altered, as shown in Fig. 2, by removing its supports which were solely for structural integrity of
 79 the turbine.
 80

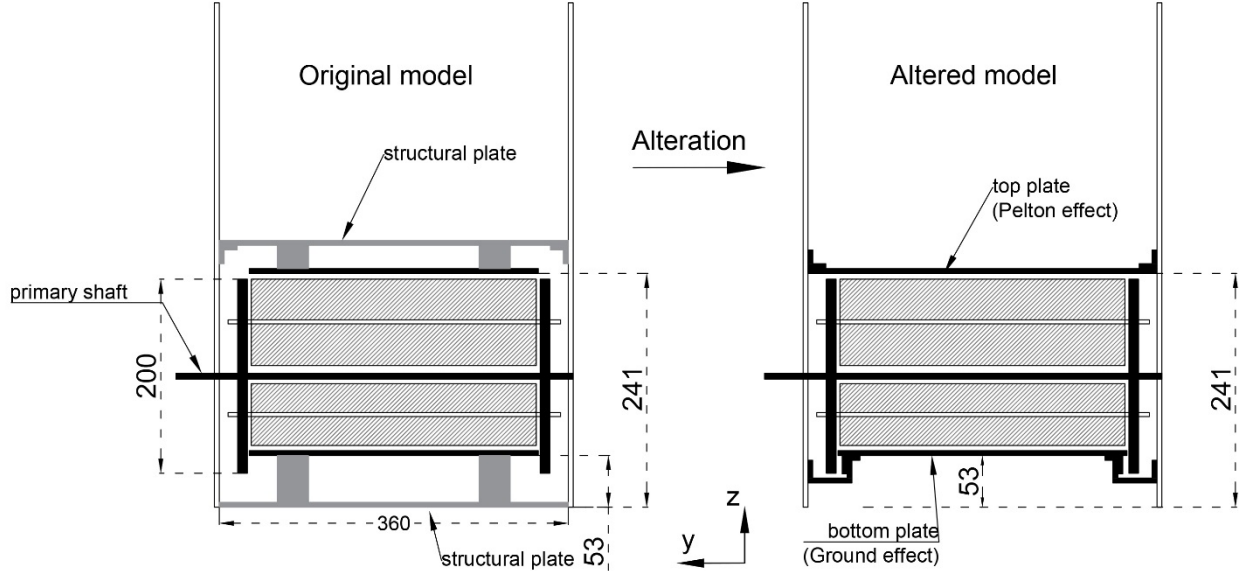


Fig. 2. Looking-downstream schematics of original (left) and altered (right) turbine models. Dimensions are in mm.

81

82 2.3. Hydraulic conditions of experiments

83 Four clear-water scour experiments were carried out with hydraulic conditions presented in Table 1.
 84 Here, R = flow Reynolds number ($= Uh/\nu$, with ν being fluid kinematic viscosity); F = Froude number
 85 ($= U/(gh)^{1/2}$, where g stands for acceleration due to gravity); d_s is the maximum measured scour depth;
 86 and x_s = longitudinal coordinates of the maximum scour depth. Reynolds number was kept within the
 87 turbulent flow regime ($R > 2000$ - 3000 , Chanson 2004) rather than ensuring strict similitude between
 88 the model and the prototype. Froude number was similarly kept within the subcritical regime ($F < 1$).
 89 Two rotation cases were examined; with the turbine fixed (non-rotating) and with it allowed to freely
 90 rotate. In the latter case, the turbine rotation speed is determined by a balance of the hydrodynamic
 91 forces with the frictional forces in the bearing, and therefore alters according to the hydrodynamic
 92 forces both between and during the experiments (as scour affects the hydrodynamic flow).

93

Table 1. Maximum scour depth measured in the present experiments

Run ^a	Description	h (± 1 mm)	Q (± 0.1 L/s)	R	F	U/U_{cr}	d_s (mm)	x_s (mm)
H1	With bottom plate (40 mm from bed)						95.7	376
H2	Without bottom plate	260	70	115702	0.28	0.93	69.7	519
H3	Stationary blades without bottom plate						$> 150^b$	$\sim 410^b$
P1	Without bottom plate						80.4	600

^a H and P experiments were carried out with turbine hanging from above (representing floating turbine) and turbine mounted on piers buried in sand bed, respectively. In all experiments vertical elevation of the turbine was identical to test H1.

