1 2	Bone Remodeling Following Mandibular Reconstruction using Fibula Free Flap
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Abstract

25 To investigate bone remodelling responses to mandibulectomy, a joint external and internal 26 remodelling algorithm is developed here by incorporating patient-specific longitudinal data. 27 The primary aim of this study is to simulate bone remodelling activity in the conjunction region 28 with a fibula free flap (FFF) reconstruction by correlating with a 28-month clinical follow-up. 29 The secondary goal of this study is to compare the long-term outcomes of different designs of 30 fixation plate with specific screw positioning. The results indicated that the overall bone density 31 decreased over time, except for the Docking Site (namely DS1, a region of interest in 32 mandibular symphysis with the conjunction of the bone union), in which the decrease of bone 33 density ceased later and was followed by bone apposition. A negligible influence on bone 34 remodeling outcome was found for different screw positioning. This study is believed to be the first of its kind for computationally simulating the bone turn-over process after FFF 35 36 maxillofacial reconstruction by correlating with patient-specific follow-up.

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38 Keywords: Bone remodelling, Maxillofacial reconstruction, Placement design of fixation plate,
39 Time-dependent remodelling algorithm. Clinical follow-up

1. Introduction

A large number of mandibular bone defects coupled with the loss of muscular and soft 41 42 tissue attachments due to trauma, atrophy, or following ablation for tumors, potentially generate 43 several significant problems, such as facial disfigurement, malocclusion and impaired oral 44 function. Free vascularized tissue grafting has become a well-established clinical procedure and 45 is now widely used for managing post-ablative defects to overcome such problems (Gbara et 46 al., 2007; Hakim et al., 2015). Of various surgical options with free vascularized tissues 47 available, fibula free flap (FFF) grafting has demonstrated fairly high reliability and adaptability 48 for the reconstruction of substantial mandibular defects, due to its adequate length for even 49 subtotal mandibular reconstruction and long vascular pedicle (Hidalgo, 1989; Hidalgo and 50 Pusic, 2002; Hidalgo and Rekow, 1995). Despite these proven benefits, loss of several 51 masticatory muscles due to resection can still cause unbalanced jaw movement and abnormal 52 mastication, resulting in significant biomechanical changes over time (Narra et al., 2014; Wong et al., 2010). Thus, the mechanobiological responses for a reconstructed jaw may be largely 53 54 altered, and would in-turn affect subsequent bone healing and remodeling activities (Frost, 55 1993; Zheng et al., 2019a). In our previous clinical study (Yoda et al., 2018), the morphological 56 changes in the conjunction region of the host mandible and FFF were investigated. However, 57 evaluation of longitudinal density change due to bone remodeling at each conjunction region 58 of bone union, especially apposition and resorption process within the reconstructed structure, 59 remains an open research question.

60 CT-based three-dimensional (3D) finite element (FE) models have exhibited compelling 61 advantages in biomechanical analysis by precisely capturing anatomical features of an 62 individual subject in a time-dependent fashion. This technique has been widely applied in 63 orthopedic and prosthodontic research to assess, predict and manage bone adaptation processes 64 as a result of various clinical interventions (Chen et al., 2015; Lin et al., 2010a). In maxillofacial 65 reconstruction, for example, several studies have assessed the biomechanical roles of a fixation 66 plate on the bridging/supporting reconstruction process (Knoll et al., 2006; Narra et al., 2014; 67 Schuller-Götzburg et al., 2009), where stability of the whole system could have significant 68 contribution on long term survival rate and clinical success. In this regard, Knoll et al. (2006) 69 and Narra et al. (2014) explored different plate shapes, while Schuller et al. (2009) investigated 70 the effects of different plate materials. Unfortunately, there has been no specific study on either 71 the associated mandibular bone remodeling biomechanics or the role of the number and position 72 of screws. With a proper bone remodelling algorithm, the effects of fixation plate can be 73 assessed in a predictive way, thereby providing a means to optimizing placement of the fixation 74 plate for long-term promotion of bone reunion and apposition.

A better understanding of mechanobiological responses and associated bone remodelling at the bone union regions can provide fundamental data for enhancing orofacial reconstruction outcomes. Therefore, this study aims to (1) investigate the time-dependent bone remodelling activity around the conjunction regions by correlating with patient-specific clinical follow-ups; and (2) assess the long-term effects of fixation plate and screwing placement on clinical outcomes. The methodological procedure developed and the results obtained are anticipated to provide some important insights into surgical planning for mandibular reconstruction.

