

1 **Comparative analysis of System Dynamics and Object-Oriented Bayesian Networks**
2 **modelling approaches for aquifer systems management: application to the Kairouan**
3 **aquifer (Tunisia)**

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12

13 **Abstract**

14 A comparative analysis of two different modelling approaches, System Dynamics Modelling
15 (SDM) and Object-Oriented Bayesian Networks (OOBN) is presented, with application to
16 aquifer management in Tunisia. Both techniques have recently become extensively used for
17 environment and water resources modelling due to their relative advantages, mainly with
18 regard to their flexibility, effectiveness in assessing different management options, ease of
19 operation and suitability for encouraging stakeholder involvement. On the other hand, both
20 approaches have several differences in the underlying mathematical background that make
21 them complementary and/or suitable for different water and environmental systems problems.
22 SDM is more suitable for simulating dynamics and behaviour of the processes, considering

23 feedback loops, non-linearity, the simulation of many interacting sub-systems, or facilitating
24 the communication with various water actors. OOBN modelling is a very powerful tool for
25 modelling systems with uncertain inputs (or outputs) characterised by probability
26 distributions, thus incorporating uncertainty, facilitating the use of hierarchical modelling by
27 improving the efficiency and communication between the different parts of a model. This
28 comparative analysis is applied to the overexploited Kairouan aquifer system in Tunisia,
29 where the groundwater supplied by this aquifer plays an essential role for the socio-economic
30 development in the region. Considering the geopolitical context in that area, aquifer
31 management is becoming ever more important due to the groundwater resources being
32 predominantly the only or most stable available fresh water source. Both models produced
33 comparable results using the baseline data, and generally agreed on scenario tests, showing
34 that pumping to coastal cities may prove key to reducing the current aquifer deficit. It is
35 suggested here that water management assessment should be tackled by using both models in
36 parallel to complement each other, adding depth and insight to results and giving a more
37 coherent picture of the problem being addressed, allowing for more robust policy decisions to
38 be made.

39 **Keywords:** aquifer, Object-Oriented Bayesian Networks, System Dynamics, water
40 management.

41

42 **1. Introduction**

43 Water scarcity in semiarid regions is a serious and expanding threat to many people living in
44 these areas. Population increases and the general consensus from climate change studies,
45 which suggest lower rainfall totals and/or more erratic rainfall or changes to the seasonality
46 of rainfall in critical regions such as the Mediterranean (Arnell et al., 2004), suggest that

47 this threat is likely to intensify in the near future. Water consumption increases with
48 population and with local and regional development as living conditions improve, while the
49 supply is either stable or falling, leading in some cases to 'closed basins', where the entire
50 renewable water resource in a given hydrological basin is being exploited (Falkenmark and
51 Molden, 2008). The total volume of groundwater resources used annually is estimated at 600-
52 700 km³, representing c. 20% of global water use (WWAP, 2009), and is rising rapidly,
53 particularly in arid and semiarid regions. Many of the Northern African and Middle Eastern
54 countries largely rely on (fossil) groundwater resources. Consequently, there is an urgent
55 need to assess groundwater management in these critical parts of the globe. This issue has
56 been brought up at the Rio and Dublin Earth Summits (World Water Assessment Programme,
57 2009). This assessment in its most basic form entails estimation of the volume of water supply
58 and demand. Subsequently, more detailed investigations into planning and management
59 practices (e.g. regulatory reform, policies, efforts to save water or be more efficient) can be
60 investigated.

61 In this paper we compare and contrast two methods for the assessment of groundwater
62 resources in a Tunisian aquifer that is undergoing over-exploitation. At the WaterMatex 2011
63 conference (8th IWA Symposium on Systems Analysis and Integrated Assessment, 19-22
64 June 2011, San Sebastian, Spain), discussions made clear that the development of new
65 systems analysis and management tools is not necessarily required. More important is the
66 proper characterisation and assessment of existing tools such that their full capabilities can be
67 exploited. In line with this point of view, this paper contributes to the characterisation and
68 comparative assessment of two modelling approaches applied for water resources analysis:
69 System Dynamics Modelling (SDM) and Object-Oriented Bayesian Network (OOBN)
70 modelling.

71 SDM and BNs have been previously combined for modelling water management in the same
72 case study (Ribarova et al., 2011, Vamvakeridou-Lyroudia et al, 2009), but the application in
73 this case was complementary and supplementary, rather than comparative. SDM was applied
74 for simulating industrial water management, while BN modelling targeted domestic water
75 demand. A systematic comparison of both methods applied for the same water system, with
76 the same data, has not been published before, to the best of the authors' knowledge.

77 The paper is organised as follows. The two methods and modelling techniques are described
78 (Section 2). Then the case study is introduced (Section 3) followed by descriptions of the
79 model formulation, structure and implementation using the two methods (Sections 4 and 5).
80 Complete descriptions of the scenarios together with the modelling results are presented in
81 the context of the case study in Section 6. Finally, the two modelling approaches are
82 discussed, and their suitability to groundwater assessment is assessed.

83

84 **2. Methods**

85 **2.1 System Dynamics Modelling**

86 SDM is a methodology for studying complex feedback systems. Forrester (1961) introduced
87 SDM as a modelling and simulation methodology for long-term decision-making in dynamic
88 industrial management problems. SDM has been applied to business policy and strategy
89 problems (Barlas, 2002; Sterman, 2000), and to the study of complex environmental (Ford,
90 1999; Mazzoleni et al., 2004; Mulligan and Wainwright, 2004) and water systems (Chung et
91 al., 2008; Li and Simonovic, 2002; Simonovic, 2002), and has been applied at a range of
92 scales from local (Khan et al., 2009) to global (Kojiri et al., 2008; Simonovic, 2002). SDM is
93 particularly useful when studying complex systems with many interacting elements, the

94 behaviour of which cannot be easily predicted, if at all. It allows one to examine behaviour
95 modes and system response as different variables are altered. As such, it is not accurate
96 numerical prediction that is sought. Rather it is a deeper understanding of what drives system
97 response, and how this manifests in terms of behaviour on the larger scale. This behaviour is
98 driven by all the interconnecting elements, and not by any single factor. A classic example of
99 the behaviour-mode type of analysis is given in *The Limits to Growth* (Meadows et al.,
100 1972).

101 Development of SDMs typically follows an iterative approach. Initially, non-numeric models
102 are drawn up to define the system structure and to identify the key feedbacks and causal
103 relationships in a system. Feedback polarity between elements (positive feedback polarity
104 represents a self-supporting loop and vice-versa) is identified. Understanding the causal
105 structure in a SDM is critical to further model development. Quantitative models are then
106 developed gradually until the desired level of detail and complexity is shown (Haraldsson and
107 Sverdrup, 2004).

108 SDM components are described as interlinked compartments (stocks), flows (directed links)
109 and converters (influences) (Ford, 1999). Stocks represent nodes where a material (e.g. water
110 in a reservoir, money, population) is accumulated. Flows represent the physical movement of
111 material into or out of stocks (e.g. river inflow or evaporation, cash deposits or withdrawals,
112 births or deaths). Converters act to modify the rate of the flows according to some prescribed
113 rules (e.g. evaporation rate, interest rate on a bank account or birth and death rates).

114 Converters also act to create feedback within a system along with connecting arrows (links).

115 The causal relationships between parameters lead to model behaviour patterns. SDM

116 simulates a system over time by solving the mathematical functions for each element

117 iteratively for the duration of the simulation. Due to the feedback driven nature of SDMs, the

118 value of a stock from one model timestep influence the values of the converters, and thus the
119 flows and stocks, at the next model timestep in a feedback loop.

120 The most well-known SDM packages include: SIMILE (Muetzelfeldt and Massheder, 2003),
121 VENSIM (www.vensim.com), STELLA (www.iseesystems.com), POWERSIM
122 (www.powersim.com) and SIMULINK – an add-on to MATLAB (www.mathworks.com).

123 Mathematically, most existing SDM environments are similar. With the aid of graphical
124 development environments, model development can occur with the help of non-specialist
125 stakeholders, allowing the model to gradually develop complexity and to have a structure
126 suited to the problem under study. Scenario testing can be easily undertaken, allowing users
127 to fully explore a system. For example, the values in converters can quickly be altered and the
128 model re-run to provide simulation results under new conditions. This also allows for a 'what-
129 if' style of analysis. SDM is not explicitly spatially-based. SDM is not designed as a
130 replacement of more specific geo-spatial models (e.g. physically-based rainfall-runoff
131 models); it focuses rather on broad-scale system behaviour patterns than on fine-scale
132 accurate physical representation. SIMILE (Muetzelfeldt, 2010; Muetzelfeldt and Massheder,
133 2003) (www.simulistics.com) has been used in this study. It attempts to overcome issues
134 including: increased system complexity, the skill required to program a more traditional
135 model, the lack of transparency and the lack of re-usability of existing models (Muetzelfeldt
136 and Massheder, 2003). Ultimately, the inability of some modelling approaches (e.g.
137 physically-based catchment models) to be able to handle many widely different, but
138 interconnected sub-systems simultaneously (Muetzelfeldt, 2010). All of these, SIMILE (and
139 other SDM programs) overcome by combining System Dynamics and object orientated
140 programming.

141

142 **2.2 Object-Oriented Bayesian Networks Modelling**

143 Bayesian Networks (BNs) are based on a branch of statistics developed in the 18th century by
144 Thomas Bayes and have been around since 1921. BNs have been used as a modelling tool as
145 part of the development of decision support systems in diverse fields such as medicine, road
146 safety and artificial intelligence; however, they have not been widely applied to
147 environmental systems until recently (Ordoñez Galán et al., 2009). Increasingly, BNs are
148 being used to model diverse problems of high complexity for water management applications
149 (Varis and Fraboulet-Jussila, 2002; Borsuk et al., 2004; Little et al., 2004; Bromley et al.,
150 2005; Martin de Santa Olalla et al., 2006; Castelletti and Soncini-Sessa, 2007; Henriksen and
151 Barlebo, 2007; Ticehurst et al., 2007; Farmani et al., 2009a; Malekmohammadi et al., 2009;
152 Morteza Mesbah et al., 2009, Vamvakeridou-Lyroudia et al, 2009).

153 BNs can be defined as a graphical representation of Bayesian probabilities, formally known
154 as 'Directed Acyclic Graphs' (Cain, 2001; Molina et al., 2010). The acyclic part in this
155 definition is crucial, as it implies a lack of ability to handle feedback. This technique is found
156 to be applicable as a type of Decision Support System (DSS) based on a probability theory
157 which implements Bayes' rule (Pearl, 1988; Bayes, 1991; Jensen, 1996; Jensen, 2001). The
158 multilateral properties of BNs allow their use in resource and environmental modelling (Varis
159 and Kuikka, 1999). Cain (2001) defined BNs as "some nodes that represent random variables
160 that interact with others. These interactions are expressed like connections between
161 variables". The use of BNs presents a series of advantages over other environmental DSSs
162 (Bromley et al., 2005; Castelletti and Soncini-Sessa, 2007; Molina et al., 2010). According to
163 Borsuk et al. (2004), the graphical structure explicitly represents a cause-effect relationship
164 between system variables that may be obscured under other approaches.