^b scour reached flume bed and x_s is approximated value of location of maximum scour depth if bed thickness was not finite.

95

96 A schematic and photo of the looking-downstream cross section of the experiments are shown in Fig.
 97 3. Two sets of experiments were carried out: 1) H Runs with turbine hanging from above (representing

98 floating turbine) without extended side piers and 2) P Runs with the turbine being secured by
 99 extending its side piers into the sand and all the way to the flume bed (representing installation on
 100 piers). In all experiments, the turbine was installed at an elevation so that the bottom plate of the
 101 turbine was 40 mm from the bed. This elevation was chosen to maximise the scour seen during the
 102 experiment. To investigate the impact of the bottom plate, this was removed from certain runs as
 103 shown in Table 1.

104 The flow depth was identified as $h = 260$ mm to generate the maximum, streamwise, flow
 105 velocity (shown by the enhanced dot in Fig. 3) at the centre of the upper blade of the turbine. This
 106 was expected to be 89 mm from the free surface due to the dip phenomenon (Wang et al. 2001), where
 107 the maximum velocity occurs at a location below the free surface for cases with small aspect ratio
 108 B/h .

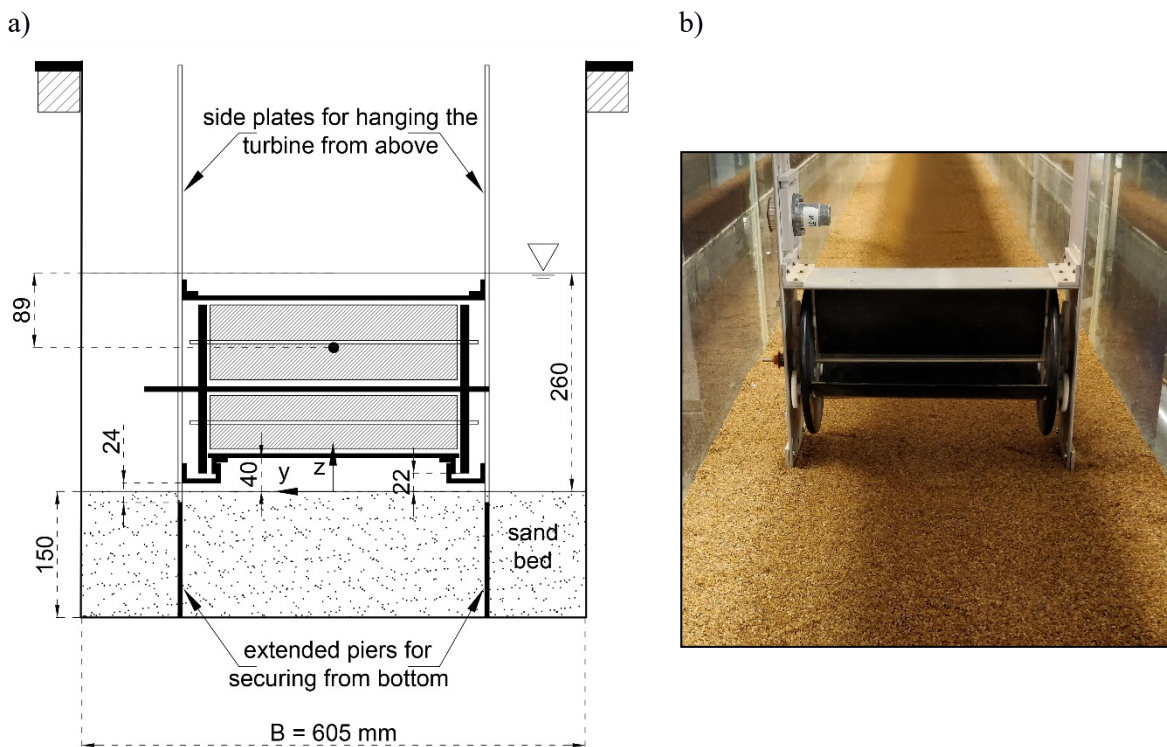


Fig. 3. Looking-downstream, cross-sectional schematic (left) and photo (right) of Run P1. The turbine was installed in two ways: 1) H Runs with turbine hanging from above (representing floating turbine) without extended side piers and 2) P Run secured by extended black plates buried in the bed. Enhance dot shows elevation of flow maximum velocity due to dip phenomenon (Wang et al. 2001).