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2. Materials and Methods

85 2.1 Clinical acquisition

In this study, a 66-year-old male patient who underwent mandibular reconstruction for the tumor removal with osteotomized FFF was selected. A universal titanium fixation plate (Synthes, Solothurn, Switzerland), which was pre-bent based upon a CT-based 3D patient model prior to surgery and fixed monocortical with 11 titanium screws (Synthes, Solothurn, Switzerland). Multi-detector helical follow-up CT scans were performed at 4, 16, and 28 months after surgery (namely, M4, M16, and M28, respectively).

In this study, 18 volumes of interest (VOIs) of 2 mm³ each were considered for two 92 93 purposes: (1) as the reference to correlate the simulated remodeling results with clinical follow-94 up data; (2) as the region of interest to analyze long-term bone remodeling outcomes. To define 95 the VOI, six planes parallel to the mandibular plane were selected at three docking sites (DS1, 96 DS2, and DS3, Fig. 1a) with 2 mm intervals by multiple planar reconstructions (MPR). On each 97 plane, the VOI was defined with a 2 mm area on each plane along the superior-inferior axis 98 (Fig. 1b). The VOIs were created as a cube of the same size and placed in the constructed bone 99 model (Fig. 2c). The fixation screws were modeled in Solidworks 2013 (SolidWorks Corp, 100 Waltham, MA, USA) closely following the manufacture's specifications.

101 2.2 Finite element modeling

Three surface models were created for this specific patient based upon the CT scans at three dedicated time points (M4, M16, and M28) by using ScanIP Ver. 4.3 (Simpleware Ltd, Exeter, UK) for segmentation; and Rhinoceros 4.0 (Robert McNeel & Associates, Seattle, USA) for parametrization of the reconstructed 3D models in terms of non-uniform rational B-spline (NURBS) function. Our previous clinical study on this specific subject found that the morphological bone surface changes almost ceased from M16-M28. We then assume that the

108 combination of the surface models at all these three-time points defines the surface boundary 109 that the bone could potentially grow to the maximum for this patient. Therefore, a "resultant" 110 model was obtained by merging all three surface models. This is because leaving extra room in 111 the jaw model for assigning very low Young's modulus allows accomodating the potential 112 growth of bone surface during remodelling. In order to achieve this, a CT pixel-based mapping 113 algorithm (Field et al., 2010) was adopted to create the heterogeneous bone density distribution 114 at time point M4, specifying initial bone morphology and extra space with a relatively low 115 Young's modulus. All other material properties used in this study were summarized in Table 1. 116 Hinge constraints were prescribed for the corresponding mandibular condyles (Narra et al., 117 2014). In this subject, the extensive bone resection was accompanied by functional loss of the 118 right masseter, medial pterygoid and temporalis muscles; consequently, masticatory conditions 119 changed dramatically post-surgery. The magnitudes and directions of individual muscle forces 120 were derived in our previous study (Zheng et al., 2019a) (Fig. 2a).

121 Four additional models were generated by rearranging the number and position of fixation 122 screws, along with different screwing configurations (Fig. 2c). The final assemblies were 123 exported to ABAQUS 6.13.1 (Dassault Systèmes, Tokyo, Japan) for the FE analysis (Fig. 2b). 124 The implant components, including plate and screws, were assumed to be perfectly bonded with 125 the bone for simplification, as the bone remodeling process simulated in this study started from 126 month 4 after sugery when full osseointegration has been established (Yoda et al., 2018, 127 Ferguson et al. 2021). This assumption would not take substantial effects on the regions where 128 the surface bone remodeling is a main concern in this present study.

129 2.3 Bone remodeling algorithm

The FE-based bone remodeling simulation is based upon the Wolff's law, where four
phases of bone remodelling activities, namely underloading resorption, equilibrium (lazy zone),
apposition (Frost, 1987; Huiskes et al., 1987), and overloading resorption (Crupi et al., 2004;

Oosterwyck et al., 2002, Li et al., 2007), are considered in response to a different degrees of
mechanical stimulus from the specific homeostatic level (Carter, 1987, 1984; Frost, 1993).