165 A BN consists of three main elements: (1) a set of variables representing the factors relevant
166 to a particular environmental system; (2) the relationships between these variables that
167 quantify the links between variables; and (3) the set of conditional probability tables (CPTs)
168 quantifying the links between variables that are used to calculate the state of nodes. The first
169 two elements form a Bayesian Diagram and the addition of the third forms a full network.
170 The CPTs are defined within the BN modelling software based on the characteristics of the
171 input data used.

172 Object-Oriented Bayesian Networks (OOBNs) are an advance on traditional BNs based on
173 Object-Oriented Programming (Molina et al., 2010). OOBNs are hierarchical descriptions of
174 real-world problems that mirror the way in which humans conceptualise complex systems. To
175 cope with complexity, humans think in terms of hierarchies of different classes (Molina et al.,
176 2010). There are several important features that characterise the use of OOBNs over
177 traditional BNs. First, they allow consideration of the uncertainty in every single variable of
178 the models through the implementation of the CPTs, which allows for the possibility of
179 taking into account the error or noise in the variable(s). For hydrological processes this can
180 become important due to the stochastic nature of the processes. Encapsulation of the internal
181 details of a class means that some objects can be hidden and only those objects required for
182 interfacing with other classes need to be exposed, making the modelling environment more
183 user-friendly. Inheritance allows a class to inherit the attributes and methods of another class.
184 Polymorphism allows objects to be of different types or nature, allowing a more accurate
185 representation of the real-world. This means for instance that economic, physical, social and
186 other variables can all be represented together, something which is essential if real-world
187 environmental problems are to be realistically modelled. A further feature is that because
188 systems are often composed of collections of identical or almost identical components,

189 models of many systems contain repetitive patterns and the notion of instance nodes makes it
190 very easy to construct multiple identical instances of a network fragment.

191 Although traditional BNs are not intended for dynamic analysis, which forms one of its main
192 disadvantages, 'time slicing' techniques provide one way to generate predictive simulations.
193 In this sense, dynamic BNs work like Markov Chains of multiple time order (Petri nets) that
194 are aimed to be a transient way of BN modelling, considering each time step of a transient
195 and/or predictive model (Molina et al., 2011a). OOBNs can be easily coupled with other
196 simulation or optimisation models (Farmani et al., 2009b; Molina et al., 2011b), tools or
197 algorithms. Finally, the BN representation through a graphical display makes communication
198 between stakeholders or water actors simple, thus promoting their involvement in water
199 management problems.

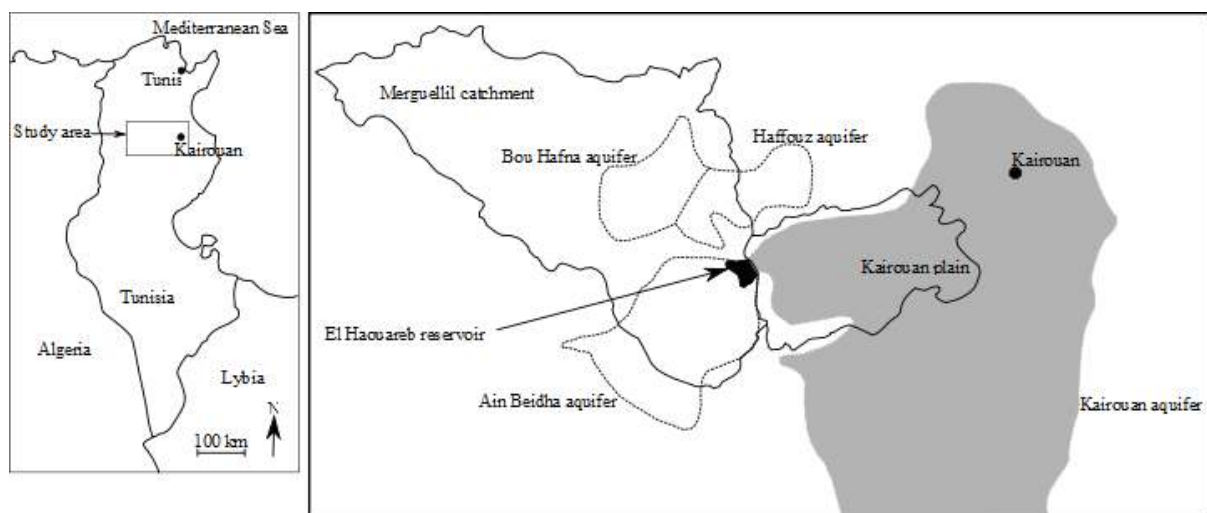
200 Table 1 compares the main features of the SDM and OOBN approaches. Both modelling
201 approaches have been used widely in order to assist in (sustainable) aquifer/groundwater
202 management studies, illustrating the applicability of each method to the present study (e.g.
203 Stave, 2003; Henriksen et al., 2007; Khan et al., 2009; Martinez-Santos et al., 2010).

204

205 **3. Case Study description and model development**

206 The same case study has been formulated in each modelling approach using the same input
207 data. The case study is the Kairouan aquifer region in Tunisia, covering an area of c. 3000
208 km² (Figure 1). Rainfall is low (c. 300-500 mm yr⁻¹, with variability of 100-700 mm yr⁻¹) and
209 falls in discrete, intense showers. The Kairouan aquifer, which is the main stable water source
210 in the region, is subject to over-abstraction with the water table in the area observed to be
211 dropping (Le Goulven et al., 2009), with subsequent impacts on water quality and future

212 water availability. Agriculture is the largest regional water user, accounting for 80% of local
213 water consumption (Chahed et al., 2008), and is the main socio-economic activity. Domestic
214 and industrial uses make up the remainder of the local consumption with both forecasted to
215 increase. Officially, re-use of treated waste water is not permitted for either domestic or
216 irrigation use due to concerns over the quality of the returning water. Despite this, a fraction
217 is re-used due to illegal recharge and leakage from pipes and tanks. There is also a small, but
218 critical natural water demand which goes to maintaining fragile *sebkha* (salt-flat/marsh)
219 regions. Protecting this fragile ecosystem type is critical, but depends strongly on available
220 water (quality) from the aquifer. Modelling may help determine if these sensitive regions may
221 be threatened in the near future as a result of aquifer overexploitation.



222
223 Figure 1: Map showing the Tunisia case study area.

224
225 Once local water uses have been accounted for, most of the remaining water is pumped out of
226 the Kairouan aquifer and transferred to the coast in order to satisfy the water demands of
227 tourist resorts (e.g., swimming pools, golf courses). This transfer represents volumetrically
228 the major abstraction from the aquifer, and is the main reason for the current over-

229 exploitation. Current government policy is to reduce this pumped volume by c. 50% by 2030
230 in an attempt to reduce the water deficit.

231 The SDM used here is a simplified version of a more complex model developed for the
232 European Commission Seventh Framework (EC FP7) research project 'Water Availability
233 and Security in Southern Europe and the Mediterranean (WASSERMed) (Susnik et al, 2012).
234 The WASSERMed model has been simplified for the purposes of this comparative study. The
235 WASSERMed model was developed closely with local Tunisian project partners and
236 stakeholders INAT (Institut National Agronomique de Tunisie). Model development represents a
237 cooperative, participatory effort, with the local experts informing on critical aspects of the model
238 structure and the available data for different parts of the model. They also gave critical information
239 regarding potential policy measures aimed at reducing future water demand. Model development was
240 carried out in stages, each stage iteratively assessed and improved in participatory mode. So, at each
241 stage the model was assessed by INAT to ensure that the Kairouan system was being accurately
242 represented, and to ensure that model behaviour was representative according to local knowledge and
243 observation. Several iterations were completed until the model was deemed satisfactory by INAT and
244 the research team (University of Exeter) alike. It is noted that before any quantitative model
245 development took place, conceptual (Vamvakeridou-Lyroudia et al, 2008) and causal loop (Susnik et
246 al, 2012) modelling was conducted. This was done in order to help define the system boundaries and
247 key interactions, to help define data requirements, and to act as a guide for quantitative model
248 development. There are other examples of SDMs being developed in a cooperative nature with close
249 guidance from local experts and stakeholders (e.g. Ahmad and Simonovic, 2000; Stave, 2003; Tidwell
250 et al., 2004).

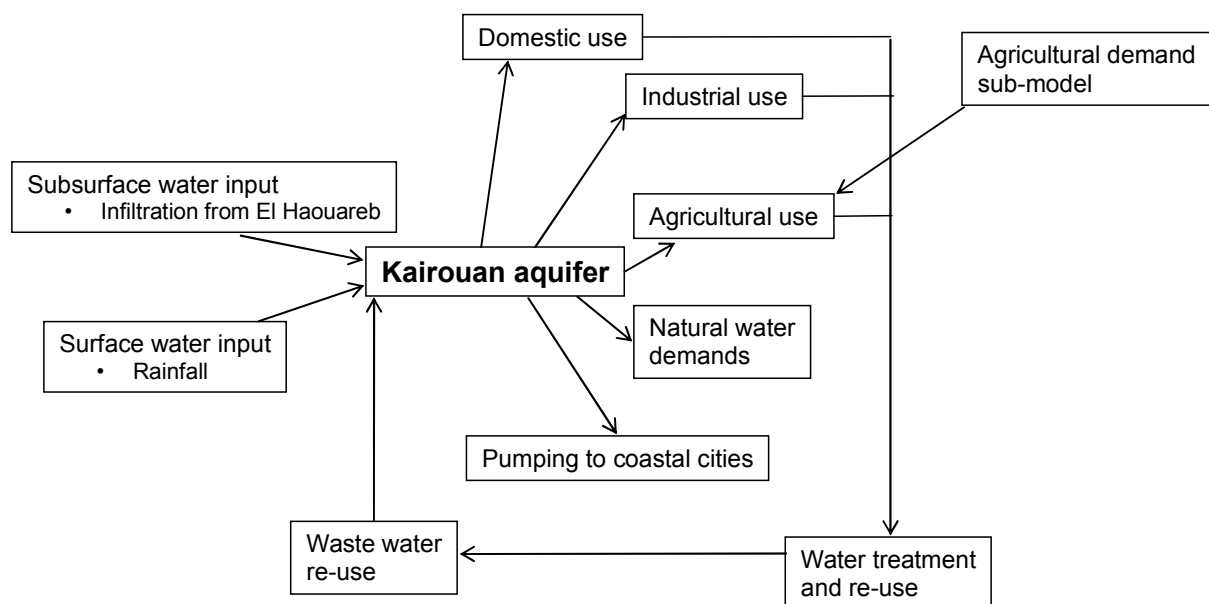
251 OOBN model development was largely informed by the developments of the SDM as it was not part
252 of the WASSERMed project. The key SDM aspects (i.e. the various interconnections and feedbacks,
253 inflows, demands) were used to inform the OOBN model structure and connections. However, the
254 OOBN was developed in a way viable and suitable for OOBN representation. Therefore, the two

255 models do not agree exactly in structure. As with SDM, there are also examples of OOBNs being
256 developed in a participatory, cooperative nature (e.g. Castelletti and Soncini-Sessa, 2007; Henriksen
257 et al., 2007; Ross and Martinez-Santos, 2010).