109 Each experiment lasted 300 minutes at $U/U_{cr} = 0.93$. Although this duration was not sufficient
 110 to reach equilibrium scour depth, it was deemed acceptable to investigate the overall effect of turbine
 111 and its bottom plate on bed erosion. In Fig. 4, temporal variation of scour depth is shown in
 112 experiment P1 near the location of maximum scour downstream the turbine.
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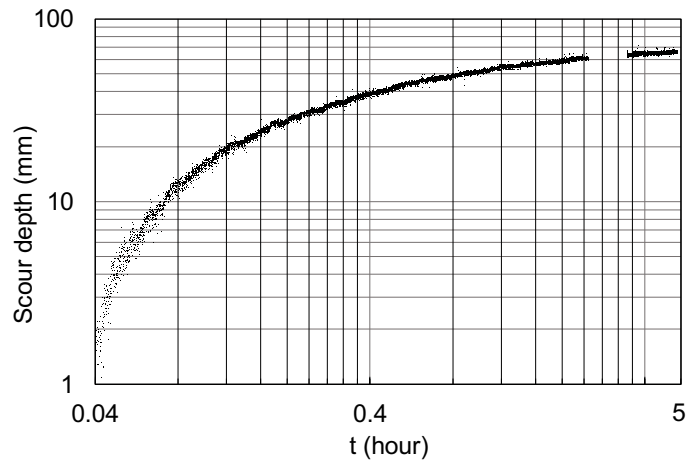


Fig. 4. Temporal variation of scour depth near the location of maximum scour depth in Run P1

114

115 3. Measurements

116

117 3.1. Flow discharge and free surface

118 Flow discharge was set by using a variable-speed drive on a centrifugal pump driving the flow. It was
 119 measured using an electromagnetic flowmeter (resolution ± 0.1 L/s) installed in the suction pipe of
 120 the water recirculating system. A digital point gauge was used to read the elevation of free surface at
 121 the centreline of the flume. The precision of this measurement was ± 0.5 mm due to free surface
 122 fluctuations.

123

124 3.2. Scour

125 In each scour experiment, the final scour topography (after 300 minutes) was mapped using an echo
 126 sounder. This was carried out in still water conditions after stopping the flow very gradually and
 127 removing the turbine. Scour topography was mapped by measuring distances from the bed on a grid
 128 of approximately 150 (x, y) points. The echo sounder utilised was one built into a Nortek Vectrino
 129 Profiler mounted on the traverse system of the flume. In this study, the Vectrino Profiler was used
 130 solely to measure bed topography; velocity profiles were not measured. The echo sounder used the
 131 time of flight of an acoustic signal to measure the distance to the bed and had an advertised accuracy
 132 of ± 0.5 mm. To improve the spatial resolution, additional manual measurements were taken at $x = x_s$
 133 and at the upstream end of the scour hole. This was carried out with a precision of ± 0.5 mm using the
 134 digital point gauge after slowly draining the flume. Measurements were generally only taken on one
 135 side of the flume due to the observed symmetry in the scour profile about the x - z plane. This symmetry
 136 was confirmed for Run H2 using scour measurements taken on both sides of the flume. The
 137 repeatability of the experiments was confirmed by comparing the maximum scour depth and overall
 138 scour pattern obtained after 300 minutes over two repetitions for a couple of scenarios. A final map
 139 of the scour was produced to a conservative accuracy of ± 2 mm by combining all the measured points.

140

141 3.3. Turbine revolution

142 In Runs H1 and H2, the temporal variation of the turbine rotation speed caused by the impact of the
 143 evolving scour pit on the hydrodynamics of the turbine was investigated. This was carried out by
 144 measuring the speed of the turbine rotation by video recording at $t = 0, 6, 12, 18$ and 295 minutes.