135 In literature, the strain energy density (SED) per unit apparent density has been widely 136 accepted as an appropriate mechanical stimulus for jawbone remodeling (Lin et al., 2010a; 137 Weinans et al., 1992). In general, the rate equation in terms of density increment ($\Delta \rho$) over a 138 time interval (Δt) can be formulated as,

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$$\Delta \rho = \begin{cases} C_{ap} [\Xi - K(1+s)] \Delta t - C_{or} [\Xi - K(1+s)]^2 \Delta t; & \text{if } \Xi > K(1+s) \\ 0; & \text{if } K(1-s) \le \Xi \le K(1+s) \\ C_{ur} [\Xi - K(1-s)] \Delta t; & \text{if } \Xi < K(1-s) \end{cases}$$
(1)

140 where the reference stimulus is given as K = 0.00036 (I/g) (Lin et al., 2010b) and the width of lazy zone given as 2s = 0.2 (Rungsiyakull et al., 2010). Ξ is the mechanical stimulus in 141 terms of strain energy density (SED) divided by local apparent bone density. Cap, Cor and Cur 142 143 are the rate constants for bone apposition, overloading resorption, and underloading resorption, 144 respectively. All these rate constants were determined by using an inverse identification 145 procedure through correlation with the image data acquired from the dedicated clinical follow-146 up in months 4 (after initial healing) to 28 over a two-year time span. Note that the identification of the remodelling parameters was based upon the first stage through our patient-specific 147 148 longitudinal study in clinic. The remodeling algorithm and parameters established in the first 149 stage was then used to futher predict the outcome of the second stage (from 2 years to 4 years), 150 which was considered critical (e.g. 4-year mid-term outcome) for the surgeons and patients . As a result, C_{ap} , C_{or} and C_{ur} were determined to be 20 month g/cm⁵, 5000 month³ g/cm⁷ and 20 151 month g/cm^5 , respectively, for this specific patient study. 152

The minimum and maximum densities of reconstructed bone were set to be 0.7 and 2.0 g/cm³, respectively (Lin et al., 2010a). It should be noted that the density change evaluated in Eq. (1) allows updating the boundary surface in the region of interest (RoI) through gradually 156 upgrading void elements to solid elements in the boundary/interface (or other way around), 157 thereby moving the surface. Therefore, the algorithm integrates both internal remodeling (bone 158 density) and surface remodeling (bone front).

The time step in this study represented one month. The remodeling was implemented through a FORTRAN subroutine in ABAQUS, where the bone material properties in each element are evaluated as per the user-defined constitutive models. Fig. 3 provides a flowchart to depict the unified bone remodeling procedure.

In order to quantify the remodeling algorithm defined in Eq. (1), a python script was developed to convert the user-defined variables into virtual CTs (Liao et al., 2017). In this case, the FE-based virtual CT images were generated from the simulated densities at M4, M16 and M28, respectively, in order to quantitatively match the longitudinal CT data obtained from the clinical follow-up. The discrepancy of mean grayscale values in these 18 VOIs were obtained from clinical CT and FE virtual CT using MATLAB (MathWorks, Inc., Massachusetts, USA).

In this study, Pearson correlation analysis in Graph-Pad Prism 7 (GraphPad Software, Inc. CA,USA), was performed to quantify the correlation between the FE and clinical data at different time steps. The root mean square error (RMSE) was also calculated to report the possible prediction error from the present bone remodeling algorithm in Graph-Pad Prism 7.

173 To calculate the variations in bone density and mechanical stimulus in the regions of 174 interest more appropriately, their volume averages were calculated as:

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$$\rho = \frac{1}{V} \int_{V} \rho dV \cong \frac{\sum_{e=1}^{n} \rho_e V_e}{\sum_{e=1}^{n} V_e}$$
(2)

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$$\Xi = \frac{1}{V} \int_{V} \Xi dV \cong \frac{\sum_{e=1}^{n} \Xi_e V_e}{\sum_{e=1}^{n} V_e}$$
(3)

3. Results

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179 3.1 Bone remodeling outcome

180 Fig. 4 shows the correlations between the clinical CT and FE virtual CT images at two time 181 periods, in which the Pearson correlation coefficient r values were evaluated to be 0.743 and 182 0.771 for durations M4-M16 and M4-M28, respectively (p < 0.001). In line with the 183 biostatistics text (Norman and Steiner, 2008), $r \ge 0.7$ indicates a strong linear correlation in 184 biological studies. Note that it is very difficult (if not impossible) to achieve a perfect correlation 185 (r = 1) in the present circumstance, due to the coupled effects between physiological variation 186 and mechanical stimulus, in which biological/genetic factors such as systemic mineral 187 homeostasis, can to a certain extent influence the correlation between the FE simulation and the 188 clinical follow-up. The root mean square error (RMSE) of both correlation period M4-M16 and 189 M4-M28 are calculated as 11.15 and 9.81, respectively, which indicating that the present bone 190 remodeling algorithm might have a possible average error of 10.48% for bone change 191 prediction.