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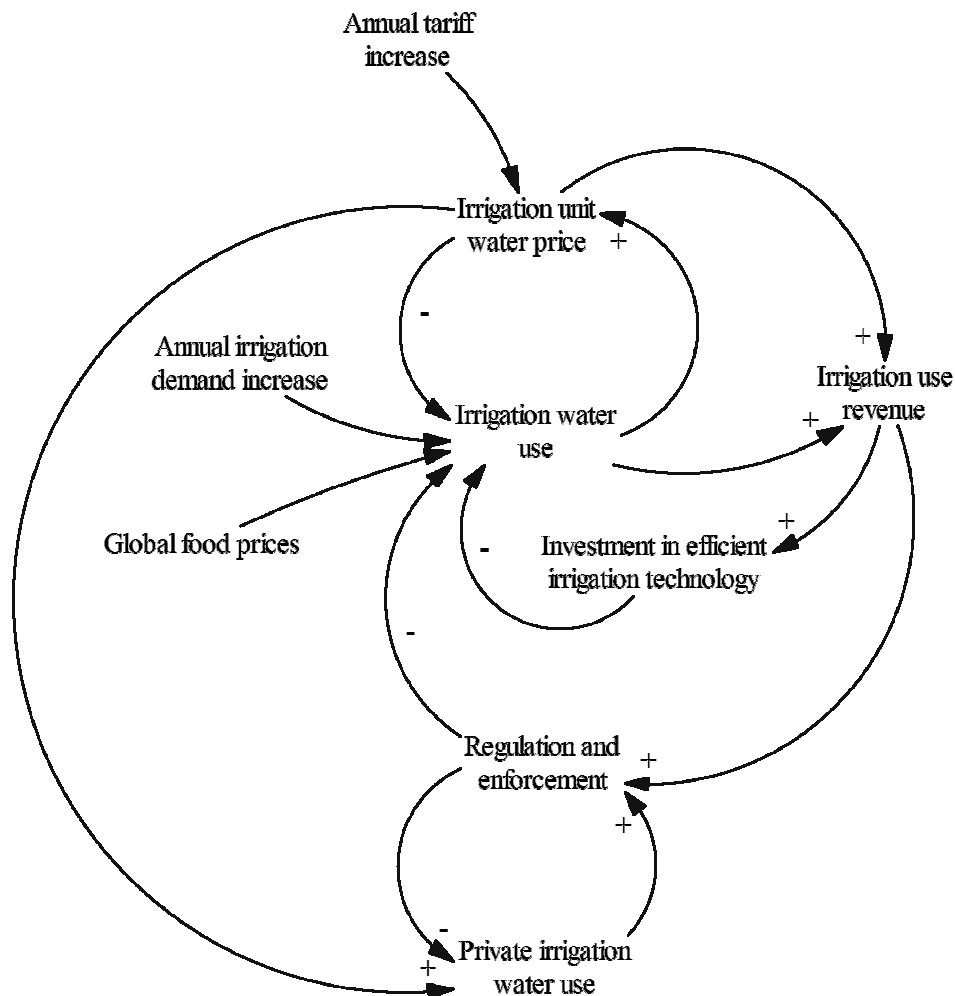
259 4. SDM implementation

260 For the purposes of this comparison, a simplified version of a more complicated SDM
261 developed for the Kairouan aquifer (Sušnik et al., 2011a; Sušnik et al., 2011b, Sušnik et al,
262 2012) has been implemented (Section 3 and Figure 2a). Sufficient information has been
263 retained to suggest that model results should correlate closely to those from the more
264 comprehensive model. It is noted that the behaviour of the model in terms of the pattern of
265 water volume in the Kairouan aquifer over time is more important than accurate numerical
266 prediction of water volumes. It was critical to ensure that the simplified model still exhibited
267 sufficient complexity, and that it integrated the water-balance aspect with socio-economic
268 concepts.



269

270 Figure 2a: Schematic representation showing the main links and relationships in the SDM
271 implemented here. This does not show the full complexity of the model. Agricultural water
272 demand is predicted using a more complex separate sub-model (Figure 2b).



273

274 Figure 2b: Causal loop diagram illustrating the complexity of the agricultural demand sub-
275 model. Arrows are labelled with polarity. Positive polarity indicates positive feedback, and
276 vice-versa.

277

278 The main simplifications from the WASSERMed model (Sušnik et al., 2011a, b; Sušnik et
279 al., 2012) are related to the aquifer inputs, and the domestic, industrial and coastal pumping

280 demands. In these cases, the complex sub-models from the WASSERMed model have been
281 replaced with time-series' and therefore do not exploit the full utility of SDM. However, the
282 agricultural demand sub-model has been retained (Figure 2b), for three reasons: i) it allows
283 some investigation into the complexity of this sub-system, utilising the capability of SDM to
284 represent feedback loops and non-linearity; ii) agriculture is the main water consumer in the
285 region, and is the dominant economic activity with socio-economic implications; and iii) the
286 model is still simple enough to allow for meaningful comparison with the OOBN model, but
287 also allows for good contrast of the relative merits of the two modelling paradigms.

288 The SDM (Figure 2) includes as inflows: infiltration leakage from the El Haouareb dam and;
289 infiltrating rainfall. These are the two most significant inputs to the aquifer, of which leakage
290 from the dam is dominant. The El Haouareb dam, due to high evaporation rates, over-use and
291 leakage down a fissure at the downstream end of the dam, has been (nearly) empty for parts
292 of the last decade. The volume of leakage is estimated at about 50% of any water stored
293 behind the dam (Leduc et al., 2007), and it is this volume that is used in the model as
294 recharge. The rainfall contribution is highly uncertain. Rain does not fall evenly, rather it falls
295 in discrete 'cells' covering only a fraction of the catchment. For this study, a value of 5%
296 coverage (i.e. the proportion of the catchment area over which rains fall) was assumed with
297 guidance from local partners in INAT during the model development process.

298 As outputs from the aquifer, the model incorporates domestic, industrial and agricultural
299 water uses, water transfers to the coastal cities and 'natural' outflow that accounts for the
300 sebkha regions. In addition, there is a waste-water reuse feedback loop. The proportion of this
301 reuse is estimated at 10% of the water use in each sector (Chahed et al., 2008). The
302 wastewater reuse acts as input to the aquifer with a time-delay of one time unit (i.e. one

303 month, as it cannot be used as input until the water has been extracted). The simulation time
304 step is monthly.

305 The complex agricultural sub-model has been retained (Figure 2b). Agricultural water
306 demand is influenced by, and influences a number of factors. Agricultural demand changes
307 per time step according to official predictions of annual water demand change. It also
308 changes in response to global food prices. The logic here is that an increase in global food
309 prices leads to an increase in agricultural water demand as farmers grow more crops in order
310 to exploit the higher prices. Farmers also raise their prices to offset increases in the water
311 tariff, thus affecting food prices. Additionally, demand is affected by the water tariff. The
312 tariff increases by a given percentage annually, and is influenced by the water consumption.
313 The equation for price elasticity of demand equation was used to estimate the change in water
314 demand. For example, by doubling the tariff increase per timestep, the demand is decreased
315 at each timestep according to the price elasticity of demand equation (Lipsey and Chrystal,
316 1999):

$$317 \quad \Delta D = D_{t-1} \times \{PeoD_t \times (\Delta P/P_{t-1})\}, \quad (1)$$

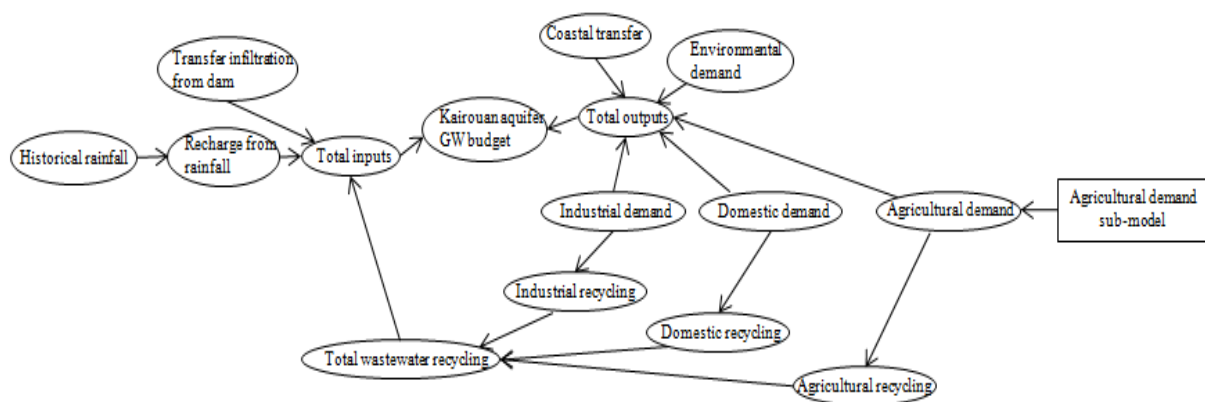
318 where D_{t-1} is the demand at time step t-1, P_{t-1} is the tariff at time step t-1, $PeoD_t$ is the price
319 elasticity of demand at time step t. ΔD and ΔP represent the change in water demand and
320 tariff from the previous timestep respectively. $PeoD$ was set to -0.3, representing an inelastic
321 market. The demand and the tariff contribute to the revenue generated from agricultural water
322 use. Of this, a proportion is invested for efficient irrigation techniques, which acts to reduced
323 demand (assuming that either cropping intensity or cropped area do not increase). Also, some
324 revenue is invested for water regulation and law enforcement. Greater levels of enforcement
325 and regulation may help to lower consumption. Finally there is the 'private' irrigation use
326 which is not regulated, and sometimes illegal. It is assumed that higher tariffs will lead to

327 increased private demand as farmers seek to reduce costs, although this trend can be
 328 influenced and mitigated by better regulation and particularly, better enforcement. Thus, this
 329 sub-model represents a complex system where the main factor of interest (the agricultural
 330 demand) is influenced by, and influences, many other factors in the sub-model, including
 331 governance issues. The value for demand at each timestep is fed into the main aquifer water-
 332 balance of Figure 2a.

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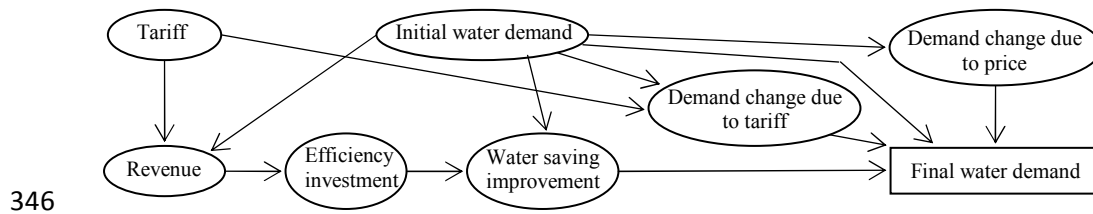
334 5. OOBN model implementation

335 The OOBN model (Figure 3) describes an aggregated model representing the Kairouan
 336 aquifer water budget, incorporating uncertainty through conditioned probability in every
 337 variable. The OOBN model is divided in three main parts and two classes. The inputs to the
 338 aquifer and the outputs from the aquifer are included in the first class, and a third part that
 339 represents agricultural demand (Figure 3b) is designed as the second class. The difference
 340 between inputs and outputs represents the aquifer water budget, represented by the variable
 341 “Kairouan aquifer GW Budget” (Figure 3). Furthermore, this allows the indirect estimation of
 342 the cumulative status of aquifer storage over time.