145

146 4. Results

147

148 4.1. Scour depth

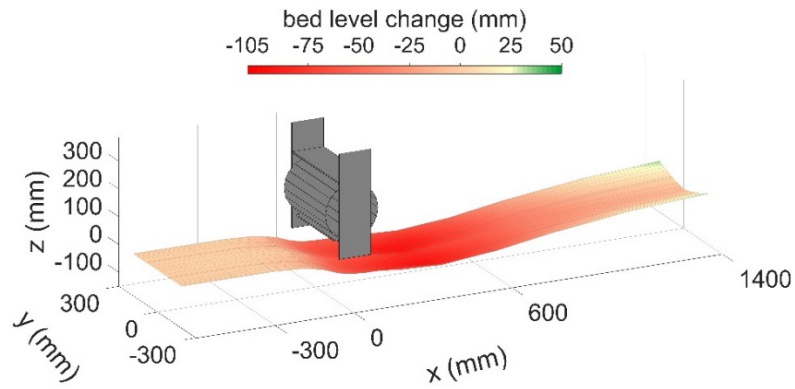
149 Fig. 5 illustrates scour maps, between $y = -190$ and 190 mm, measured at $t = 300$ minutes. The
150 maximum scour depth d_s was located downstream of the turbine anywhere between $x = 300 \sim 600$
151 mm. The eroded material was deposited further downstream at $x = 1500 \sim 4000$ mm in the form of a
152 $4.5 \sim 7$ cm-height dune which is not recorded here. This large dune started developing at the onset of
153 each experiment from the accumulation of eroded sand on the bed and could affect downstream
154 environment and navigation if reproduced for a real installation. As shown in the figure, the bed
155 significantly upstream of the turbine is not disturbed. This is due to the clear-water scour conditions
156 in the experiments. The turbine obstructs the flow and diverts it toward the bed thereby causing
157 significant scour downstream of the installation.

158 The first main observation is that the turbine caused significant erosion. This is presumed to
159 be due to the large cross-sectional blockage, being $\sim 35\%$ of cross-sectional area, at $t = 0$, of the
160 approach flow. By assuming an average scour depth of 100 mm after 300 minutes, the blockage ratio
161 is estimated to decrease to $\sim 29\%$ due to scour evolution. The exact values of maximum scour depth
162 d_s are summarised in Table 1. The largest scour depth among four experiments, occurred for Run H3
163 where the turbine blades were stationary and not spinning. The next greatest scour depths were for
164 Run H1 with bottom plate, Run P1 with extended legs and Run H2 without the bottom plate.
165 Removing the bottom plate in Run H2 caused the maximum scour depth to decrease by 28%
166 compared to Run H1. In Run H1, the bottom plate split the flow into two parts, i.e. the flow over the
167 plate and the accelerated flow beneath the plate, which separately rotated the turbine and eroded the
168 bed, respectively. In Run H2, however, the flow is not split and its entire momentum is used to rotate
169 the turbine as well as erode the bed. In Run H3, however, the turbine was still with a particular
170 orientation of blades that caused a large obstruction to the flow and directed the flow energy toward
171 the sand bed (see Fig. 6). This explains the larger scour depth in Run H3. In fact, the largest difference
172 in maximum scour depth, of over 80 mm, was between Runs H2 and H3. It must be emphasized that
173 an orientation of the turbine blades that is different to the one shown in Fig. 6 and poses a much
174 smaller obstruction to the flow, may lead to significantly reduced scour. This highlights the
175 importance of continuously monitoring the turbine operation since excessive scour may result
176 depending on the position in which the turbine stopped working.

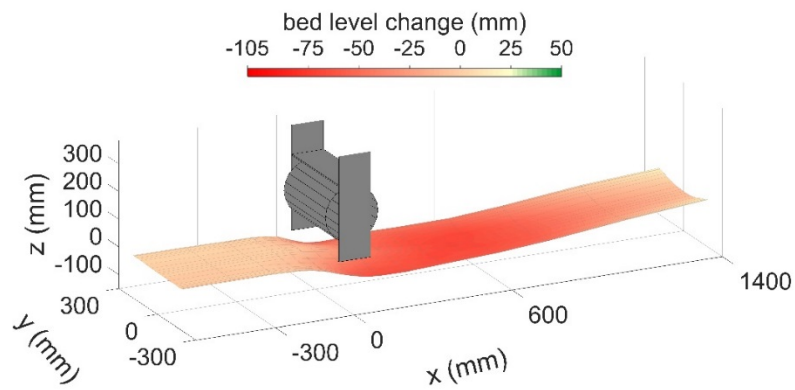
177 What is notable in Run P1, was local scour occurring around each of extended side piers of
178 the turbine which was ~ 7 mm deeper than scour downstream of the turbine. This also highlights the
179 importance of regular monitoring of bed status at the legs when the turbine is installed on buried legs.
180 The aforementioned scour made Run P1 stand out from the other three experiments. In addition, side
181 legs appear to have constricted the flow further toward the middle of the channel and slightly
182 increased scour depth.