192 Fig. 5 shows the simulated density distribution in the whole mandible and from each cross-193 sectional DS view. Four-time points were selected at M4, M16, M28, and M48 (predicted). In general, the bone density varies substantially from M4 to M16, but the variation is leveled off 194 195 from M16. Commencing from the bone structure at M4, we also simulated the structural surface 196 change together with internal bone remodeling. It is observed that in DS1, the growth of cortical 197 region dilated from M4 to M16, but ceased from M16 onward. The bone apposition mainly 198 occurred in the superior region of the bone, exhibiting formation of cortical bridging, which is 199 considered as a predictor of establishing bone union strength (Akashi et al., 2015). In the 200 cancellous region, on the other hand, decrease of density can be observed, suggesting the 201 resorption in the inner region of the mandibular bone. In DS2, a similar trend of bone formation

is observed, and bone apposition in the cortical region also occurred mainly on the superior
surface. However, the decrease of bone density in the cancellous region is not as dramatic as in
DS1. In DS3, the decrease of bone density is observed for both cortical and cancellous regions.

205 3.3 Effects of different screw positioning

206 Fig. 6 plots the longitudinal change of density at each DS for different screwing designs. 207 For all the DSs, the overall density decreases in the course of bone remodeling. In DS1, the 208 density rapidly reduced in the first 12 months and continues to decrease at a slower rate until 209 month 33, followed by a density increase thereafter. These observations suggest that although 210 the cortical bone region is expanding, the decrease of density in the cancellous bone progressed 211 at a relatively faster rate, which dominated the overall density variation. Starting from month 212 33, resorption in the cancellous region halted, while the cortical bridge density kept increasing 213 and resulted in increase of the overall density. In DS2, the overall bone density increased for 214 the first 12 months and thereafter gradually decreased with time. For DS3, the density continued 215 to decrease from M4 onward at almost a constant rate. This trend of density variation agrees 216 with the change in density contour in Fig. 5b, where no much bone apposition was observed in 217 DS3.

Concerning different designs of screwing number and position, Design 4, with the most screws installed, does have a relatively lower resorption rate for the first 12 months and a higher apposition rate from month 27 in DS1. In DS2, Design 1 with the least screws, had a faster bone resorption rate than the other designs with more screws. There is no significant difference with all these designs in DS3. While there are certain differences in bone remodeling outcomes with different fixation placements, the deviation is considered too small to draw a clinical recommendation from a remodeling prediction perspective.

4. Discussion

226 Note that the simulation of bone remodeling in this study started from month 4, as initial 227 healing is known to generally take 6 to 12 weeks to a significant degree (Marsell and Einhorn, 228 2011). This stage acts substantially different from bone remodeling, and thereby cannot simply 229 be interpreted and simulated by the current bone remodeling algorithm established (Calvo-230 Echenique et al., 2019; Isaksson et al., 2006). This study developed a joint remodeling 231 procedure for accommodating morphological variation in both internal density and external 232 shape of bony structure by following a topology optimization algorithm developed for 233 engineering structures. Specifically, we placed some void regions by assigning a virtually low 234 Young's modulus material, allowing to be gradually evolved into bony materials, thereby 235 simulating surface growth of bone.

236 In this study, the simulated remodeling results respond to the functional load measured for 237 this specific patient. During functional loading, the maximum stress is observed around region 238 DS1 of the symphysis. Due to distortion induced by unilateral loading in the reconstructed 239 mandible, the overall functional loading can be described as a combination of sagittal and 240 transverse bending (Wong et al., 2010). As a result, the primary loading reaches the maximum 241 in the middle plane of the mandible (i.e. DS1 in this case). In addition, the large difference in 242 the cross-sections between the mandible and the fibula free flap in the DS1 region results in 243 high-stress gradients in this area. Therefore, the overall mechanical stimulus (i.e. strain energy 244 density per unit apparent density) in the symphysis region reaches a maximum and then 245 gradually decreases upon approaching the end of the mandibular arch (i.e. towards the ramus 246 area). As shown in Fig. 2b, higher SEDs were observed in both DS1 and DS2, compared to 247 DS3. In other words, there was insufficient mechanical stimulation in DS3, thereby leading to 248 bone resorption at a constant rate.