343

344 Figure 3a: The OOBN model. Note the agricultural sub-model is represented as a separate
345 class (square box, Figure 3b).



347 Figure 3b: Detail of the BN agricultural sub-model. Note the lack of feedback when
348 compared with the SDM version (Figure 2b).

349

350 The OOBN includes as inflows to the aquifer (Table 2): infiltration leakage from the El
351 Haouareb dam, recharge produced directly from rainfall and the volume of wastewater
352 recycling that is returned to the aquifer. Like the SDM implementation, leakage from the dam
353 and recharge from rainfall are the two most significant inputs to the aquifer, of which leakage
354 from the dam is probabilistically dominant in the BN model.

355 As outputs from the aquifer, the model incorporates (Table 2) domestic, industrial,
356 agricultural demands, water transfers to the coastal cities and natural outflow accounting for
357 environmental water requirements. The agricultural demand is abstracted to a separate sub-
358 model (class) (Figure 3b), and accounts for change to tariff, revenue, and savings from
359 investment and water saving measures.

360 Probability distributions for each variable were calculated according to the following general
361 criteria. First, the timeframe is monthly. Second, the probabilistic discretisations were created
362 considering same range intervals for all nodes. Finally, the data records for all variables
363 involved in the model are three years in length.

364 Specific criteria in regards to each variable are as follows. First, the controlling factor
365 rainfall, is not conditioned by any other variable, so the three year time series was discretised
366 in five intervals from 0 to 80 mm per month. The other parent node that is not conditioned is
367 the transfer infiltration from the dam which has been discretised in four equal range intervals
368 from 0 to 12 m³ per month. Furthermore, all the outputs that represent the abstraction from
369 the aquifer were also considered as parent nodes (except the agricultural demand, explained
370 below), which means that they are not influenced by other nodes. The industrial demand is
371 made up of five intervals from 0.012 to 0.018 m³ per month, domestic demand varies from
372 0.49 to 0.73 m³ per month, coastal transfer from 1.8 to 2.76 m³ per month and environmental
373 demand is considered as a constant value of 0.63 m³ per month.

374 The rest of the variables are conditioned by other variables, so their probability distributions
375 are defined by Conditioned Probability Tables (CPTs) under the Bayes Theory (Molina et al.,
376 2010). CPTs can be calculated in different ways: from real observation; by outputs from other
377 models; or by expert opinion. In this case, for the input nodes the CPT associated with the
378 “Recharge from rainfall” node has been estimated using data provided by local Tunisian
379 partners. CPTs for agricultural, industrial and domestic water reuse nodes have been
380 calculated by means of a constant coefficient of 10% of the corresponding demand. In this
381 case, CPTs were calculated using arithmetic expressions such as *agricultural_demand* 0.1*;
382 *industrial_demand*0.1* and *domestic_demand * 0.1*, respectively. The summation of the three
383 recycling nodes was made by a node named “Total Wastewater recycling” that has been
384 discretised in three intervals from 0.05 to 0.2 m³ per month. All the inputs to the aquifer are
385 summed in a node called “Total Inputs”. Finally, the goal of the whole OOBN model is
386 established through the node “Kairouan aquifer GW Budget”. The probability distribution is
387 made up of ten intervals from -6 to 14 x 10⁶ m³ per month.

388 Agricultural demand is considered in a separate sub-model which represents a second class,
389 coupled with the first class through an instance node called “Final Agricultural Water
390 Demand”. This class comprises two parent nodes. First, the node “Initial Agricultural Water
391 Demand” represents the original water demand for agriculture at the beginning of the model
392 time frame; “Water Tariff” expressed in units of the local currency (Tunisian Dinars, TD) per
393 cubic meter represents the water price for agricultural activities. Both nodes condition the
394 "Agricultural Water Revenue" (TD), which drives the node "Efficiency Irrigation
395 Investment". The node “Improvement Water Efficiency Savings” is a child and consequently
396 depends on the nodes "Investment for Efficiency Investment" and the "Initial Water
397 Demand". The node “Water Demand Change due to Water Price” is dependent on “Water
398 Tariff” and “Initial Agricultural Water Demand”.

399

400 **6. Results**

401 For both model formulations, datasets representing the latest three years of data available
402 (2004-2007), which were provided by local partners INAT, were simulated first to define a
403 baseline scenario against which a suite of hypothetical scenarios were then compared. This
404 section presents the results from the OOBN model simulations, followed by the results from
405 the SD modelling. During the various scenarios, only the values being tested were changed.
406 All other values were defined by baseline data.

407

408 **6.1 OOBN model**

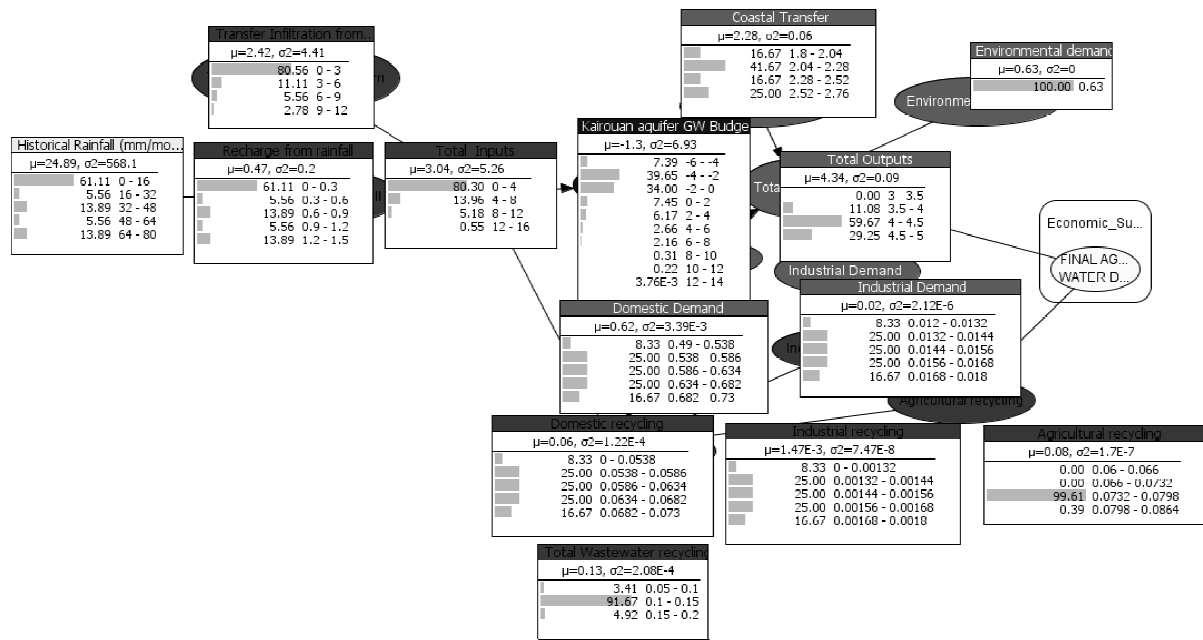
409 *6.1.1 Baseline*

410 The average value for the leakage from El Haouareb dam to the aquifer is $2.42 \times 10^6 \text{ m}^3$ per
411 month. The leakage is shown to increase over the time during the simulation, suggesting that
412 this component is becoming more important for water management in the area. Average
413 rainfall is 24.89 mm/month and it contributes c. $0.47 \times 10^6 \text{ m}^3$ per month to aquifer recharge
414 (Figure 4a), but with large uncertainty. The average value of wastewater return to the aquifer
415 is estimated at $0.13 \times 10^6 \text{ m}^3$ per month. With regard to abstractions, the most important
416 demand is the coastal transfer with an average value of $2.28 \times 10^6 \text{ m}^3$ per month, although
417 there is considerable variation.

418 Regarding agricultural water use, the demand is c. $0.78 \times 10^6 \text{ m}^3$ per month (Figure 4b).
419 Agricultural water revenue is c. 47212 TD per month and water savings due to improvement
420 in water efficiency are c. 4298 m^3 per month.

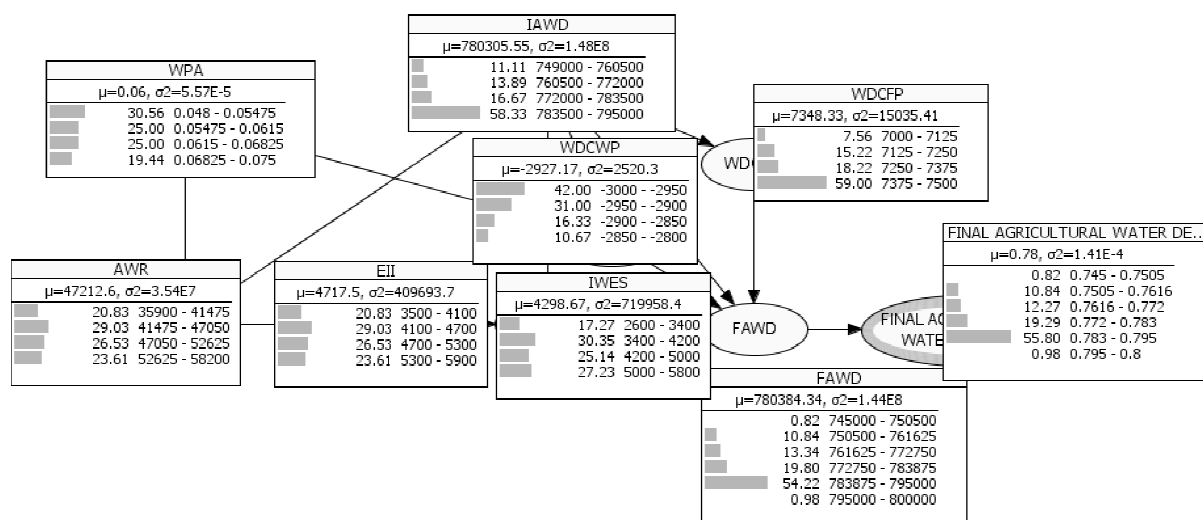
421 The baseline analysis of the Kairouan aquifer budget shows a negative value of -1.33×10^6
422 m^3 per month ($-15.96 \times 10^6 \text{ m}^3 \text{ yr}^{-1}$), implying decreasing aquifer storage and the consequent
423 depletion of reserves. This value is close to that produced by the SDM baseline simulation
424 (Section 6.2.1), and agrees well with other observations (Leduc et al., 2007).

425



426

427 Figure 4a: Baseline results for the OOBN model.



428

429 Figure 4b: Baseline results for the agricultural sub-model in the OOBN.

430

431 6.1.2 Hypothetical model scenarios

432 The scenarios here represent hypothetical water management options, and are not reflective

433 of actual policies being implemented in Tunisia. The scenarios were designed to minimise or

434 maximise the main variables of the system which were deemed to be, for the inputs: the
435 transfer infiltration from El Haouareb, for the outputs: the coastal transfer and finally, as the
436 objective: the Kairouan aquifer water budget. These scenarios are defined as follows:

437 1. Maximization of the leakage infiltration from the dam

438 The monthly leakage volume from the upstream El Haouareb dam was maximised (i.e., make
439 it as large as possible within CPT constraints).