183 Further in this work, the local scour at the legs was excluded from the analysis to facilitate the
184 comparison with the other experiments.

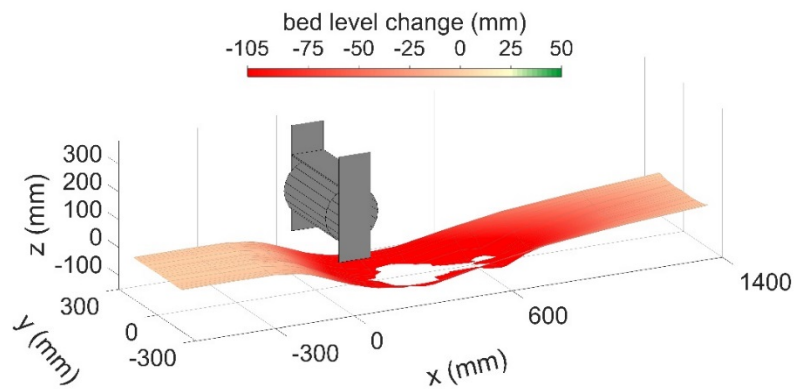
a) Test H1, $d_s = 95.7$ mm



b) Test H2, $d_s = 69.7$ mm



c) Test H3, $d_s > 150$ mm



d) Test P1, $d_s = 80.4$ mm

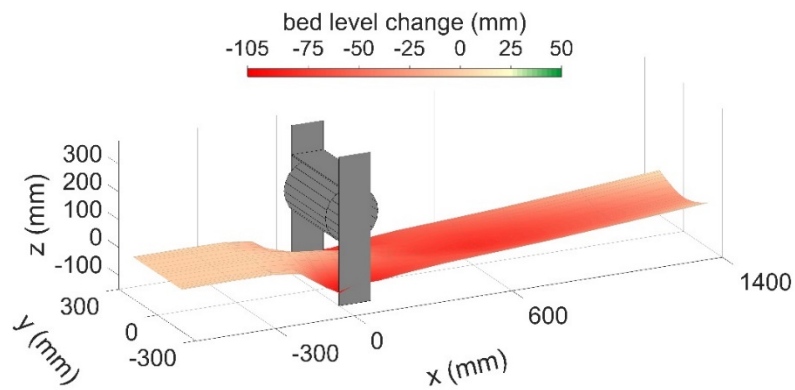


Fig. 5. Scour maps measured after 300 minutes

187 Fig. 6 illustrates longitudinal profiles of the bed topography along the centreline (CL) of the flume,
 188 i.e. at $y = 0$. For Run H1 an additional profile is shown at $y = -82$ mm (i.e. to the right of the centreline)
 189 which serves to point out the minor asymmetry of the bed topography. As seen earlier in Fig. 5,
 190 maximum scour depth is observed for Run H3 with the shown orientation of stationary blades. In this
 191 experiment, erosion reached the flume steel bed at about $t = 3$ hours. The exact value of the
 192 longitudinal coordinate of the maximum scour depth is presented in Table 1. In Run H1, maximum
 193 scour was observed closer to the turbine than in Runs H2 and P1. This can be explained by the
 194 presence of the bottom plate in Run H1 which channelled the flow towards the bed, while Runs H2
 195 and P1 had no bottom plate to direct the flow downward. This made the scour profile shallower but
 196 longer in Runs H2 and P1 compared to Runs 1 and 3.