249 Since the mechanical stimulus is considered to be a trigger to initiate bone remodeling, 250 high accumulation of SED on both DS1 and DS2 results in bone formation in the conjunction 251 areas. Similar to the cortical bridging forming in DS1, bone apposition on the superior region 252 of DS2 was also triggered by the high SED. However, in DS1, once the cortical bridge is 253 established properly, the mechanical stimulus ceases increasing as less strain could develop in 254 those regions, which to a certain extent, explains why the cortical region stops growing from 255 M16 afterward. For the same reason, the mechanical stimulus decreased in the cancellous 256 region, and such an under-loading condition casued bone resorption.

It is interesting to note that the inferior cortical region experienced bone resorption after M28 (Fig. 5b), while the superior aspect of cortical bone remains in equilibrium. The possible reason may be related to formation of a proper cortical bridge from M4 to M28, whereby the increasing strength on the superior surfaces enabled it to withstand more loads and consequently, less load was transferred to the inferior side. The associated reducation in mechanical stimulation appears to approach the lower thresholds of the effective SED, thereby triggering underloading bone resorption in the region.

264 The accumulation of stress in the DS1 region due to the altered functional loading in the 265 reconstructed mandible also explains why bone resorption in DS1 can be reversed from 33 266 month post-surgery. The latter was followed by a gradual increase in overall bone density, in 267 which the mechanical stimulus exceeded the upper threshold of the SED, thus changing from 268 overall resorption to overall apposition. The bone apposition ceased once an equilibrium was 269 reached, implying that the reduced mechanical stimulus falled into the lazy zone at this stage. 270 In comparison, bone resorption in DS2 and DS3 continued over time as the relatively lower 271 mechanical loading and stimuli were transferred to these areas. It is speculated that an implant-272 supported denture may be a possible solution that has been commonly considered as an option 273 for functional rehabilitation following mandibular reconstruction (Hakim et al., 2015). This

may lead to different biomechanical conditions and remodelling outcomes. Although the timing
of such implant placement remains controversial, increasing biomechanical stimulation through
the application of symmetrical functional loading might enable to better engage bony tissues in
regions DS2 and DS3.

278 There are few studies in literature that have investigated the longitudinal bone variation for 279 patients undergone mandibular reconstruction using fibula free flap. Disa et al. (1999) and 280 Zoumalan et al. (2009) reported, on average, there are 10 and 20% bone height loss in the fibula 281 free flaps following reconstruction, respectively. Disa et al. (1999) also investigated the 282 different loss percentage of bone height for the patient with a 48 month follow-up in three 283 specific regions: anterior (DS1), body (DS2), ramus areas (DS3), which are 5.8, 10 and 4.1%, 284 respectively. In comparison, the predicted bone losses over the 48 months in the present study 285 of these three regions are 4.2, 2.7 and 3.1%, respectively. To be noted, the both above literature 286 studies suggested bone height loss by measuring the midportion of the region of interest on X-287 Ray scans; while in the our study, the bone loss percentage is measured by comparing the overall 288 changes of bone volume in 3D space. This might explain why the overall bone loss in the 289 present study is less than that reported in Disa et al.'s study (1999). Our results could have been 290 more conservative as more remodeling information was captured. Moreover, in Disa et al's 291 study (1999), the DS2 is substantially higher than the other two regions, which might be due to 292 the fact that the inclined angle of DS2 to the image plane is likely to cause excessive X-ray 293 scattering compared to the other two regions where DS1 and DS3 is more parallel and 294 perpendicular to the image plane, respectively.

Fixation plates are commonly used to connect and support the grafted bone with the mandibular stumps. The role of the fixation plates is to stabilize the mechanical environment and transfer the loading to the transplant in a controllable manner. For this reason, the appropriate positioning of these screws is thought to be critically important surgically. Despite 299 the different options of numbers and positioning of screws, they have one particular aspect in 300 common, i.e. there are always two screws placed on each side of the conjunction region of bone 301 union (i.e. DS1, DS2 and DS3), where the pairs of screws play a critical role in establishing 302 substantial structural stability. This also explains why different designs led to marginal 303 differences in bone remodeling outcomes in those regions. Design 4 has the most screw 304 numbers, which does show a relatively slower bone resorption rate than the other designs (Fig. 305 6). For this reason, Design 4 has the highest the bone apposition rate in DS1 after month 33, 306 and the lowest bone resorption rate in DS2 and DS3. It is believed that use of more screws does 307 provide a more stable and stiffer system, in which the plate transfers more loading, thereby 308 either slowing down bone loss or increasing bone formation in the union regions. Nevertheless, 309 while this appears to an area of limited consequence for the present patient model, this could 310 be a research question for further study on other patients.