440 2. Minimisation of the leakage infiltration from the dam

441 The monthly leakage volume from the upstream El Haouareb dam was minimised (i.e., make
442 it as small as possible within water balance constraints set by the CPTs).

443 3. Maximisation of the coastal transfer

444 The objective was to maximise the monthly transfer of water to the coastal cities (i.e., make it
445 as large as possible within water balance constraints set by the CPTs).

446 4. Minimisation of the coastal transfer

447 The objective was to minimise the monthly transfer of water the coastal cities (i.e., make it as
448 small as possible within water balance constraints set by the CPTs).

449 5. Maximisation of the Kairouan aquifer water budget

450 With this scenario, the objective was set such that the monthly volume of water held in the
451 aquifer was as large as possible. This meant that the OOBN adjusted influencing inputs to
452 make them as large as possible while outputs were adjusted to make them as small as
453 possible, all within the constraints of the CPTs.

454 6. Minimisation of the Kairouan aquifer water budget

455 With this scenario, the objective was set such that the monthly volume of water held in the
456 aquifer was as small as possible (an undesirable situation). The OOBN model adjusted inputs
457 to make them as small as possible. Outputs were adjusted to make them as large as possible.
458 The maximisation and minimisation of variables is achieved by assigning 100% chance to the
459 highest and lowest interval of the variable, respectively. For example, in order to maximise
460 the variable “leakage infiltration from the dam”, a 100% chance for the highest interval (9-12
461 $\text{m}^3 \text{ month}^{-1}$) was assigned.

462 The impacts of minimising or maximising the main variables on the volume of water held in
463 the Kairouan aquifer produced by every scenario are shown as probabilistic distributions in
464 Figure 5 and are explained as follows:

465 1. Maximization of the leakage infiltration from the dam (Figure 5a)

466 The main impact of this scenario is an increase to the Kairouan aquifer water budget by $8 \times$
467 10^6 m^3 per month when compared to the historical average. This leads to recharge of $6.45 \times$
468 10^6 m^3 per month ($77.16 \times 10^6 \text{ m}^3 \text{ yr}^{-1}$).

469 2. Minimization of the leakage infiltration from the dam (Figure 5b)

470 The main impact of this scenario is a reduction in the Kairouan aquifer water budget by 2.24
471 $\times 10^6 \text{ m}^3$ per month, leading to an annual deficit of $-26.88 \times 10^6 \text{ m}^3$.

472 3. Maximization of the coastal transfer (Figure 5c)

473 The main result from this scenario suggests a Kairouan aquifer budget decrease (i.e. greater
474 net deficit) to a value of $-1.7 \times 10^6 \text{ m}^3$ per month ($-20.4 \times 10^6 \text{ m}^3 \text{ yr}^{-1}$).

475 4. Minimization of the coastal transfer (Figure 5d)

476 The main impact resulting from this scenario was a lower net annual aquifer deficit of $-0.89 \times 10^6 \text{ m}^3$ per month ($-10.68 \times 10^6 \text{ m}^3 \text{ yr}^{-1}$).

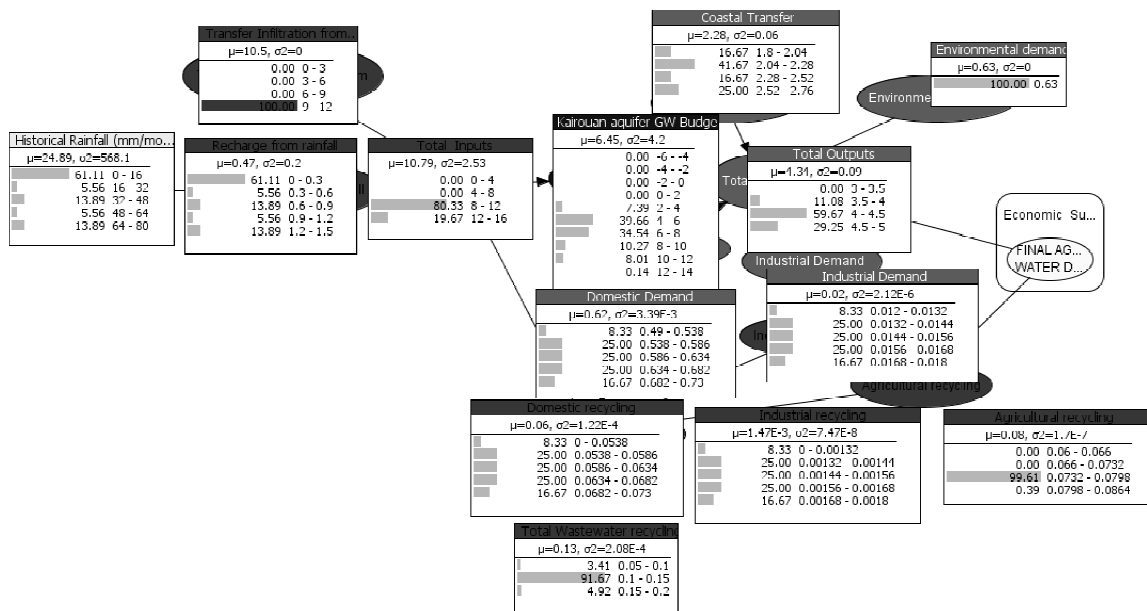
478 5. Maximization of the Kairouan aquifer water budget (Figure 5e)

479 There are two main impacts from this scenario: first, an increase in the infiltration from El
 480 Haouareb to an average rate of $10.5 \times 10^6 \text{ m}^3$ per month; and second, a reduction to the
 481 coastal transfer to a rate of $1.93 \times 10^6 \text{ m}^3$ per month. This scenarios does not produce a
 482 significant impact on the socioeconomic agricultural sub-model.

483 6. Minimization of the Kairouan aquifer water budget (Figure 5f)

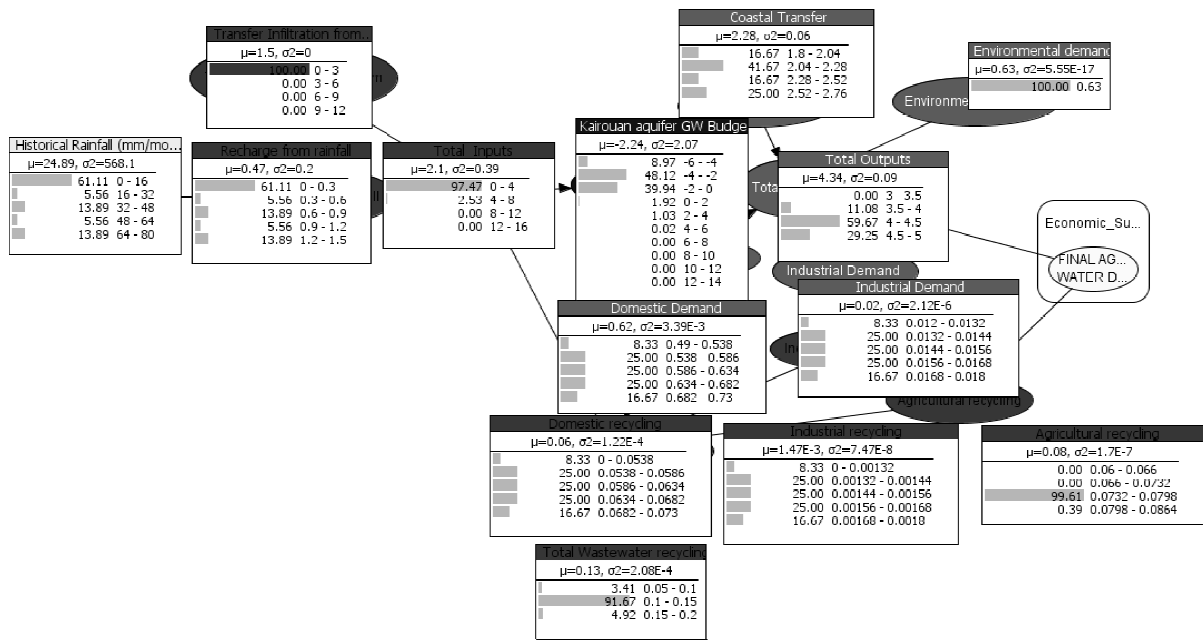
484 Again, there are two main impacts produced by this scenario: a reduction of the infiltration
 485 from El Haouareb to an average rate of $1.57 \times 10^6 \text{ m}^3$ per month and; a small increase to the
 486 coastal transfer to a rate of $2.43 \times 10^6 \text{ m}^3$ per month.