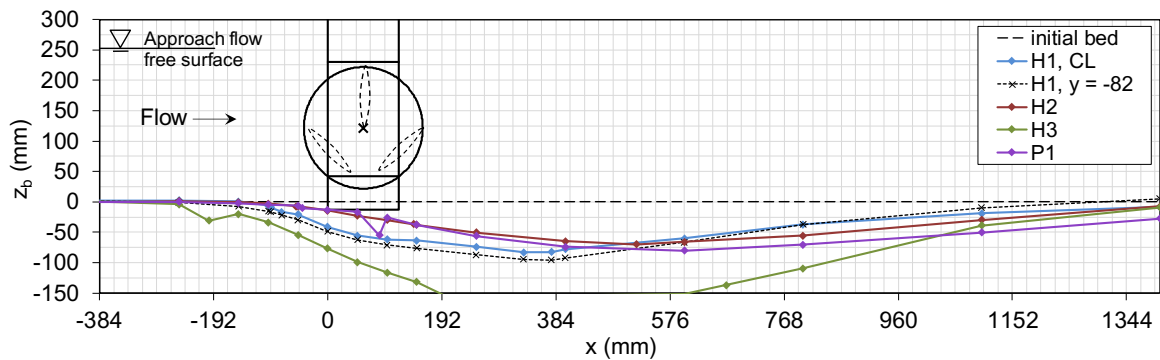


Fig. 6. Longitudinal scour profiles measured at centreline (CL) and $y = -82$ mm. Orientation of the blades at $t = 0$ is shown in the turbine circular disk.

197

198 4.3. Free surface profile

199 Fig. 7 shows variation of the elevation of the flow free surface, at the centreline, along the flume
 200 (except for Run P1 where the measurements downstream of the turbine were not available). This is
 201 presented in the form of differences of elevation relative to the elevation of the approach flow. The
 202 measured values are estimated to be accurate to within ± 1 mm. The location of the turbine is
 203 represented by the black vertical rectangle with the flow being from left to right. As shown, changes
 204 in the free surface profile follow a similar trend for all four runs. There is a free surface rise
 205 immediately upstream of the turbine followed by a sudden and notable drop just beyond the turbine
 206 downstream. Afterwards, the free surface would start to regain some of its approach elevation, but
 207 due to the limited length of the flume it was not possible to determine whether it would ever fully
 208 attain its initial elevation. The free surface drop was largest in Run H3 because of the orientation of
 209 the stationary blades of the turbine which caused a larger acceleration to the flow. In Run H1 with
 210 bottom plate, the free surface rise and drop-off were smallest. This agrees with Gebreslassie (2012)
 211 who found that the bottom plate reduces free surface disturbances in the wake region of the turbine.
 212 For Run H2, approximate measurements suggested a profile shown by the dashed line which is
 213 between those of Runs H1 and H3. This implies a smaller adverse effect of the turbine on downstream
 214 flow compared to Run H3. For Run P1, the free surface profile downstream of the turbine is expected
 215 to be closest to Run H2.

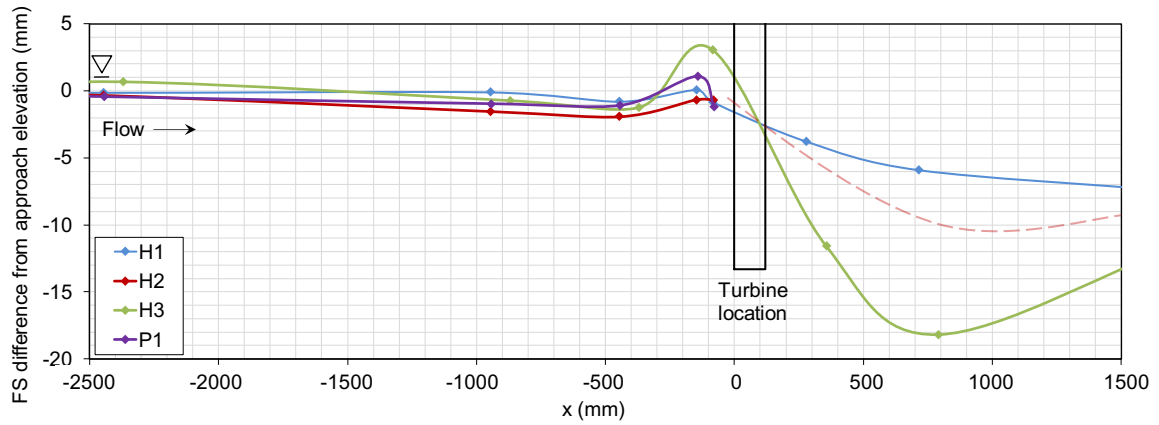


Fig. 7. Variation of flow free surface elevation along the flume at $t = 0$

216

217 4.4. Turbine tip-speed ratio (TSR)

218 The tip-speed ratio (TSR) of the turbine will determine the efficiency in producing electricity from
 219 the turbine. Although electricity production was not examined in this work, the effect of scour on
 220 TSR was investigated. TSR is defined as the ratio between the tangential speed of the tip of a blade
 221 and the flow velocity as following