311 Regarding application of the proposed unified time-dependent algorithm for estimating 312 surface remodeling, it is still controversial in literature as some researchers have claimed 313 external and internal bone remodeling exhibit different mechanisms (Carter, 1984; Weinans et 314 al., 1992). Along with incorporating virtual soft (void) materials with a very low Young's 315 modulus surrounding the cortical region, the simulated surface remodeling results exhibit a 316 reasonable match with the clinical data acquired. It is noted that there exist certain discrepancies 317 when matching the simulation with the clinical data, such as the superior region in DS3. The 318 clinical complexity of such reconstructed regions (e.g. DS3) introduces some challenges for a 319 comprehensive correlation between them. However, for a relatively less complicated region, 320 such as DS2, the current remodeling algorithms provided a fairly realistic simulation. 321 Regarding the density prediction in the region surrounding the VOIs, where the internal bone 322 remodeling may have dominated bone turnover, the simulated results correlate better with the 323 clinical follow-up.

Another limitation would be the patient-specific nature of this study. The remodeling algorithm, parameters and simulation results were based upon only one particular subject. Other patient factors, such as their systemic background, bone's conditions and surgical procedures, could be considered as additional decisive factors influencing the bone remodeling process. Further evaluation and data acquisition of other subjects with inevitably varied conditions are necessary before generalizing these clinical and biomechanical findings.

330 Regarding the possible evolution of remodelling parameters, it remains an open research 331 question in literature. The remodelling parameters per se are patient-specific due to the fact 332 that the physiological and biomechanical environments vary with ageing, health status, medication, and life-styles, etc. The interaction between physiological and mechanical 333 334 conditions can be rather complex; so from our point of view, whether using evolving or constant 335 remodeling parameters depends on the accepted level of correlation with clinical data. One of 336 our previous studies did consider envoling remodeling parameters (Liao et al. 2017) at different 337 remodeling stages. While such a method is more realistic in principle, we decided to use the 338 constant remodeling coefficient as it is more efficient and easier to handle, given the bone 339 remodeling results (i.e. correlation coefficient) derived from the both methods are quite 340 indifferent.

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5. Conclusion

In this patient-specific case study on the biomechanics of the orofacial reconstruction using fibula free flap (FFF), a time-dependent finite element (FE) based remodelling algorithm is developed by correlating longitudinal clinical data. A unified internal and external remodeling procedure was proposed here to investigate the bone's responses in three specific regions of bone union (namely DS1, DS2, DS3) over a four-year treatment period (up to 48 months). It is

348	found that the overall bone density decreased over time, except for region DS1, where bone
349	apposition started at 33 months after undergoing a certain period of resorption. A neglectable
350	effect was observed for the different splint designs of screw numbers and positioning. In spite
351	of the intrinsic limitations, this study is believed to be the first of its kind by developing a unified
352	remodeling procedure for major orofacial reconstruction.

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Conflict of interest

359 Authors have no conflict of interest concerning the present manuscript.

Table 1. Material properties adopted in FE models

Materials	Young's Modulus (MPa)	Poisson's ratio
Bone	Heterogeneous	0.30
Periodontal ligament (PDL)	Hyperelastic (Marlow)	0.45
Teeth (enamel and dentine)	20,000	0.20
Titanium (Implant, abutment, screw)	110,000	0.35



Figures





- 367 and DS3) for the bone union; (b) VOIs placement in each docking site; and (c) VOIs definition
- in the 3D FE model.



Fig. 2. The schematic of finite element modeling. (a) illustration of loading and boundary
conditions applied; (b) Contour of strain energy density (SED) distribution simulated in the
assembly; and (c) illustration of the plate – screwing configuration with different designs.



374 Fig. 3. Flowchart of the unified bone remodeling procedure for correlating with clinical follow-

up data.



Fig. 4. (a) Demonstration of the correlation between clinical CT and virtual CT images. Pearson
correlation analysis between the changes of VOI grayscale values in the clinical CT and FE
virtual CT, for (b) M4 – M16 (Month 4 – Month 16) and (c) M4 -M28 (Month 4 – Month 28).

- **Fig. 5.** Longitudinal changes of density from M4 to M48. (a) Overview of the density change
- 382 on the whole mandible; and (b) cross-sectional images of the density variation in each DS.



Fig. 6. Remodeling progresses in the regions of interest at (a) DS1, (b) DS2 and (b) DS3 region
from 4 to 48 months.

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