487



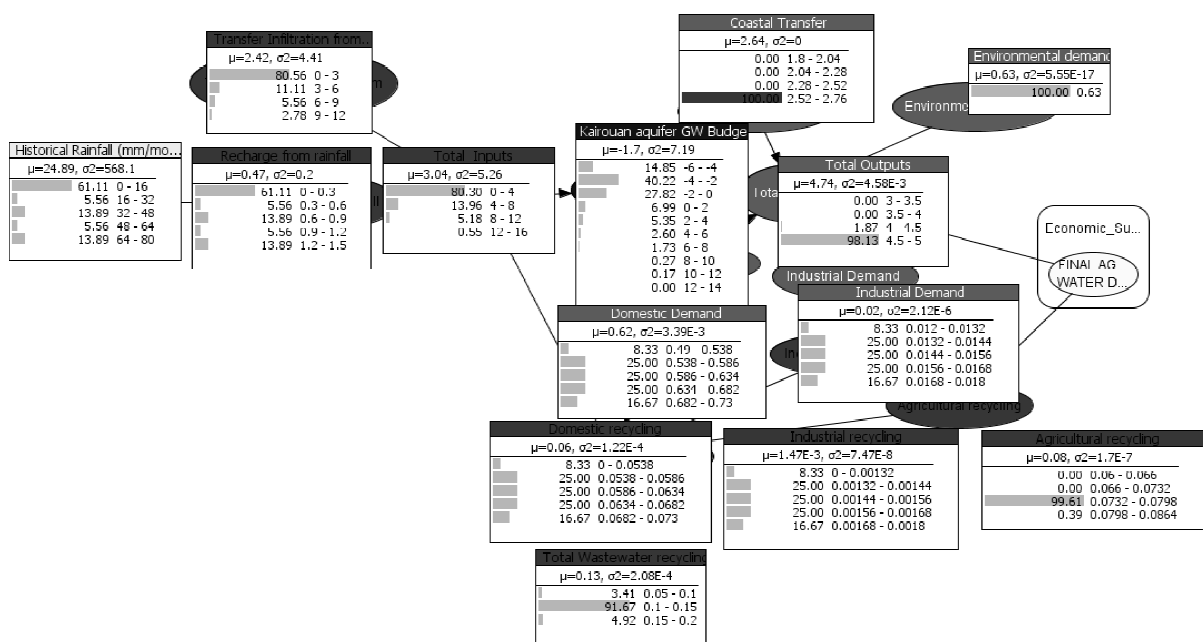
488

489 Figure 5a: OOBN results for hypothetical test 1 - maximisation of leakage infiltration.



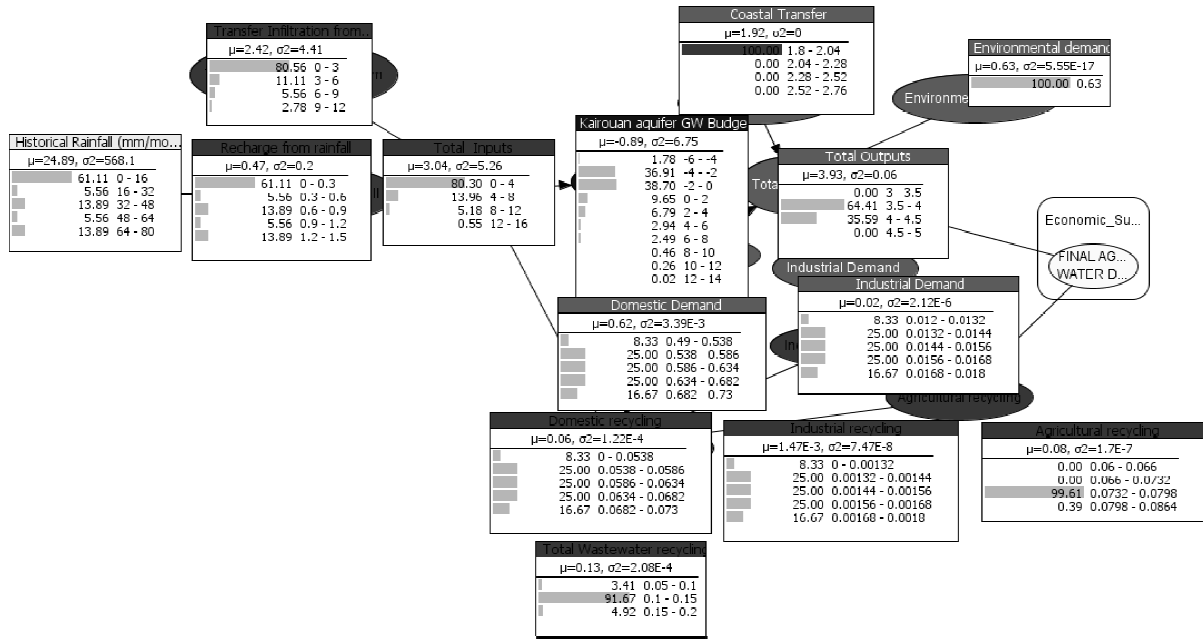
490

491 Figure 5b: OOBN results for hypothetical test 2 - minimisation of leakage infiltration.



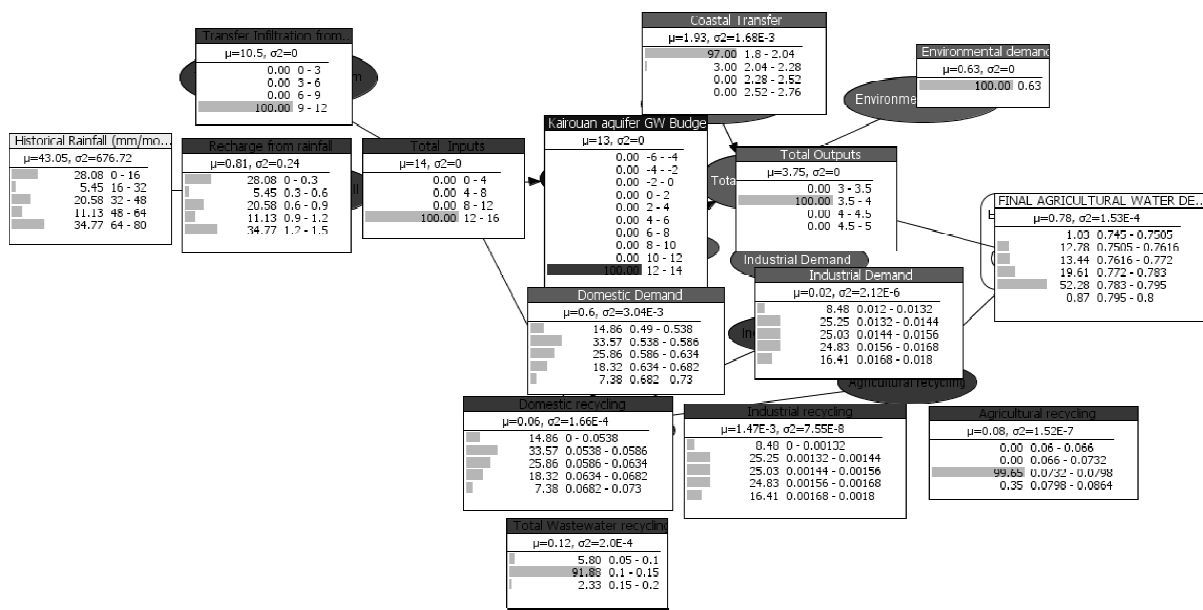
492

493 Figure 5c: OOBN results for hypothetical test 3 - maximisation of coastal transfer.



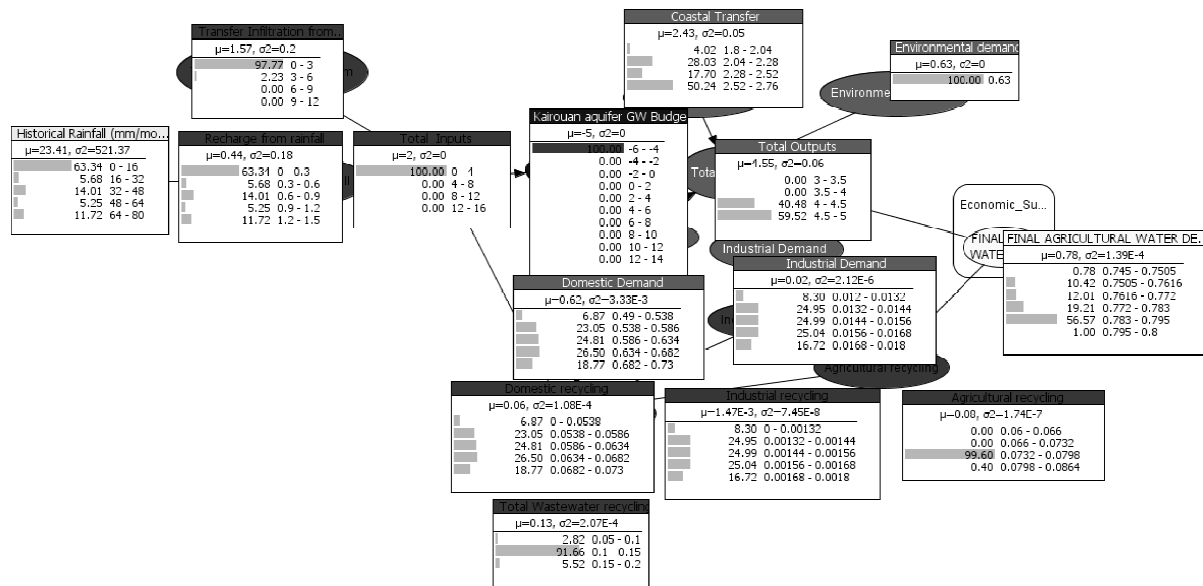
494

495 Figure 5d: OOBN results for hypothetical test 4 - minimisation of leakage infiltration.



496

497 Figure 5e: OOBN results for hypothetical test 5 - maximisation of the Kairouan aquifer water
498 budget.



499

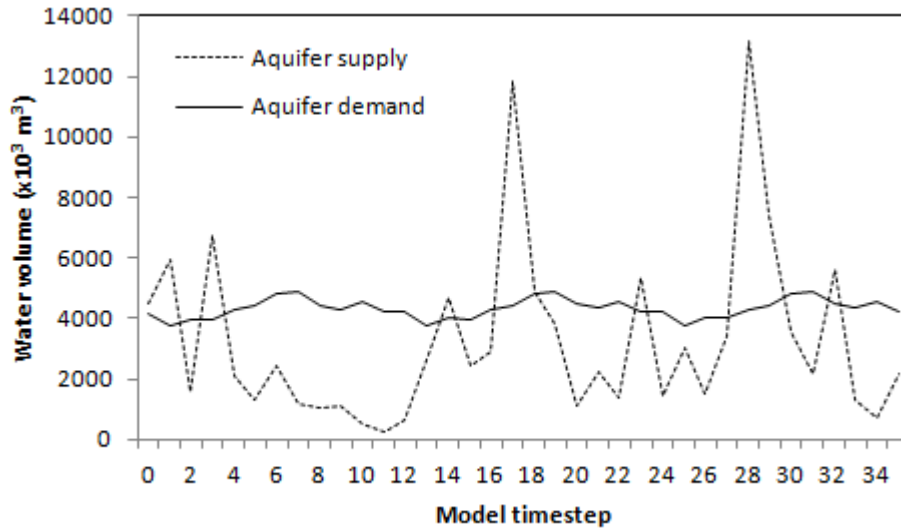
500 Figure 5f: OOBN results for hypothetical test 6 - minimisation of the Kairouan aquifer water
501 budget.

502

503 6.2 System Dynamics Model

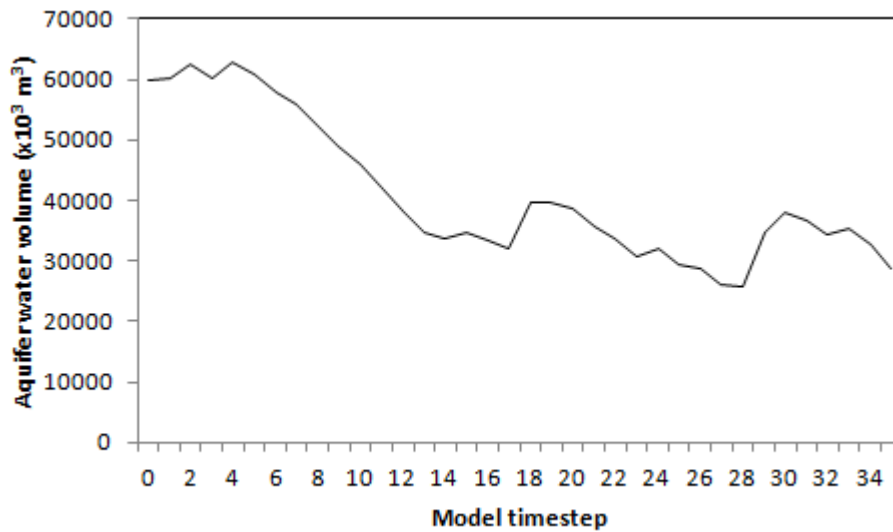
504 6.2.1 Baseline

505 Figure 6 show the time-series' for the model inputs, outputs and aquifer water volume. For
506 the most part, the aquifer is being over-exploited, with demand exceeding supply. The
507 average annual water deficit is estimated at c. $10.3 \times 10^6 \text{ m}^3$, which corresponds reasonably to
508 other published results (Luc, 2005). The pattern of the model result is similar to observations
509 of local water-table levels from piezometric readings (Le Goulven et al., 2009). Thus, the
510 SDM is representing the current system behaviour well.