222

$$\text{TSR} = \frac{\omega \times \text{turbine radius}}{U}$$

223

224 where ω is the rotational speed of the turbine in rad/s, turbine radius is assumed 0.2m (see Fig. 2),
 225 and U is mean velocity of approach flow. Temporal variation of TSR is shown in Fig. 8. Dash lines
 226 show curves visually fitted to the data. In Run H3, the turbine blades were stationary and $\text{TSR} = 0$.
 227 Run P1 was also excluded since it was expected to have a similar rotational speed to Run H2. There
 228 are three findings from Fig. 8:

229

230 1. The turbine TSR progressively decreased with scour evolution. In 300 minutes, this reduction was
 231 8% and 11% in Runs H1 and H2, respectively. It should be noted that the TSR is computed relative
 232 to the approach flow velocity U , which is constant since there has not been any scour upstream of
 the turbine.

233

234 2. The removal of the bottom plate in Run H2 reduced N by $\sim 12\%$ compared to Run H1, which is
 235 envisaged to be due to the enhancing effect of the bottom plate on the turbine performance. This
 236 highlights the importance of regular check-ups on the turbines to ensure that all structural
 components are accurately positioned and fully functional.

237

238 3. Rotational speed of the turbine in Run H1 continues to drop throughout the experiment, while in
 239 Run H2 it stabilizes after about 20 minutes. This is due to difference of scour depth, d_s , in Runs
 240 H1 and H2. In Run H2, smaller d_s is reached faster compared to Run H1 in which d_s takes longer
 to be attained.

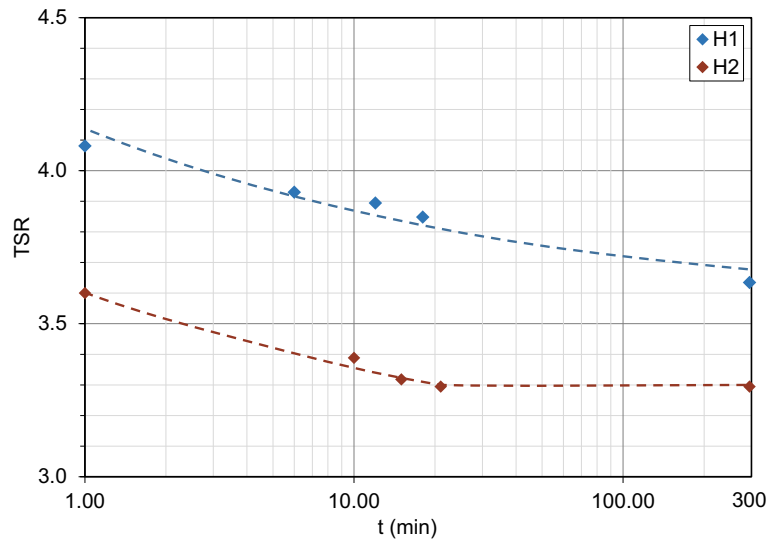


Fig. 8. Temporal variation of turbine TSR

242

243 5. Conclusions

244

245 This report presents findings from flume experiments on clear-water scour for a novel design of cross-
 246 flow turbine referred to as the MRL turbine. The main conclusions from this work are as follows.

247

- 248 1. The MRL turbine was found to produce significant downstream scour. The eroded sediment
 249 caused large deposition further downstream of the turbine which could have adverse impacts on
 250 the environment, navigation and habitat.
- 251 2. The scenario with the stationary turbine led to the largest scour. This is envisaged to be due to 1)
 252 special orientation of the blades, and 2) the turbine not spinning, both of which caused a large
 253 obstruction to the flow and directed all the flow energy toward eroding the sand bed. This result
 254 highlights the importance of continuously monitoring the turbine operation.
- 255 3. The turbine was found to run slower without the bottom plate, which is in agreement with previous
 256 findings in the literature (e.g. Gebreslassie 2012). This highlights the importance of regular
 257 inspection of the turbines to ensure all structural components are present and adequately secured.
- 258 4. Although the bottom plate was found to increase scour, it reduced flow free surface disturbance in
 259 the wake region of the turbine.
- 260 5. Temporal evolution of scour was found to reduce the rotational speed of the turbine, i.e. its
 261 efficiency in power production.
- 262 6. When the turbine was installed on piers (extended legs), it produced considerable local scour at
 263 the piers. The depth of scour at these locations could be even greater than the scour depth
 264 downstream of the turbine. This also needs regular monitoring to ensure stability of the turbine
 265 foundations.

266

267 Whilst these experiments have naturally been carried out for a specific (and novel) design of
 268 turbine, there is no reason to believe that such effects would not be at least as significant for any
 269 particular design of hydrokinetic turbine, leading the authors to emphasize the importance of further
 270 investigation of these scour effects.

271

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273

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277

278 **References**

279

- 280 Chanson, H. (2004). *Hydraulics of Open Channel Flow*. Butterworth-Heinemann.
- 281 Elghali, S. E. B., Benbouzid, M. E. H., and Charpentier, J. F. (2007). "Marine Tidal Current Electric
282 Power Generation Technology: State of the Art and Current Status." *2007 IEEE*
283 *International Electric Machines Drives Conference*, 1407–1412.
- 284 Gebreslassie, M. G. (2012). "Simplified CFD modelling of tidal turbines for exploring arrays of
285 devices." PhD thesis, Univeristy of Exeter.
- 286 Gebreslassie, M. G., Tabor, G. R., and Belmont, M. R. (2013a). "Numerical simulation of a new
287 type of cross flow tidal turbine using OpenFOAM – Part I: Calibration of energy
288 extraction." *Renewable Energy*, 50, 994–1004.
- 289 Gebreslassie, M. G., Tabor, G. R., and Belmont, M. R. (2013b). "Numerical simulation of a new
290 type of cross flow tidal turbine using OpenFOAM – Part II: Investigation of turbine-to-
291 turbine interaction." *Renewable Energy*, 50, 1005–1013.
- 292 Hill, C., Kozarek, J., Sotiropoulos, F., and Guala, M. (2016a). "Hydrodynamics and sediment
293 transport in a meandering channel with a model axial-flow hydrokinetic turbine." *Water*
294 *Resources Research*, 52(2), 860–879.
- 295 Hill, C., Musa, M., Chamorro, L. P., Ellis, C., and Guala, M. (2014). "Local Scour around a Model
296 Hydrokinetic Turbine in an Erodible Channel." *Journal of Hydraulic Engineering*, 140(8),
297 04014037.
- 298 Hill, C., Musa, M., and Guala, M. (2016b). "Interaction between instream axial flow hydrokinetic
299 turbines and uni-directional flow bedforms." *Renewable Energy*, 86, 409–421.
- 300 Janssen, A. P., and Belmont, M. R. (2009). *Initial research phase of MRL turbine. Technical Report*
301 *No: MO 562L*. U.K.
- 302 Magagna, D., and Uihlein, A. (2015). "Ocean energy development in Europe: Current status and
303 future perspectives." *International Journal of Marine Energy*, 11, 84–104.
- 304 Musa, M., Heisel, M., and Guala, M. (2018a). "Predictive model for local scour downstream of
305 hydrokinetic turbines in erodible channels." *Physical Review Fluids*, 3(2), 024606.
- 306 Musa, M., Hill, C., Sotiropoulos, F., and Guala, M. (2018b). "Performance and resilience of
307 hydrokinetic turbine arrays under large migrating fluvial bedforms." *Nature Energy*, 3, 839.
- 308 Ordonez-Sanchez, S., Sutherland, D., Payne, G. S., Bruce, T., Gebreslassie, M., Belmont, M. R.,
309 and Moon, I. (2017). "Experimental evaluation of the wake characteristics of cross flow
310 turbine arrays." *Ocean Engineering*, 141, 215–226.
- 311 Sutherland, D., Ordonez-Sanchez, S., Belmont, M. R., Moon, I., Steynor, J., Davey, T., and Bruce,
312 T. (2018). "Experimental optimisation of power for large arrays of cross-flow tidal
313 turbines." *Renewable Energy*, 116, 685–696.
- 314 Wang, X., Wang, Z.-Y., Yu, M., and Li, D. (2001). "Velocity profile of sediment suspensions and
315 comparison of log-law and wake-law." *Journal of Hydraulic Research*, 39(2), 211–217.
- 316 Yalin, M. S., and da Silva, A. M. F. (2001). *Fluvial processes*. IAHR, Delft.

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