511

512 Figure 6a: Time-series of aquifer inputs and outputs for the baseline SDM scenario.



513

514 Figure 6b: Time-series showing the evolution of aquifer water volume for the baseline SDM
515 scenario.

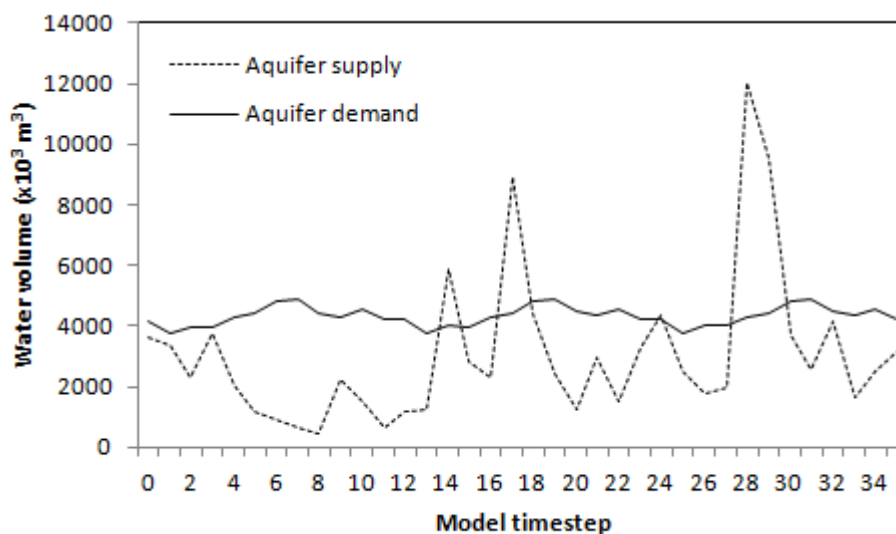
516

517 6.2.2 Hypothetical model scenarios

518 Using SDM, a suite of tests were performed that aimed to shed light on the impacts of
519 changing various parameters. Of particular importance here are the impacts from agricultural
520 demand, so that the complex sub system, with interlinked, feedback-driven structure, could
521 be explored. The simpler input/output parameters are dealt with first, followed by analysis of
522 the agricultural demand sub-model.

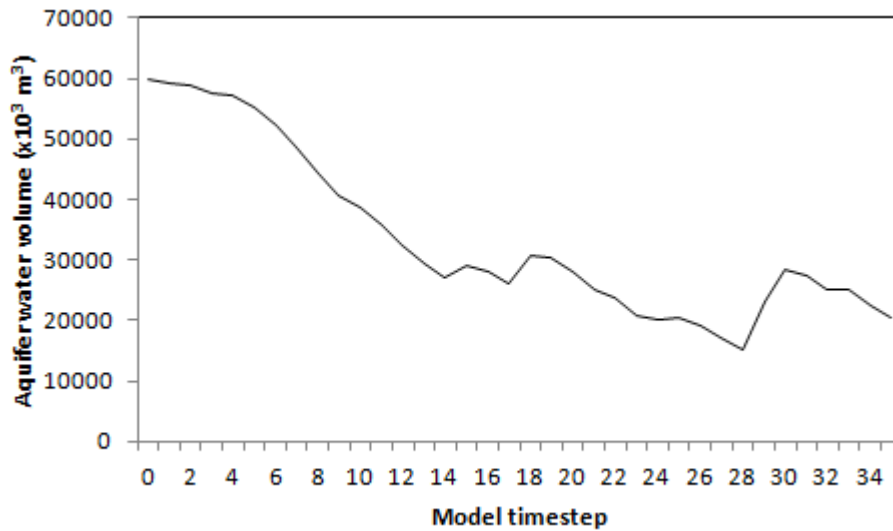
523 6.2.2.1 Input rainfall

524 For this model run, predictions of rainfall in 2050 from a regional climate model were used (a
525 regional climate model was forced by ECHAM5 with the IPCC A1B emissions scenario.
526 Data were provided at monthly timestep with a resolution of 25x25 km by CMCC, a
527 WASSERMed partner). Rainfall totals are 19% lower with respect to the baseline. Under this
528 scenario, the deficit increases to c. $13 \times 10^6 \text{ m}^3 \text{ yr}^{-1}$ (Figure 7).



529

530 Figure 7a: Showing the supply to and demand from the Kairouan aquifer under predicted
531 future rainfall.



532

533 Figure 7b: Simulated evolution of the aquifer water volume under future rainfall conditions.

534

535 6.2.2.2 Domestic and industrial demand

536 For this series of tests, the baseline industrial demand was doubled and halved, while the
537 domestic demand was changed by factors of 0.5, 0.8, 1.2 and 2. When industrial demand was
538 halved, the average annual aquifer deficit was c. $10.1 \times 10^3 \text{ m}^3 \text{ yr}^{-1}$. When it was doubled, the
539 deficit was c. $10.4 \times 10^3 \text{ m}^3 \text{ yr}^{-1}$. For the domestic demand tests, the aquifer water deficit
540 ranged from $7 \times 10^3 \text{ m}^3 \text{ yr}^{-1}$ to $16.7 \times 10^3 \text{ m}^3 \text{ yr}^{-1}$ as demand was scaled from 0.5 to 2 times
541 baseline respectively. Due to the relatively small domestic and industrial water demand,
542 doubling or halving the present values for domestic and industrial use had relatively little
543 impact on the deficit, and a pattern of over-abstraction is simulated in all cases.

544 6.2.2.3 Pumping to coastal cities

545 Volumetrically, pumping water to coastal cities is the largest exploitation of the Kairouan
546 aquifer. The baseline pumping was scaled from 0.6 to 1.4 of the baseline value at increments

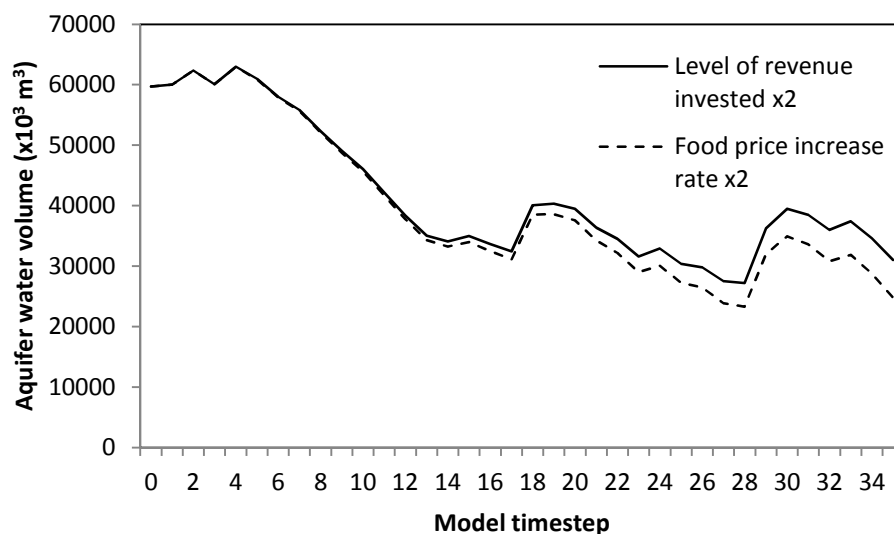
547 of 0.2. As a result of these changes, the water balance ranged from $0.4 \times 10^6 \text{ m}^3 \text{ yr}^{-1}$ to $-20.9 \times$
548 $10^3 \text{ m}^3 \text{ yr}^{-1}$. By reducing pumping by 40%, net recharge can be achieved. However, if
549 pumping increases, the viability of the aquifer, and of the surrounding ecosystems and
550 agricultural economy are placed at serious risk.

551 *6.2.2.4 The agricultural sub-model*

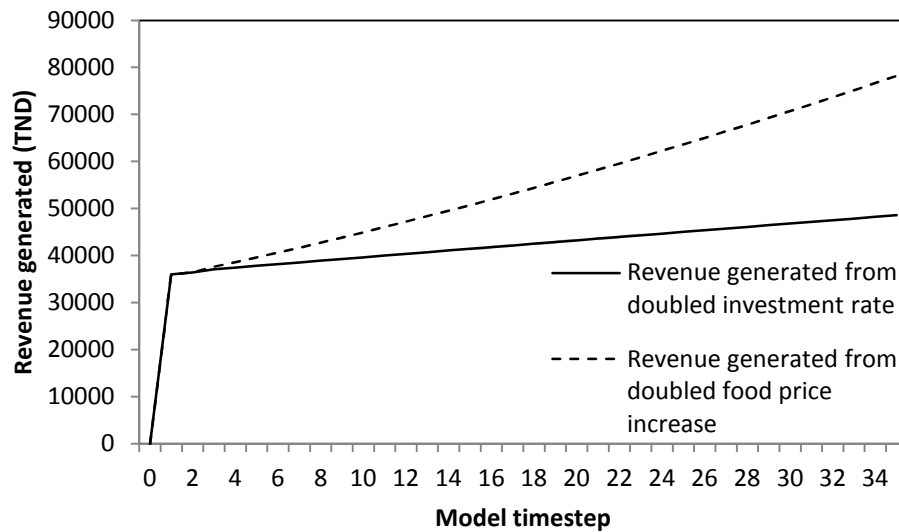
552 This sub-model (Figure 2b) allows the full potential of SDM to be explored. By changing any
553 parameter, the value for agricultural demand will change according to the feedback
554 relationships in the model. Unlike the other demands, this is not a pre-defined time-series.
555 Water use is calculated for each timestep based on the sub-model relationships and the initial
556 values for parameters such as the monthly tariff increase. In addition to water demand,
557 revenue generated from water sales can also be output from this sub-model. In this sub-
558 model, the parameters that were changed during these tests are:

- 559 1. the value for the annual agricultural water demand change (baseline = -0.014881%
560 per month - equivalent to 5% reduction over 28 years (Chahed et al., 2008)). This was
561 changed by factors of 0.5 and 2, i.e. halved and doubled respectively.
- 562 2. the value for the proportion of revenue invested in efficient irrigation (baseline =
563 10%). This was changed by factors of 0.5 and 2.
- 564 3. the annual tariff increase (baseline = 1.25% per month or 15% per year (Chenini et al.,
565 2003)). This was changed by factors of 0.5 and 2.
- 566 4. the amount of water saving possible by implementing water saving measures
567 (baseline = 20%. Estimated value). This was changed by factors of 0.5 and 2.
- 568 5. the change to global food prices (baseline = 0.9416% per month based on 11.3%
569 average annual change from 2000-2012. fao.org). This was changed by factors of 0.5
570 and 2.

571 All ten tests had negligible impact on the overall Kairouan water balance (Figure 8a). The
572 range of average annual Kairouan deficit under all scenarios is from $9.5 \times 10^6 \text{ m}^3 \text{ yr}^{-1}$
573 (doubling the amount of revenue invested for efficient irrigation) to $11.6 \times 10^6 \text{ m}^3 \text{ yr}^{-1}$
574 (doubling the global food price increase rate). None of the changes led to a significant
575 improvement in the current situation. Figure 8b, which shows how the revenue generated
576 changed in these tests, suggests that a trade-off must be made between increasing the revenue
577 generated and at the same time to decrease the amount of water use to protect the aquifer
578 water quantity and quality, ecosystem services and agricultural viability in the region (e.g.
579 while doubling the food price increase rate offers a better revenue, it also leads to greater
580 overexploitation of the Kairouan aquifer, Figure 8).



581
582 Figure 8a: Aquifer water trends produced from doubling the level of investment and doubling
583 the global food price increase rate. The results from all other tests in Section 6.2.2.4 fall
584 between these trends.



585

586 Figure 8b: Simulated revenue generated for the tests that doubled the level of investment and
587 the global food price increase rate. The trends show different responses, with a doubling of
588 the food price increase rate leading to a much greater level of revenue generated by the end of
589 the simulation. The results from all other tests in Section 6.2.2.4 fall between these trends.

590

591 7. Discussion

592 Both modelling approaches indicate that at present, Kairouan aquifer is undergoing depletion.
593 OOBN modelling showed greater depletion than SDM, with both approaches showing deficit
594 lower than estimations from rudimentary mass balance calculations (Luc, 2005), but are
595 consistent with the pattern of decline observed by Le Goulven et al. (2009). Hypothetical
596 water management scenarios allowed a more thorough comparison of the two methods.

597 Both approaches use a sensitivity-type approach to the scenarios - changing one value and
598 observing the effects. However, how these approaches were carried out, and the merits and
599 limitations of each are different. In the OOBN framework, the hypothetical scenarios
600 consisted of minimising or maximising key model parameters. In addition, an objective

601 function was set such that the goal was to minimise or maximise the water volume stored in
602 the aquifer (within the constraints of the CPTs). The influencing parameters were altered by
603 the model in order to achieve this objective. The main observed impacts were to the amount
604 of infiltration recharge on the supply side and the volume of pumping to the coast on the
605 demand side. The interpretation is that if the aquifer were to undergo recharge, it is one of
606 these two parameters that would be most likely to be affecting this change, either together or
607 independently. In terms of policy interventions (governance), very little can realistically be
608 done to impact significantly on natural water supply, however the volume of water pumping
609 could be influenced. Setting objective functions to observe how influencing parameters
610 respond is not available within the SDM environment, and represents an important difference
611 between the two methods. OOBN modelling, through the use of CPTs, generates probabilistic
612 results, which may give the end user a better handle on the uncertainties associated with a
613 result set. However, these probabilities, while useful, are constrained by the data on which
614 they are based. It still represents an advantage over SDM, where the results are usually,
615 though not always, deterministic (although stochastic SDMs have been developed, Mosekilde
616 and Rasmussen, 1983). OOBN indicated that changes to the volumes pumped to the coast
617 hold the greatest promise for aquifer rehabilitation.

618 In the SDM framework, for the 'simple' parameters (e.g. rainfall and industrial and domestic
619 demand), these were scaled by various factors (Section 6.2.2) relative to the baseline and
620 resulted in linear model response. SDM allowed for the testing of the more complex
621 feedback-driven agricultural water demand sub-model. The agricultural demand sub-model
622 aimed to represent to full utility of SDM and provide a strong contrast with OOBN
623 modelling. For the more complex agricultural sub-model, while key parameters were still
624 scaled in a sensitivity-type approach, the role of the feedback structure, including non-linear
625 relationships linking some of the variables, meant that the response in agricultural water

626 demand to these changes was not linearly related to the scaling factor, nor was the ultimate
627 aquifer response. Positive (i.e. reinforcing) and negative (i.e. self-stabilising) loops are
628 incorporated. Many parameters depend on values from previous time steps. The feedback
629 representation in SDM is not available in OOBN due to the inherent acyclic nature of this
630 approach. It was expected that changing parameter values in this sub-model would lead to
631 substantial changes in demand. However, this was not the case (Section 6.2.2.4). All model
632 results except for one (doubling the global food price increase) were within 10% of each
633 other.

634 Based on the interconnected feedback loops simulating agricultural water demand (Figure 2b)
635 the behaviour of this factor is more complex: Any change in demand, ΔD , is subtracted from
636 the previous agricultural water demand value, while a decrease in demand decreases the
637 revenue generated. This, consequently, leads to decreases in the amount of revenue invested
638 for efficient irrigation practices and for regulation and enforcement of water laws. Because
639 both of these values will be lower than in the previous time step, the subsequent effect from
640 the water savings parameter produces no changes on water demand at the next time step. By
641 contrast, the effect from the regulation parameter (governance/policy) is to decrease water
642 demand, as farmers move towards private (unregulated) irrigation from the public
643 (monitored) system. The lower level of enforcement is assumed to encourage farmers to
644 illegally take water as they are more under pressure from the higher tariff and less under
645 pressure from strict regulation enforcement. Additionally a slight, constant, decrease in
646 agricultural demand at each time step is imposed.

647 Finally, there is an increase in demand due to the influence of rising global food prices. The
648 impact of these interactions is a net decrease in total agricultural water demand, but the level
649 of decrease is lower than expected from changing the tariff alone. This, in turn, suggests that

650 raising tariffs in order to lower demand, or changing the proportion of revenue invested to
651 promote efficient irrigation, may not be as effective as hoped. These interactions are in no
652 way exhaustive regarding the socio-economic and governance factors influencing agricultural
653 water demand; there may be other interactions at work that are neglected in this (rather
654 simplified) sub-model. They are, however, sufficient for giving a clear trend of the
655 complexity and the issues at hand for the region and the potential of SDM to explore them.

656 Agriculture is by far the largest employer and the largest economy in the region. It is unlikely
657 that a policy would be put in place that would threaten this socio-economic driver. Policies
658 for promoting the growth of less water-intensive crops or improving irrigation efficiency are
659 likely to be preferred. It is unclear how these socio-economic factors will impact on
660 agricultural water demand, and how effective they will be, especially under future climate
661 change scenarios, but the model indicates that they will be critical in determining future
662 agricultural water use, as well as being a useful (decision maker's) tool for the qualitative
663 and quantitative assessment of the impacts of different policies.

664 Both approaches suggest that transferring water from the aquifer to coastal cities has a large
665 impact on Kairouan aquifer water volumes. OOBN modelling suggested that significant
666 improvement or worsening of the water deficit can occur depending on whether the pumped
667 volume is minimised or maximised (within the constraints of the CPTs) respectively.

668 However, while the OOBN approach is constrained by the limits of the CPTs, the SDM
669 approach is not. Here, coastal pumping was scaled between 0.6 and 1.4 times the baseline
670 values, but could have been scaled to any value. As with the OOBN results, significant
671 impacts in aquifer response were observed. Both approaches suggest that reductions in the
672 volume pumped out to coastal cities offers the best realistic option for reducing the over-
673 exploitation in the future and also for preserving the sensitive nearby sebkha regions and

674 local water quality. By maintaining Kairouan aquifer water volumes, the agricultural
675 economy of the region could also be sustained. Despite this, due to the current situation it is
676 suggested that efforts should also be made to reduce domestic consumption (e.g. through
677 subsidies for water-saving measures or a tariff increase), and to restrain industrial
678 consumptive growth (e.g. through tariff or abstraction controls).

679 This study has highlighted the advantages and limitations of both modelling approaches.
680 While OOBN modelling is ideally suited to generating results that can incorporate and
681 account for uncertainty in input data, giving probability distributions as output, and can set
682 objective functions to observe the corresponding impacts on influencing variables, it is an
683 acyclic modelling paradigm preventing its use in assessing complex feedback-driven systems.
684 It is in the simulation of non-linear feedback processes that SDM excels, helping to deepen
685 understanding of how a system operates and of how feedbacks may result in consequences
686 differing to those intended. Additionally, OOBN is unable to handle time series data, unlike
687 SDM.

688 This study suggests that in some cases, using both methods to complement each other in the
689 evaluation of water resources can add depth and insight to the results produced. By using
690 these approaches together, instead of considering them in isolation, a more robust systems
691 analysis may be undertaken that can lead to better informed policy decisions, the conclusion
692 being that exploiting the merits of both methods is better than choosing between them; they
693 are complementary rather than rival methodologies. In the context of this study, this means
694 using both approaches to better understand the impacts of potentially implemented policy
695 options aimed at securing the regional water resource and the associated uncertainty. Those
696 options that are likely to have the most favourable impact on water quantity and quality,

697 ecosystem conservation and the development of the agricultural economy can be fully
698 assessed, leading to better informed decision making.

699

700 **8. Conclusions**

701 This paper describes the use of two different modelling approaches, System Dynamics
702 Modelling and Object-Oriented Bayesian Network Modelling for simulation of the same
703 groundwater system. The volume of water in the Kairouan aquifer, Tunisia was the main
704 parameter being studied. Both models were in good agreement when the baseline dataset was
705 used, indicating current overexploitation of the aquifer. A number of hypothetical
706 management scenarios were tested. The results from the two approaches agreed that only
707 changing the volume of water pumped to coastal cities has a significant impact on aquifer
708 water volumes, and reductions offer the best solution for aquifer rehabilitation and an end to
709 overexploitation.

710 The main aim was to compare and contrast the modelling paradigms. The model
711 implementations and discussion showed that each approach has its own advantages and
712 disadvantages. It is shown that OOBN modelling is well suited to modelling systems where
713 the parameters are uncertain, and where the uncertainty can be quantified as a probability
714 distribution. It also allows for probabilistic model outputs, giving policy makers a better
715 handle on uncertainties associated with predictions, though the probabilities generated are
716 constrained by the data used in the model. OOBNs are particularly useful for examining what
717 impact fixing an objective function to a given value has on influencing inputs and outputs.
718 This means for example that should a minimum aquifer volume be set, those parameters most
719 important to affecting this limit could be identified, lending focus to potential policy
720 decisions.

721 System Dynamics is used to investigate the behaviour of complex systems which are
722 governed by feedback and non-linearity, something which may not be done using OOBNs
723 due to their acyclic nature. Unintended, and sometimes counter-intuitive system behaviour
724 might be uncovered that was not predictable beforehand. A feedback-driven agricultural sub-
725 model was built in order to highlight to utility of SDM and to show the contrast with OOBN.
726 It was shown for example, that doubling one parameter did not result in as much lowering of
727 the water demand as might have been intended as a result of the competing actions of the
728 various feedback loops.

729 It is suggested that in some cases, rather than using these approaches in isolation, coupling
730 the methods and using one to complement the other may add significant value to the
731 outcomes of a study as opposed to if only one approach was adopted. For example, OOBNs
732 modelling can provide a better understanding of uncertainty in inputs and outputs, while
733 SDM can shed light on the complex, non-linear response of a system to alterations in various
734 initial states. The modeller should think carefully about which approach to adopt, and should
735 not rule out using both to complement each other.

736 Finally, the combined use of SDM and OOBN may provide an improved insight leading to
737 better informed decision makers. For instance, in this study it was shown that significant
738 changes to the annual tariff increase did not lower the agricultural water demand as much as
739 expected because of the other feedback processes acting within this sub-model, while OOBN
740 modelling indicated that if minimum aquifer volumes were required by policy, then the
741 biggest impact would most likely be forced upon the water pumped to the coast, which would
742 have to decrease in volume to meet the requirement. By combining the two approaches, better
743 informed decisions based on deeper systems understanding can be made, and decisions which

744 may unintentionally prove detrimental long term water resources management can be
745 avoided.

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765 **7. References**

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